



# The pragmatics of STAIRS

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# Today's topics

- Explain the practical relevance of STAIRS
- Give guidelines on
  - the use of STAIRS operators
  - refinement
- Illustrated by a running example
- Present some new operators and refinement types
- Some repetition
  
- The paper can be found on the syllabus/achievement page for INF5150
  - note: updated on Tuesday!

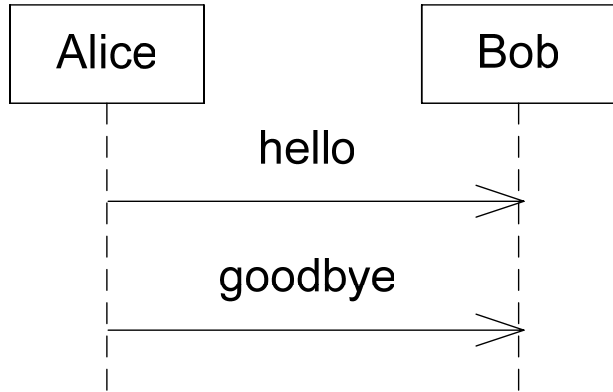


## Weak sequencing of trace sets (1)

- $s_1 \succcurlyeq s_2$  denotes the set of all traces that may be constructed by selecting one trace  $t_1$  from  $s_1$  and one trace  $t_2$  from  $s_2$  and combining them in such a way that for each lifeline, the events from  $t_1$  comes before the events from  $t_2$ .
- Note: if  $s_1$  or  $s_2$  is empty then  $s_1 \succcurlyeq s_2$  is also empty
- Remember: if the message hello is sent from  $l_1$  to  $l_2$ , then the event !hello occurs on  $l_1$  and ?hello occurs on  $l_2$

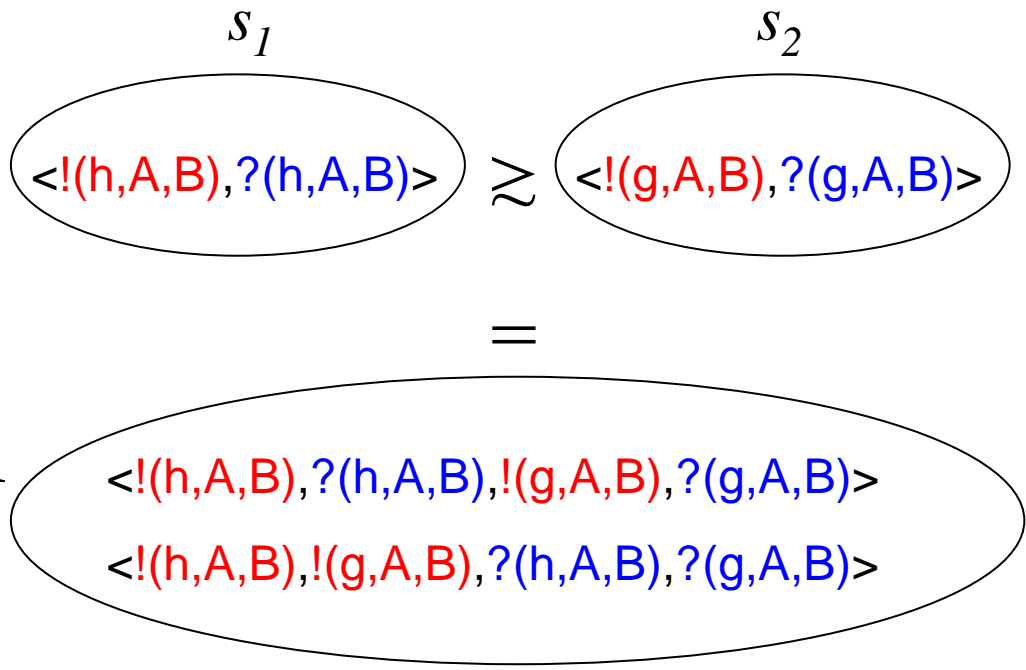


# Weak sequencing of trace sets (2)



Red events occur on Alice,  
blue events on Bob

$s_1 \approx s_2$  is the set of positive traces for the diagram



# Weak sequencing of interaction obligations

- $(p_1, n_1) \succsim (p_2, n_2) \stackrel{\text{def}}{=} (p_1 \succsim p_2, (n_1 \succsim p_2) \cup (n_1 \succsim n_2) \cup (p_1 \succsim n_2))$
- Traces composed exclusively by positive traces become positive
- Traces composed with at least one negative trace become negative



# Formal semantics of seq

- $[[d_1 \text{ seq } d_2]] \stackrel{\text{def}}{=} \{o_1 \succ o_2 \mid o_1 \in [[d_1]] \wedge o_2 \in [[d_2]]\}$
- seq is the implicit composition operator
- $o_i$  is shorthand for  $(p_i, n_i)$
- Note: For better readability we give the binary versions of the operators in this presentation. N-ary versions are used in the paper.





# The pragmatics of creating interactions



## Example: an appointment system

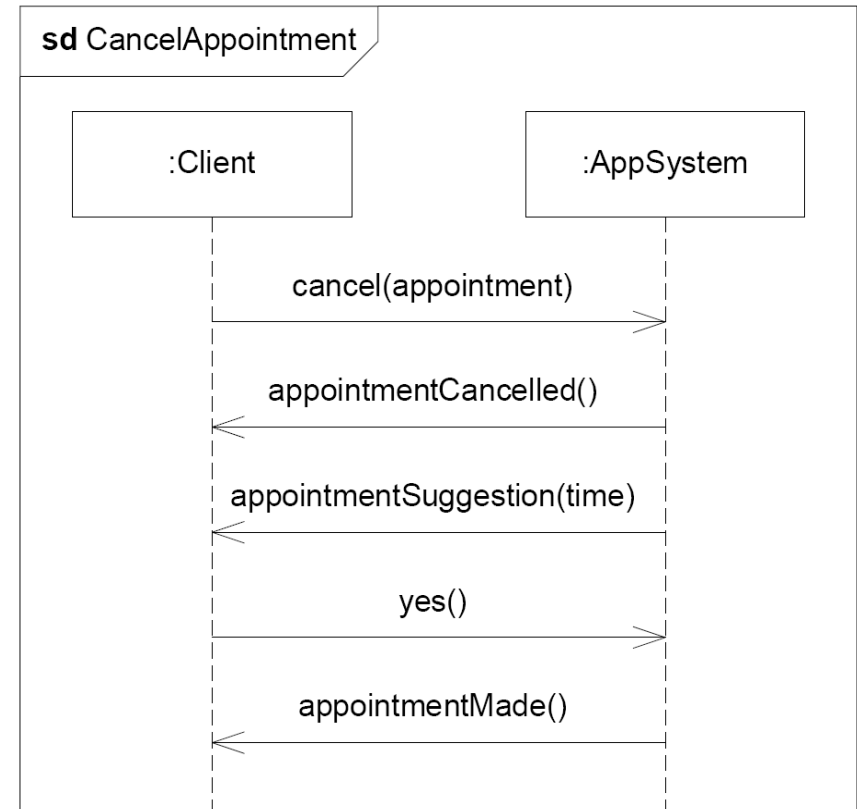
- A system for booking appointments used by e.g. dentists
- Functionality:
  - MakeAppointment: The client may ask for an appointment
  - CancelAppointment: The client may cancel an appointment
  - Payment: The system may send an invoice message asking the client to pay for the previous or an unused appointment.
- The interactions specifying the system will be developed in a stepwise manner
- Steps will be shown to be valid refinement steps





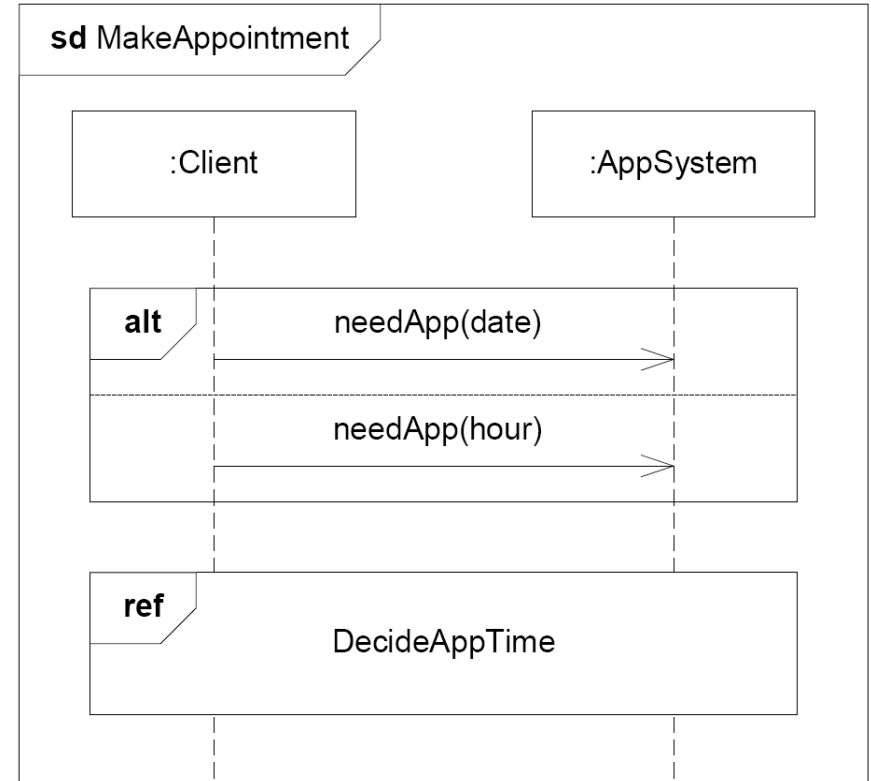
## xalt vs alt (1): CancelAppointment

- This specification has two positive traces
- Whether reception of `appointmentCancelled()` occurs before or after sending of `appointmentSuggestion(...)` is not important
- Underspecification due to weak sequencing



