

AST5770
Solar and stellar physics

University of Oslo, 2022

Sven Wedemeyer

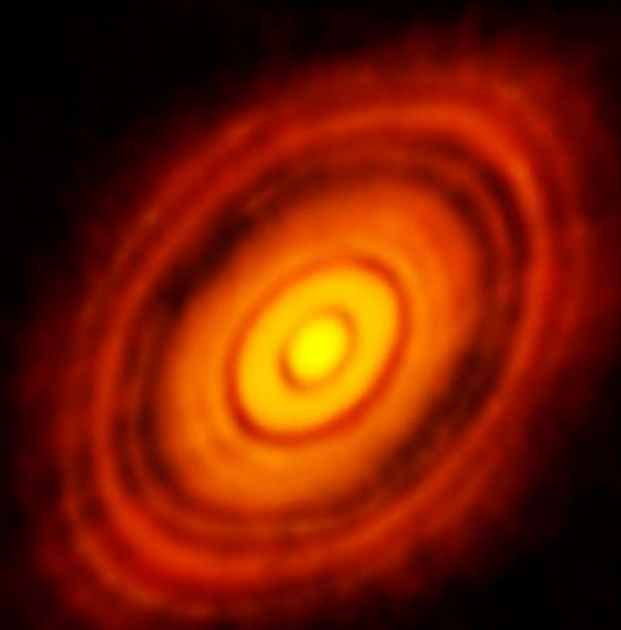
Stellar evolution

Star formation

- Star formation: Collapse of giant molecular cloud, fragmentation
 ➔ Stars typically form in groups (e.g., Pleiades)
- Formation of protostar once core becomes hot and dense enough to establish hydrostatic equilibrium
- Further contraction, approaching Zero Age Main Sequence (ZAMS) on Hayashi tracks (fully convective)

T Tauri stars:

pre-main sequence
 (age $\sim 10^6$ yr),
 accretion disk still
 optically thick,
 large IR excess
 observed



HL Tauri ALMA (ESO/NAOJ/NRAO)



Pleiades (M45)

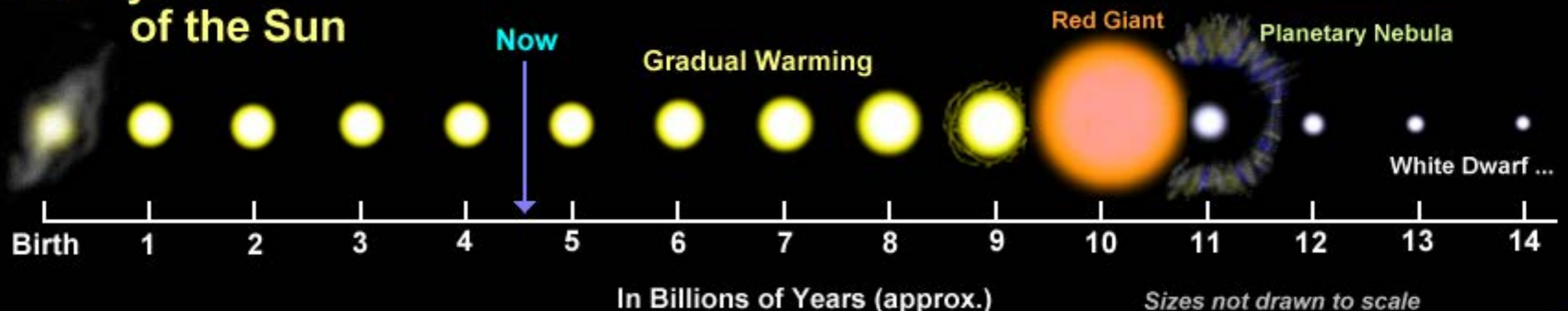
Stellar evolution

Overview

- **Main sequence**
 - Begins when reaching Zero Age Main Sequence (ZAMS)
 - Hydrogen fusion (H burning) in the core
 - Longest evolution stage
- **Post-main sequence evolution**
 - More complicated due to different fusion stages (element) in the core and/or shells
 - Reached fusion stage highly mass-dependent
 - **Mirror principle** for stars with shell burning — expansion and contraction opposite of a shell (core — envelope)
 - **Equation of state** — beyond ideal gas

Life Cycle

of the Sun



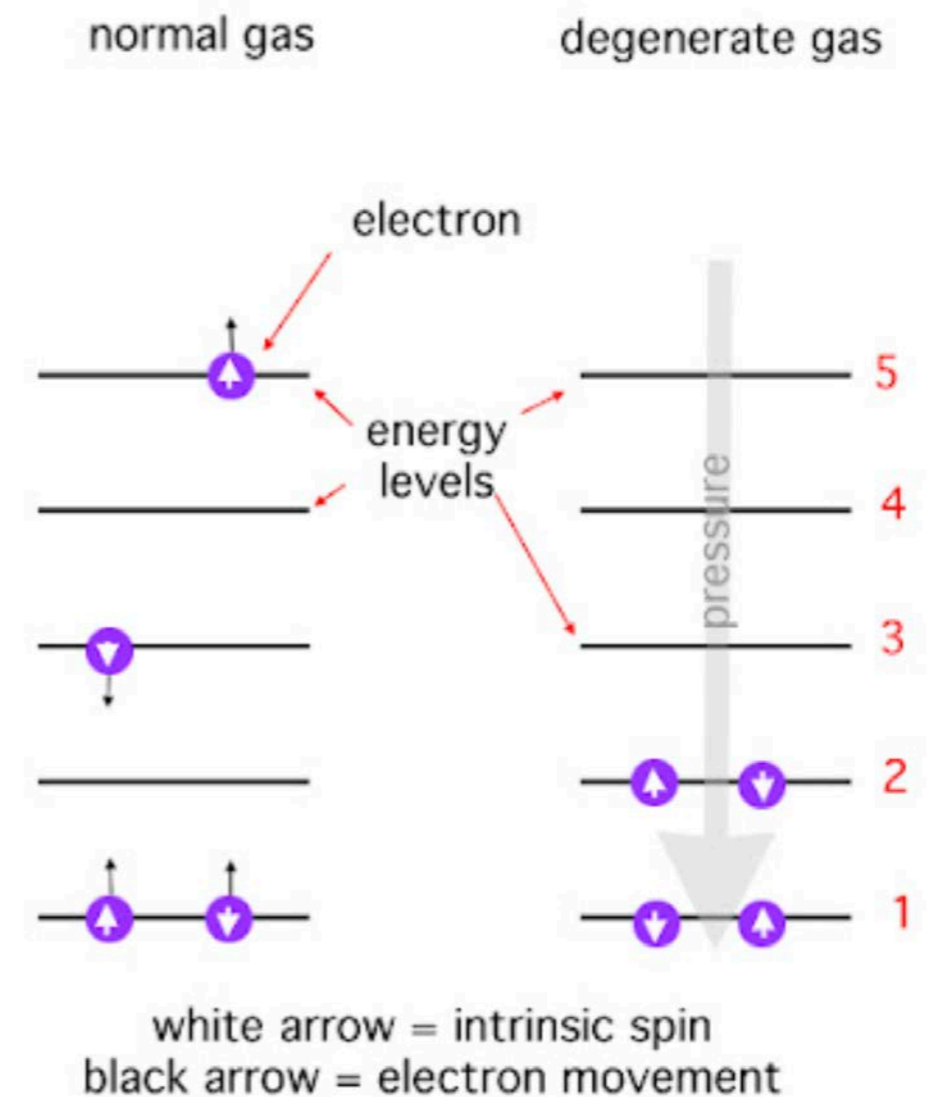
Post-main sequence evolution

Degenerate Matter

- He core: mixture of He nuclei and electrons.
- Electrons obey **Pauli Exclusion Principle**
(2 electrons cannot occupy the same quantum state)
- If phase space is full at high density: Any additional electron cannot fit anymore unlike for an ideal gas at same temperature
- Higher pressure than for an ideal gas at same temperature

➔ Electron Degeneracy Pressure

- Electrons would repel each other if tried to be forced closer together.
 - Repulsion much stronger than the usual repulsion between charged particles.
- Degeneracy pressure $>$ thermal pressure
- ➔ Gas called **degenerate**.



Post-main sequence evolution

Degenerate Matter

- Degenerate gas behaves differently than ideal gas.

- Ideal gas: Pressure depends on density and temperature.
$$P_{\text{gas}} = \frac{kT\rho}{m} = \frac{kT\rho}{m_H \mu} = \frac{RT\rho}{\mu}$$

- Degenerate gas: Pressure depends only on density
 ➔ Pressure won't change if temperature changes
 (as long as T low enough to stay in degeneracy regime)

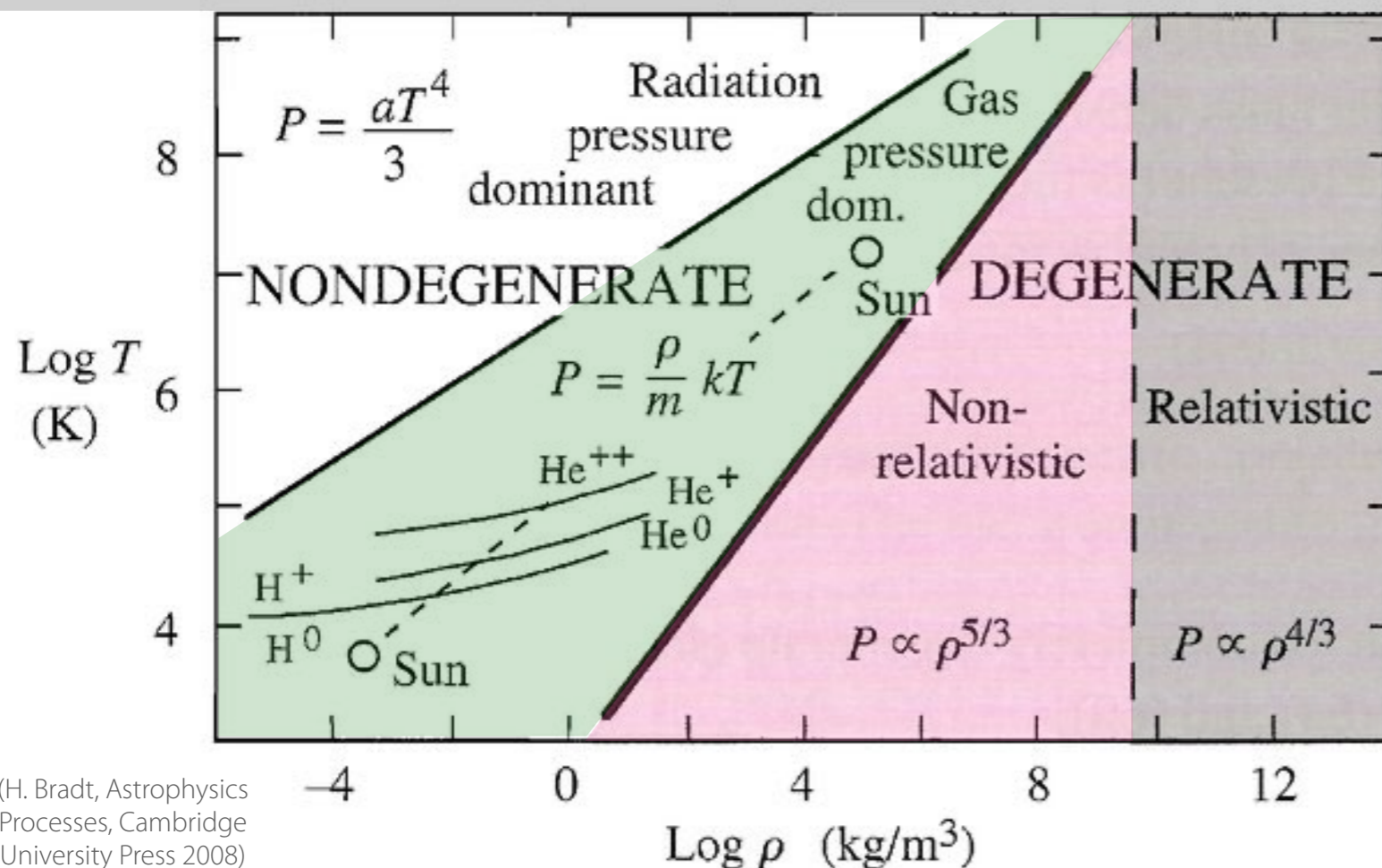
$$P = K_1 \rho^{\frac{5}{3}} \quad K_1 = \frac{h^2}{20m_e} \left(\frac{3}{\pi}\right)^{\frac{2}{3}} \left[\frac{(1+X)}{2m_H}\right]^{\frac{5}{3}}$$

- ➔ For a relativistically degenerate gas (i.e. $p_0 \gg m_e c$):

$$P = K_2 \rho^{\frac{4}{3}} \quad K_2 = \left(\frac{hc}{8}\right) \left(\frac{3}{\pi}\right)^{\frac{1}{3}} \left[\frac{(1+X)}{2m_H}\right]^{\frac{4}{3}}$$

The density (as the mean molecular weight) depends on chemical composition, which changes as result of nuclear fusion (He content!)

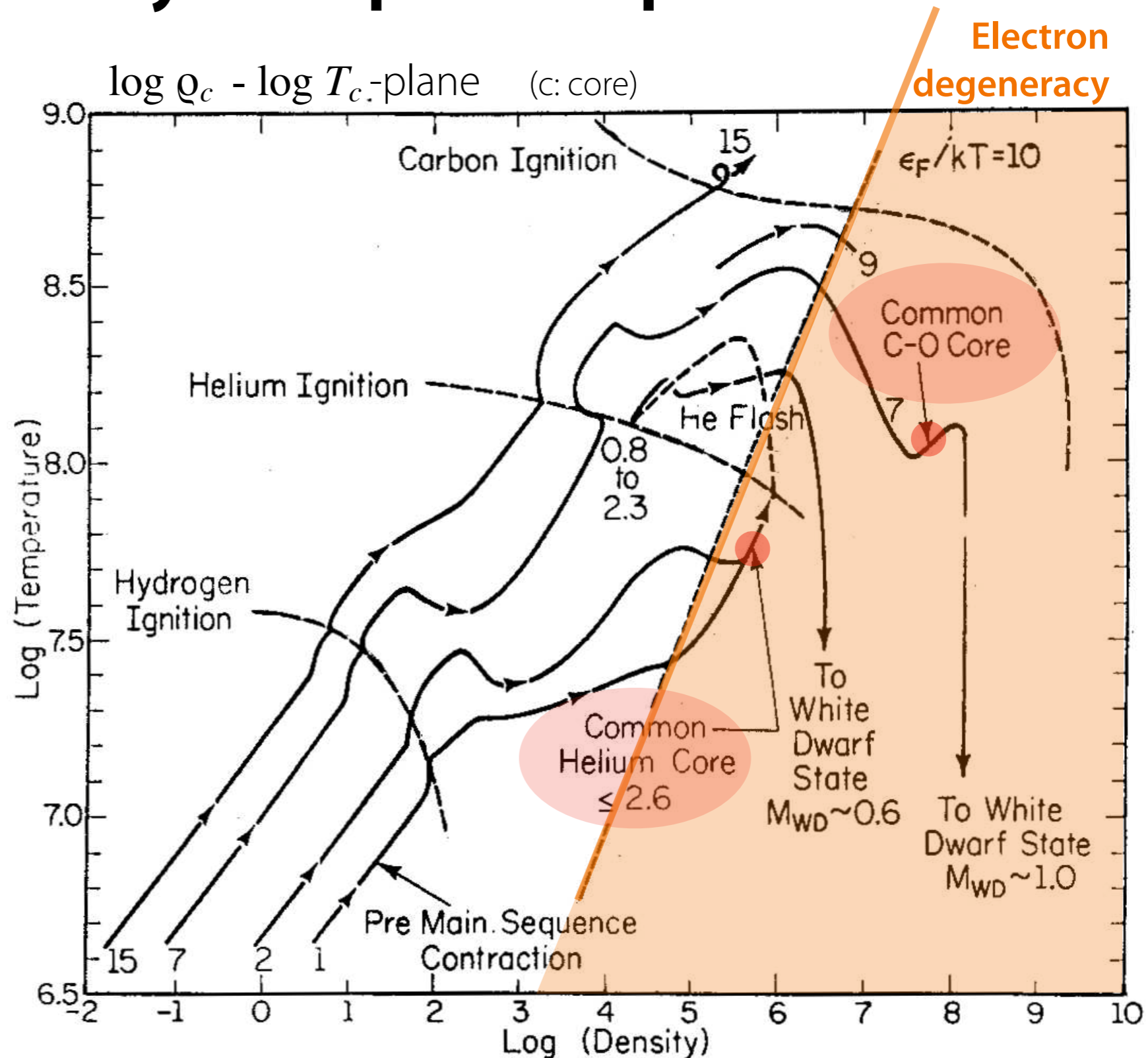
- Note: No sharp transition between ideal gas equation of state and the corresponding degenerate equation of state!
 Continuous transition!



