

UiO: Fysisk institutt

Det matematisk-naturvitenskapelige fakultet

Lecture 4

This week

- **Monday:** Symmetries of systems (Section 2.3)
- **Wednesday:** Energy conservation, velocity dependent potentials. (Sections 2.3 and 2.4)
- **Problem session:** Problem set 2 (main topic: finding the e.o.m. from Lagrange's equation)

Recap

• The essence of Lagrange-Hamilton formalism is

• The Lagrange equation dealing with part 3 is where the Lagrangian *L* is given by *d* dt \int \hat{c} ∂ *L* $\partial\, \dot{q}^{}_i\Big\vert$ − ∂ *L* ∂*qⁱ* = 0, *j*=1,2*,*…*,d* $L(q, \dot{q}, t) = K(q, \dot{q}, t) - V(q, t)$

Plan for today

- Symmetries of systems (Section 2.3)
	- ― Conserved quantities (constants of motion)
	- ― Noether's theorem
	- ― Cyclic coordinates
	- ― Generalized momentum/conjugate momentum
	- ― More general symmetries of the Lagrangian
	- ― A proof of conservation of angular momentum! (If we have time)

Summary

- Cyclic coordinates are generalized coordinates qi that do not appear in the Lagrangian
- The corresponding **conjugate momentum** p_i is conserved ∂ *L*

$$
p_i \equiv \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{q}_i} \right)
$$

i

• If Q is the parameter of a transformation leaving the Lagrangian invariant the conserved quantity K is $K=\sum$ ∂ *L Qi*

 $∂$ \dot{q} _{*i*}