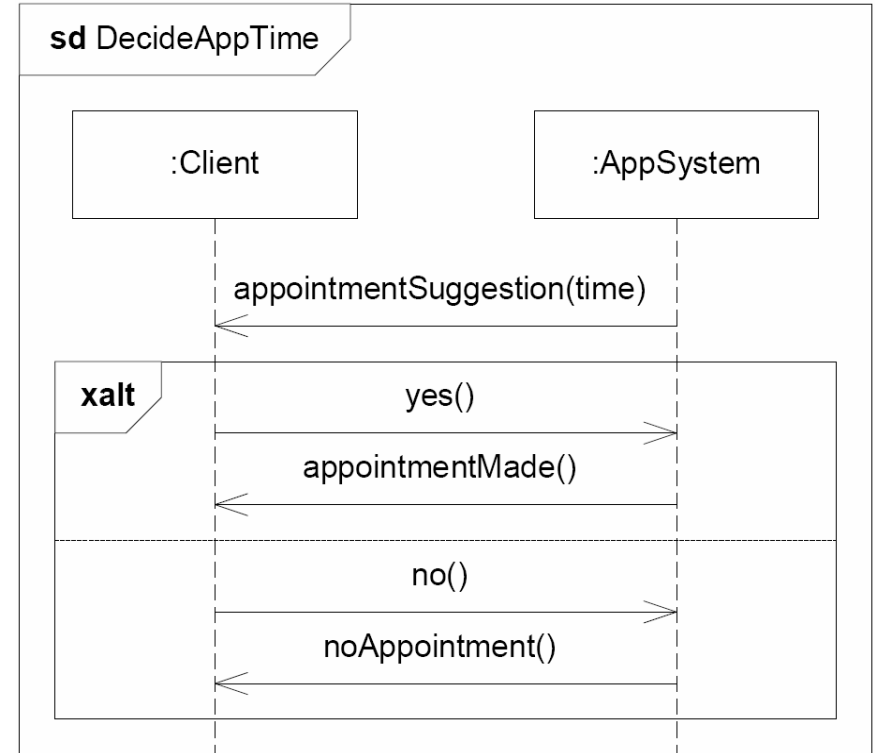
## xalt vs alt (2): MakeAppointment

- May ask for either a specific date or a specific hour of the day (e.g. in the lunch break)
- The system is not required to offer both alternatives
- Underspecification expressed by the alt operator



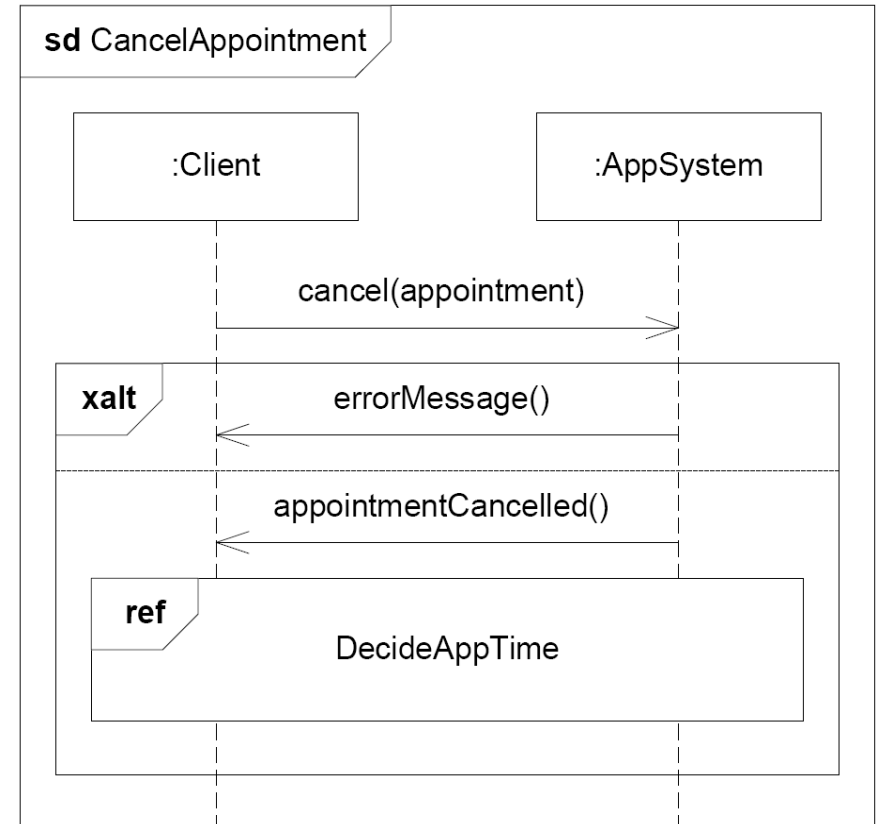
## xalt vs alt (3): DecideAppTime

- The system must be able to handle *both* `yes()` and `no()` as reply messages from the client
- This is *not* underspecification
- Therefore the alternatives are expressed by the `xalt` operator



## xalt vs alt (4): CancelAppointment

- The condition for choosing `errorMessage()` or `appointmentCancelled()` is not shown
- Both alternatives should be possible
- The choice is made by the system



## xalt vs alt (5)

- A third use of xalt: to specify inherent nondeterminism
  - for example when specifying a coin toss
- The crucial question when specifying alternatives: Do these alternatives represent similar traces in the sense that implementing only one is sufficient?
  - if yes, use alt
  - otherwise, use xalt



## Formal semantics of alt and xalt

- $[[d_1 \text{ alt } d_2]] \stackrel{\text{def}}{=} \{o_1 \uplus o_2 \mid o_1 \in [[d_1]] \wedge o_2 \in [[d_2]]\}$ , where
- $(p_1, n_1) \uplus (p_2, n_2) \stackrel{\text{def}}{=} (p_1 \cup p_2, n_1 \cup n_2)$
- $[[d_1 \text{ xalt } d_2]] \stackrel{\text{def}}{=} [[d_1]] \cup [[d_2]]$