Post-main sequence evolution

Tracks in the core density—temperature plane

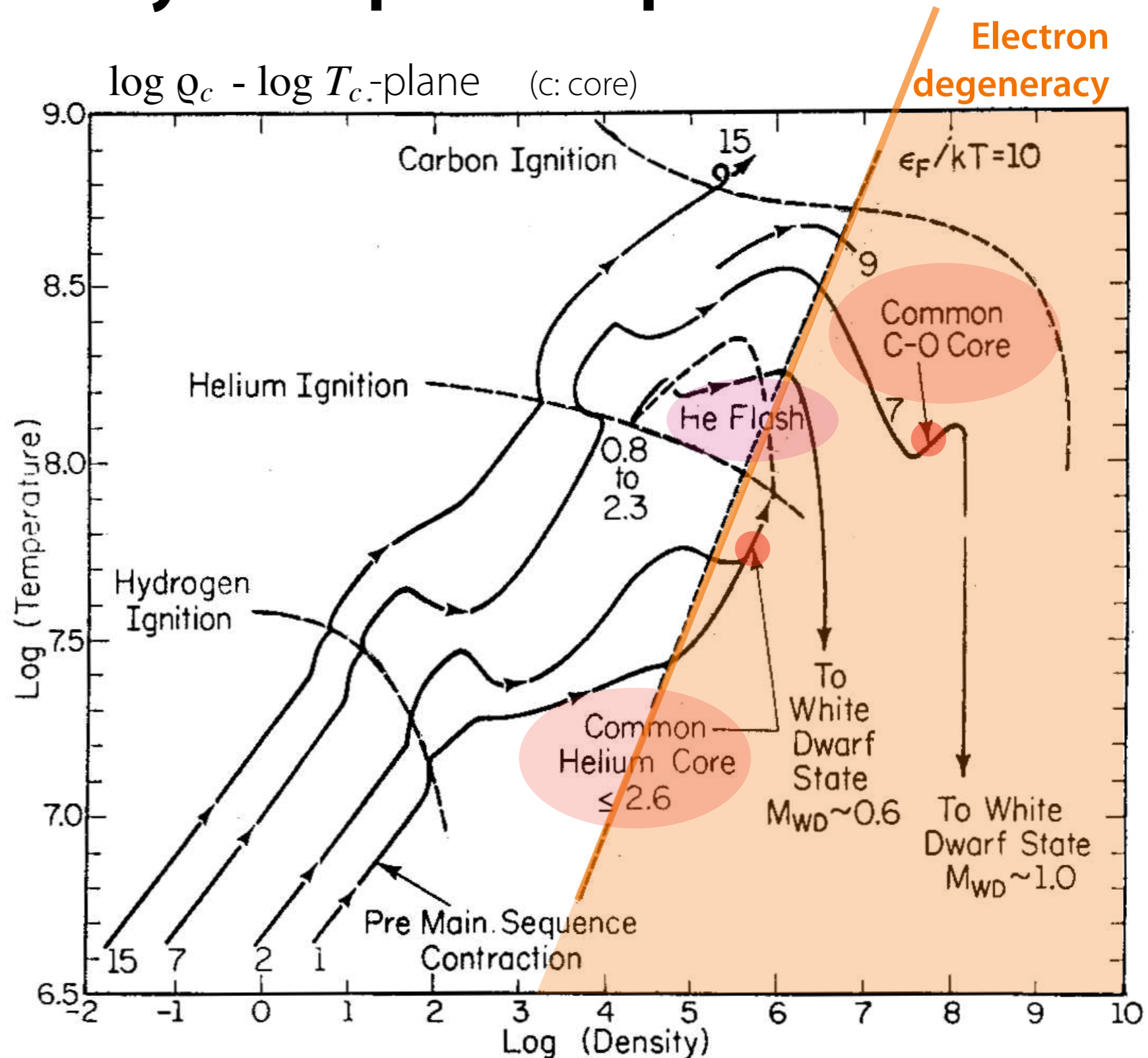
- Evolution tracks in core density-temperature plane ($\log \rho_c - \log T_c$)
- Sun's core becomes degenerate at $\rho_c > 10^6 \text{ kg/m}^3$, $T \sim 2 \cdot 10^7 \text{ K}$.
 ➔ Degenerate core early during red giant phase.
- All low-mass stars, degenerate He core during red giant phase.
- Intermediate and high-mass stars not degenerate while red giants.



Post-main sequence evolution

Tracks in the core density—temperature plane

- **At end of H-burning:** core contracts while outer layers expand (mirror principle!)
 - ➔ Higher core density
 - Occurs for each nuclear burning stage.
- **Core of 7 M_{\odot} stars:** electron degeneracy before C-ignition temperature is reached,
 - ➔ C-O white dwarf.
- **Core of 1 and 2 M_{\odot} stars:**
 - low mass ($0.3 M_{\odot}$),
 - become degenerate before igniting He-burning
 - Degenerate He cores keep getting more massive and hotter due to H-shell burning
 - Ignite helium in an unstable manner (**He flash**)



Post-main sequence evolution

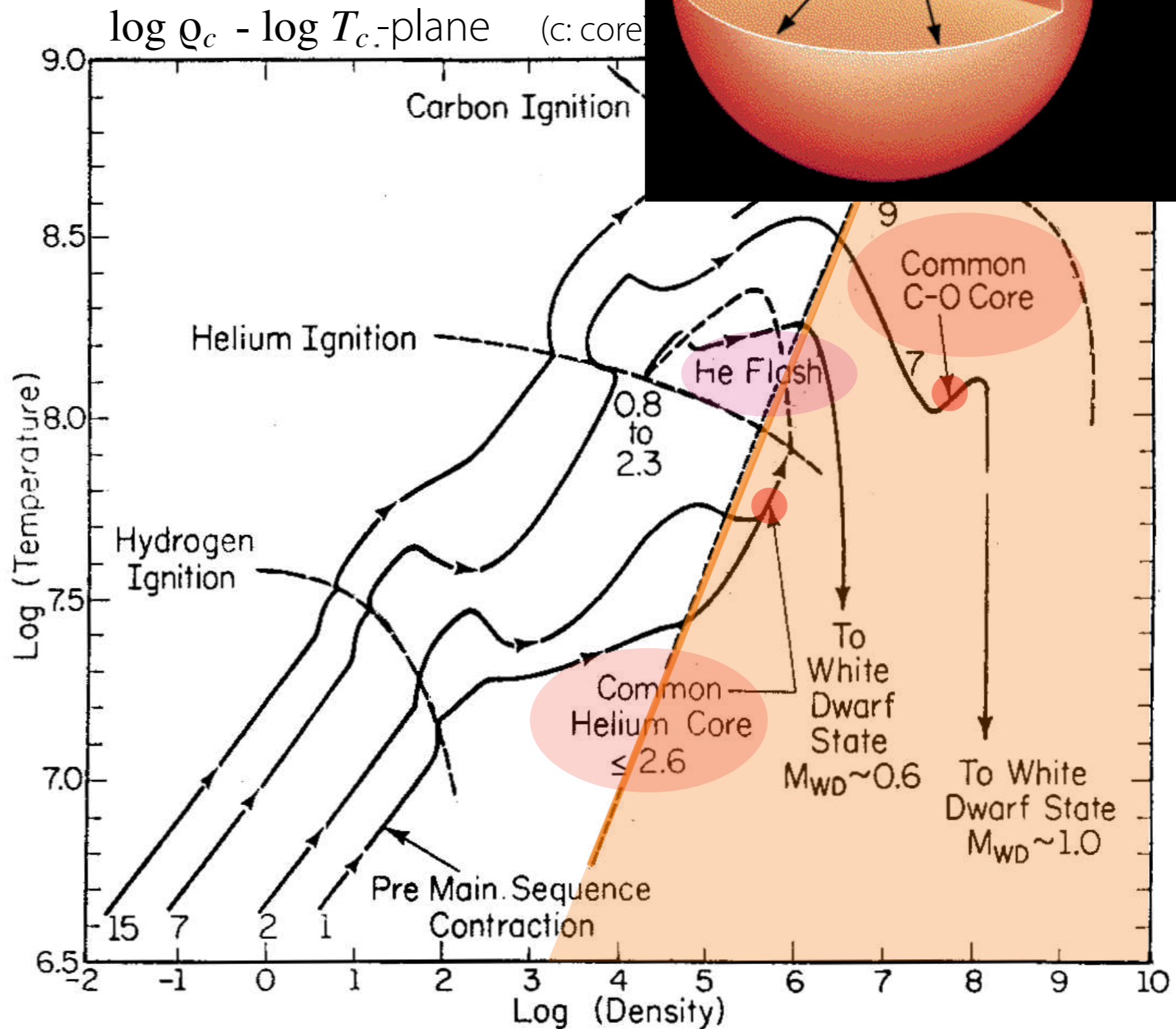
Tracks in the core density—temperature

- **Schönberg-Chandrasekhar** (S-C) limit: Max. mass of an inert (isothermal) He core that can be supported (unstable if core more exceeds limit):

$$M_c/M < q_{sc} \approx 0.10$$

(M_c : core mass, M : total mass)

- $M < 1.5 M_\odot$: core becomes degenerate before reaching S-C limit
- $M > 6 M_\odot$: star leaves main sequence with core $>$ S-C limit (core never isothermal before He-burning)
- $1.5 M_\odot > M > 6 M_\odot$: core grows until reaching S-C limit, then contracts rapidly until He-burning ignites in core



Post-main sequence evolution

Helium flash in low-mass stars

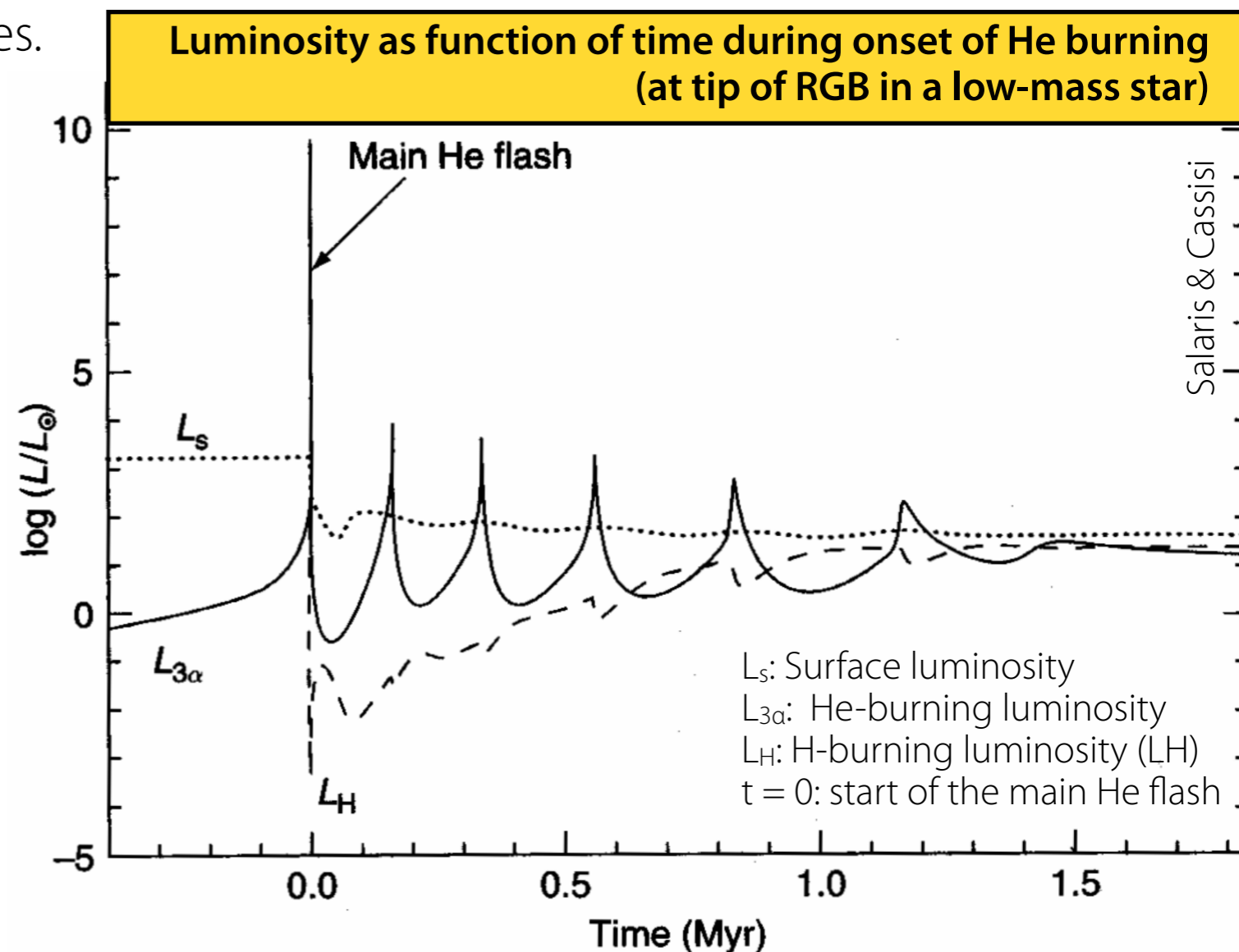
- He burning (3α reaction) thermally unstable under conditions in degenerate He core
- Degenerate pressure is independent of T ! (ideal gas: pressure increases, expands and cools)
- Energy released by fusion does not increase the pressure (negligible expansion / work)
- All nuclear energy released goes instead into raising the internal energy

➔ Temperature increases.

➔ Nuclear energy production rate increases.

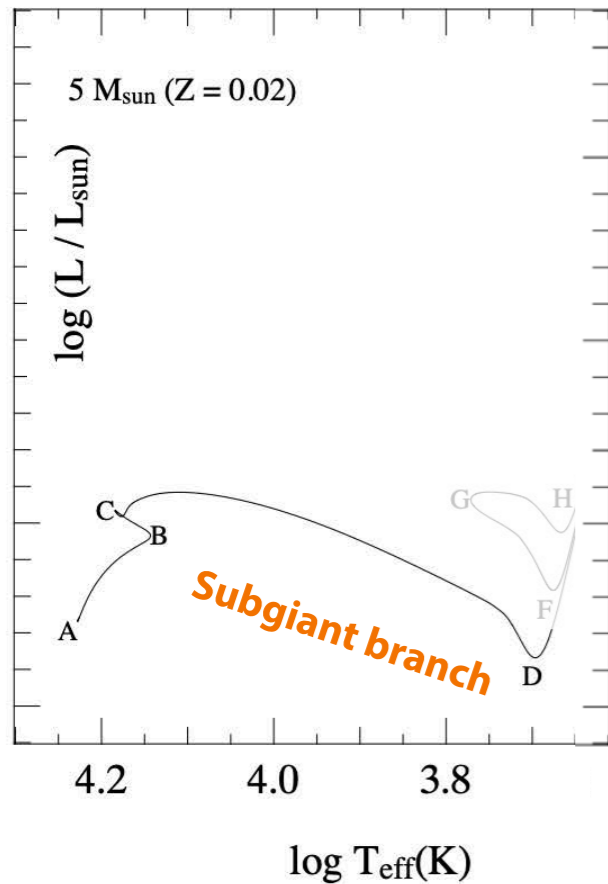
➔ **Thermonuclear runaway.**

- Energy output at max. equivalent to small galaxy (but only for a few seconds)
- Eventually temperature increased so much that degeneracy is lifted, gas starts behaving like an ideal gas
- Released energy increases pressure, causes expansion and cooling.
- All released energy absorbed in expansion of core, none reaches the surface!



Post-main sequence evolution

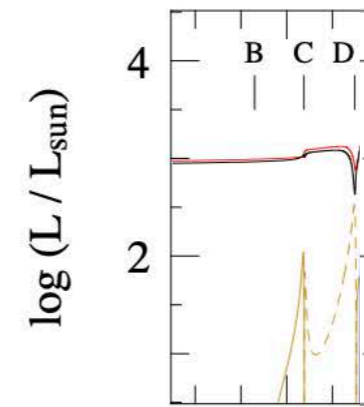
Hydrogen-shell burning in intermediate-mass stars



- **A:** Start at ZAMS
- **B:** start of overall contraction phase, near end of MS phase
- **C:** exhaustion of H in centre,
 - convective core disappears
 - core mass remains below Schönberg-Chandrasekhar (S-C) limit, in thermodyn. equilibrium at beginning of H-shell burning

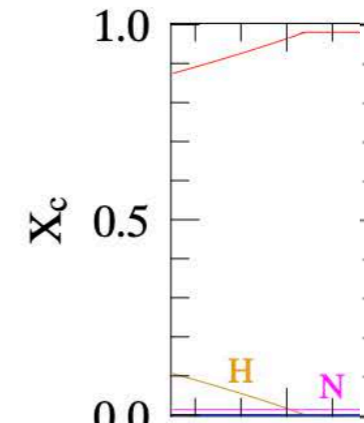
- **C–D:** H-shell burning, relatively slow, lasting about 2×10^6 yr
 - (thick) burning shell initially occupies large region in mass
 - He-core gradually grows until exceeding the S-C limit,
- **After C:**
 - Core contraction speeds up (all layers below burning shell contract)
 - At the same time: all layers above shell (=envelope) expand ('mirror principle')
 - Changes at accelerating rate towards end of C-D phase.
 - Density + temperature gradients grow — shell gets thinner

Model of internal evolution of a $5 M_{\odot}$ star, initial composition $X = 0.7, Z = 0.02$.



