## INF 4300 - Digital Image Analysis

## OBJECT

REPRESENT ATION


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## Today

## G \& W Ch. 11.1 Representation <br> - Curriculum includes lecture notes.

We cover the following:
11.1.1 Boundary following (self study)
11.1.2 Chain Codes
11.1.3 Polygonal Approximations using MPP (omitted)

Recursive boundary splitting
Sequential polygonization
11.1.5 Boundary Signatures
11.1.6 Boundary Segments (convex hull)
11.1.7 Skeletons

Fourier representation and Fourier descriptors
Region representation by Run Length Encoding (RLE)

## Shape representations vs. descriptors

- After the segmentation of an image,
its regions or edges are represented and described in a manner appropriate for further processing.
- Shape representation:
the ways we store and represent the objects
- Perimeter
- Interior
- Shape descriptors:
methods for characterizing object shapes.
- The resulting feature values should be useful for discrimination between different object types.


## Assumptions for shape representation

- The image objects can be represented as:
- Whole regions
- grey level or color image
- compressed image
- binary image
- Contours (region boundaries)
- in cartesian coordinates
- in polar coordinates
- in some other coordinates
- through a chain code / transform
- as coefficients of some transform (e.g. Fourier)
- through a run length code / transform


## Considerations

- Input representation form, boundaries or whole regions?
- Object reconstruction ability?
- Incomplete shape recognition ability?
- Local/global description?
- Mathematical or heuristic techniques?
- Statistical or syntactic object description?
- Robustness of description to
translation, rotation, and scale transformations?
- Shape description properties in different resolutions?
- description changes discontinuously.
- Robustness against
- image noise
- geometric sampling (discretization)
- intensity quantization


## What is "shape"?

- A numerical description of the spatial configurations in the image.
- There is no generally accepted methodology of shape description.
- Location and description of high curvature points give essential information about the shape.

$\triangle$ Three curvature points

Ellipses with different size and orientation

Objects with more irregular shape

## What is shape

Is invariance needed?

- Numerical description of spatial configurations in an image.
- No generally accepted methodology of shape description.
- Location and description of high curvature points give essential information.
- Many useful, application-dependent heuristics.
- Shape description of 2D planar objects is "easy".
- Shape is often defined in a 2D image, but its usefulness in a 3D world depends on 3D -> 2D mapping.
- Invariance is an important issue.

-Translation invariance
- Scale invariance
-Rotation invariance, but what about 6 and $9 ?$
-Warp invariance
-For grey-level regions:
- invariance to contrast and mean gray level


## Shape invariants

- Shape descriptors depend on viewpoint, => object recognition may often be impossible if object or observer changes position.
- Shape description invariance is important
- shape invariants represent properties which remain unchanged under an appropriate class of transforms.
- Stability of invariants is a crucial property which affects their applicability.
- The robustness of invariants to image noise and errors introduced by image sensors is of prime importance.


## Region identification

- Goal of segmentation was to achieve complete segmentation, now, the regions must be labeled.
- Search image pixel for pixel, and sequentially number each foreground pixel you find according to the labeling of its neighbors.
- The algorithm is basically the same in 4-connectivity and 8 -connectivity, the only difference being in the neighborhood mask shape.
- Result of region identification is a matrix the same size as the image with integers representing each pixels region label.
- This representation of regions will be the input to our shape descriptors
- Matlab function implementing this is bwlabel
- XITE: regionAnalyse

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## Creating the region objects

- Start in upper left corner.
- Find first object pixel.

- Traverse the border of this object
- (recursive programming efficient)
- Continue with other pixels not yet visited
- Implementing this is time consuming
- (but may be interesting)


## Software for generating regions from a segmented image

- Matlab: Functions bwlabel and regionprops are the starting point:
$B 1=$ bwlabel $(B)$; $B$ is a binary image, obtained by segmentation;
$\mathrm{D}=$ regionprops(B1,'area','boundingbox'); Compute area and boundingbox for all regions in the image.
aa=[D.area];
See help regionprops for a list of all descriptors.
Typical use: get a list of pixels for each region
$g=$ bwperim( $B, 8$ ); Find perimeter pixels of all region in binary image $B$
- XITE - I mage processing library/ software in C
- http://www.ifi.uio.no/research/groups/dsb/software/xite/
- Main program: xshow <filename.biff>
- Region tools program: regionAnalyse
- Main function to call from your C-program: regionYline - creates the region objects.


## Contour representation

- Goal of contour methods is to describe objects in images
- Hopefully, our contour detection method delivers a sequence of pixel coordinates in the image!
- The contour can be represented as:
- Cartesian coordinates
- Polar coordinates from a reference point (usually image origin)
- Chain code and a starting point
- Connectivity: 4- or 8-neighbors
- Note: chain code is very sensitive to noise, image resolution and object rotation.
- Not well suited for classification directly, but useful for computation of other features.