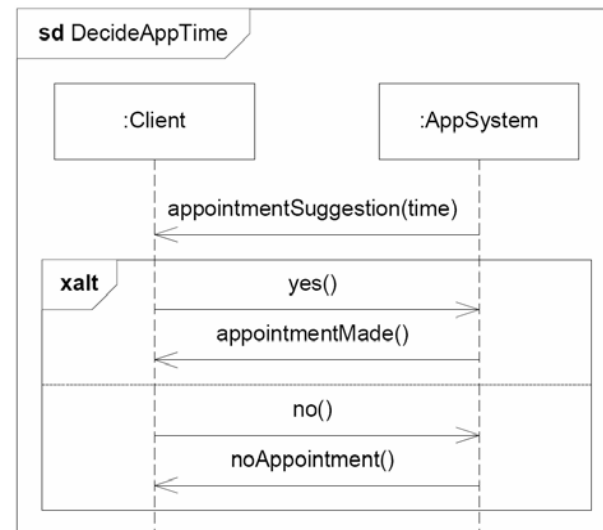
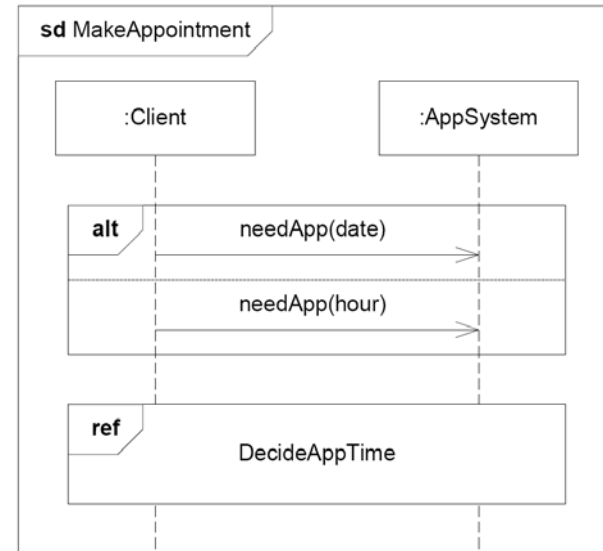
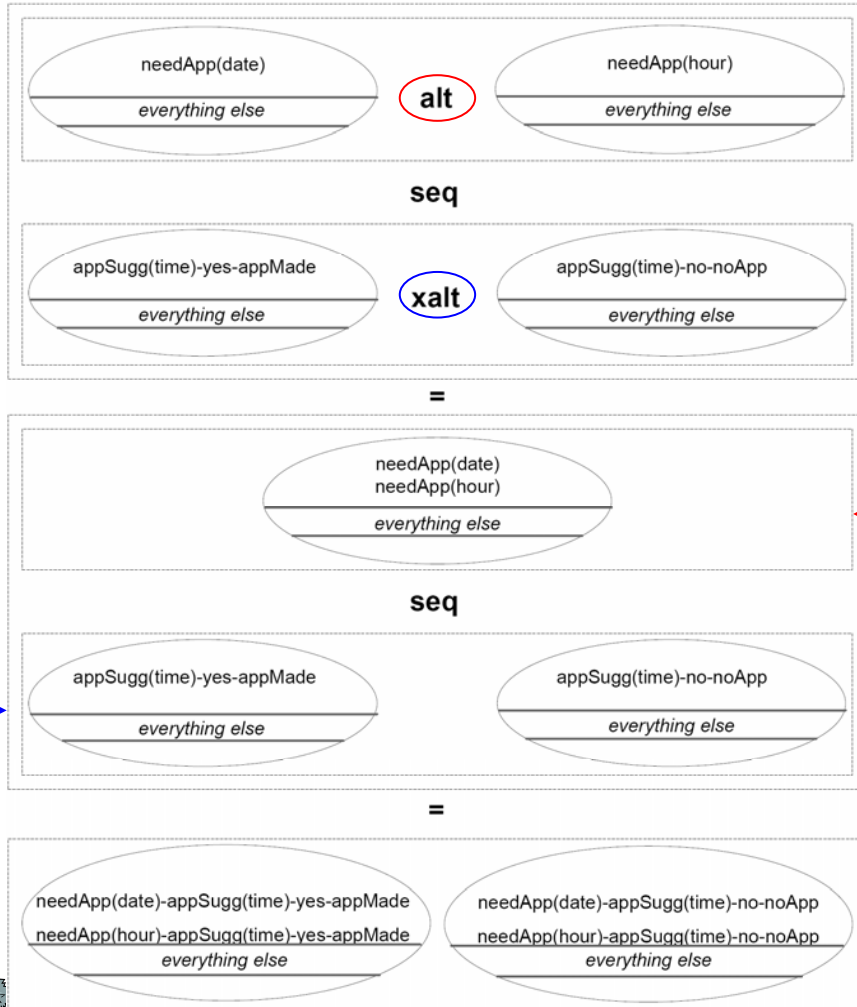


## opt and skip

- $[[\text{opt } d]] \stackrel{\text{def}}{=} [[\text{skip alt } d]]$
- $[[\text{skip}]] \stackrel{\text{def}}{=} \{(\{\langle \rangle\}, \emptyset)\}$ 
  - A single interaction obligation where only the empty trace  $\langle \rangle$  is positive and the set of negative traces is empty



# Informal illustration of MakeAppointment





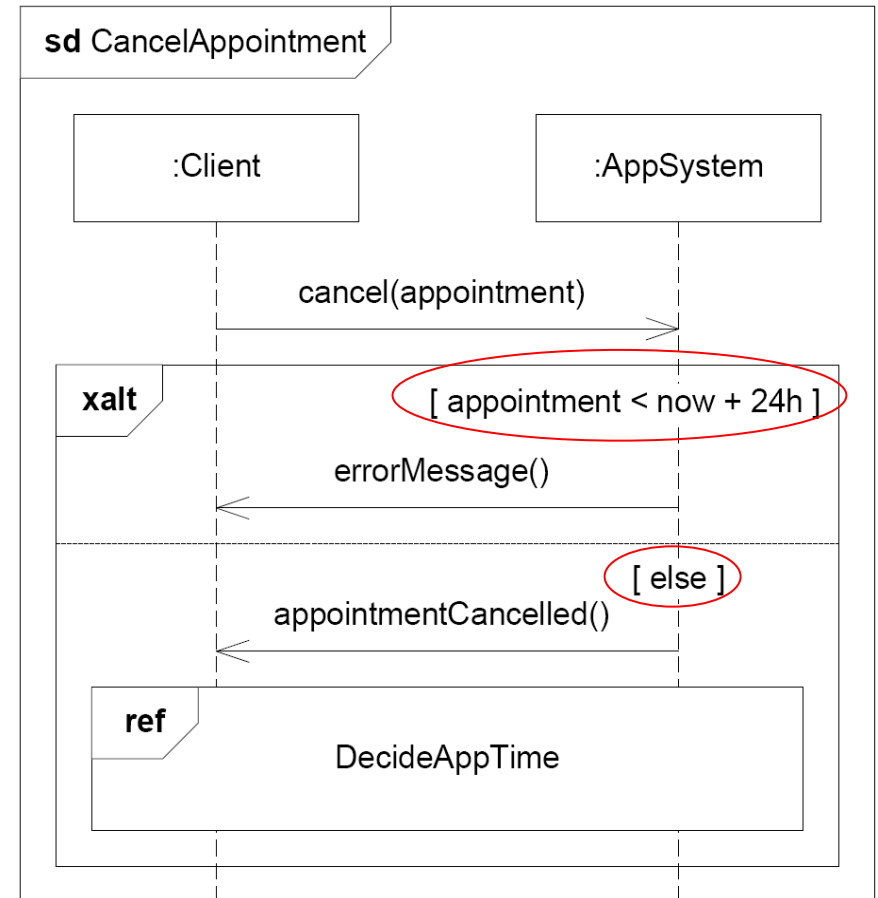
## The pragmatics of alt vs xalt

- Use alt to specify alternatives that represent similar traces, i.e. to model
  - underspecification
- Use xalt to specify alternatives that must all be present in an implementation, i.e. to model
  - inherent nondeterminism, as in the specification of a coin toss
  - alternative traces due to different inputs that the system must be able to handle (as in DecideAppTime)
  - alternative traces where the conditions for these being positive are abstracted away (as in CancelAppointment on slide 12)



## Guards (1)

- Guards may be used to express conditions for choosing between alternatives
- Here: an error message is sent if the client tries to cancel an appointment less than 24 hours before it is due



## Guards (2)

- Semantically, a guard is represented by a special check-event
- The check-event ensures that for each operand to alt/xalt, its traces (including the check-event) become negative if the guard is false
  - otherwise they remain positive or negative as before
- Therefore the guard must be true in all possible situations in which the specified traces are positive
- An alt/xalt operand without a guard can be interpreted as having the guard  $\top$  (always true)
- More than one guard may be true at a time



# The pragmatics of guards

- Use guards in an alt/xalt construct to constrain the situations in which the different alternatives are positive
- Always make sure that for each alternative, the guard is sufficiently general to capture all possible situations in which the described traces are positive
- In an alt-construct, make sure that the guards are exhaustive. If doing nothing is valid, specify this by using the empty diagram, skip
  - This is in order to avoid confusion with the UML standard



# Negative behavior

From 0 to 4 iterations (with seq between)

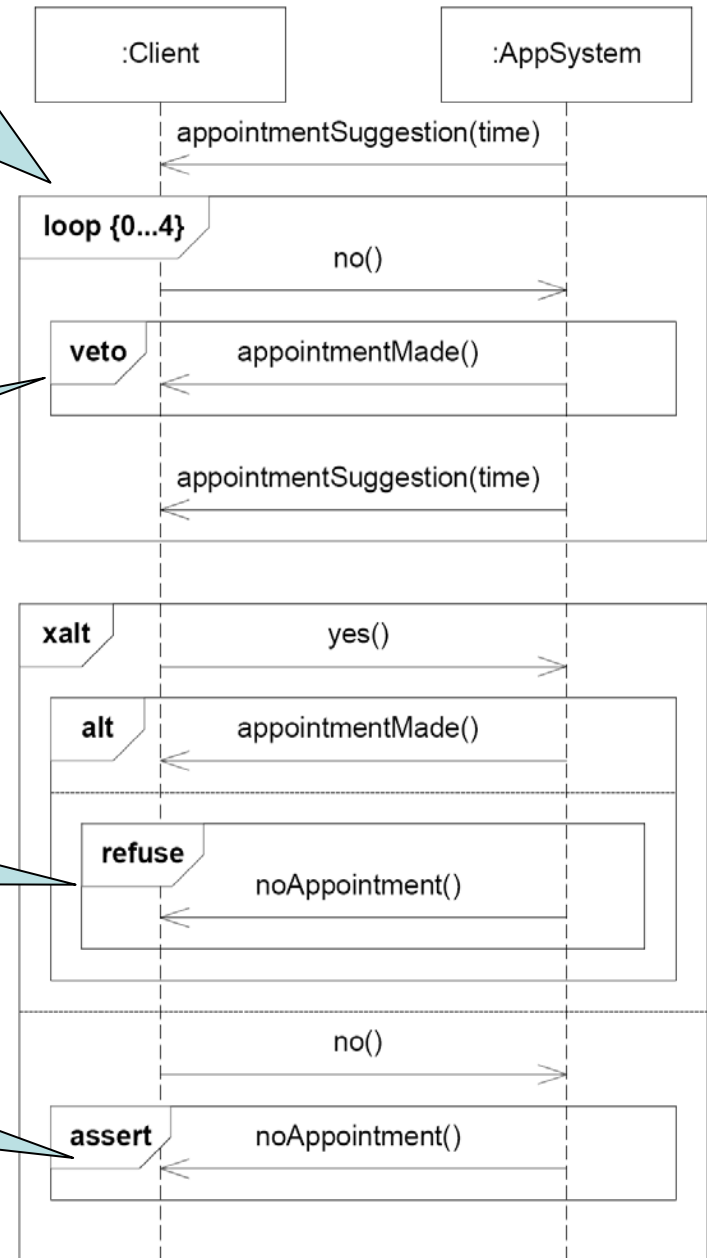
- veto, refuse and assert introduce negative behavior