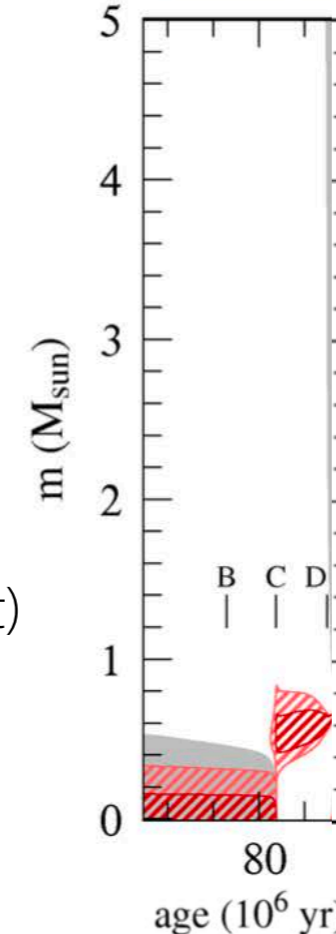
Luminosity contributions

- H burning (red line),
- He burning
- gravitational energy release
- surface luminosity.



Central mass fractions

$^1\text{H}, ^4\text{He}, ^{12}\text{C}, ^{14}\text{N}$ and ^{16}O



Kippenhahn diagram:

Internal structure as function of mass coordinate m

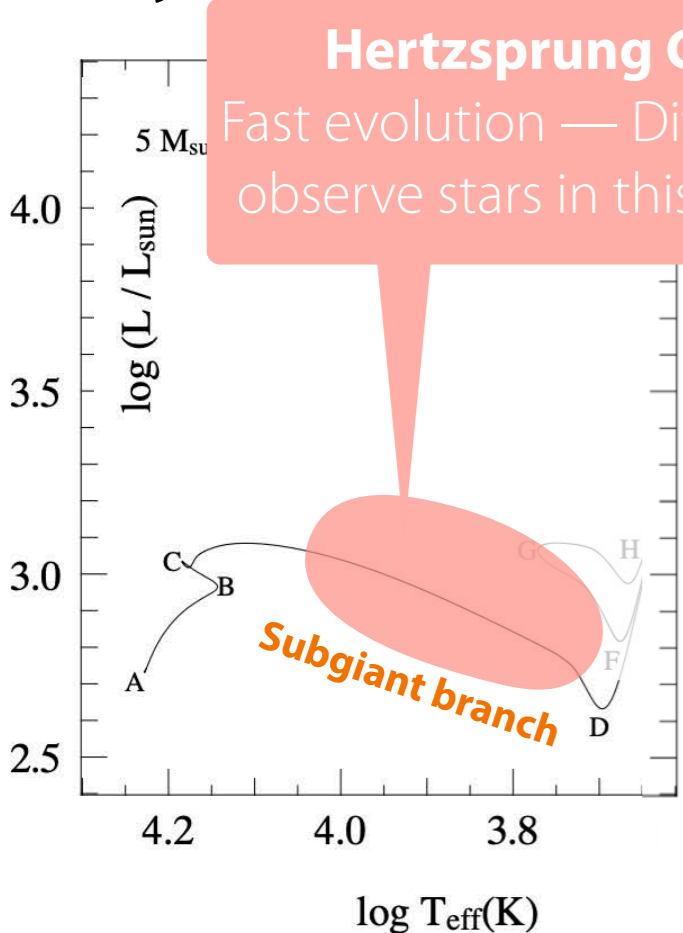
Gray areas: convective
Red hatched: nuclear energy generation

Dark red $\epsilon_{\text{nuc}} > 10 \text{ L/M}$

Light red $\epsilon_{\text{nuc}} > 2 \text{ L/M}$

Post-main sequence evolution

Hydrogen-shell burning in intermediate-mass stars

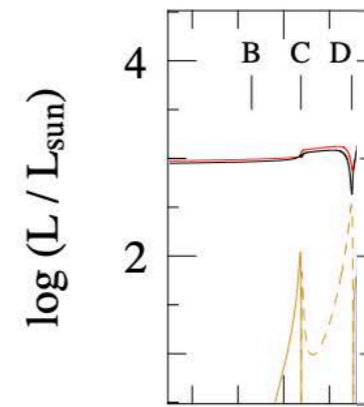


Hertzsprung Gap
Fast evolution — Difficult to observe stars in this phase.

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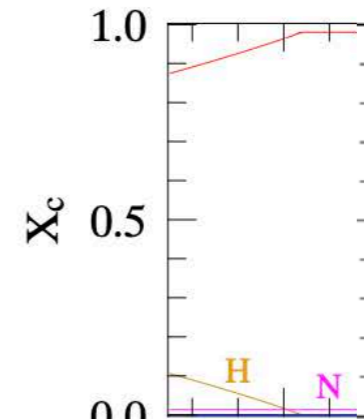
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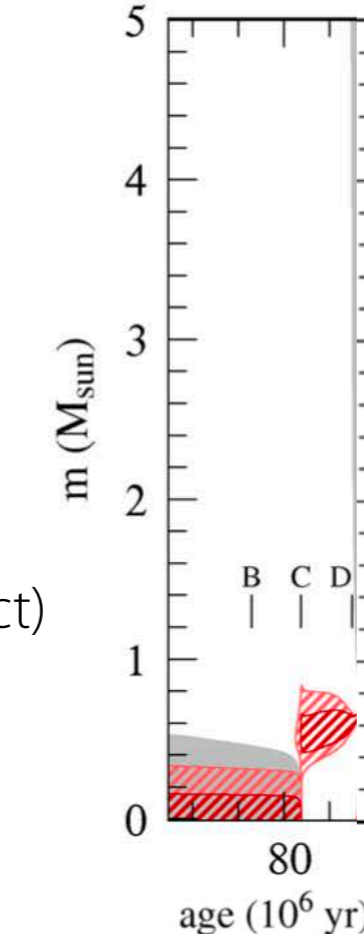
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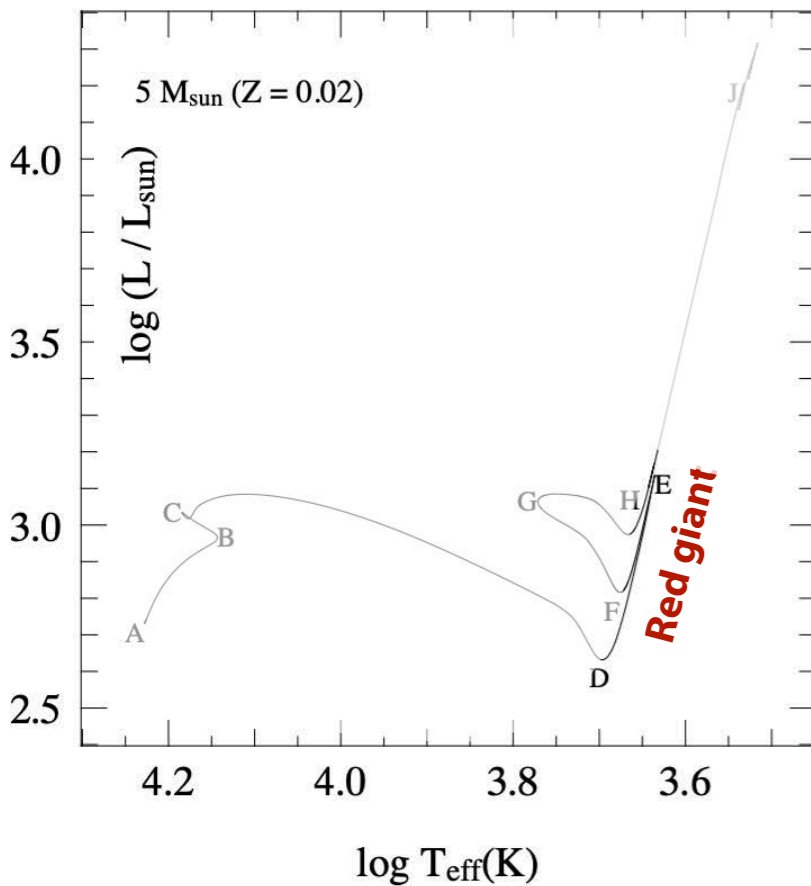
Kippenhahn diagram:

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Post-main sequence evolution

Model of internal evolution of a $5 M_{\odot}$ star, initial composition $X = 0.7, Z = 0.02$.

Red giant phase

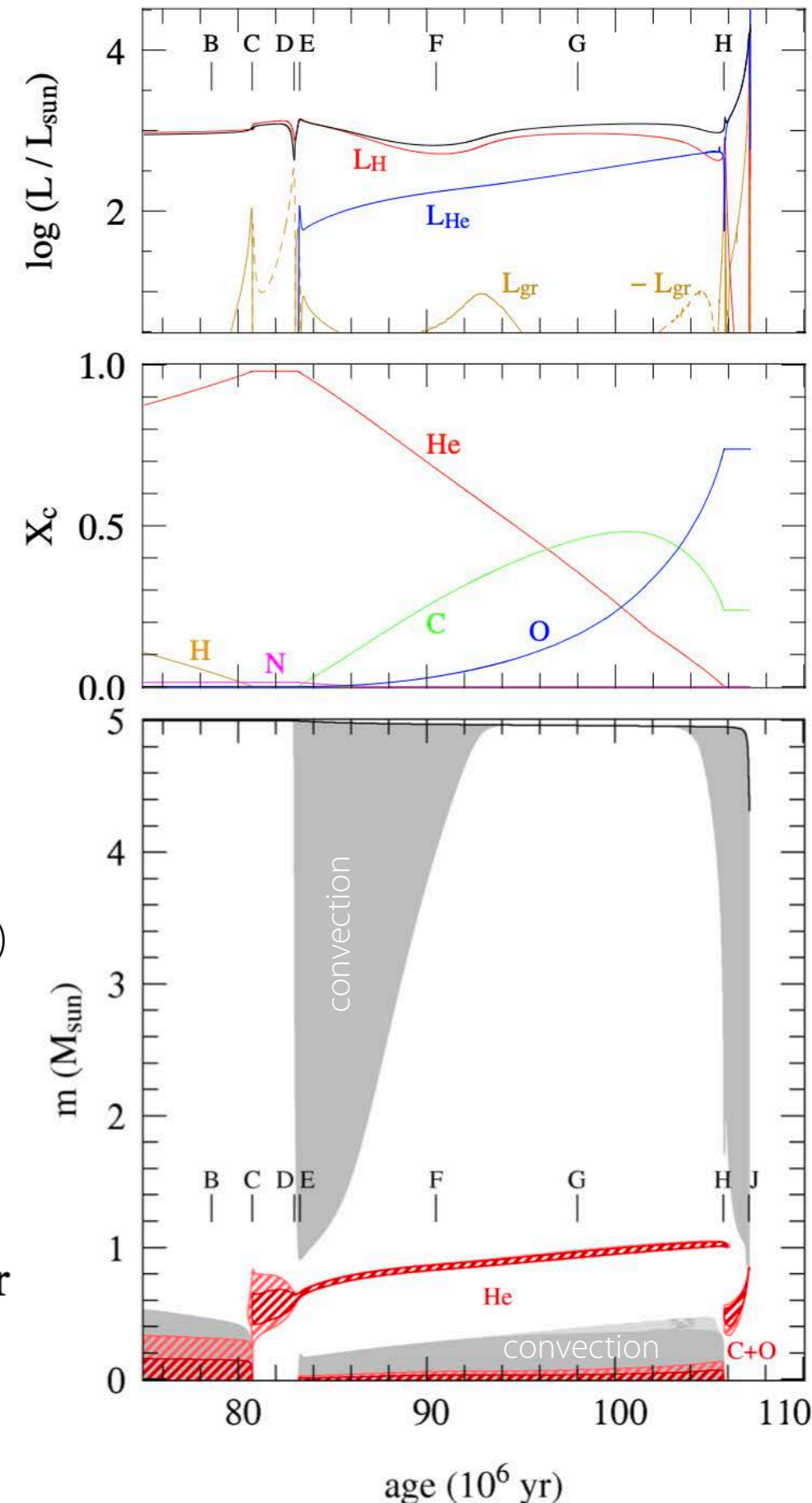


- **D**: Opacity in thin shell increases
 - Radiative energy transport inefficient, convection sets in
- **D-E**: Red giant phase
 - Convection in core + deep convection zone (up to surface)
 - Relatively short lived phase ($\sim 10\%$ of main sequence) lifetime
- **E**: Outer convection zone reaches into former (thick) H-burning shell
 - Fusion product (CNO cycle) brought to surface (“dredge-up”)

- **E**: envelope becomes loosely bound, relatively easy to remove mass from surface driven by large radiation (still open questions...)

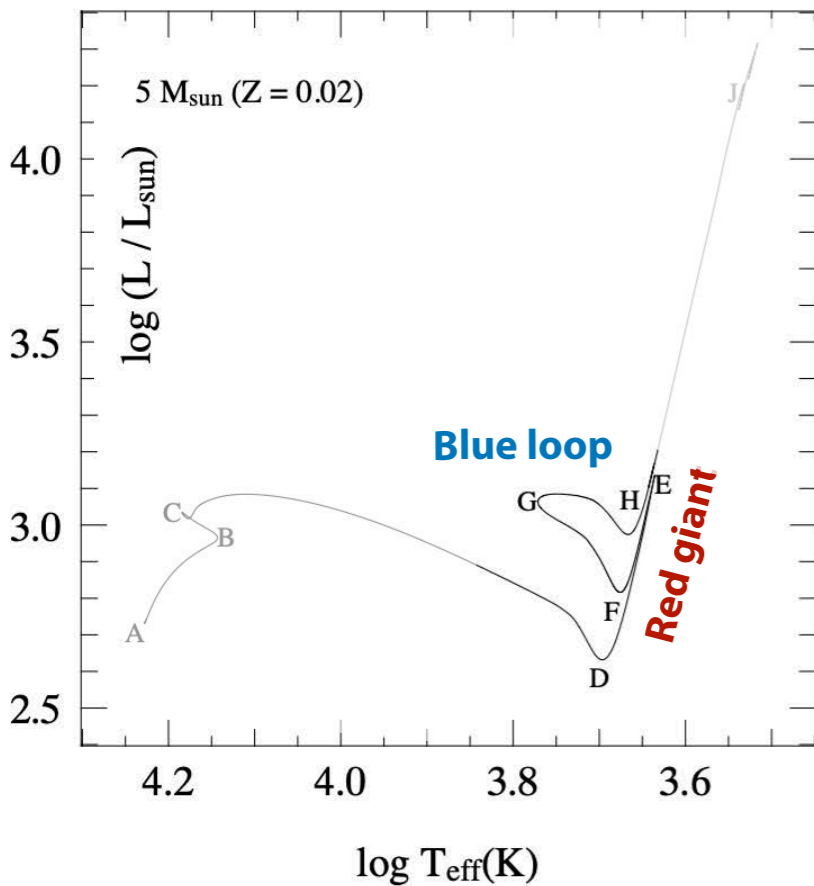
➡ Strong **mass loss** on the red giant branch (stellar wind)

- Mass loss rate (Reimers): $\dot{M} = -4 \times 10^{-13} \eta \frac{L}{L_{\odot}} \frac{R}{R_{\odot}} \frac{M_{\odot}}{M} M_{\odot}/\text{yr}$
- Typically used: $\eta \sim 0.25 - 0.5$
- $1 M_{\odot}$ star lost about $0.3 M_{\odot}$ when reaching tip of giant branch (E).



