

## VARIABLE STEPLENGTH

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The steplength can be varied by using the form of the explicit equations. They are all of a form where

$$\begin{aligned}dV &= f dm \\V_{i+1} &= V_i + dV\end{aligned}$$

where  $V$  is the variable we are interested in stepping forward,  $m$  is the primary variable and  $f$  is a function not dependent on  $dm$ . The question is now how large can we make  $dm$  without getting into trouble. For a constant steplength,  $dm$  is given and constant, so we can directly calculate the changes of the dependent variable  $dV$ , but by choosing  $dm$  in advance we cannot guarantee that  $dV$  does not become too large, so that either the solution is imprecise or that we get a value for  $V + dV$  that is unphysical.

We now make the following modification

$$\frac{dV}{dm} = f$$

and we now require that for a step forward in  $dm$  the corresponding  $dV$  satisfies

$$\frac{|dV|}{V} < p$$

where  $|dV|$  is the absolute value of  $dV$  and  $p$  is a fraction that  $V$  is allowed to change and  $p$  must therefore generally be less than one and 0.1 is a safe place to start.

In practice we just do the following:

Calculate  $f$  without multiplying with  $dm$ :

$$\frac{dV}{dm} = f$$

now use  $f$  and the chosen  $p$  to calculate  $dm$

$$dm = \frac{dV}{f} = \frac{pV}{f}$$

and then  $V$  can be advanced by

$$V_{i+1} = V_i + \frac{dV}{dm} dm = V_i + f dm$$

where it is now guaranteed that  $V$  does not change by more than  $pV$ .

If there are several equations that need to be advanced, then the  $dm$  is calculated for each of them producing several  $dm_1, dm_2, \dots$ . The used  $dm$  is then the smallest value,

$$dm = \text{MIN}[dm_1, dm_2, \dots]$$

where it has now been assumed that all of  $dm_1, dm_2, \dots$  are all positive.