appointmentMade() may not occur here (veto=neg)

noAppointment() may not occur instead of appointmentMade() here

noAppointment () is the only message that may occur here

sd DecideAppTime



## refuse

- $[[\text{refuse } d]] \stackrel{\text{def}}{=} \{(\emptyset, p \cup n) \mid (p, n) \in [[d]]\}$
- All interaction obligations in  $[[\text{refuse } d]]$  have empty positive sets
- This means that all interaction obligations in  $[[d_1 \text{ seq } (\text{refuse } d_2)]]$  have empty positive sets
  - and the same applies to  $[[(\text{refuse } d_1) \text{ seq } d_2]]$



## veto

- $[[\text{veto } d]] \stackrel{\text{def}}{=} [[\text{skip alt (refuse } d)]]$
- ... which means that
$$[[\text{veto } d]] = \{(\{\langle \rangle\}, p \cup n) \mid (p \cup n) \in [[d]]\}$$
- veto and neg have identical semantics

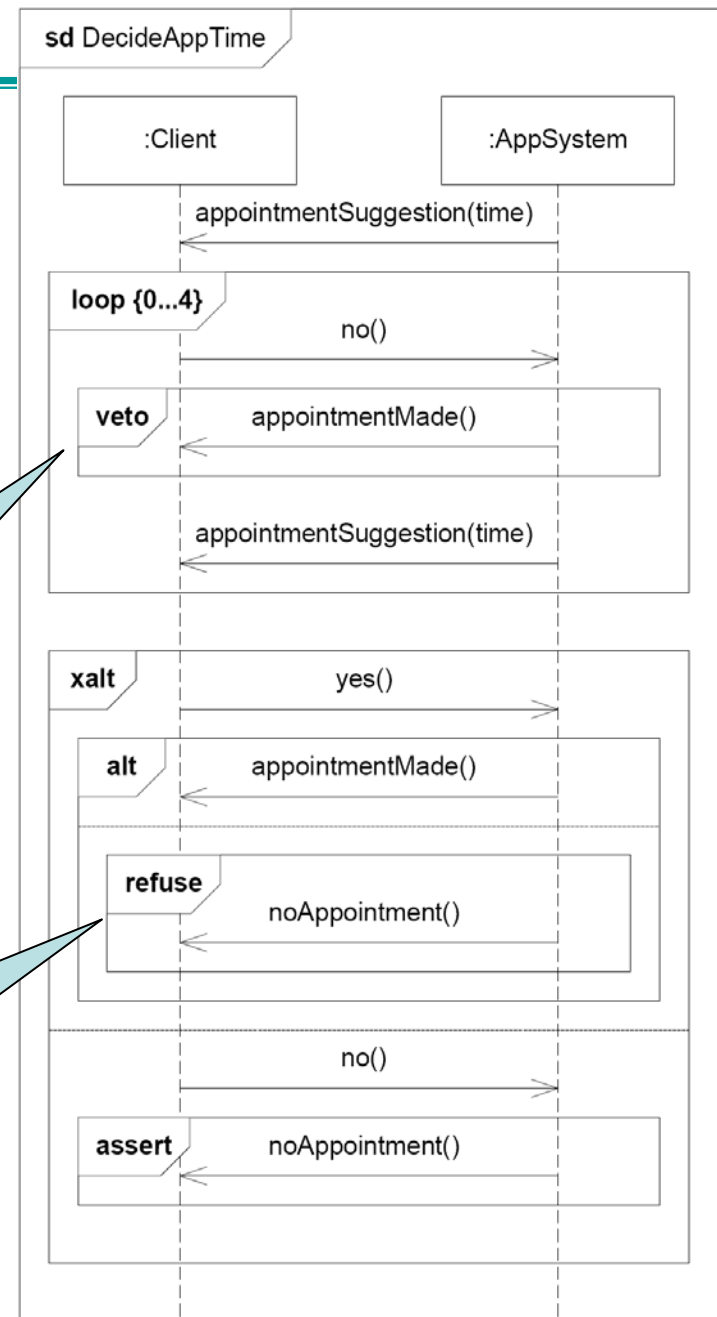


## veto or refuse?

- Should doing nothing be possible in the otherwise negative situation?
  - If yes, use veto
  - If no, use refuse

It is OK to do nothing between no() and appointmentSuggestion(time)

It is not OK to do nothing after yes()





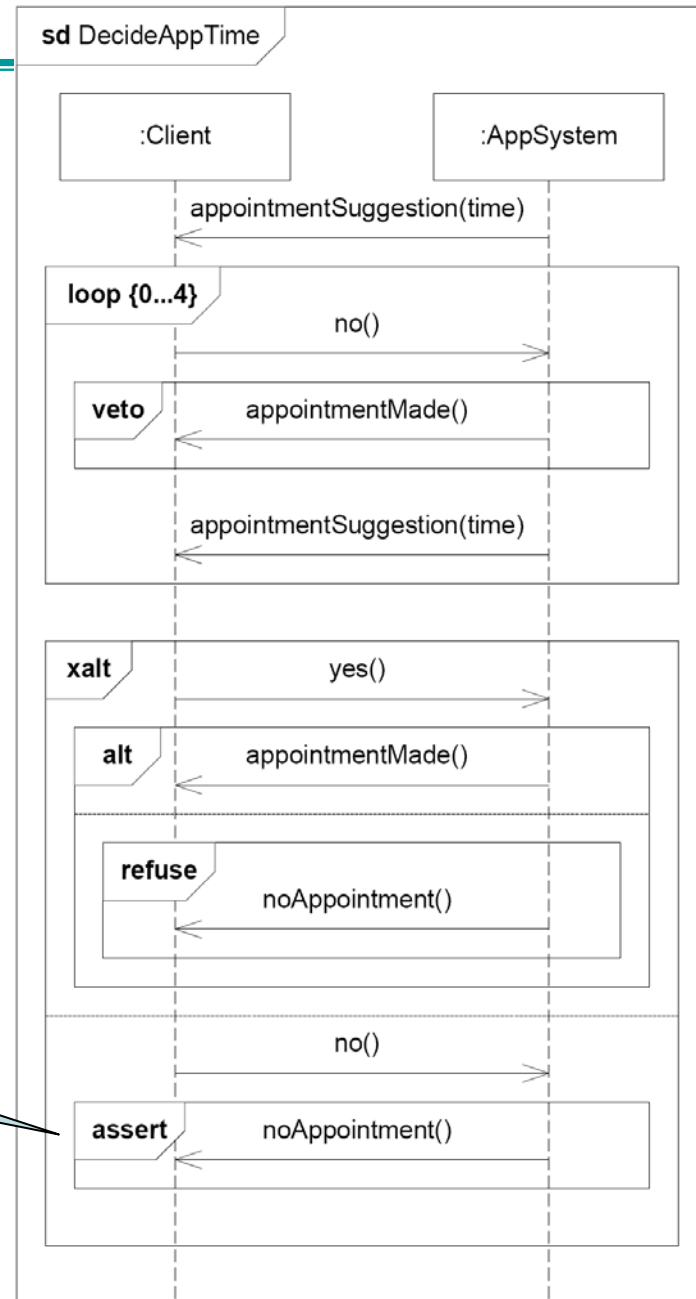
## assert (1)

- By using assert, all inconclusive traces are redefined as negative
- This ensures that for each interaction obligation, at least one of its positive traces will be implemented in the final implementation
- $[[\text{assert } d]] \stackrel{\text{def}}{=} \{(p, n \cup (\mathcal{H} \setminus p)) \mid (p, n) \in [[d]]\}$



# assert (2)

Sending noAppointment() is the only acceptable response to the no() message at this point



# The pragmatics of negation

- To effectively constrain the implementation, the specification should include a reasonable set of negative traces
- Use `refuse` when specifying that one of the alternatives in an `alt`-construct represents negative traces
- Use `veto` when the empty trace (i.e. doing nothing) should be positive, as when specifying a negative message in an otherwise positive scenario
- Use `assert` on an interaction fragment when all positive traces for that fragment have been described