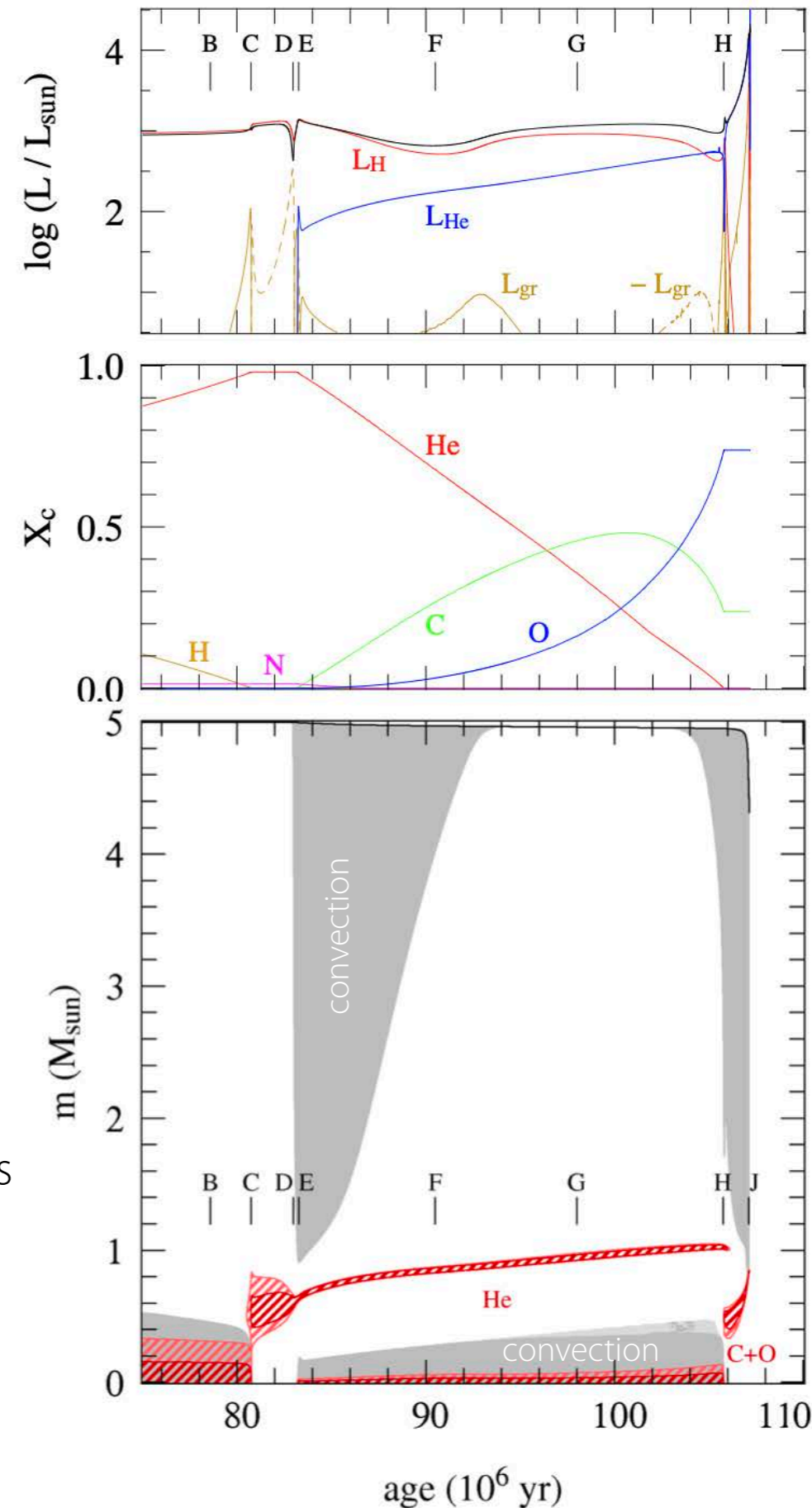
Post-main sequence evolution

Red giant phase and blue loop



- **E**: He core mass reaches $0.6 M_{\odot}$, central temperature 10^8 K
 - C, O-burning ignites in core (H-burning continues in thin shell)
 - For low-mass stars: degenerate core — H-shell burning and mass growth at increasing until He-burning suddenly ignites (He flash)
- **E-F**: envelope contracts, stellar radius decrease, luminosity decreases
 - Star forced to evolve along its Hayashi line.
 - Outer convection zone becomes shallower, envelope becomes radiative
- **F-G-H**: Blue loop — min. radius reached at G
- **H**: end of core He burning

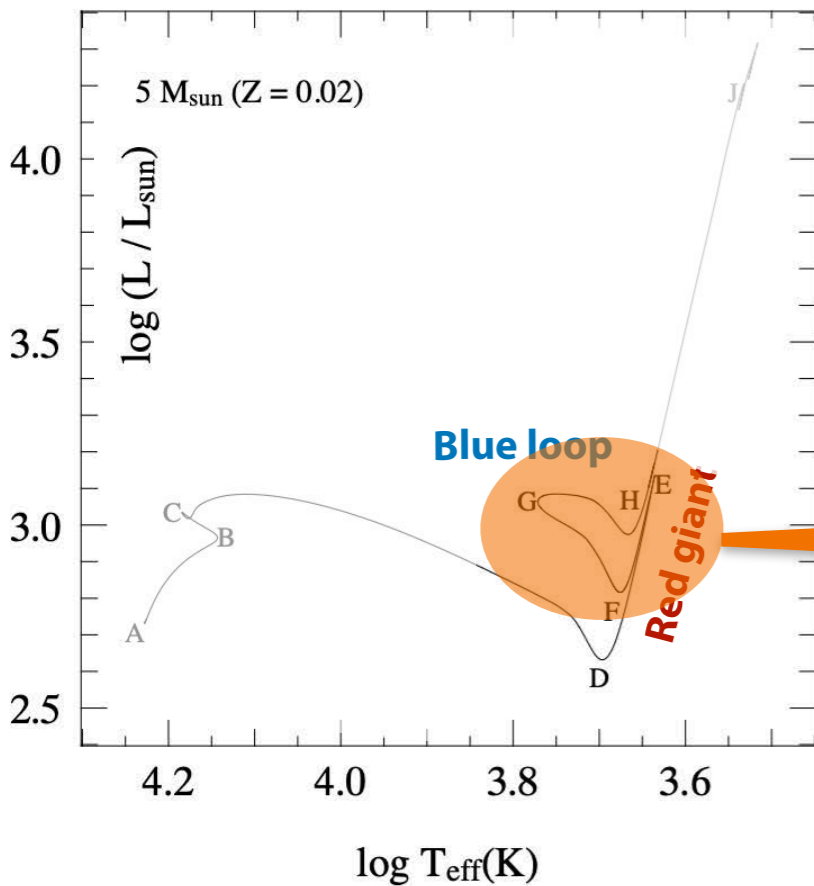
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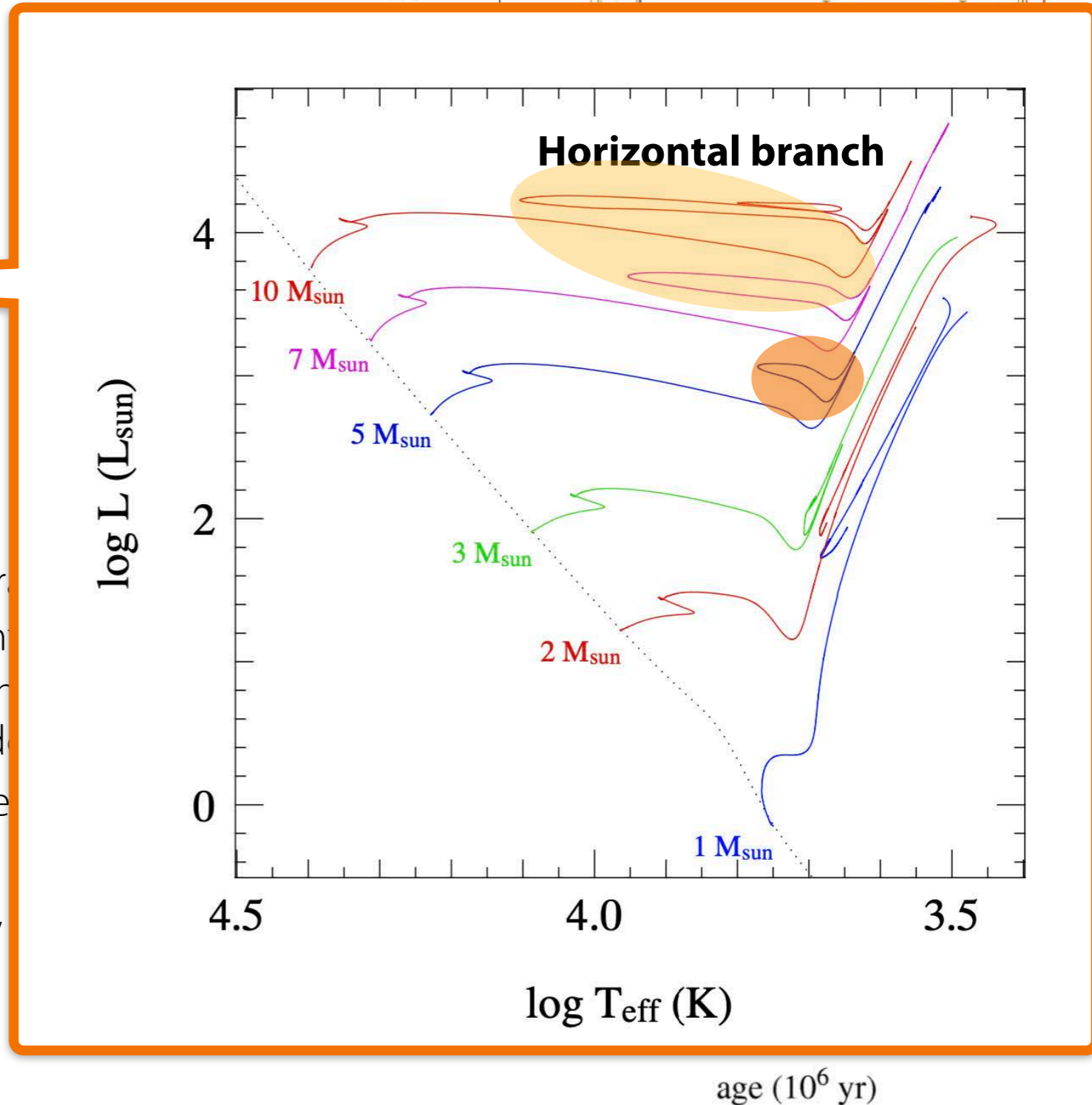
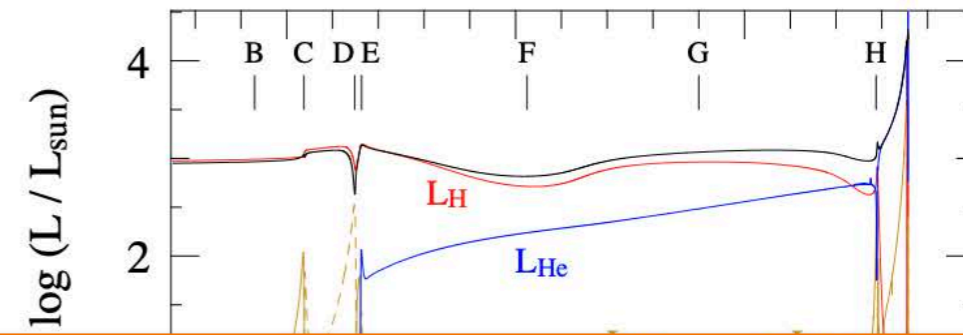
Post-main sequence evolution

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Red giant phase and blue loop



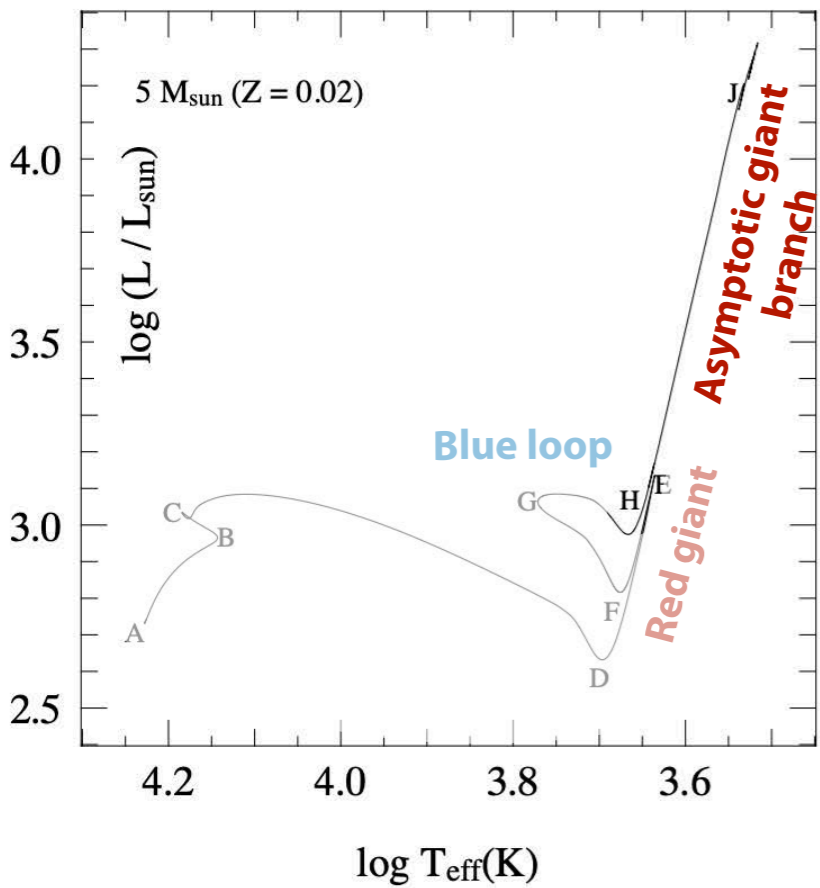
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age (10^6 yr)

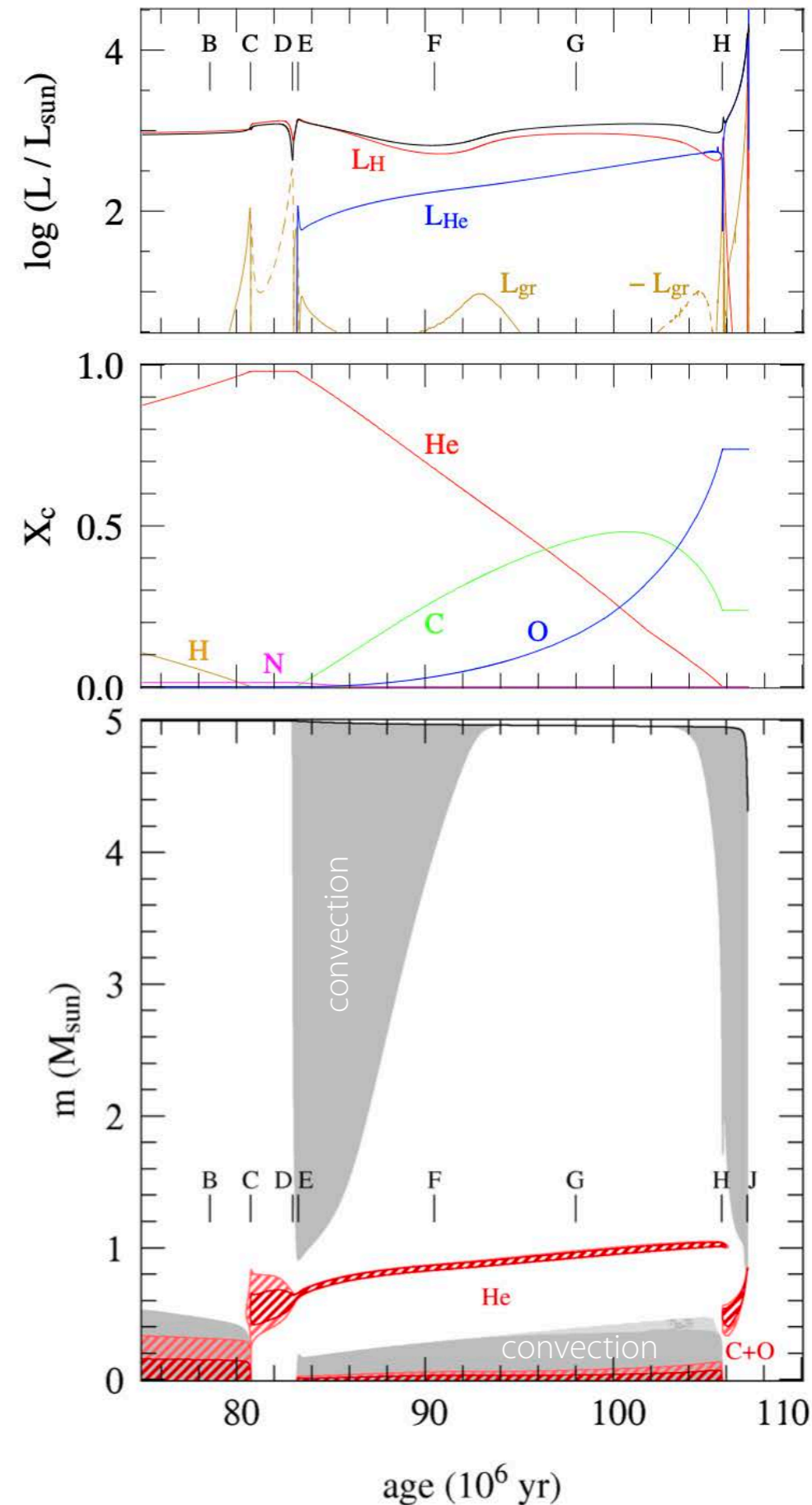
Post-main sequence evolution

Asymptotic Giant Branch



- **H**: end of core He burning
- ➡ back on Hayashi track (close to E)
- ➡ Beginning of asymptotic giant branch (AGB) phase

