SPR4106 – Syntax and semantics in formal terms

Lecture II: Functional structure

12 February 2015

What's in an f-structure?

- The functional structure is where LFG models grammatical functions
- Grammatical functions do not correspond one to one to either c-structure or semantics (thematic roles), so they need a separate representation
- The functional structure is modelled in an attribute-value matrix, i.e. a set of attributes with certain values
- The attributes are either grammatical functions (subject, object etc.), or syntactically relevant features such as *tense*, *number*, *gender* etc.
- Three types of values:
 - linguistic "atoms" such as plural, singular, present etc.
 - new. embedded feature structures
 - semantic symbols, "predicators"

Sample f-structure

```
PRED 'SEE <SUBJ, OBJ>'
TENSE PRESENT

SUBJ PRED 'PETER'
NUMBER SG

OBJ PRED 'MARY'
NUMBER SG
```

- The value of PRED is always a semantic symbol
- Syntactic features such as TENSE and NUMBER take atomic values such as PRESENT
- The values of grammatical functions are feature structures

Features

- There is a "received set" of grammatical functions in LFG, but no corresponding received set of features that are not grammatical functions
- The usual suspects are traditional features like TENSE, NUMBER, GENDER, DEF; there are also less typical features like PCASE
- Will vary with the morphological resources of the language, but should *not* be equated with morphological features
 - Morphological features are only present in the f-structure if they are syntactically relevant
 - Words can "speak about their environment": contribute features to other f-structures than their own (agreement)

Semantic symbols

Semantically contentful words are represented with semantic symbols

```
saw 'SEE <SUBJ, OBJ> '
John 'JOHN'
him 'PRO'
rains 'RAIN <> SUBJ'
```

- the semantic symbol includes a representation of the meaning (conventionally in English)
- words that require arguments also list these
- semantic arguments are listed inside angular brackets, non-thematic (purely syntactic) arguments outside
- unique to each instance!

Argument functions

```
\begin{array}{lll} {\rm SUBJ} & {\rm subject} \\ {\rm OBJ} & {\rm object} \\ {\rm OBJ2} & {\rm second\ object\ (NB:\ sometimes\ called\ OBJ_{\theta})} \\ {\rm OBL_{\theta}} & {\rm oblique} \\ {\rm COMP} & {\rm complement\ clause} \\ {\rm POSS} & ({\rm certain})\ {\rm arguments\ of\ nouns} \end{array}
```

Non-argument functions

FOCUS focus
TOPIC topic
ADJ adjunct

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Classifying grammatical functions

- In stating generalizations it is often useful to refer to certain classifications of GFs
- \bullet $\mathrm{SUBJ},~\mathrm{OBJ}$ and OBJ_2 are collectively known as core functions or term functions
- Many grammatical process are sensitive to the functional hierarchy
 - SUBJ > OBJ > OBJ₂ > OBL θ
- TOPIC, FOCUS and sometimes SUBJ are referred to as grammaticized discourse functions or overlay functions

Subcategorization

- Our VP rule \to V DP DP PP* (IP|CP) would seem to allow the following sentences (given that all nodes are optional)
- (1) I donated a book to the library.
- (2) *I donated to the library.
- (3) *I donated the university a book to the library.
 - The c-structures are all well-formed. Instead, the ungrammaticality is accounted for at f-structure

(In)completeness

$$\begin{bmatrix} \text{PRED} & \text{`DONATE} < \text{SUBJ}, \text{ OBL}_{goal} \text{ OBJ} > \text{`} \\ \text{SUBJ} & \begin{bmatrix} \text{``I''} \end{bmatrix} \\ \\ \text{OBL}_{goal} & \begin{bmatrix} \text{PCASE} & \text{OBL}_{goal} \\ \text{OBJ} & \begin{bmatrix} \text{``THE} \text{ LIBRARY''} \end{bmatrix} \end{bmatrix}$$

- (4) *I donated to the library.
 - All argument functions specified in the value of the PRED feature must be present in the local f-structure