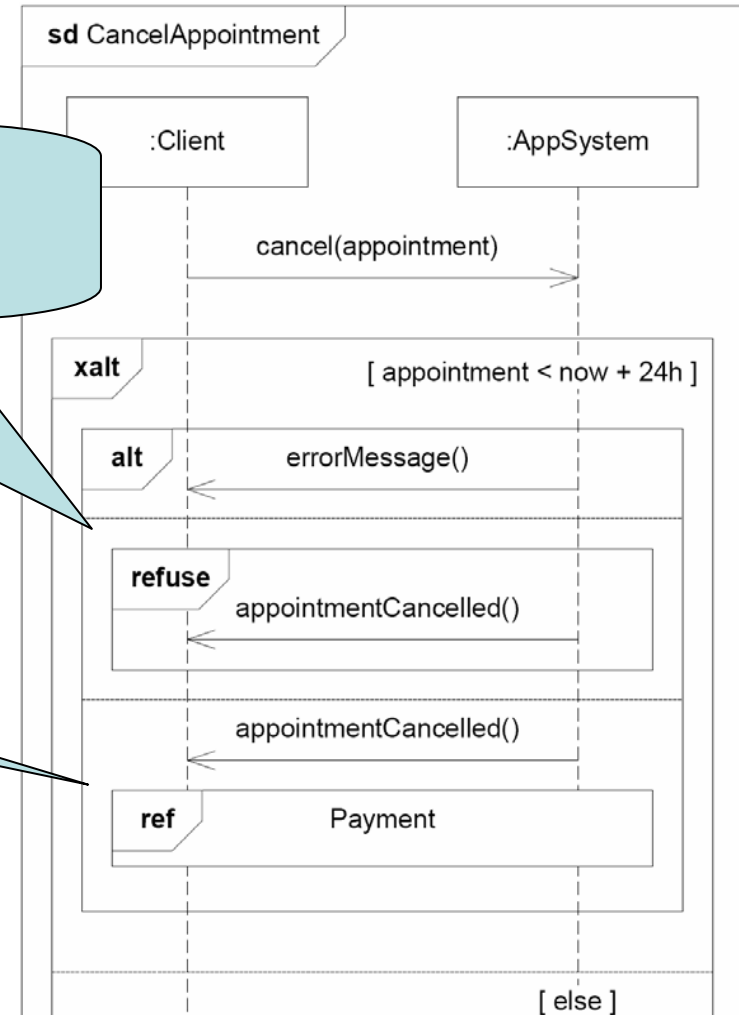


# The use of seq

cancel(appointment) followed by  
appointmentCancelled() followed by  
nothing is negative

cancel(appointment) followed by  
appointmentCancelled()  
followed by the positive traces  
of Payment is positive

- A trace is not necessarily negative even if a prefix of it is negative
- The total trace must be considered when categorizing it as positive, negative or inconclusive



# The pragmatics of weak sequencing

- Be aware that by weak sequencing
  - a positive sub-trace followed by a positive sub-trace is positive
  - a positive sub-trace followed by a negative sub-trace is negative
  - a negative sub-trace followed by a positive sub-trace is negative
  - a negative sub-trace followed by a negative sub-trace is negative
  - the remaining trace combinations are inconclusive

- Remember the definition:

$$(p_1, n_1) \succsim (p_2, n_2) \stackrel{\text{def}}{=} (p_1 \succsim p_2, (n_1 \succsim p_2) \cup (n_1 \succsim n_2) \cup (p_1 \succsim n_2))$$





# The pragmatics of refining interactions



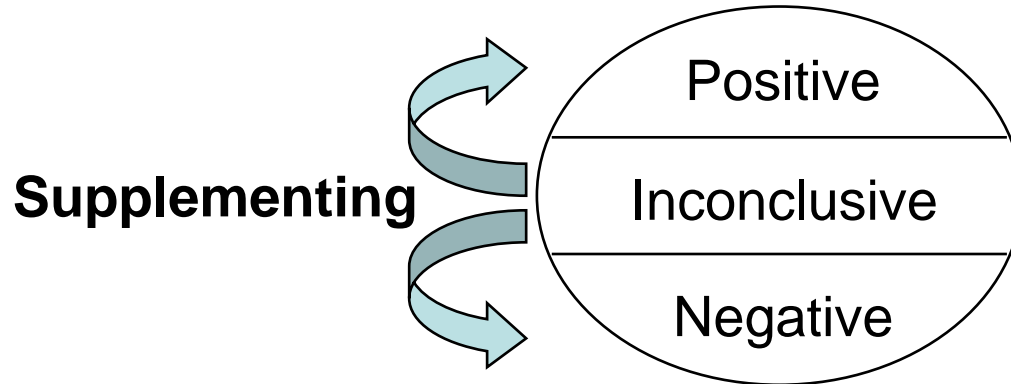
## The use of supplementing

- Inconclusive trace are recategorized as either positive or negative (for an interaction obligation)
- New situations are considered
  - adding fault tolerance
  - new user requirements
  - ...
- Typically used in early phases



# Supplementing of interaction obligations

- $(p, n) \rightsquigarrow_s (p', n') \stackrel{\text{def}}{=} p \subseteq p' \wedge n \subseteq n'$

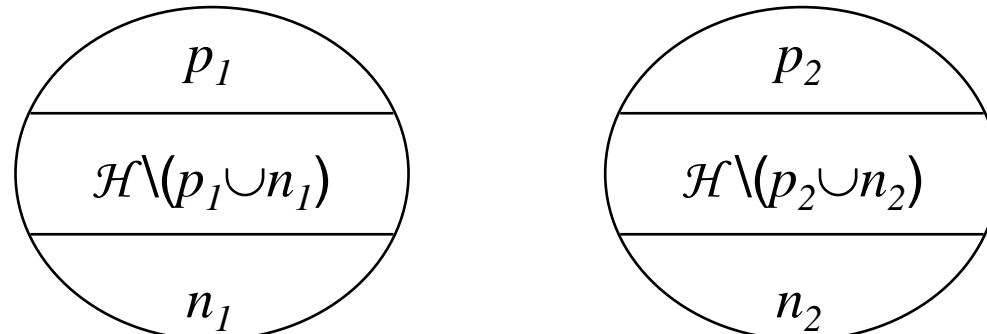




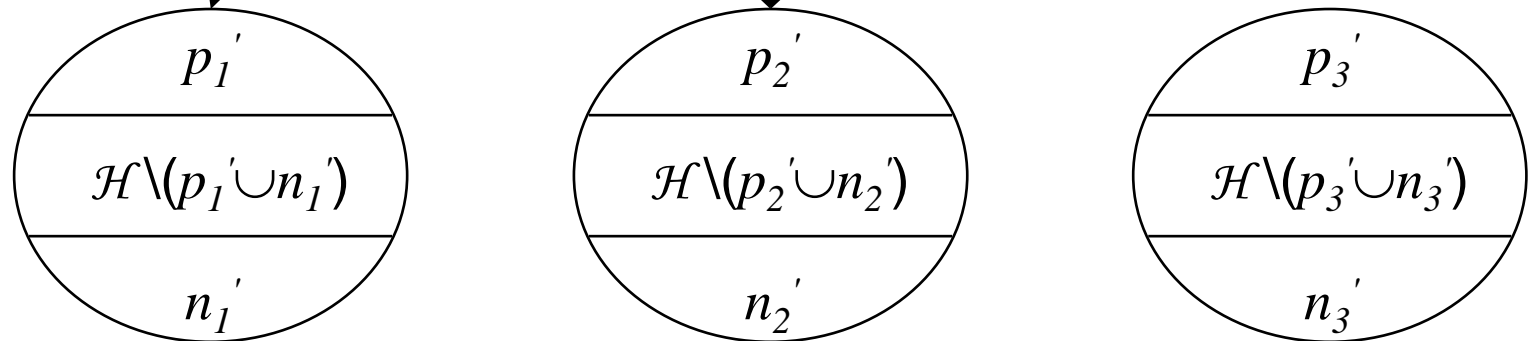
# Supplementing of specifications

- $d \rightsquigarrow_s d' \stackrel{\text{def}}{=} \forall o \in [[d]]: \exists o' \in [[d']]: o \rightsquigarrow_s o'$