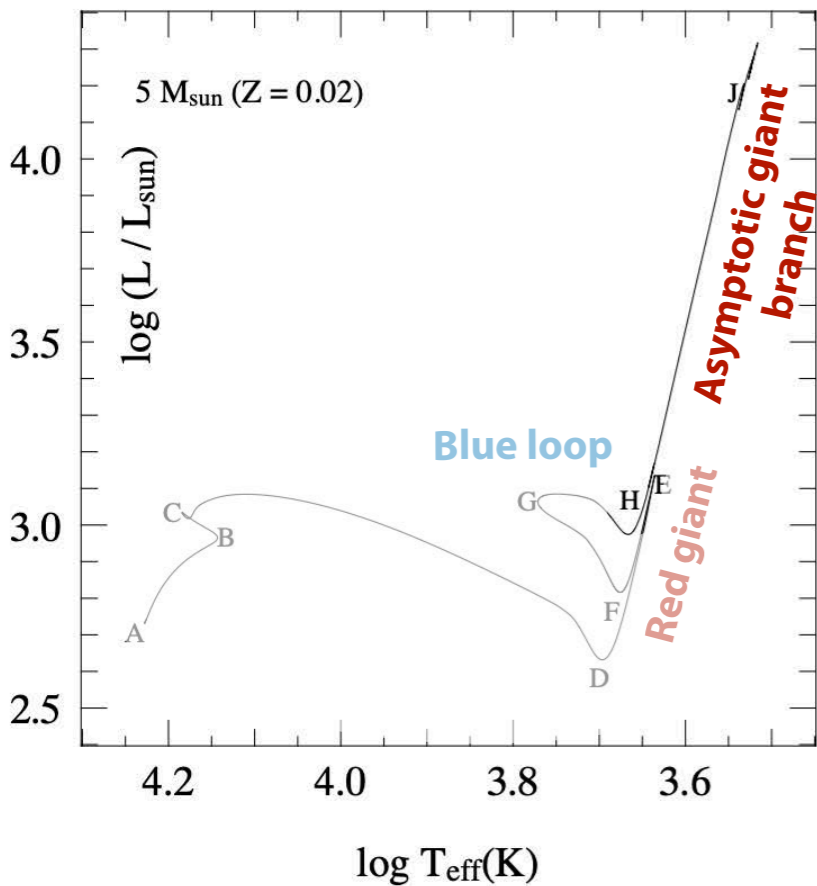
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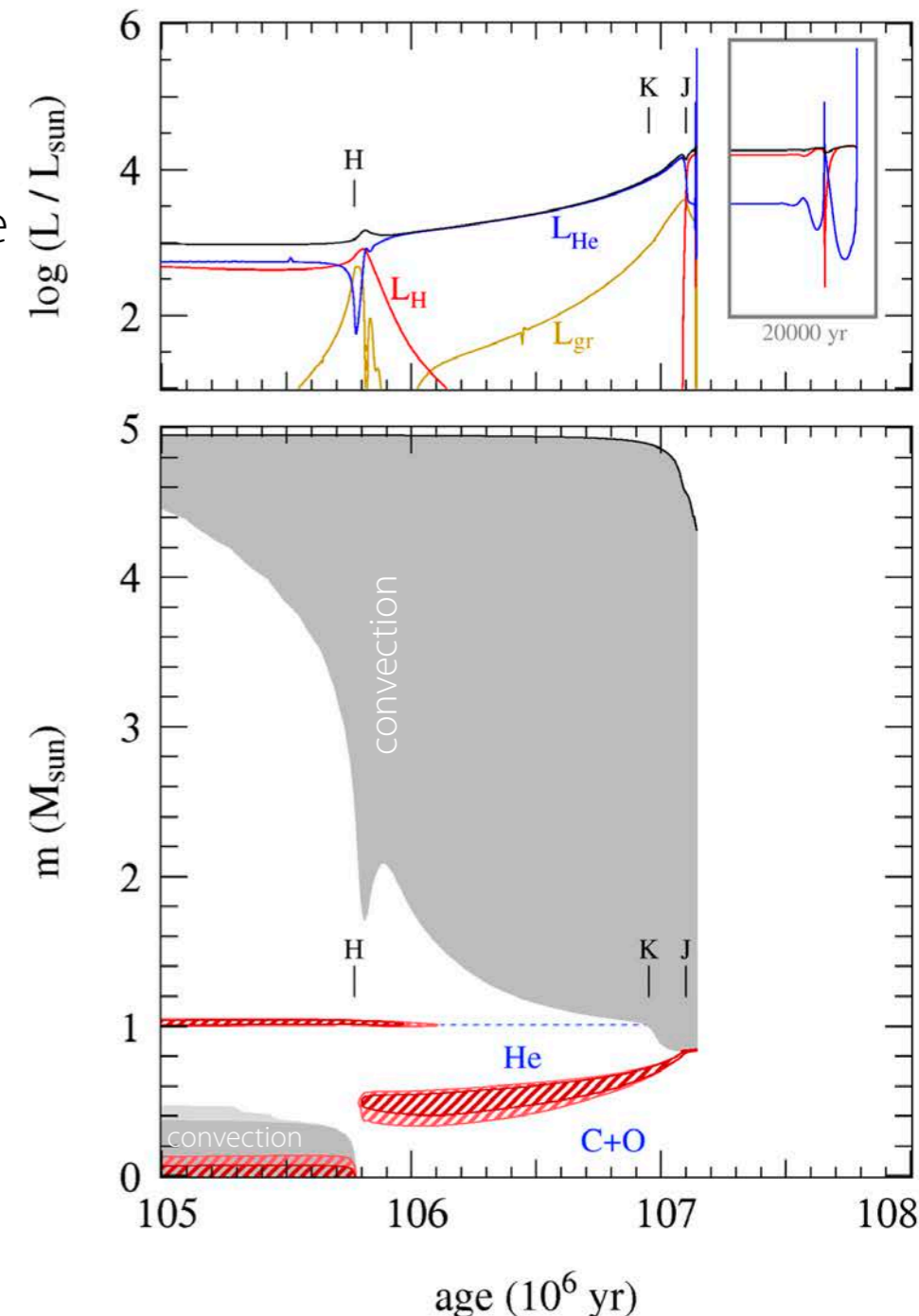
Post-main sequence evolution

Model of internal evolution of a $5 M_{\odot}$ star, initial composition $X = 0.7, Z = 0.02$.

Asymptotic Giant Branch



- **H**: end of core He burning
 - ➡ back on Hayashi track (close to E)
 - ➡ Beginning of asymptotic giant branch (AGB) phase
- **H**: start of early AGB phase — He-burning shifts rapidly from core to shell (around former convective core, now rich in C+O)
 - H-burning shell extinguishes
- **K**: outer convection zone reaches deep down again into region of previous H shell burning
 - ➡ second dredge-up.
- (For lower-mass stars: H-shell remained active, prevents convective envelope from extending deeper, no second dredge-up)

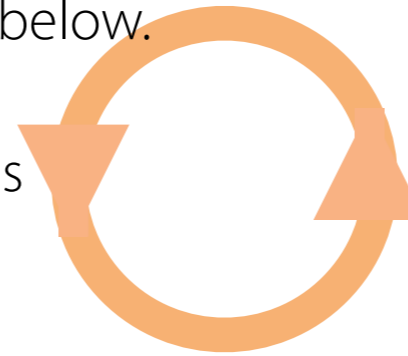


Post-main sequence evolution

Model of internal evolution of a $5 M_{\odot}$ star, initial composition $X = 0.7, Z = 0.02$.

Asymptotic Giant Branch

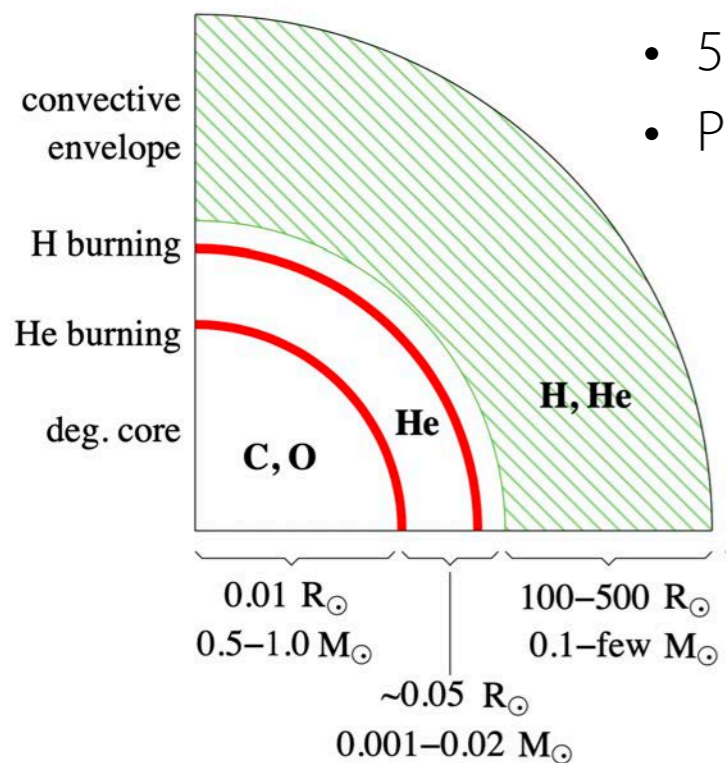
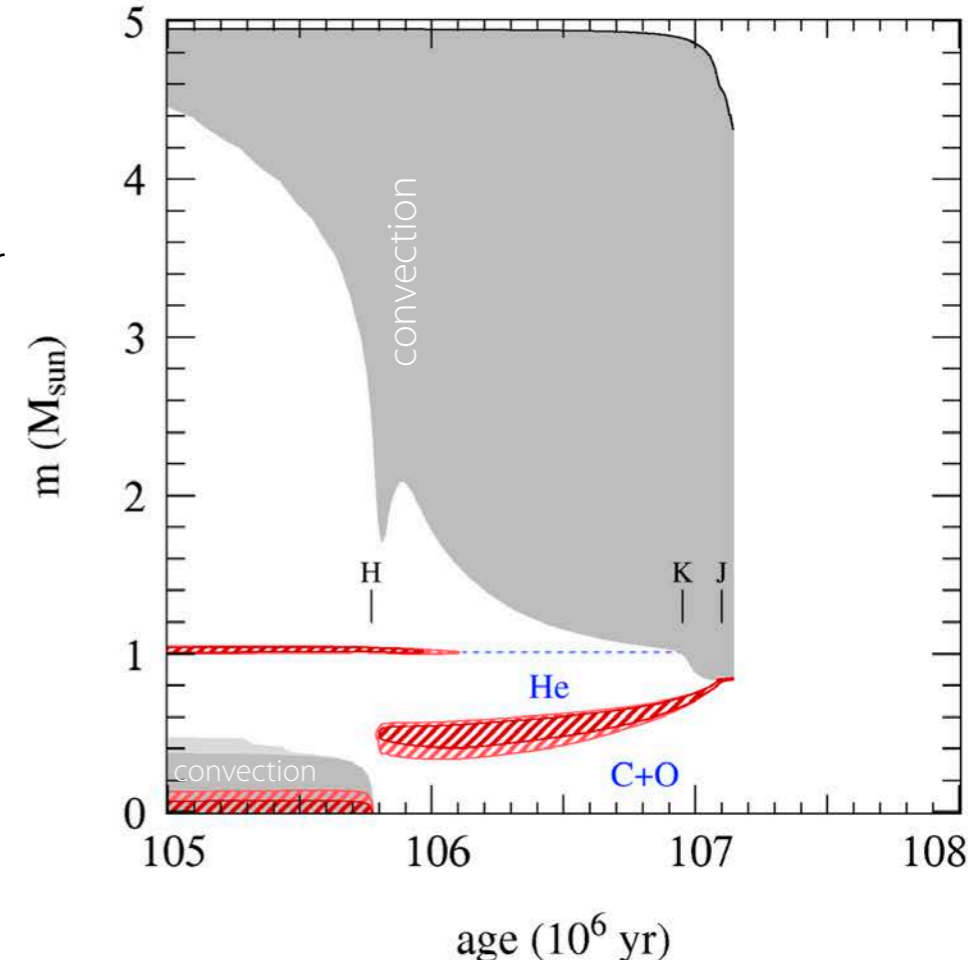
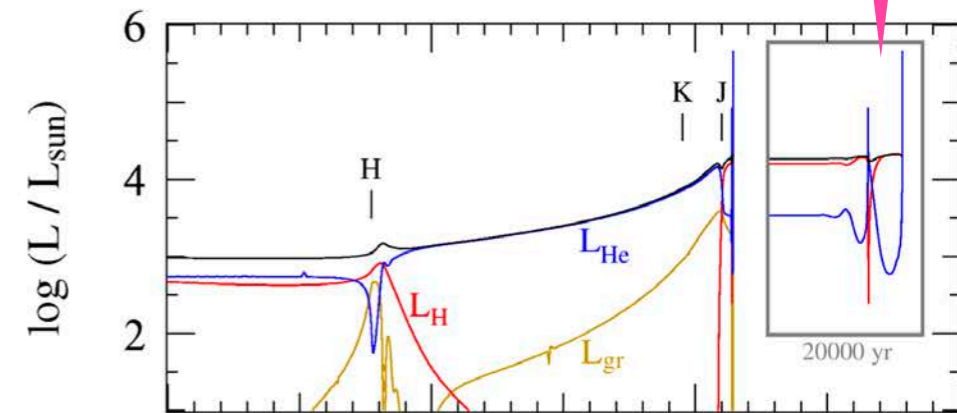
- **J**: H-burning shell re-ignites — Double shell-burning phase
- **Beyond J**: Radius of an AGB star typically (several) $1 \text{ AU} \sim 100$ solar radii
 - H shell active, providing “fresh” He to layers below.
 - He-shell burning switches on, pushes H-shell outwards, which then ceases
 - He burning eventually slows down again, H shell burning recovers
 - Several thermal pulses can occur pulses (not captured by shown model)



➔ Thermal Pulse (TP)-AGB phase

- $5 M_{\odot}$: period between initial pulses 10^3 - 10^5 yr
- Period is a function of mass

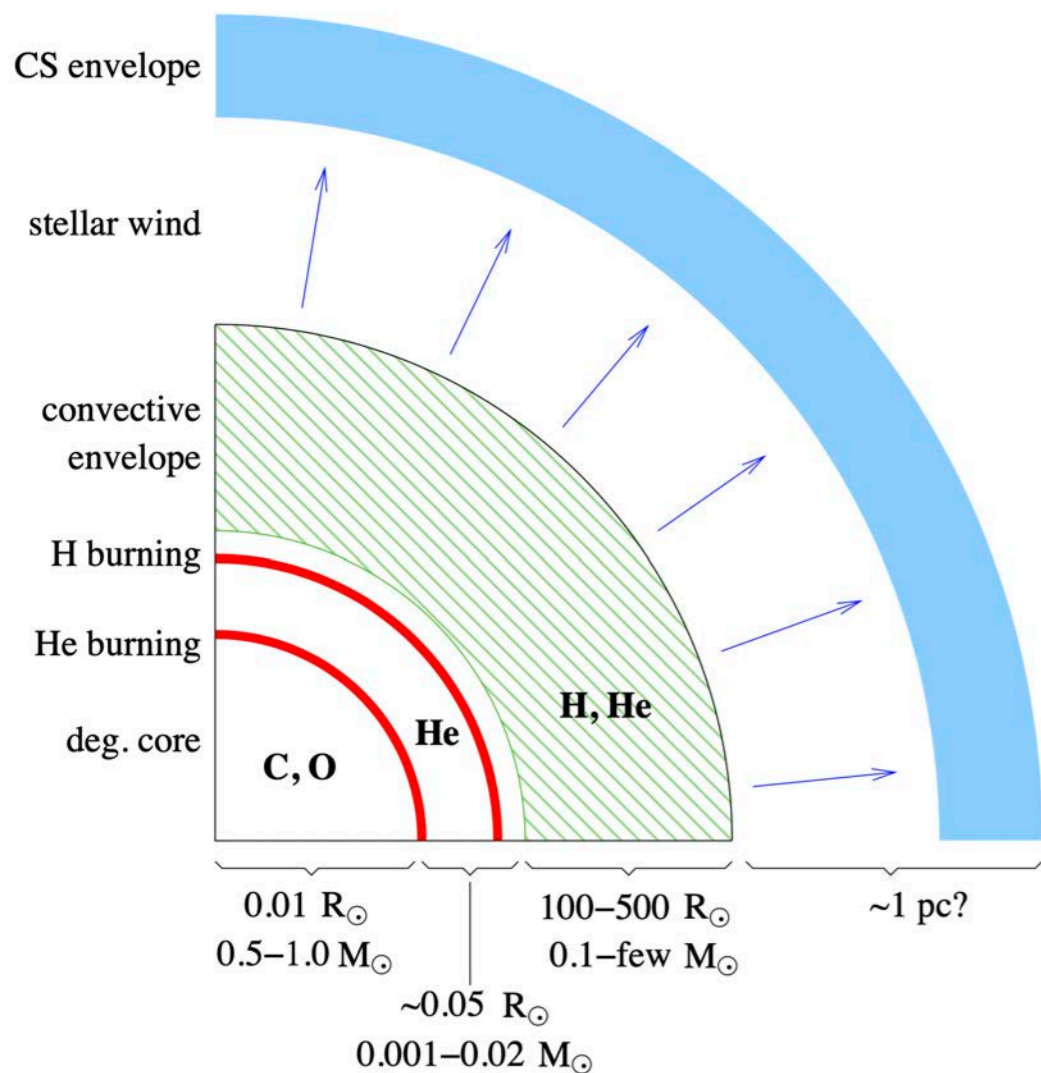
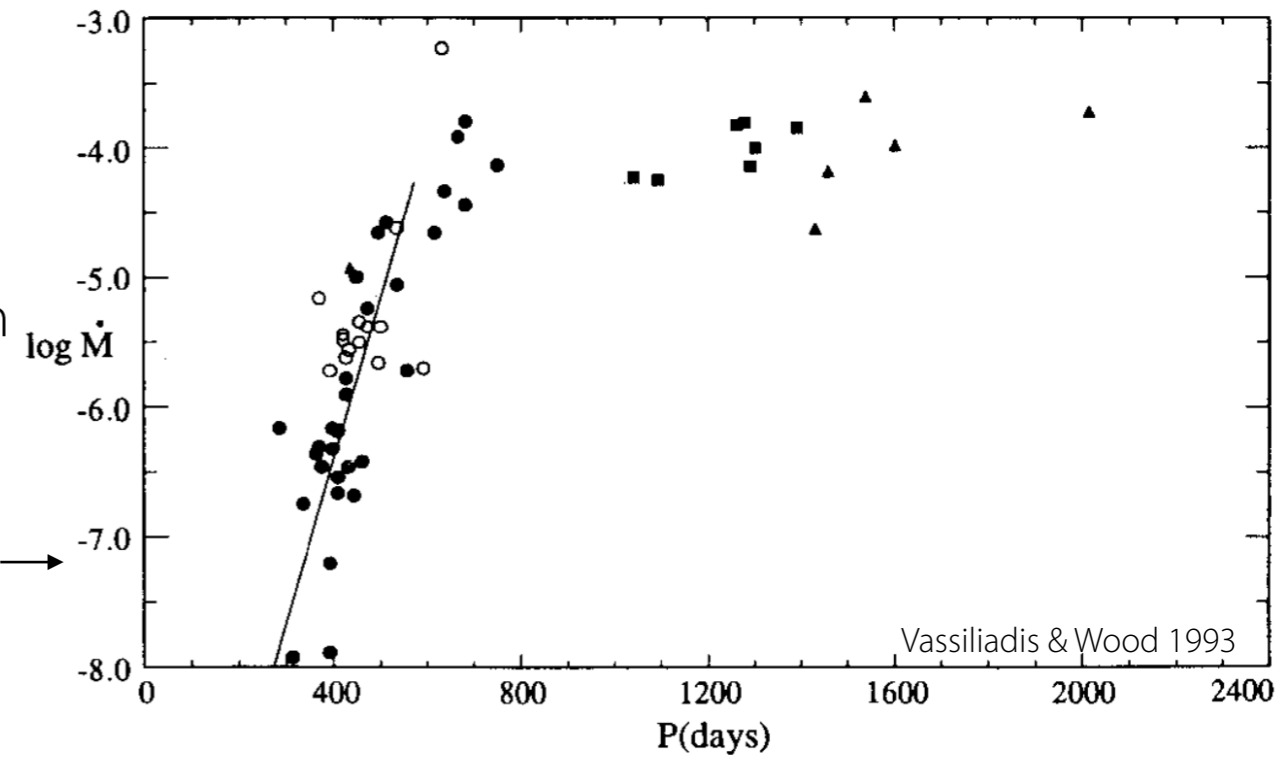
Thermal pulses



