Chapter 8: Classes part 2 - special methods

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0.1 Special methods

- The class constructor has a special name: __init__
- The name is recognized by Python, and ensures this method is called when a new class instance is created; e.g. y = MyClass(4)
- The constructor is an example of a special method
- $\bullet\,$ Special methods have names with leading and trailing double underscores
- Special methods are recognized by Python, and automatically called when we perform various operations on the class instances

0.2 The call special method; motivation

Recall the class for representing a function: $% \left(1\right) =\left(1\right) \left(1\right)$

```
class Y:
    def __init__(self, v0):
        self.v0 = v0
        self.g = 9.81

    def value(self, t):
        return self.v0*t - 0.5*self.g*t**2

y = Y(3)
v = y.value(0.1)
```

But it would be more natural to use the class like this:

```
y = Y(3)
v = y(0.1)
```

0.3 The call special method; implementation

Simply replace the value method by a *call* special method:

```
class Y:
    def __init__(self, v0):
        self.v0 = v0
        self.g = 9.81

    def __call__(self, t):
        return self.v0*t - 0.5*self.g*t**2

Now we can write

y = Y(3)
v = y(0.1) # same as v = y.__call__(0.1) or Y.__call__(y, 0.1)
```

Note:

- The instance y now behaves and looks as a function!
- The value(t) method does the same, but __call__ allows nicer syntax for computing function values

0.4 Special method for printing

- In Python, we can usually print an object a by print(a), works for built-in types (strings, lists, floats, ...)
- Python does not know how to print objects of a user-defined class, but if the class defines a method __str__, Python will use this method to convert an object to a string

Example:

0.5 The repr special method: eval(repr(p)) creates p

```
class MyClass:
     def __init__(self, a, b):
    self.a, self.b = a, b
     def __str__(self):
    """Return string with pretty print."""
          return f'a={self.a}, b={self.b}'
     def __repr__(self):
    """Return string such that eval(s) recreates self."""
    return f'MyClass({self.a}, {self.b})'
>>> m = MyClass(1, 5)
>>> print(m)
                    # calls m.__str__()
a=1, b=5
                     # calls m.__str__()
>>> str(m)
'a=1, b=5'
>>> s = repr(m) # calls m.__repr__()
'MyClass(1, 5)'
\Rightarrow m2 = eval(s) # same as m2 = MyClass(1, 5)
                     # calls m.__repr__()
>>> m2
'MyClass(1, 5)'
```

0.6 Class Y revisited with print and repr method

```
class Y:
    """Class for function y(t; v0, g) = v0*t - 0.5*g*t**2."""

def __init__(self, v0):
    """Store parameters."""
    self.v0 = v0
    self.g = 9.81

def __call__(self, t):
    """Evaluate function."""
    return self.v0*t - 0.5*self.g*t**2

def __str__(self):
    """Pretty print."""
    return f'v0*t - 0.5*g*t**2; v0={self.v0}'

def __repr__(self):
    """Print code for regenerating this instance."""
    return f'Y({self.v0})'
```

0.7 Special methods for arithmetic operations

```
c = a + b # c = a.\_add\_(b)

c = a - b # c = a.\_sub\_(b)

c = a*b # c = a.\_mul\_(b)

c = a/b # c = a.\_div\_(b)

c = a**e # c = a.\_pow\_(e)
```

0.8 Special methods for comparisons

```
a == b # a.__eq__(b)

a != b # a.__ne__(b)

a < b # a.__lt__(b)

a <= b # a.__le__(b)

a > b # a.__gt__(b)

a >= b # a.__ge__(b)
```

0.9 The programmer is in charge of defining special methods!

How should, for instance, __add__(self, other) and __mul__(self, other) be defined?

This is completely up to the programmer, depending on what are meaningful results of object1 + object2 and object1 * object2.