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(In)coherence

```
PRED 'DONATE <SUBJ, OBJ, OBLgoal OBJ>'
SUBJ ["I"]
OBJ ["A BOOK"]
OBJ2 ["THE UNIVERSITY"]
OBLgoal OBJ ["THE LIBRARY"]
```

- (5) *I donated the university a book to the library.
 - All argument functions in an f-structure must be selected by their local PRED

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Grammaticality

```
PRED 'DONATE <SUBJ, OBJ, OBL<sub>goal</sub> OBJ>'
SUBJ ["I"]
OBJ ["A BOOK"]
OBL<sub>goal</sub> [PCASE OBL<sub>goal</sub>
OBJ ["THE LIBRARY"]]
```

Expletives

- Some lexical items e.g. expletives (there, it) and idiom chunks (keep the tabs on) are meaningless; they do not provide a PRED-value
- Some predicates, e.g. rain, require purely syntactic (non-thematic) arguments
- We modify completeness and coherence to account for these
- Completeness All argument functions specified in the value of the PRED feature must be present in the local f-structure. All functions that receive a thematic role must have a PRED feature.
 - Coherence All argument functions in an f-structure must be selected by their local PRED. Any argument function that has its own PRED feature must be assigned a thematic role

What goes wrong here?

(6) *We rain

```
\begin{bmatrix} \text{PRED} & \text{`RAIN} < > \text{SUBJ'} \\ \\ \text{SUBJ} & \begin{bmatrix} \text{PRED} & \text{`PRO'} \\ \text{NUMBER} & \text{PLURAL} \\ \text{PERSON} & 1 \end{bmatrix} \end{bmatrix}
```

Incoherent!

What goes wrong here?

(7) *I donated there to the library

```
PRED
          'DONATE <SUBJ, OBJ, OBLgoal OBJ>'
           PRED 'PRO'
PERSON 1
NUMBER PL
SUBJ
           PERSON 3
OBJ
           PCASE
                     OBL<sub>goal</sub>
```

Extended coherence

- What about discourse functions and adjuncts?
- There something wrong with these:
 - *It that came rained.
 - *The man who I saw the woman crossed the street.
- Intuitively, meaningless items cannot be modified, and discourse functions (who) must not "dangle"

Extended coherence

All functions in an f-structure must be incorporated into the semantics. Argument functions are subject to the Coherence condition. Discourse functions must be identified with arguments or adjuncts. Adjuncts must be in f-structures containing PREDs.

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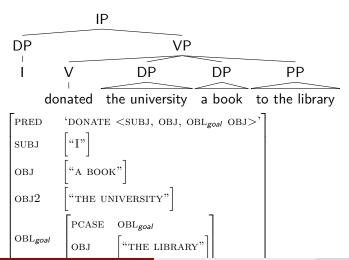
Uniqueness

- Every attribute has a single value.
- This falls out of the formal setup of LFG
- So we disallow f-structures with, say, two different tense values or two different objects
- What about adjuncts?

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Relating c- and f-structures

(8) *I donated the university a book to the library.



Relating c- and f-structure

- The c-structure is well-formed by the phrase structure rules and the first f-structure is well-formed by the principles we just saw, and yet something is clearly wrong.
- Informally, the c-structure and the f-structure do not *correspond* in the required way
- The second, incoherent f-structure is intuitively the correct correspondent to the c-structure
- Intuitively, the f-structure that corresponds to the c-structure is the one that contains all the information in the c-structure (and nothing more)
- Technically, we will say that a c-structure and an f-structure correspond iff the f-structure is the minimal solution to the f-description offered by the c-structure

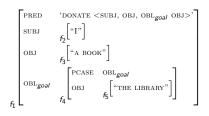
F-structures as functions

$$\begin{bmatrix} \text{PRED} & \text{`DONATE} < \text{SUBJ}, \text{ OBL}_{goal} \text{ OBJ} > \text{`} \\ \text{SUBJ} & f_2 \begin{bmatrix} \text{``I''} \end{bmatrix} \\ \text{OBJ} & f_3 \begin{bmatrix} \text{``A BOOK''} \end{bmatrix} \\ \text{OBL}_{goal} & \begin{bmatrix} \text{PCASE} & \text{OBL}_{goal} \\ \text{OBJ} & f_5 \end{bmatrix} \\ \text{``THE LIBRARY''} \end{bmatrix} \end{bmatrix}$$