Post-main sequence evolution

Asymptotic Giant Branch

- **Thermal Pulse** (TP)-AGB phase
 - several pulses can occur
- **Strong mass loss** occurs in connection with pulsation but mechanism not fully understood (pulsations + radiation pressure on dust particles !?)
 - Observed mass loss as function of pulsation period →

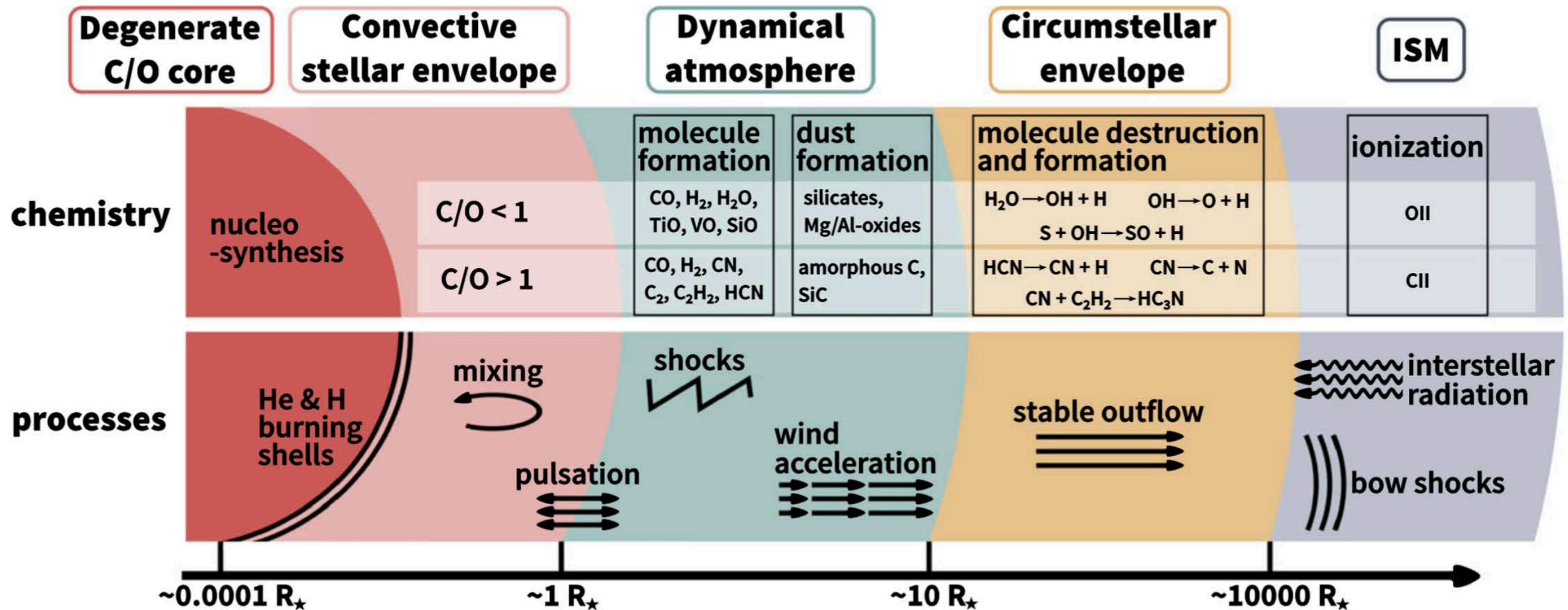


- Star evolves towards larger radii along AGB
 - ➡ Pulsation period increases
 - ➡ Mass-loss rate increases from $10^{-8} M_{\odot}/\text{yr}$ to $\sim 10^{-4} M_{\odot}/\text{yr}$
- Strongest mass loss sometimes referred to as **superwind** phase
- Pulsation periods of several years
- Pulsations induce shock waves
- Envelope expelled within $< 10^6 \text{ yr}$
- Remnant: Degenerate CO core — cooling white dwarf.

Post-main sequence evolution

Asymptotic Giant Branch (AGB)

- Circumstellar environment around AGB stars:
 - Complicated chemistry of the CSE
 - Detailed formation and destruction of molecules and dust grain important
 - Impact on chemical abundances

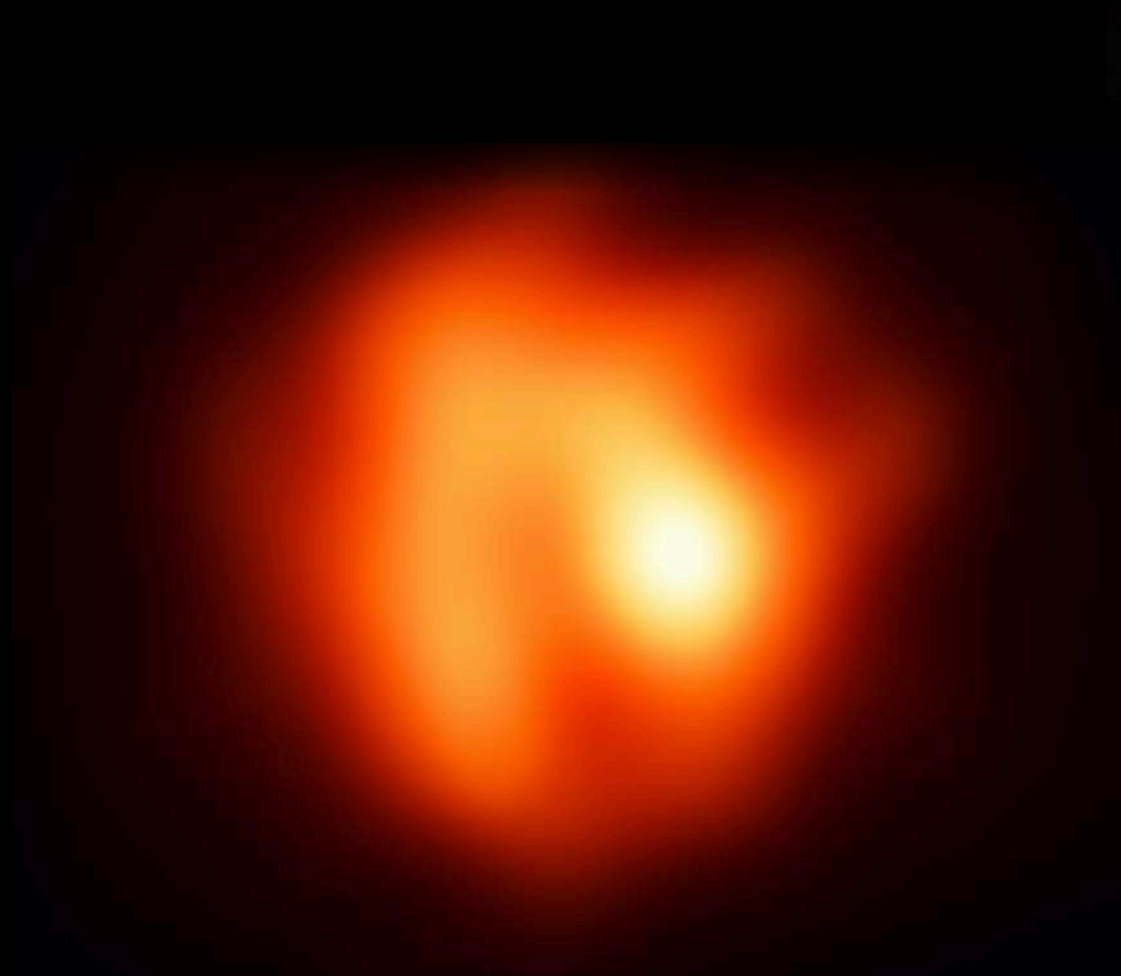


Post-main sequence evolution

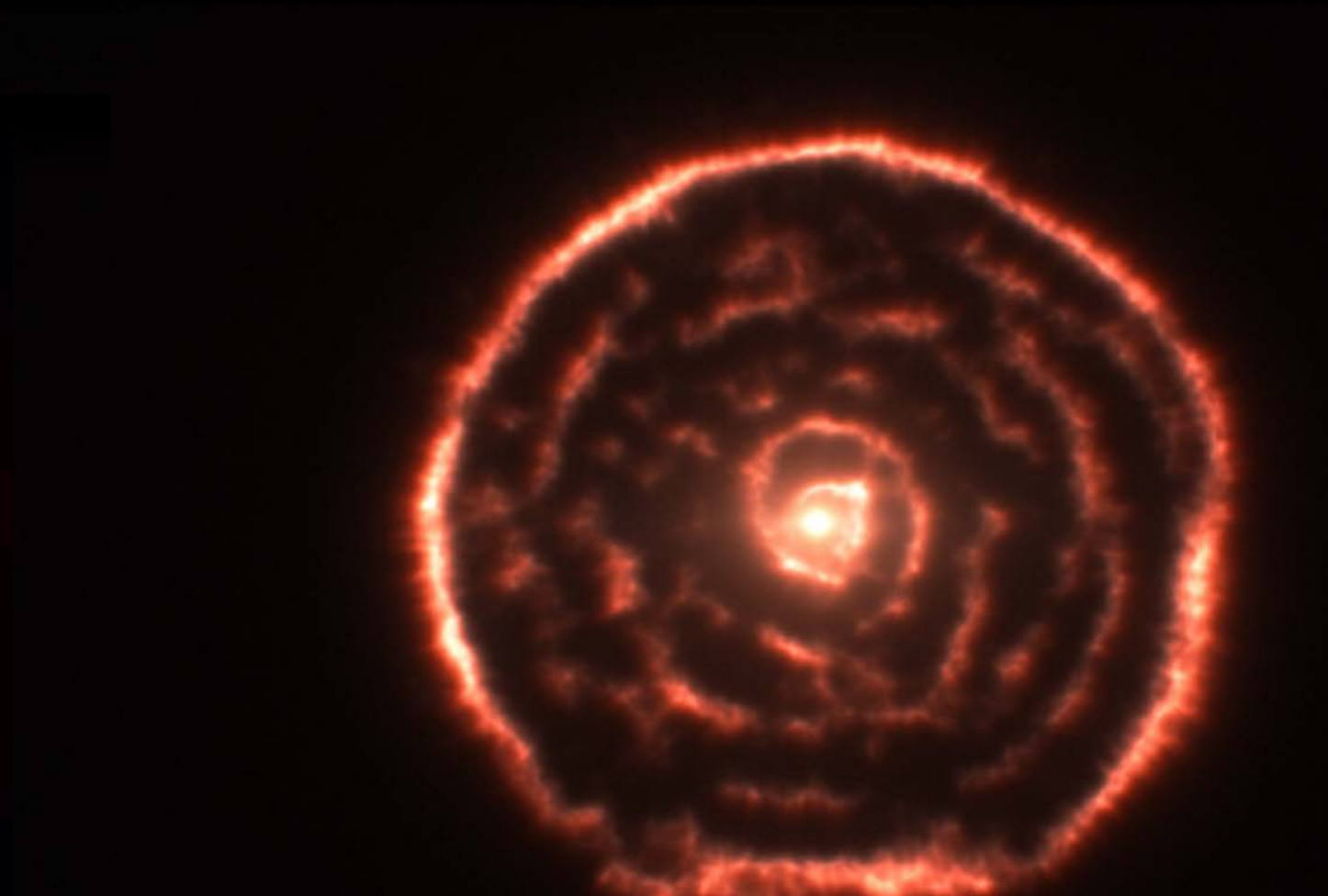
Asymptotic Giant Branch (AGB)

R Sculptoris

- $R \sim 340 R_{\odot}$ — if at Sun's location, its photosphere would reach beyond the orbit of Mars!
- Strong mass loss — expulsion of envelope and production of (inhomogeneous) circumstellar envelope (CSE)
- Contains dust and molecules



VLT/PIONEER — optical interferometry
(9mas diameter) [ESO/M. Wittkowski]



ALMA — mm interferometry
(345 GHz, CO) [ALMA / M. Maercker et al.]