## Chain codes

- Chain codes represent the boundary of a region
- Chain codes are formed by following the boundary in a given direction (e.g. clockwise) with 4-neighbors or 8-neighbors
- A code is associated with each direction
- A code is based on a starting point, often the upper leftmost point of the object



## Chains

- Chains represent objects within the image or borders between an object and the background

$\square$ Object pixel
- How do we define border pixels?
- 4-neighbors
- 8-neighbors
- In which order do we check the neighbors?
- Chains represent the object pixel, but not their spatial relationship directly

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## Chain codes



Chain code in clockwise direction:
000776655555566000000644444442221111112234445652211

Using all border point vs. resampling the border


- If chain codes are generated from every point on the border, the chain will be both long and can be sensitive to small disturbances along the border.
- The border is often resampled to a larger grid before chain coding is done. The accuracy of the chain code depends on the grid size.


## Comments about chain code

- The chain code depends on the starting point.
- It can be normalized for start point by treating it as a circular/periodic sequence, and redefine the starting point so that the resulting number is of minimum magnitude.
- We can also normalize for rotation by using the first difference of the chain code: (direction changes between code elements)
- Code: 10103322
- First difference: 33133030

- Minimum circular shift: 03033133

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- This invariance is only valid if the boundary itself is invariant to rotation and scale.

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## Chain code example with smoothing

## Recursive boundary splitting

- Draw straight line between contour points that are farthest apart. These two points are the initial breakpoints.

1. For each intermediate point:
2. Compute the point-to-line distance
3. Find the point with the greatest distance from the line.
4. If this distance is greater than given threshold, we have a new breakpoint.
5. The previous line segment is replaced by two, and 1-4 above is repeated for each of them.

- The procedure is repeated until all contour points are within the threshold distance from a corresponding line segment.
- The resulting ordered set of breakpoints is then the set of vertices of a polygon approximating the original contour
- This is probably the most frequently used polygonization.
- Since it is recursive, the procedure is fairly slow.


## Sequential polygonization

## Signature representations

- Start with any contour point as first "breakpoint".
$f(x){ }^{\dagger}$
- Step through ordered sequence of contour points.
- Using previous breakpoint as the current origin, area between contour and approximating line is:

$$
A_{i}=A_{i-1}+\frac{1}{2}\left(y_{i} x_{i-1}-x_{i} y_{i-1}\right), \quad s_{i}=\sqrt{x_{i}^{2}+y_{i}^{2}}
$$

- Let previous point be new breakpoint if
- area deviation $\boldsymbol{A}$ per unit length $\boldsymbol{s}$ of approximating line segment exceeds a specified tolerance, $\boldsymbol{T}$.
- If $\left|\mathbf{A}_{\mathbf{i}}\right| / \mathbf{s}_{\mathbf{i}}<\mathbf{T}, \mathbf{i}$ is incremented and $\left(\mathbf{A}_{\mathbf{i}}, \mathbf{s}_{\mathbf{i}}\right)$ is recomputed.
- Otherwise, the previous point is stored as a new breakpoint, and the origin is moved to new breakpoint.
- This method is purely sequential and very fast.
- A signature is a 1D functional representation of a 2D boundary.
- It can be represented in several ways.
- Simple choise: radius vs. angle:

- Invariant to translation.
- Not invariant to starting point, rotation or scaling.

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## Normalization of $(r, \theta)$ signature

- Normalization for starting point and rotation:
- Find unique point on the boundary according to some criteria:
- Farthest away from the center (may not be unique)
- Obtain the chain code and normalize as described for chain codes.
- Normalization for scale:
- If the boundary is sampled at equal intervals in angle, changes in size only affect the amplitude ( $r$ ).
- The function can be scales so that it always spans the range $[0,1]$.
- This is not robust for extreme values of $\mathrm{min} / \mathrm{max}$.
- Scaling by subtracting the mean and dividing by the standard deviation is more robust.

$$
\frac{r-\mu}{\sigma}
$$

Signature example


## Boundary segments from convex hull

## Descriptors extracted from the CH

- The boundary can be decomposed into segments.
- Useful to extract information from concave parts of the objects.
- Convex hull H of set S is the smallest convex set containing S .
- The set difference H-S is called the convex deficiency D.
- If we trace the boundary and identify the points where we go in and out of the convex deficiency, these points can represent important border points charaterizing the shape of the border.
- Border points are often noisy, and smoothing can be applied first
- Smooth the border by moving average of $k$ boundary points.
- Use polygonal approximation to boundary.
- Simple algorithm to qet convex hull from polyaons.