- $f_1(SUBJ) = f_2$, or in LFG notation $(f_1 SUBJ) = f_2$
- ullet (f₁ OBJ) = f₃, (f₁ OBL_{goal}) = f₄ , (f₄ OBJ) = f₅
- $(f_1 PRED) = 'donate < SUBJ, OBJ, OBL_{goal} OBJ > '$
- $(f_4 \text{ PCASE}) = OBL_{goal}$

F-descriptions

- ullet Equations such as $(f_1 \ {
 m SUBJ}) = f_2$ are known as functional descriptions
- We extracted f-descriptions from the f-structure, but it works the other way around too: we can build an f-structure from the f-description



•
$$(f_1 \text{ SUBJ}) = f_2$$

•
$$(f_1 \text{ OBJ}) = f_3$$

•
$$(f_1 \text{ OBL}_{goal}) = f_4$$

•
$$(f_4 \text{ OBJ}) = f_5$$

•
$$(f_1 \text{ PRED}) = \text{'donate} < \text{SUBJ},$$

OBJ, OBL_{goal} OBJ >'

•
$$(f_4 \text{ PCASE}) = OBL_{goal}$$

The f-structure contains all and only the information in the f-descriptions

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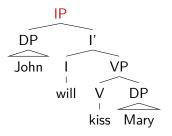
An aside: Identification

- We have several statements about f₁, e.g.
 - $(f_1 \text{ SUBJ}) = f_2$ • $(f_1 \text{ OBJ}) = f_3$
- We could also state this in the following way:
 - $(f_1 \text{ SUBJ}) = f_2$
 - $(f_5 \text{ OBJ}) = f_3$
 - $f_1 = f_5$
- The minimal solution remains the same, because the labels aren't essential

$$\begin{bmatrix} \text{SUBJ} & f_2 \\ \text{OBJ} & f_3 \end{bmatrix}$$

Unification

- Why would we want to do such a thing?
- Syntactic information can arise in different places in the c-structure
- We want to be able to unify this information in a single f-structure



- The IP node "knows" that John is the subject
- The VP node "knows" that Mary is the object
- The I node "knows" that the tense is future
- The V node "knows" that PRED is 'kiss <SUBJ, OBJ >'
- We want to unify this information

Unification II

- The unification of two f-structures A and B is the f-structure C such that it contains all attribute value-pairs of from A and B
- So we collect all features from both f-structures
- If there are duplicated attribute-value pairs, that is not a problem
- If there are conflicting values for the same attribute, the result will fail uniqueness and hence not be a licit f-structure

Unification III

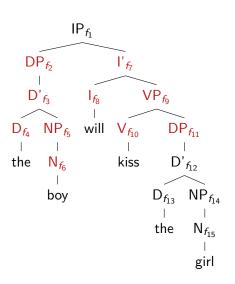
$$\begin{bmatrix} \text{NUMBER SG} \\ \text{PERSON 3} \end{bmatrix} + \begin{bmatrix} \text{GENDER FEM} \end{bmatrix} = \begin{bmatrix} \text{NUMBER SG} \\ \text{PERSON 3} \\ \text{GENDER FEM} \end{bmatrix}$$

$$\begin{bmatrix} \text{NUMBER SG} \\ \text{PERSON 3} \\ \text{GENDER FEM} \end{bmatrix} + \begin{bmatrix} \text{GENDER FEM} \end{bmatrix} = \begin{bmatrix} \text{NUMBER SG} \\ \text{PERSON 3} \\ \text{GENDER FEM} \end{bmatrix}$$