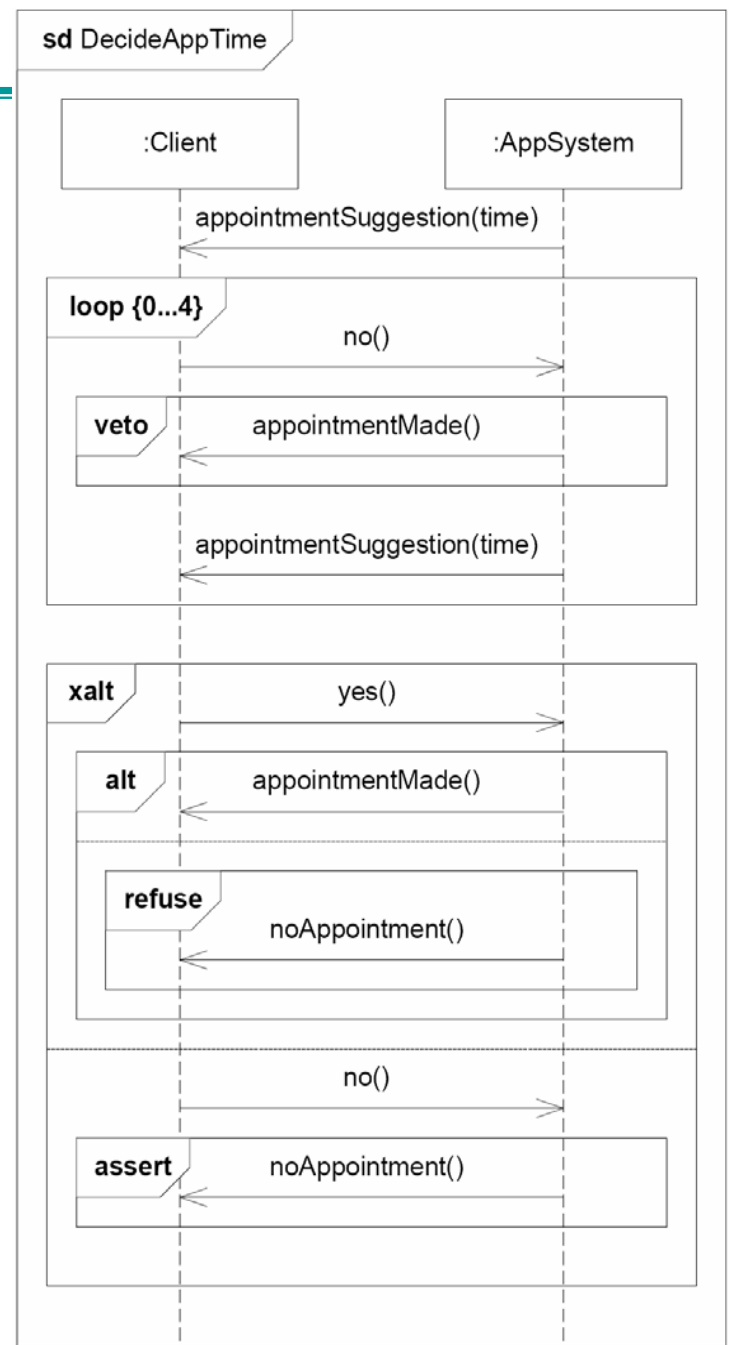
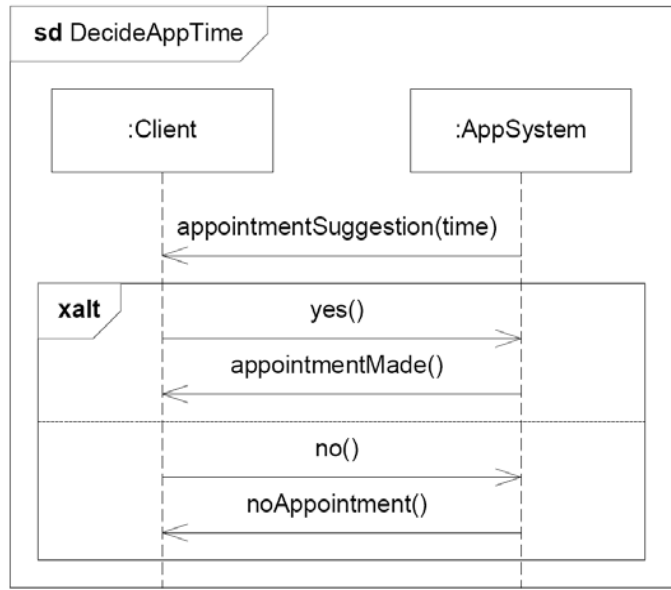
$[[d]]$ :



$[[d']]$ :



# Example of supplementing



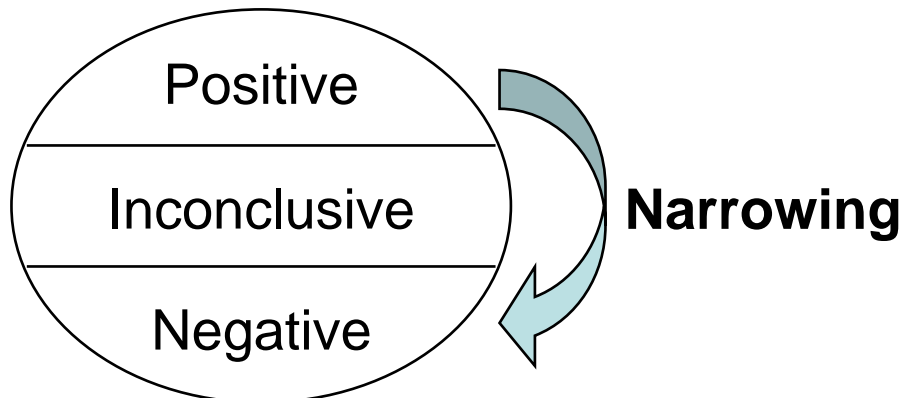
# The pragmatics of supplementing

- Use supplementing to add positive or negative traces to the specification
- When supplementing, all of the original positive traces must remain positive, and all of the original negative traces must remain negative
- Do not use supplementing on the operand of an assert
  - no traces are inconclusive in the operand

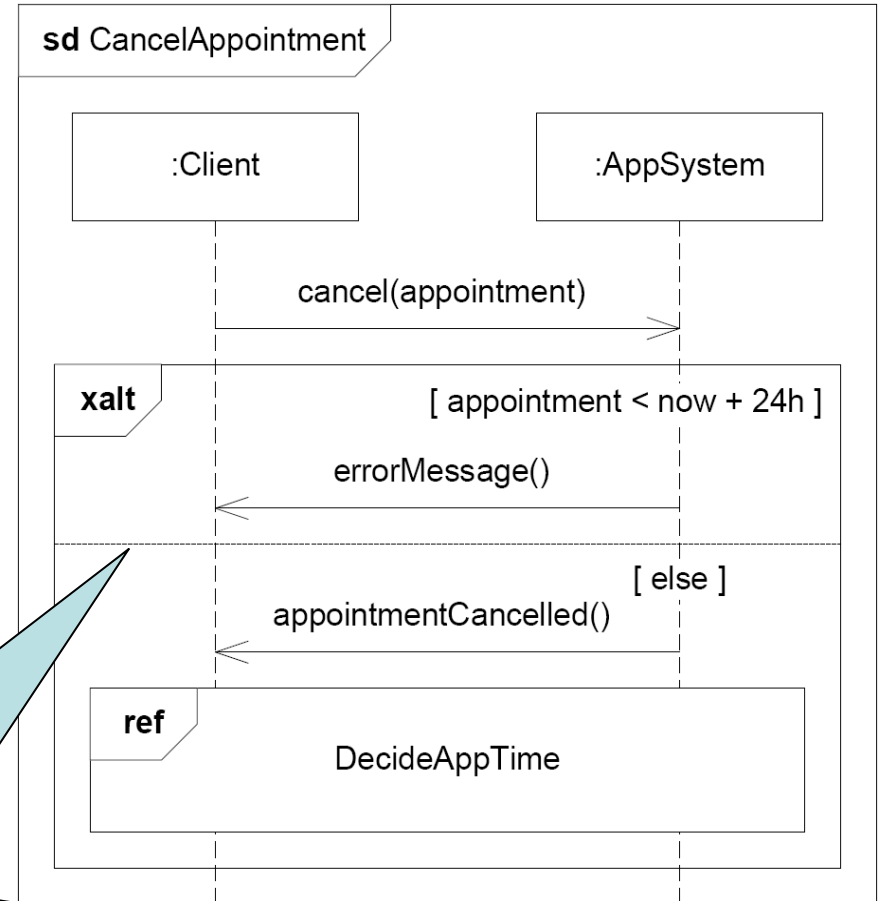
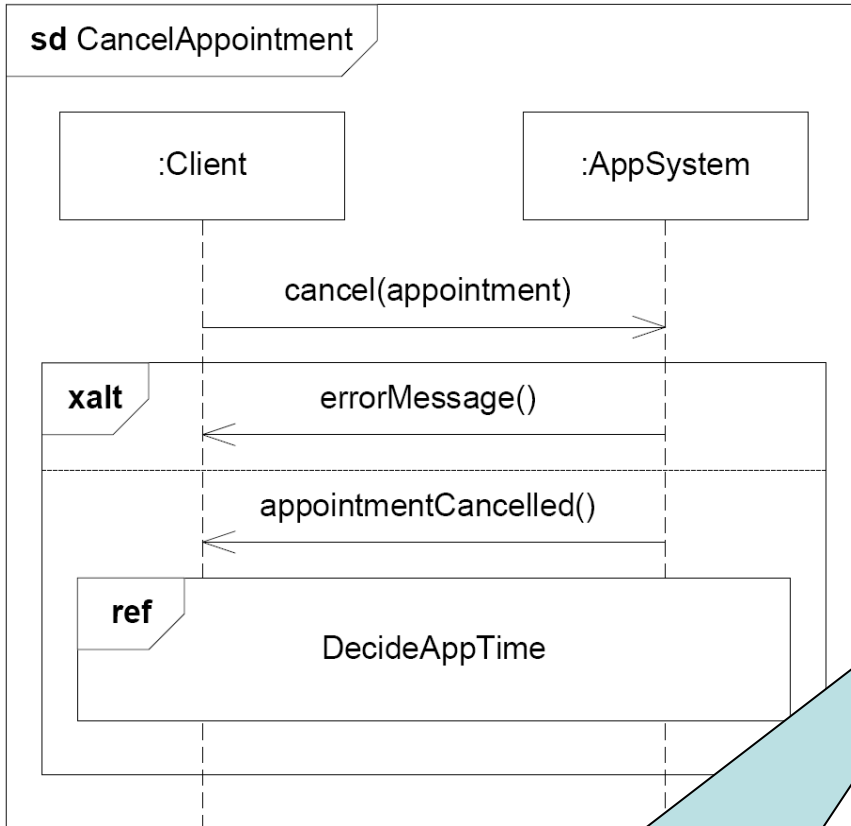