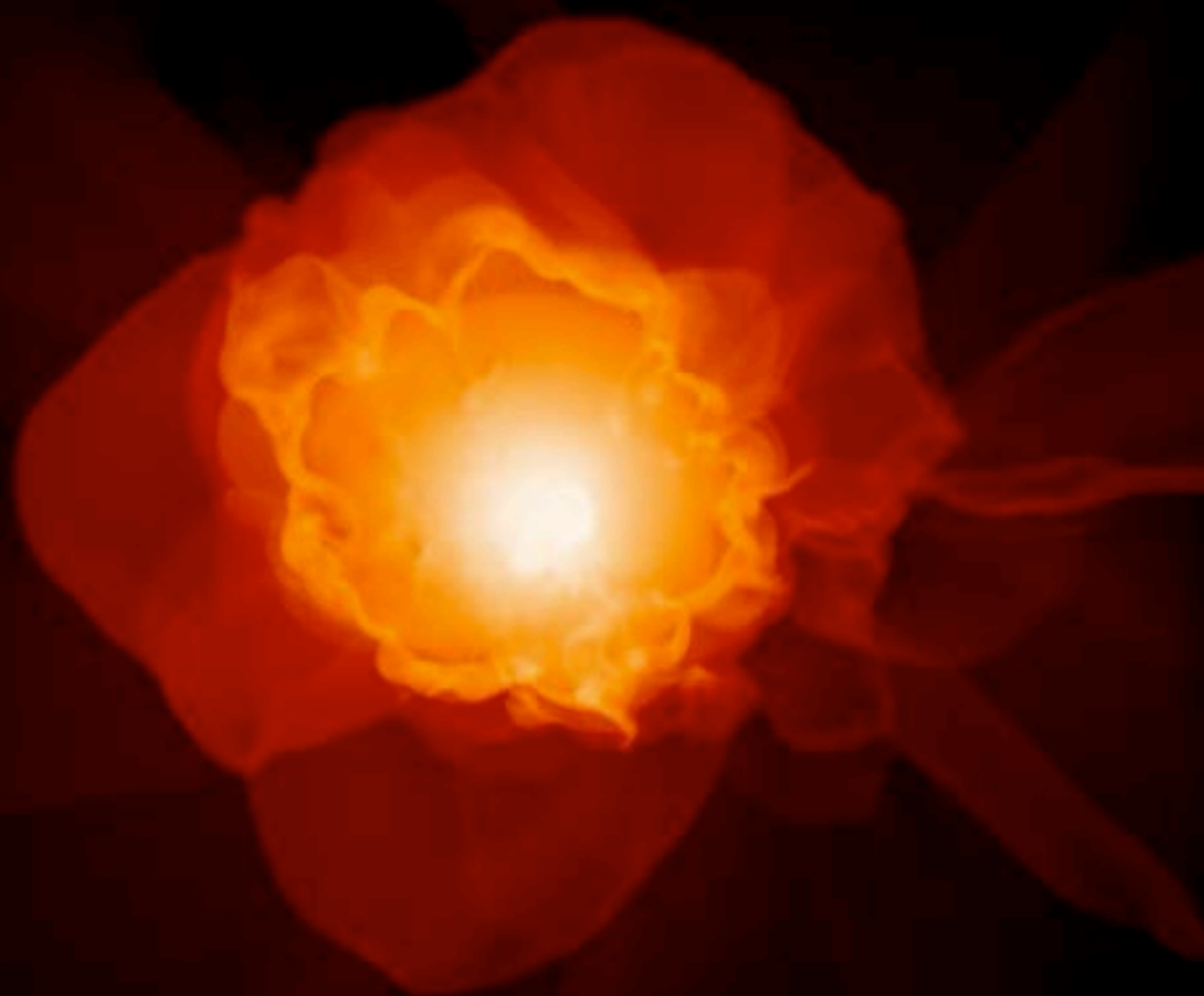
Post-main sequence evolution

Asymptotic Giant Branch (AGB)

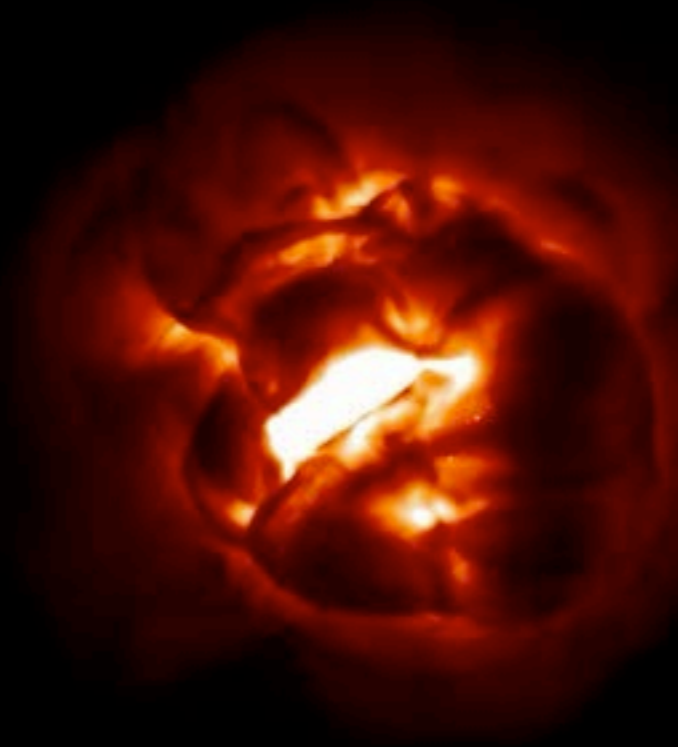
- Numerical simulation of an AGB star (star-in-a-box): $1 M_{\odot}$, $400 R_{\odot}$
 - Possible due to the large size of convection cells and long time scales

st28gm06n25: Density, time(1)= 6.346 yrs

st28gm06n25: Surface Intensity(3r), time(1)= 6.346 yrs



Log. mass density



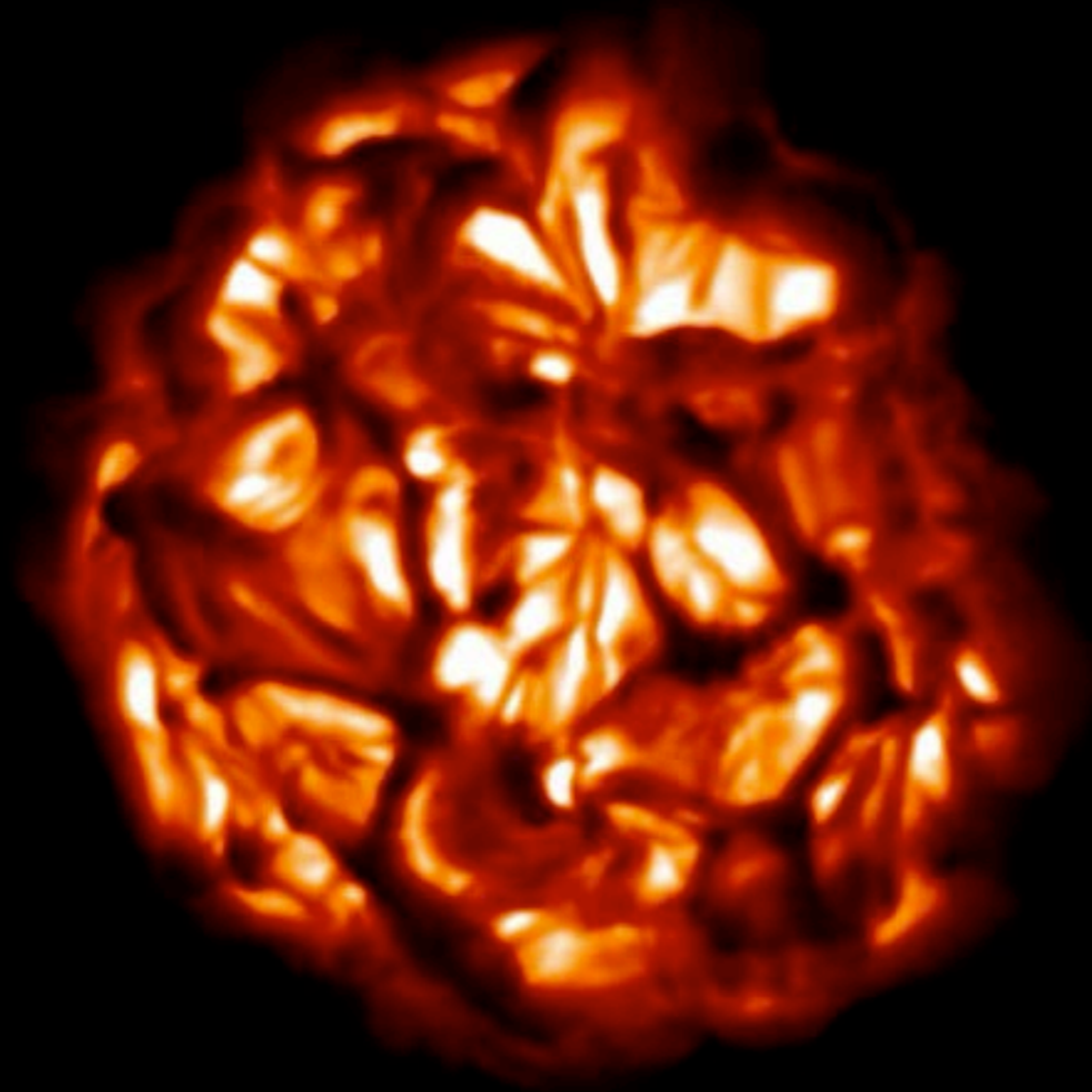
Emergent bolometric intensity

Post-main sequence evolution

Red supergiant

- Numerical simulation of a magnetic red supergiant ($5 M_{\odot}$)