$$\begin{bmatrix} \text{NUMBER SG} \\ \text{PERSON 3} \\ \text{GENDER FEM} \end{bmatrix} + \begin{bmatrix} \text{GENDER MASC} \end{bmatrix} = \begin{bmatrix} \text{NUMBER SG} \\ \text{PERSON 3} \\ \text{GENDER FEM} \end{bmatrix}$$

$$\begin{bmatrix} \text{PERD 'RAIN < > SUBJ'} + \begin{bmatrix} \text{PRED 'RAIN < > SUBJ'} \end{bmatrix} = \begin{bmatrix} \text{PRED 'RAIN < > SUBJ'} \\ \text{PRED 'RAIN < > SUBJ'} \end{bmatrix}$$

Back to the c-/f-structure mapping



•
$$(f_1 \text{ SUBJ}) = f_2$$

•
$$f_2 = f_3$$

•
$$f_3 = f_4$$
, $(f_4 \text{ DEF}) = +$

•
$$f_3 = f_5$$

•
$$f_5 = f_6$$
, $(f_6 \text{ PRED}) = 'boy'$

•
$$f_1 = f_7$$

•
$$f_7 = f_8$$
, $(f_8 \text{ TENSE}) = fut$

•
$$f_7 = f_9$$

•
$$f_9 = f_{10}$$
, $(f_{10} \text{ PRED}) = \text{`kiss} < \text{SUBJ, OBJ} >'$

•
$$(f_9 \text{ OBJ}) = f_{11}$$

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The minimal solution

$$\begin{bmatrix} \text{PRED} & \text{`KISS} < \text{SUBJ}, \text{ OBJ} > \text{`} \\ \text{TENSE} & \text{FUT} \\ \text{SUBJ} & \begin{bmatrix} \text{PRED} & \text{`BOY'} \\ \text{DEF} & + \end{bmatrix} \\ \text{OBJ} & \begin{bmatrix} \text{PRED} & \text{`GIRL'} \\ \text{DEF} & + \end{bmatrix} \end{bmatrix} = f_2 \\ f_{1,7,8,9,10} \end{bmatrix}$$

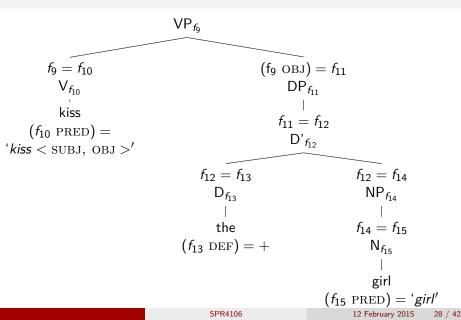
$$\begin{bmatrix} \text{PRED} & \text{`GIRL'} \\ \text{DEF} & + \end{bmatrix} = f_2 \\ f_3 = f_3 \\ f_3 = f_4, (f_4 \text{ DEF}) = + \\ f_3 = f_5 \\ f_5 = f_6, (f_6 \text{ PRED}) = \text{`boy'} \\ f_1 = f_7 \\ \end{bmatrix}$$

$$\begin{bmatrix} \text{PRED} & \text{`GIRL'} \\ \text{DEF} & + \end{bmatrix} = f_7 \\ \end{bmatrix} = f_7 = f_8, (f_8 \text{ TENSE}) = fut$$

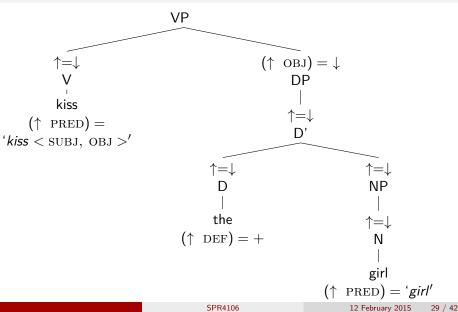
$$\begin{bmatrix} \text{PRED} & \text{`GIRL'} \\ \text{OBJ} & + \end{bmatrix} = f_{10}, (f_{10} \text{ PRED}) = \text{`kiss} < \\ \text{SUBJ}, \text{ OBJ} > \text{`} \\ \end{bmatrix}$$

$$\begin{bmatrix} \text{GPED} & \text{`BOY'} \\ \text{OBJ} & + \end{bmatrix} = f_{11}$$