# Narrowing

- Reduce underspecification by redefining positive traces as negative
- For example adding guards, or replacing a guard with a stronger one
  - traces where the guard is false become negative
- $(p, n) \rightsquigarrow_n (p', n') \stackrel{\text{def}}{=} p' \subseteq p \wedge n' = n \cup (p \setminus p')$
- $d \rightsquigarrow_n d' \stackrel{\text{def}}{=} \forall o \in [[d]]: \exists o' \in [[d']]: o \rightsquigarrow_n o'$



# Example of narrowing



For each operand, traces where the guard is false become negative



# The pragmatics of narrowing

- Use narrowing to remove underspecification by redefining positive traces as negative
- In cases of narrowing, all of the original negative traces must remain negative
- Guards may be added to an alt-construct as a legal narrowing step
- Guards may be added to an xalt-construct as a legal narrowing step
- Guards may be narrowed, i.e. the refined condition must imply the original one



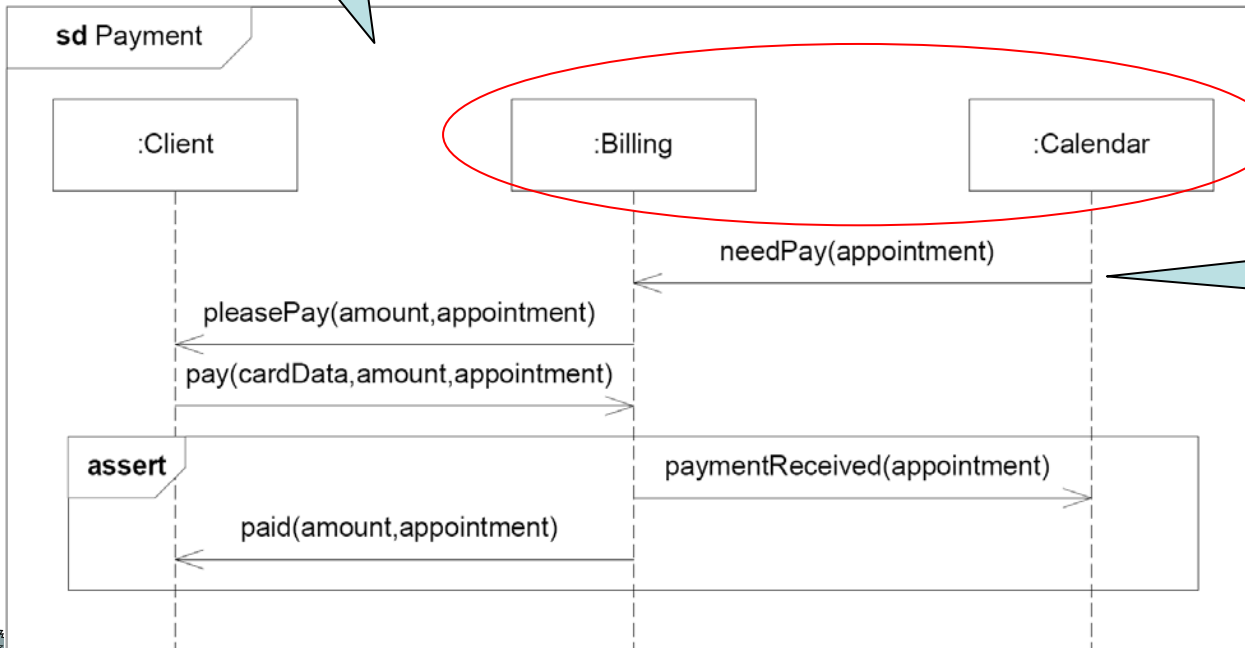
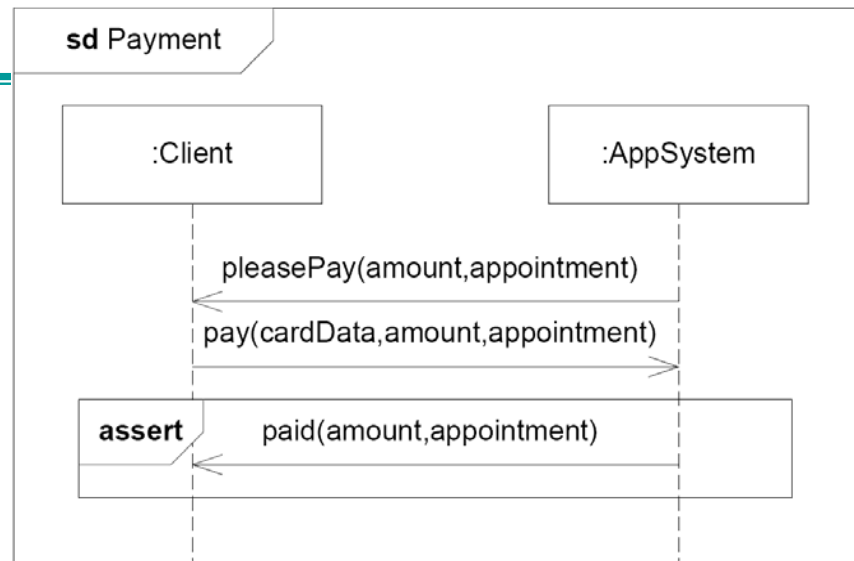
# The use of detailing

- Reducing the level of abstraction by structural decomposition
  - One or more lifelines are decomposed
- The positive and the negative traces are the same, except that
  - internal communication is hidden at the abstract level
  - events occurring on a composed lifeline at the abstract level occur instead on one of the component lifelines



# Example of detailing

Note that a UML principle has been broken here.



Components of AppSystem

Internal communication





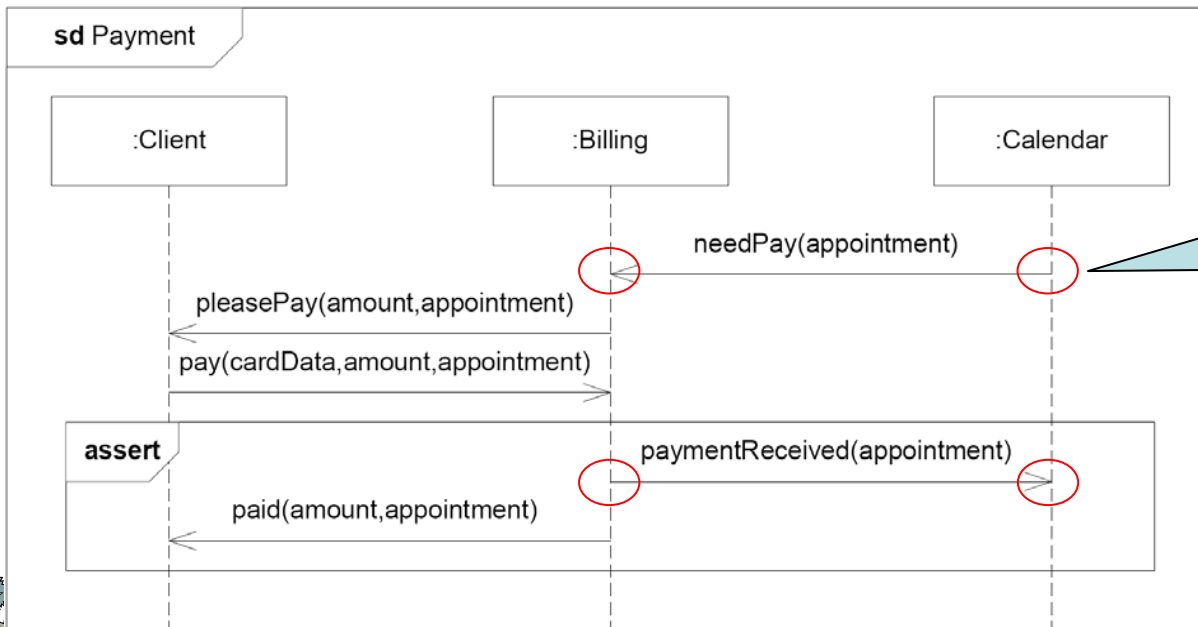
## Detailing

- $L$  is a mapping that defines the translation from concrete to abstract lifelines
  - $L = \{\text{Client} \mapsto \text{Client}, \text{Billing} \mapsto \text{AppSystem}, \text{Calendar} \mapsto \text{AppSystem}\}$
  - This implies that Billing and Calendar are components of AppSystem
- $\text{subst}(t, L)$  is a function that substitutes lifelines in the trace  $t$  according to  $L$
- $E$  is a set of abstract events
  - Necessary to allow messages that an abstract lifeline sends to itself to be visible in the abstract diagram
- $\text{abstr}(s, L, E)$  is an abstraction function that transforms a set of concrete traces  $s$  into a set of abstract traces
  - by removing all internal events (w.r.t.  $L$ ) that are not in  $E$