0.10 Class for vectors in the plane

Mathematical operations for vectors in the plane:

$$(a,b) + (c,d) = (a+c,b+d)$$

 $(a,b) - (c,d) = (a-c,b-d)$
 $(a,b) \cdot (c,d) = ac+bd$
 $(a,b) = (c,d)$ if $a=c$ and $b=d$

Desired application code:

```
>>> u = Vec2D(0,1)
>>> v = Vec2D(1,0)
>>> print(u + v)
(1, 1)
>>> a = u + v
>>> w = Vec2D(1,1)
>>> a == w
True
>>> print(u - v)
(-1, 1)
```

```
>>> print(u*v)
0
```

0.11 Class for vectors; implementation

```
class Vec2D:
    def __init__(self, x, y):
        self.x = x;        self.y = y

    def __add__(self, other):
        return Vec2D(self.x+other.x, self.y+other.y)

    def __sub__(self, other):
        return Vec2D(self.x-other.x, self.y-other.y)

    def __mul__(self, other):
        return self.x*other.x + self.y*other.y

    def __abs__(self):
        return math.sqrt(self.x**2 + self.y**2)

    def __eq__(self, other):
        return self.x == other.x and self.y == other.y

    def __str__(self):
        return f'({self.x}, {self.y})'
```

0.12 Class for polynomials; functionality

A polynomial can be specified by a list of its coefficients. For example, $1-x^2+2x^3$ is

$$1 + 0 \cdot x - 1 \cdot x^2 + 2 \cdot x^3$$

and the coefficients can be stored as [1, 0, -1, 2]

Desired application code:

```
>>> p1 = Polynomial([1, -1])
>>> print(p1)
1 - x
>>> print(p1(x=0.5))
0.5
>>> p2 = Polynomial([0, 1, 0, 0, -6, -1])
>>> p3 = (p1 + p2)
>>> print(p3.coeff)
[1, 0, 0, 0, -6, -1]
>>> print(p3)
1 - 6*x^4 - x^5
>>> p2.differentiate()
>>> print(p2)
1 - 24*x^3 - 5*x^4
```

How can we make class Polynomial?

0.13 Class Polynomial; basic code

```
class Polynomial:
    def __init__(self, coefficients):
        self.coeff = coefficients

def __call__(self, x):
        s = 0
        for i in range(len(self.coeff)):
            s += self.coeff[i]*x**i
        return s
```

0.14 Class Polynomial; addition

```
class Polynomial:
    ...

def __add__(self, other):
    # return self + other

# start with the longest list and add in the other:
    if len(self.coeff) > len(other.coeff):
        coeffsum = self.coeff[:] # copy!
        for i in range(len(other.coeff)):
            coeffsum[i] += other.coeff[i]

else:
    coeffsum = other.coeff[:] # copy!
    for i in range(len(self.coeff)):
        coeffsum[i] += self.coeff[i]
    return Polynomial(coeffsum)
```

0.15 Class Polynomial; multiplication

Mathematics: Multiplication of two general polynomials:

$$\left(\sum_{i=0}^{M} c_{i} x^{i}\right) \left(\sum_{j=0}^{N} d_{j} x^{j}\right) = \sum_{i=0}^{M} \sum_{j=0}^{N} c_{i} d_{j} x^{i+j}$$

The coeff. corresponding to power i+j is $c_i \cdot d_j$. The list \mathbf{r} of coefficients of the result: $\mathbf{r}[\mathbf{i}+\mathbf{j}] = \mathbf{c}[\mathbf{i}]*\mathbf{d}[\mathbf{j}]$ (i and j running from 0 to M and N, resp.)

Implementation:

class Polynomial:

```
def __mul__(self, other):
    M = len(self.coeff) - 1
    N = len(other.coeff) - 1
    coeff = [0]*(M+N+1) # or zeros(M+N+1)
    for i in range(0, M+1):
```

for j in range(0, N+1):
 coeff[i+j] += self.coeff[i]*other.coeff[j]
return Polynomial(coeff)

0.16 Class Polynomial; differentation

Mathematics: Rule for differentiating a general polynomial:

$$\frac{d}{dx} \sum_{i=0}^{n} c_{i} x^{i} = \sum_{i=1}^{n} i c_{i} x^{i-1}$$

If c is the list of coefficients, the derivative has a list of coefficients, dc, where dc[i-1] = i*c[i] for i running from 1 to the largest index in c. Note that dc has one element less than c.