The tree revisited



Introducing metavariables



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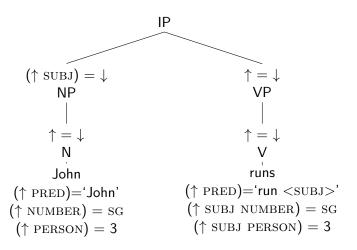
Designators

- ↓ and ↑ are metavariables referring to the f-structure of the current node and of the mother of the current node respectively
- We can form complex designators or "paths" through the f-structure
 - ($\uparrow SUBJ$) \equiv my mother's f-structure's subject
 - ($\uparrow \mathrm{COMP}\ \mathrm{SUBJ} \equiv my\ mother's\ f\text{-structure's\ complement's\ subject}$
 - $(\uparrow GF^*) \equiv$ an f-structure arbitrarily embedded under my mother's f-structure
- We can go the other way ("outside-in"):
 - (SUBJ \uparrow) \equiv the f-structure that my mother is the subject of
 - ((SUBJ \uparrow) OBJ) \equiv the object of the f-structure that my mother is the subject of

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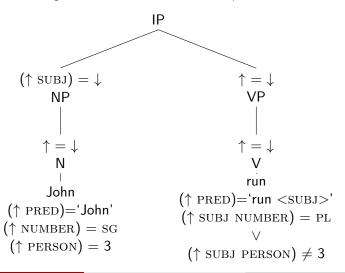
Agreement

• How can we capture agreement with lexical information?



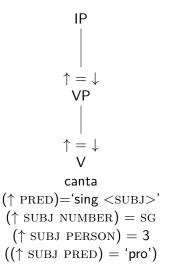
Agreement

• This one is ungrammatical - how can we capture that?



Prodrop

• This one is grammatical in Italian - how can we capture that?



Annotated phrase structure rules

Functional maximal projections

$$CP \rightarrow XP \qquad C'$$

$$(\uparrow \text{ FOCUS}) = \downarrow \qquad \uparrow = \downarrow$$

$$IP \rightarrow (DP|CP|PP) \qquad I'$$

$$(\uparrow \text{ SUBJ}) = \downarrow \qquad \uparrow = \downarrow$$

$$DP \rightarrow DP \qquad D'$$

$$(\uparrow \text{ POSS}) = \downarrow \qquad \uparrow = \downarrow$$

$$(\uparrow \text{ DEF}) = +$$

$$(\downarrow \text{ CASE}) =_{C} \text{ GEN}$$

Functional single-bar projections

$$\begin{array}{cccc} \mathsf{C'} & \to & \mathsf{C} & \mathsf{IP} \\ & & \uparrow = \downarrow & \uparrow = \downarrow \\ \\ \mathsf{I'} & \to & \mathsf{I} & \mathsf{VP} \end{array}$$

$$\begin{array}{cccc} I' & \rightarrow & I & VP \\ & \uparrow = \downarrow & \uparrow = \downarrow \end{array}$$

$$\begin{array}{cccc} \mathsf{D'} & \to & \mathsf{D} & \mathsf{NP} \\ & \uparrow = \downarrow & \uparrow = \downarrow \end{array}$$

Lexical phrases

Constraining equations

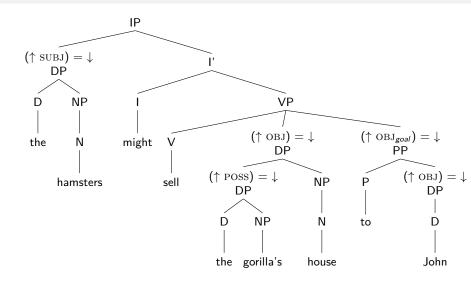
- We have already seen a couple of so-called constraining equations
 - Person $\neq 3$
 - CASE $=_c$ GEN
- Existential equations are another type
 - (↑ TENSE) means TENSE should have *some* value
 - ¬(↑ TENSE) means TENSE should have not have any value
 - Useful for capturing the selectional restrictions of the complementizers to and that