# Formal definition of detailing

- $(p, n) \rightsquigarrow_c^{L, E} (p', n') \stackrel{\text{def}}{=} p = \text{abstr}(p', L, E) \wedge n = \text{abstr}(n', L, E)$
- $d \rightsquigarrow_c^{L, E} d' \stackrel{\text{def}}{=} \forall o \in [[d]]: \exists o' \in [[d']]: o \rightsquigarrow_c^{L, E} o'$



Internal events not visible at the abstract level



# The pragmatics of detailing

- Use detailing to increase the level of granularity of the specification by decomposing lifelines
- When detailing, document the decomposition by creating a mapping  $L$  from the concrete to the abstract lifelines
- When detailing, make sure that the refined traces are equal to the original ones when abstracting away internal communication and taking the lifeline mapping into account



# The use of general refinement

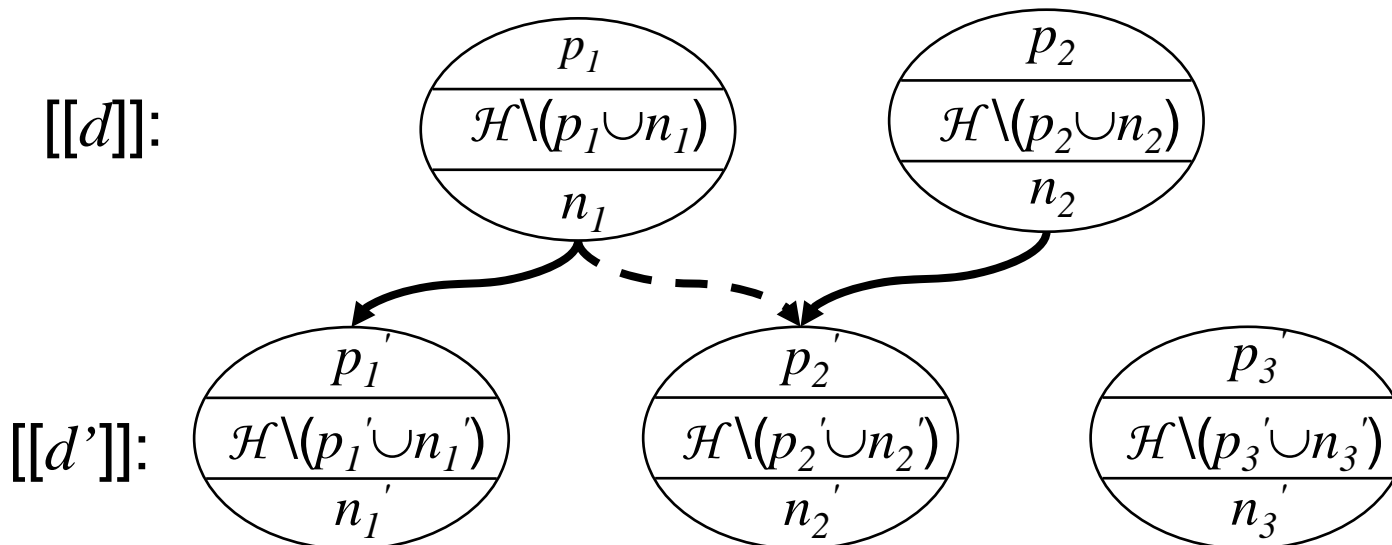
- A combination of supplementing, narrowing and detailing
  - (not necessarily all three)
- Allows all positive traces to become negative, while previously inconclusive traces become positive
- To ensure that a trace *must* be present in the final implementation we need an interaction obligation where all other traces are negative





## General refinement (of sets of interaction obligations)

- $d \rightsquigarrow d' \stackrel{\text{def}}{=} \forall o \in [[d]]: \exists o' \in [[d']]: o \rightsquigarrow o'$
- $d'$  is a general refinement of  $d$  if
  - for every interaction obligation  $o$  in  $[[d]]$  there is at least one interaction obligation  $o'$  in  $[[d']]$  such that  $o'$  is a general refinement of  $o$
- New interaction obligations may also be added
  - that do not refine any obligation at the abstract level



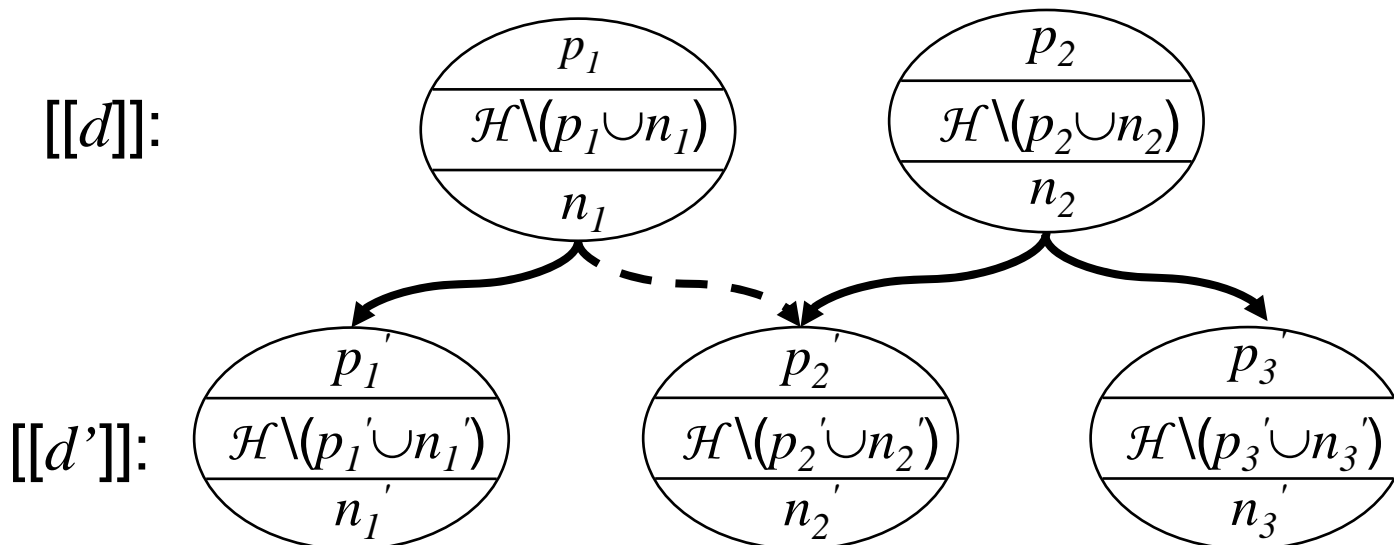
# The pragmatics of general refinement

- Use general refinement to perform a combination of supplementing, narrowing and detailing in a single step
- To define that a particular trace *must* be present in an implementation use `xalt` and `assert` to characterize an obligation with this trace as the only positive one and all other traces as negative



# Limited refinement

- Limits the possibility of adding new interaction obligations
- Typically used at a later stage
- $d'$  is a limited refinement of  $d$  if
  - $d'$  is a general refinement of  $d$ , and
  - every interaction obligation in  $[[d']]$  is a general refinement of at least one interaction obligation in  $[[d]]$





# The pragmatics of limited refinement

- Use assert and switch to limited refinement in order to avoid fundamentally new traces being added to the specification
- To specify globally negative traces, define these as negative in all operands of xalt, and switch to limited refinement



# Compositionality

- A refinement operator  $\rightsquigarrow$  is compositional if it is
  - reflexive:  $d \rightsquigarrow d$
  - transitive:  $d \rightsquigarrow d' \wedge d' \rightsquigarrow d'' \Rightarrow d \rightsquigarrow d''$
  - the operators refuse, veto, alt, xalt and seq are monotonic w.r.t.  $\rightsquigarrow$  :
    - $d \rightsquigarrow d' \Rightarrow \text{refuse } d \rightsquigarrow \text{refuse } d'$
    - $d \rightsquigarrow d' \Rightarrow \text{veto } d \rightsquigarrow \text{veto } d'$
    - $d_1 \rightsquigarrow d_1' \wedge d_2 \rightsquigarrow d_2' \Rightarrow d_1 \text{ alt } d_2 \rightsquigarrow d_1' \text{ alt } d_2'$
    - $d_1 \rightsquigarrow d_1' \wedge d_2 \rightsquigarrow d_2' \Rightarrow d_1 \text{ xalt } d_2 \rightsquigarrow d_1' \text{ xalt } d_2'$
    - $d_1 \rightsquigarrow d_1' \wedge d_2 \rightsquigarrow d_2' \Rightarrow d_1 \text{ seq } d_2 \rightsquigarrow d_1' \text{ seq } d_2'$
- Transitivity allows stepwise development
- Monotonicity allow different parts of the specification to be refined separately
- Supplementing, narrowing, detailing, general refinement and limited refinement are all compositional 😊