## Skeletons

- The skeleton of a region is defined by the medial axis transform: For a region $R$ with border $B$, for every point $p$ in $R$, find the closest neighbor in $B$.
- If $p$ has more than one such neighbor, it belong to the medial axis.
- The skeleton $\mathrm{S}(\mathrm{A})$ of an object is the axis of the object.
- The medial axis transform gives the distance to the border.


Useful features for shape characterization can be e.g.:

- Area of object and area of convex hull (CH)
- CH "solidity" aka "convexity" = (object area)/(CH area)
= The proportion of pixels in CH also in the object
- Better than "extent" = (object area)/(area of bounding box)
- Number of components of convex deficiency
- Distribution of component areas
- Relative location of
- points where we go in and out of the convex deficiency.
- points of local maximal distance to CH .


## Thinning algorithm to find the skeleton

- There are many algorithms in the literature, here is just one.
- Assume that region points have value 1 and background points 0 .
- Define a contour point as a point that has value 1 and at least one 8 -neighbor with value 0 .
- Apply successive passes of two steps to contour points of region.
- Step 1: Flag contour point $p_{1}$ for deletion if:
a) $2 \leq N\left(p_{1}\right) \leq 6$
b) $T\left(p_{1}\right)=1$
c) $p_{2} \cdot p_{4} \cdot p_{6}=0$
d) $p_{4} \cdot p_{6} \cdot p_{8}=0$


Where $\quad N\left(p_{1}\right)$ is the number of nonzero neighbors of $p_{1}$. $T\left(p_{1}\right)$ is the number of $0-1$ transitions in the ordered sequence $p_{2}, p_{3}, \ldots, p_{8}, p_{9}, p_{2}$.

## Thinning algorithm - cont.

- Step 2: change condition c) and d) to
$\mathrm{c}^{\prime}$ ) $\mathrm{p}_{2} \cdot \mathrm{p}_{4} \cdot \mathrm{p}_{8}=0$
d') $\mathrm{p}_{2} \cdot \mathrm{p}_{6} \cdot \mathrm{p}_{8}=0$
- Step 1 is applied to every border pixel in the region under consideration. If any of the conditions a)-d) are violated, the value of the point is unchanged.
- If all conditions are satisfied, the point is flagged.
- The point is not deleted until all points have been satisfied.
- After completion of step 1, the flagged points are deleted.
- Step 2 is then applied in the same manner as step 1.
- Step1+Step2 defines one iteration of the algorithm.
- More iterations are done until no further points are deleted.


## Introduction to Fourier descriptors

- Suppose that we have an object $S$ and that we are able to find the length of its contour. The contour should be a closed curve.
- We partition the contour into $M$ segments of equal length, and thereby find $M$ equidistant points along the contour of $S$.
- Traveling anti-clockwise along this contour at constant speed, we can collect a pair of waveforms $x(k)$ and $y(k)$. Any 1D signal representation can be used for these.
- If the speed is such that one circumnavigation of the object takes $2 \pi$, $x(k)$ and $y(x)$ will we periodic with period $2 \pi$. -


## Contour representation using 1D Fourier

 transform- The coordinates $(x, y)$ of these $M$ points are then put into a complex vector $s$ :

$$
s(k)=x(k)+i y(k), \quad k \in[0, M-1]
$$

- We view the $x$-axis as the real axis and the $y$-axis as the imaginary one for a sequence of complex numbers.
- The representation of the object contour is changed, but all the information is preserved.
- We have transformed the contour problem from 2D to 1D.

$s(1)=3+1 i$
$s(2)=2+2 i$
$s(3)=3+3 i$


## Fourier-coefficients from $f(k)$

- We perform a 1D forward Fourier transform
$a(u)=\frac{1}{M} \sum_{k=0}^{M-1} s(k) \exp \left(\frac{-2 \pi i u k}{M}\right)=\frac{1}{M} \sum_{k=0}^{M-1} s(k)\left(\cos \left(\frac{2 \pi u k}{M}\right)-i \sin \left(\frac{2 \pi u k}{M}\right)\right), \quad u \in[0, M-1]$
- Complex coefficients $a(u)$ are the Fourier representation of boundary.
- $a(0)$ contains the center of mass of the object.
- Exclude $a(0)$ as a feature for object recognition.
- $\mathrm{a}(1), \mathrm{a}(2), \ldots, a(M-1)$ will describe the object in increasing detail.
- These depend on rotation, scaling and starting point of the contour.
- For object recognitions, use only the $N$ first coefficients (a(N), $N<M$ )
- This corresponds to setting $a(k)=0, k>N-1$


## Fourier Symbol reconstruction

Fourer descriptor example

- Inverse Fourier transform gives an approximation to the original contour

$$
\hat{s}(k)=\sum_{k=0}^{N-1} a(u) \exp \left(\frac{2 \pi i u k}{M}\right), \quad k \in[0, M-1]
$$

- We have only used $N$ features to reconstruct each component of $\hat{S}(k)$.
- The number of points in the approximation is the same $(M)$, but the number of coefficients (features) used to reconstruct each point is smaller $(N<M)$.
- Use an even number of descriptors.
- The first 10-16 descriptors are found to be sufficient for character description. They can be used as features for classification.
- The Fourier descriptors can be invariant to translation and rotation if the coordinate system is appropriately chosen.
- All properties of 1D Fourier transform pairs (scaling, translation, rotation) can be applied.


