

**FIL1006 - Introduction to logic**  
**Spring 2016**  
**Thursday 2 June at 09:00 (4 hours)**

**No aids permitted**

**The exam assignment consists of 2 pages in total**

**The exam consists of nine assignments with a top score of 100 points. Provide answers to as many assignments as you manage. Remember that partly correct answers also are rewarded with points.**

**Assignment 1 (14 points)**

'A valid argument is a good argument'. Discuss what is right or wrong about this claim.

(This is a question for discussion. A good answer should be a short essay. But be careful to not spend too much time on this problem.)

**Assignment 2 (16 points)**

This assignment asks for some definitions and short explanations. It suffices to write two to three sentences about each of the notions to be defined.

- (a) What is it for a schema to be *unsatisfiable*?
- (b) What is the definition of one or more statements *implying* another?
- (c) Provide a brief explanation of the distinction between *numerical identity* and *qualitative identity*.
- (d) What is it for a statement to be a *truth-function*? Illustrate by using one or two examples.

**Assignment 3 (8 points)**

Show, by using truth-tables, that the following schemata are valid:

- (a)  $(\neg p \supset q) \supset p \vee q$
- (b)  $(p \supset \neg(q \vee r)) \equiv (\neg p \vee \neg q, \neg r)$

**Assignment 4 (12 points)**

Formalize the following statements using truth-functional logic:

- (a) Petter gets angry if Linn screams or makes a mess.
- (b) The reporter does not pose difficult questions unless the person interviewed smiles or laughs.

- (c) Either Askeladden gets the princess and half of the kingdom, or neither Per nor Pål receives any award.

**Assignment 5 (10 points)**

Formalize the following argument and show by using deduction for truth-functional logic that it is valid.

Premise 1	The bird expects offspring if it builds a nest or occupies a nesting box
Premise 2	The bird collects twigs or builds a nest
Premise 3	The bird does not collect twigs
Conclusion	
	The bird expects offspring

**Assignment 6 (10 points)**

Use truth-functional logic to show that:

- (a)  $p \vee \neg p$  is valid.  
 (b)  $(p, q) \supset (r \supset s)$  implies  $(p \supset q) \supset ((p, r) \supset s)$ .

**Assignment 7 (8 points)**

Formalize the following statements using predicate logic. (You may have to use Russell's analysis of definite descriptions.)

- (a) No author respects any journalists who respect themselves.  
 (b) The king of Norway is both down to earth and popular.

**Assignment 8 (8 points)**

Show, by using natural deduction, that (a) implies (b). Show, by using a counterexample, that (b) does not imply (a).

- (a)  $\exists x(Fx.Gx)$   
 (b)  $\exists xFx.\exists Gx$

**Assignment 9 (14 points)**

Formalize the following two arguments. For each argument, if it is valid, show this by using natural deduction, and, if it is invalid, show this by using a counterexample.

Premise 1	Some philosophers have read every book
(a) Premise 2	Some books are read by all enthusiasts
Conclusion	
	Some philosophers are enthusiasts
Premise 1	Some philosophers have read every book
(b) Premise 2	Some books are read only by enthusiasts
Conclusion	
	Some philosophers are enthusiasts