Exercises: English (adapted from Falk 2001)

(9) The hamsters might sell the gorilla's house to John

```
the
                D DEF = +
hamsters
                N \quad (\uparrow PRED) = 'hamster'
                       (\uparrow \text{NUMBER}) = PL
might
                   (\uparrow \text{ TENSE}) = \text{PRES}
                       (\uparrow MOOD) = POSSIBILITY
                       (\uparrow VFORM) =_c INF
                 V (\uparrow PRED) = 'sell \langle SUBJ, OBJ, OBL_{\theta} \rangle'
sell
                       (\uparrow VFORM) = INF
gorilla's
                N \quad (\uparrow PRED) = 'gorilla'
                       (\uparrow \text{NUMBER}) = \text{SG}
                       (\uparrow CASE) = GEN
                       (POSS ↑)
                 N
                       (\uparrow PRED) = \text{'house} < POSS > \text{'}
house
                       (\uparrow \text{NUMBER}) = \text{SG}
                 P (\uparrow PRED) = 'to < OBJ > '
to
                     (\uparrow PRED) = 'John'
John
                       (\uparrow \text{NUMBER}) = \text{SG}
```

The solution: c-structure



The solution: f-structure

```
DEF
               +
'HAMSTER'
SUBJ
        PRED
         NUMBER PL
TENSE
        PRES
MOOD
        POSSIBILITY
PRED
        'SELL <SUBJ, OBJ, OBLgoal>
VFORM
        INF
         PRED
                 HOUSE
         DEF
         NUMBER
                   SG
                   PRED
                          'GORILLA'
OBJ
                   DEF
         POSS
                    CASE
                             GEN
        PRED 'TO <OBJ>'
OBJ PRED 'JOHN']
```

Exercises: Warlpiri (adapted from Bresnan 2001)

- (10) Kurdu-jarra-rlu wita-jarra-rlu ka-pala maliki child-DUAL-ERG small-DUAL-ERG PRES-DUAL dog-ABS wajilipi-nyi chase-NONPAST 'The two small children are chasing the dog.'
- (11) Kurdu-jarra-rlu ka-pala maliki wajilipi-nyi child-DUAL-ERG PRES-DUAL dog-ABS chase-NONPAST wita-jarra-rlu small-DUAL-ERG 'The two small children are chasing the dog.'
- (12) Maliki ka-pala kurdu-jarra-rlu wajilipi-nyi dog-ABS PRES-DUAL child-DUAL-ERG chase-NONPAST wita-jarra-rlu small-DUAL-ERG 'The two small children are chasing the dog.'

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Exercises: Warlpiri (adapted from Bresnan 2001)

```
(Aux) X*
                                                                             (where X = NP, V)
               (\uparrow(SUBJ|OBJ)) = \downarrow \uparrow = \downarrow (\uparrow(SUBJ|OBJ))
NP
               \uparrow = \downarrow
kurdu-jarra-rlu
                          (\uparrow PRED) = 'child'
                               (\uparrow NUM) = DUAL
                               (\uparrow CASE) = ERG
                               (\uparrow PRED) = 'dog'
maliki
                      Ν
                               (\uparrow NUM) = SG
                               (\uparrow CASE) = ABS
                               (\uparrow ADJ PRED) = 'small'
wita-jarra-rlu
                      Ν
                               (\uparrow NUM) = DUAL
                               (\uparrow CASE) = ERG
wajilipi-nyi
                      V
                               (\uparrow PRED) = 'chase < SUBJ, OBJ > '
                               (\uparrow \text{ TENSE}) = \text{NONPAST}
                               (\uparrow \text{SUBJ CASE}) = \text{ERG}
                               (\uparrow OBJ CASE) = ABS
                               (\uparrow ASPECT) = PRESENT.IMPERFECT
ka-pala
                      Aux
                               (\uparrow SUBJ NUM) = DUAL
```