Implementation:

```
class Polynomial:
    ...
    def differentiate(self):  # change self
        for i in range(1, len(self.coeff)):
            self.coeff[i-1] = i*self.coeff[i]
        del self.coeff[-1]

def derivative(self):  # return new polynomial
        dpdx = Polynomial(self.coeff[:])  # copy
        dpdx.differentiate()
        return dpdx
```

0.17 Class Polynomial; pretty print

0.18 Class for polynomials; usage

Consider

$$p_1(x) = 1 - x$$
, $p_2(x) = x - 6x^4 - x^5$

and their sum

$$p_3(x) = p_1(x) + p_2(x) = 1 - 6x^4 - x^5$$

```
>>> p1 = Polynomial([1, -1])
>>> print(p1)
1 - x
>>> p2 = Polynomial([0, 1, 0, 0, -6, -1])
>>> p3 = (p1 + p2)
>>> print p3.coeff
[1, 0, 0, 0, -6, -1]
>>> p2.differentiate()
>>> print(p2)
1 - 24*x^3 - 5*x^4
```

0.19 Example; "automatic" differentiation

Given some mathematical function in Python, say

```
def f(x):
    return x**3

can we make a class Derivative and write

dfdx = Derivative(f)

so that dfdx behaves as a function that computes the derivative of f(x)?

print(dfdx(2)) # computes 3*x**2 for x=2
```

0.20 Automagic differentiation; solution

Method. We use numerical differentiation "behind the curtain":

$$f'(x) \approx \frac{f(x+h) - f(x)}{h}$$

for a small (yet moderate) h, say $h = 10^{-5}$

Implementation.

```
class Derivative:
    def __init__(self, f, h=1E-5):
        self.f = f
        self.h = float(h)

    def __call__(self, x):
        f, h = self.f, self.h  # make short forms
        return (f(x+h) - f(x))/h
```

0.21 Automagic differentiation; demo

```
>>> from math import *
>>> df = Derivative(sin)
>>> x = pi
>>> df(x)
-1.000000082740371
>>> cos(x) # exact
-1.0
>>> def g(t):
... return t**3
...
>>> dg = Derivative(g)
>>> t = 1
>>> dg(t) # compare with 3 (exact)
3.000000248221113
```

0.22 Automagic differentiation; useful in Newton's method

Newton's method solves nonlinear equations f(x) = 0, but the method requires f'(x)

```
def Newton(f, xstart, dfdx, epsilon=1E-6):
    ...
    return x, no_of_iterations, f(x)
```

Suppose f'(x) requires boring/lengthy derivation, then class Derivative is handy:

```
>>> def f(x):
... return 100000*(x - 0.9)**2 * (x - 1.1)**3
...
>>> df = Derivative(f)
>>> xstart = 1.01
>>> Newton(f, xstart, df, epsilon=1E-5)
(1.0987610068093443, 8, -7.5139644257961411e-06)
```

0.23 Class introduction - summary

- Classes pack together data and functions that naturally belong together
- We define a class, and then create *instances* (or objects) of that class
 - Different instances will have different data, but they all have the same functions operating on that data
- In IN1900 codes, classes are never really necessary, but sometimes convenient.
- In "real-world" programs, with tens of 1000s of lines, the extra organization offered by classes may be the difference between a code that works and one that doesn't

0.24 Summary of special methods

- c = a + b implies c = a.__add__(b)
- There are special methods for a+b, a-b, a*b, a/b, a**b, -a, if a:, len(a), str(a) (pretty print), repr(a) (recreate a with eval), etc.
- With special methods we can create new mathematical objects like vectors, polynomials and complex numbers and write "mathematical code" (arithmetics)
- The call special method is particularly handy: v = c(5) means $v = c._call_(5)$
- Functions with parameters should be represented by a class with the parameters as attributes and with a call special method for evaluating the function