## Fourier coefficients and invariance

- Translation affects only the center of mass (a(0)).
- Rotation only affects the phase of the coefficients.
- Scaling affects all coefficients in the same way, so ratios $a\left(u_{1}\right) / a\left(u_{2}\right)$ are not affected.
- The start point affects the phase of the coefficients.
- Normalized coefficients can be obtained, but is beyond the scope of this course.
- See e.g., Ø. D. Trier, A. Jain and T. Taxt, Feature extraction methods for character recognition - a survey. Pattern Recognition, vol. 29, no. 4, pp. 641-662, 1996.

Image, $26 \times 21$ pixels

Boundary

2 coefficients

4 coefficients

6 coefficients

## Remark about Fourier descriptors

## Note that the countour of

 is

Objects with holes, like $8,9,6$ will only by described by the outer contour.

The length of $\mathrm{a}(\mathrm{u})$ will depend on the number of boundary points (and the size of the object).
We should resample the contour by selecting M evenly spaced point along the contour.

## Run Length Encoding of Objects

- Sequences of adjacent pixels are represented as "runs".
- Absolute notation of foreground in binary images:
- Run $_{i}=\ldots ;$ row $_{\text {i }}$, column $_{i}$, runlength ${ }_{i}>; \ldots$
- Relative notation in graylevel images:
- ...;(graylevel ${ }_{i}$, runlength ${ }_{\mathrm{i}}$ ); ...
- This is used as a lossless compression transform.
- Relative notation in binary images:

Start value, length ${ }_{1}$, length ${ }_{2}, \ldots$, eol,
Start value, length ${ }_{1}$, length ${ }_{2}, \ldots$, eol,eol.

- This is also useful for representation of image bit planes.
- RLE is found in TIFF, GIF, JPEG, ..., and in fax machines.


## "Gray code"

Is the conventional binary representation of graylevels optimal?

- Consider a single band graylevel image having b bit planes.
- We desire a minimum complexity in each bit plane
- Because the run-length transform will be most efficient.
- Conventional binary representation gives high complexity.
- If the graylevel value fluctuates between $2^{k-1}$ and $2^{k}, k+1$ bits will change value: example: $127=01111111$ while $128=10000000$
- In "Gray Code" only one bit changes if graylevel is changed by 1.
- The transition from binary code to "gray code" is a reversible transform, while both binary code and "gray code" are codes.


## Gray Code transforms

- "Binary Code" to "Gray Code":

1. Start by MSB in BC and keep all 0 until you hit 1
2. 1 is kept, but all following bits are complemented until you hit 0
3. 0 is complemented, but all following bits are kept until you hit 1
4. Go to 2 .

- "Gray Code" to "Binary Code":

1. Start by MSB in GC and keep all 0 until you hit 1
2. 1 is kept, but all following bits are complemented until you hit 1 .
3. 1 is complemented, but all following bits are kept until you hit 1 .
4. Go to 2 .

## "Binary reflected gray code"

| 4 bits Gray code and binary |  |  | $1001{ }^{1000} 00000001$ |
| :---: | :---: | :---: | :---: |
| Gray | Binary | Decimal |  |
| 0000g | 0000b | 0d | 1011 |
| 0001 | 0001 | 1 | , |
| 0011 | 0010 | 2 | 1010 Cr 0010 |
| 0010 | 0011 | 3 | $1110 \rightarrow 0110$ |
| 0110 | 0100 | 4 |  |
| 0111 | 0101 | 5 | $1111 \times 0111$ |
| 0101 | 0110 | 6 |  |
| 0100 | 0111 | 7 | 1101110001000101 |
| 1100 | 1000 | 8 |  |
| 1101 | 1001 | 9 |  |
| 1111 | 1010 | 10 | Gray code shaft encoder |
| 1110 | 1011 | 11 | Gives secure reading of angle. |
| 1010 | 1100 | 12 |  |
| 1011 | 1101 | 13 | Emilie Baudot's telegraph 1878. |
| 1001 | 1110 | 14 | Code patented by Gray in 1953. |
| 1000 | 1111 | 15 |  |

Gray code in graylevel images

- MSB is the same in the two representations.
- Larger homogeneous areas in each bitplane in Gray Code than in natural binary code.
- Less noisy bitplanes in Gray Code.
- More compact run-length coding of bitplanes in Gray Code.