st35gm04b1n004: Surface Intensity(3r), time(1)= 51.383 yrs



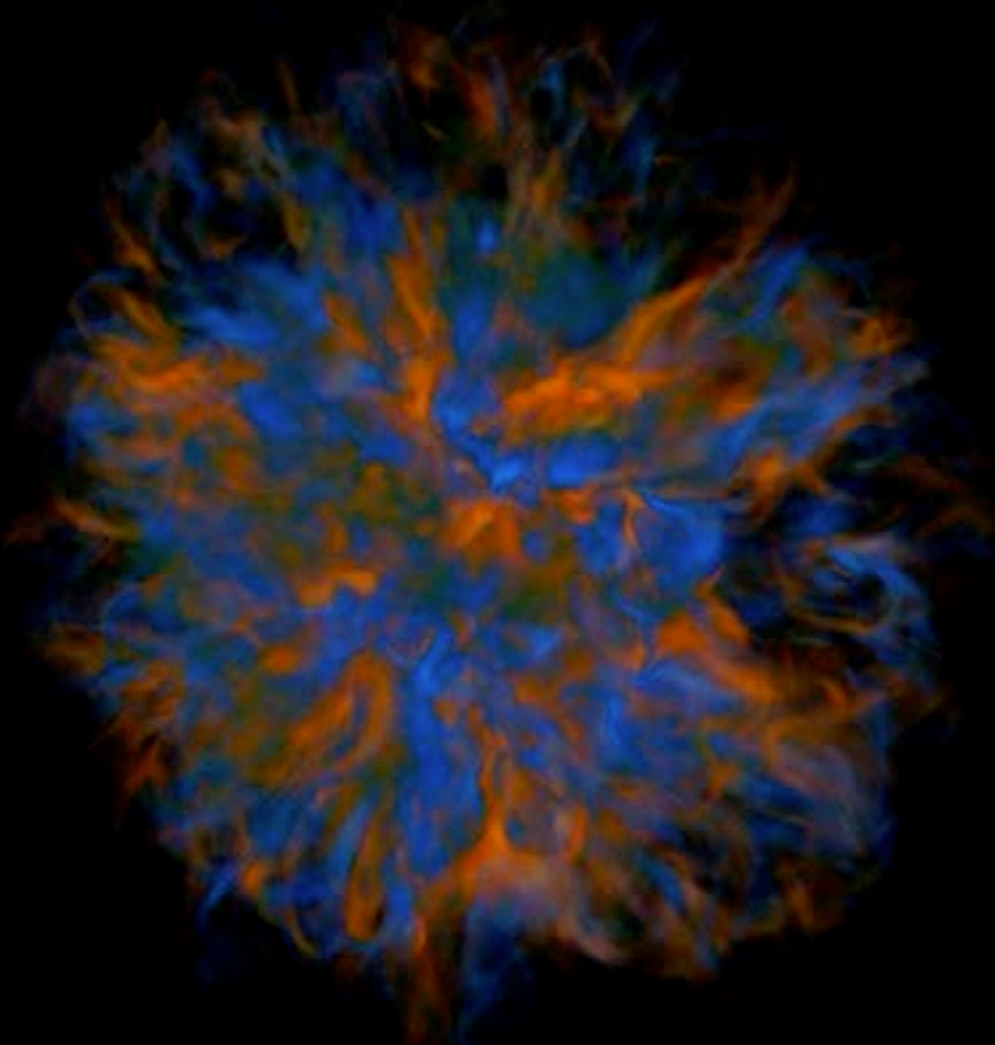
Surface intensity

Post-main sequence evolution

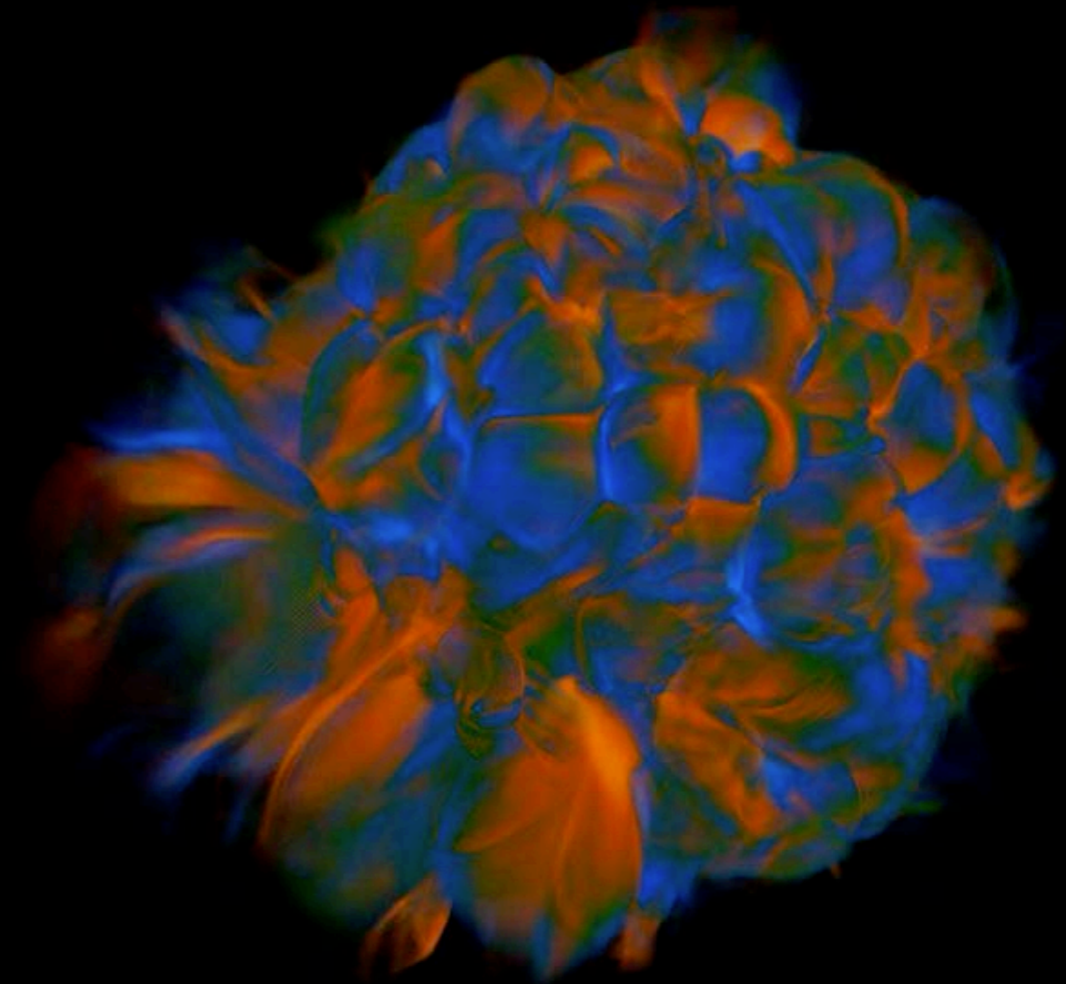
Red supergiant

- Numerical simulation of $5 M_{\odot}$ red supergiant

Volume rendering of the magnetic field



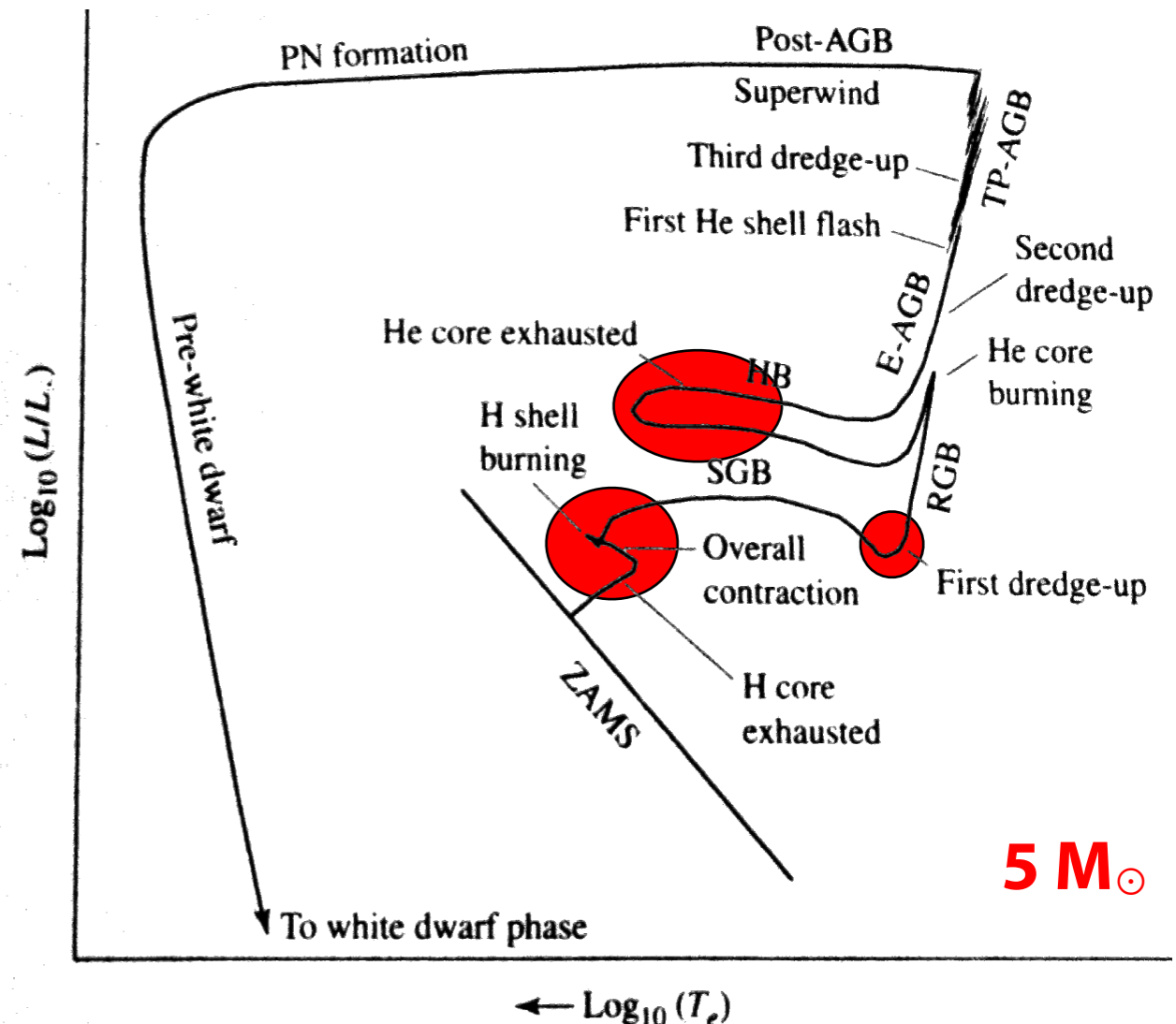
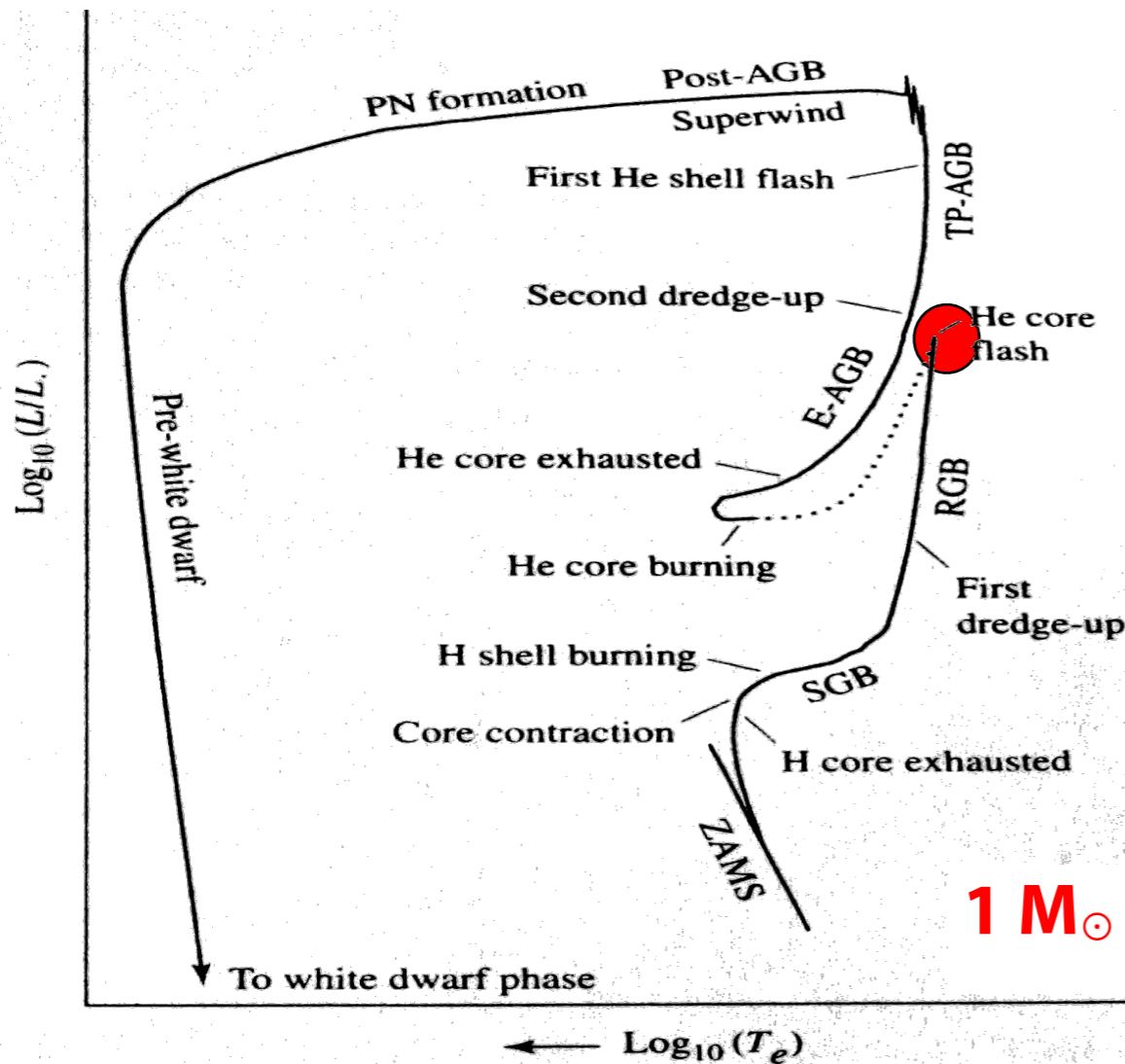
Interior



Surface

Post-main sequence evolution

Comparison low-mass to intermediate-mass evolution

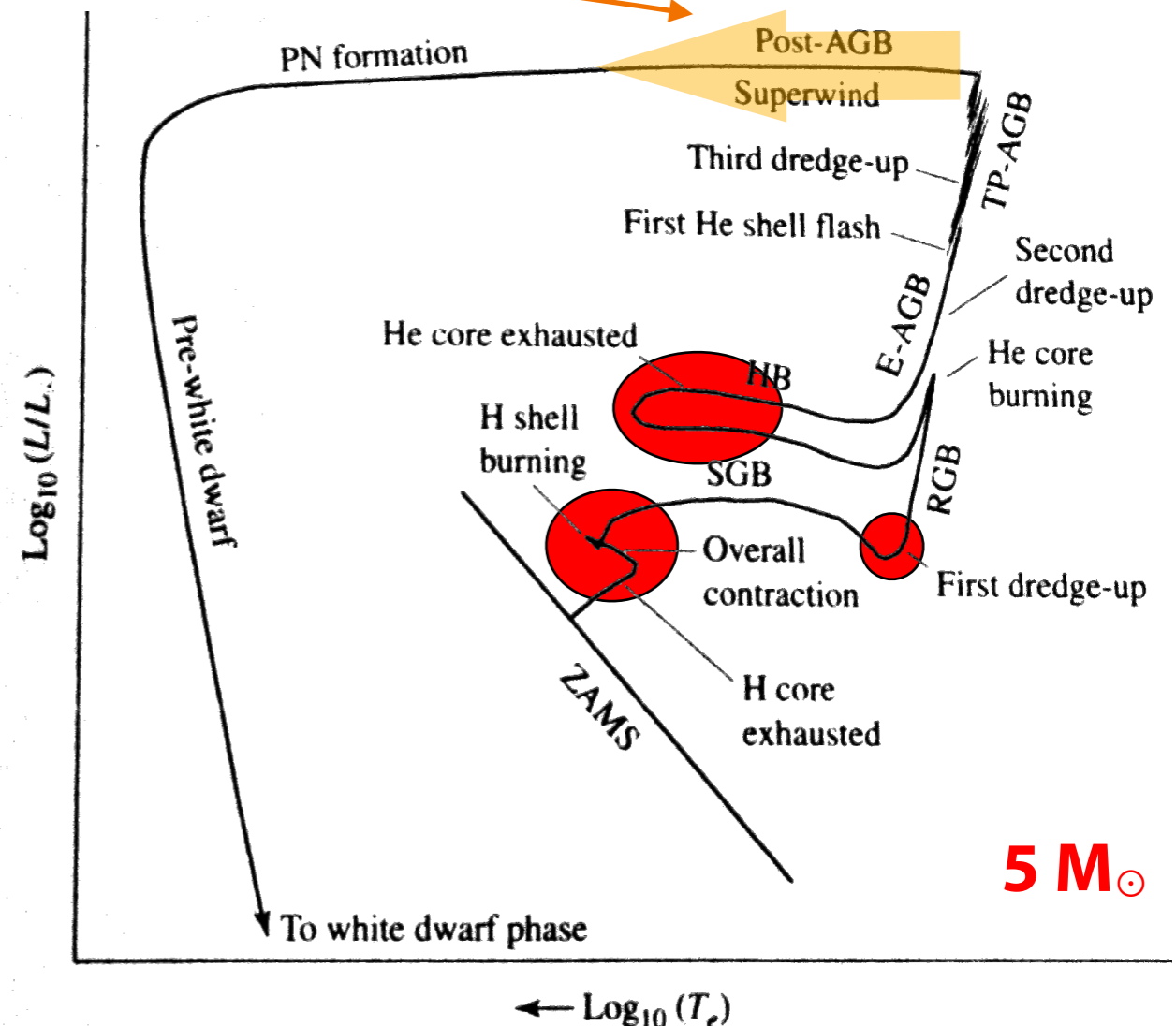
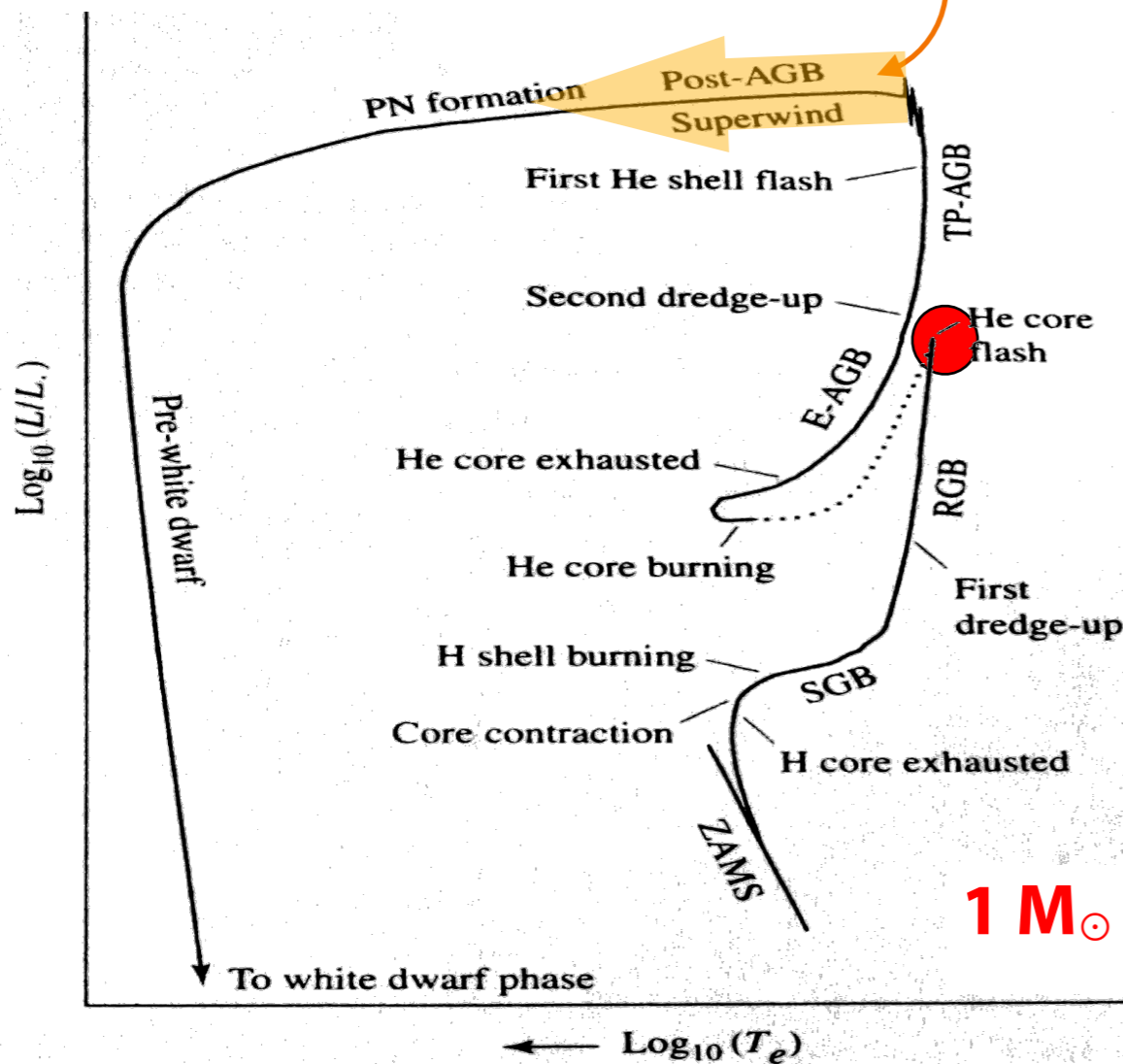


- He core flash at tip of RGB phase

- Larger temperature differences on the horizontal branch
- Helium flash in shell
- Instabilities - variable stars

Post-main sequence evolution

Post-AGB evolution

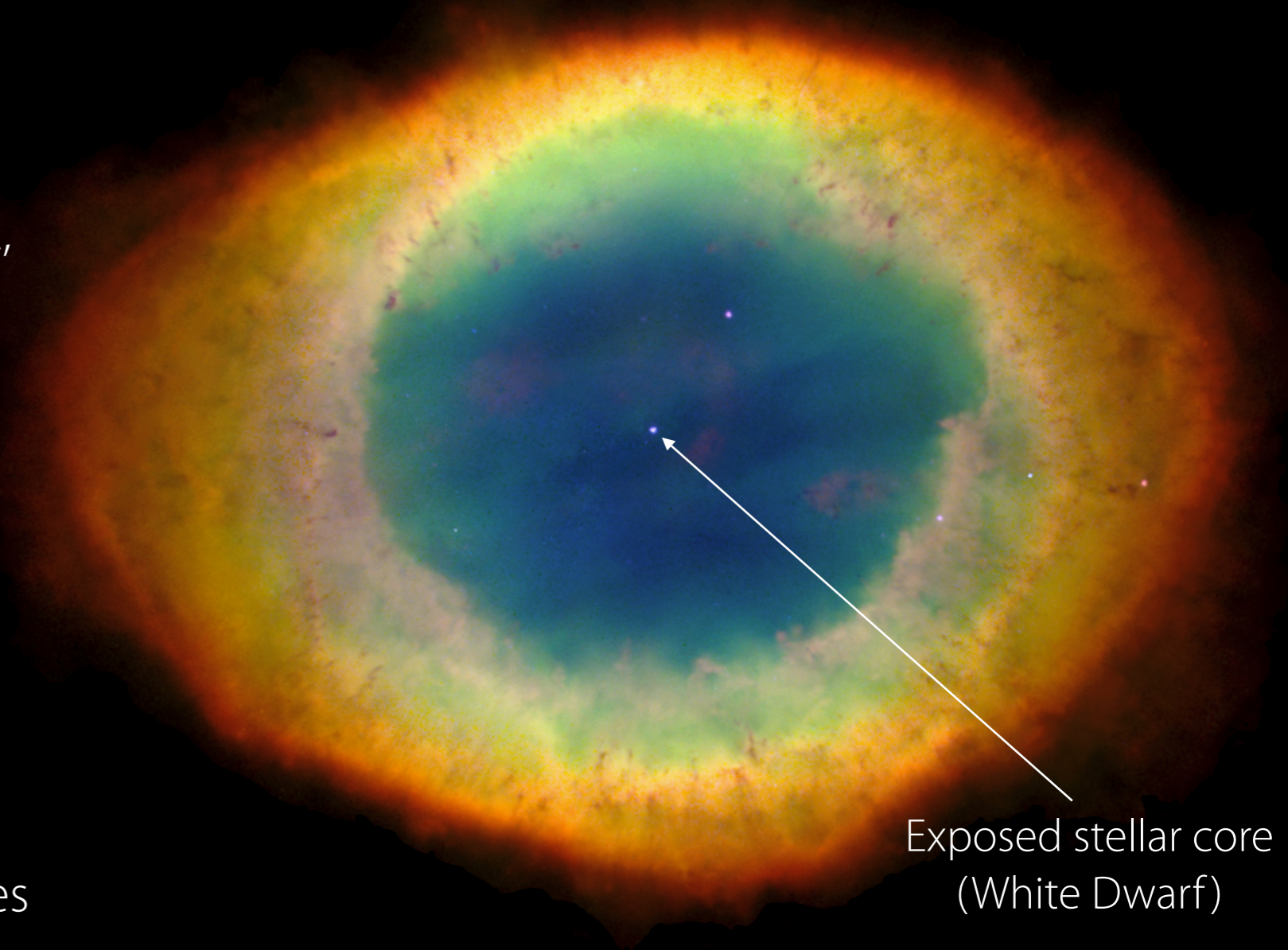


- H-rich envelope becomes very small due to mass loss (only 10^{-3} - $10^{-2} M_{\odot}$ left depending on core mass)
- Star leaves AGB — stellar radius decreases at \sim constant luminosity (horizontal track in HRD) as H-burning shell is still fully active (obeys core mass-luminosity relation)
- Typical timescale for post-AGB phase is $\sim 10^4$ yrs.

Post-main sequence evolution

Planetary nebula

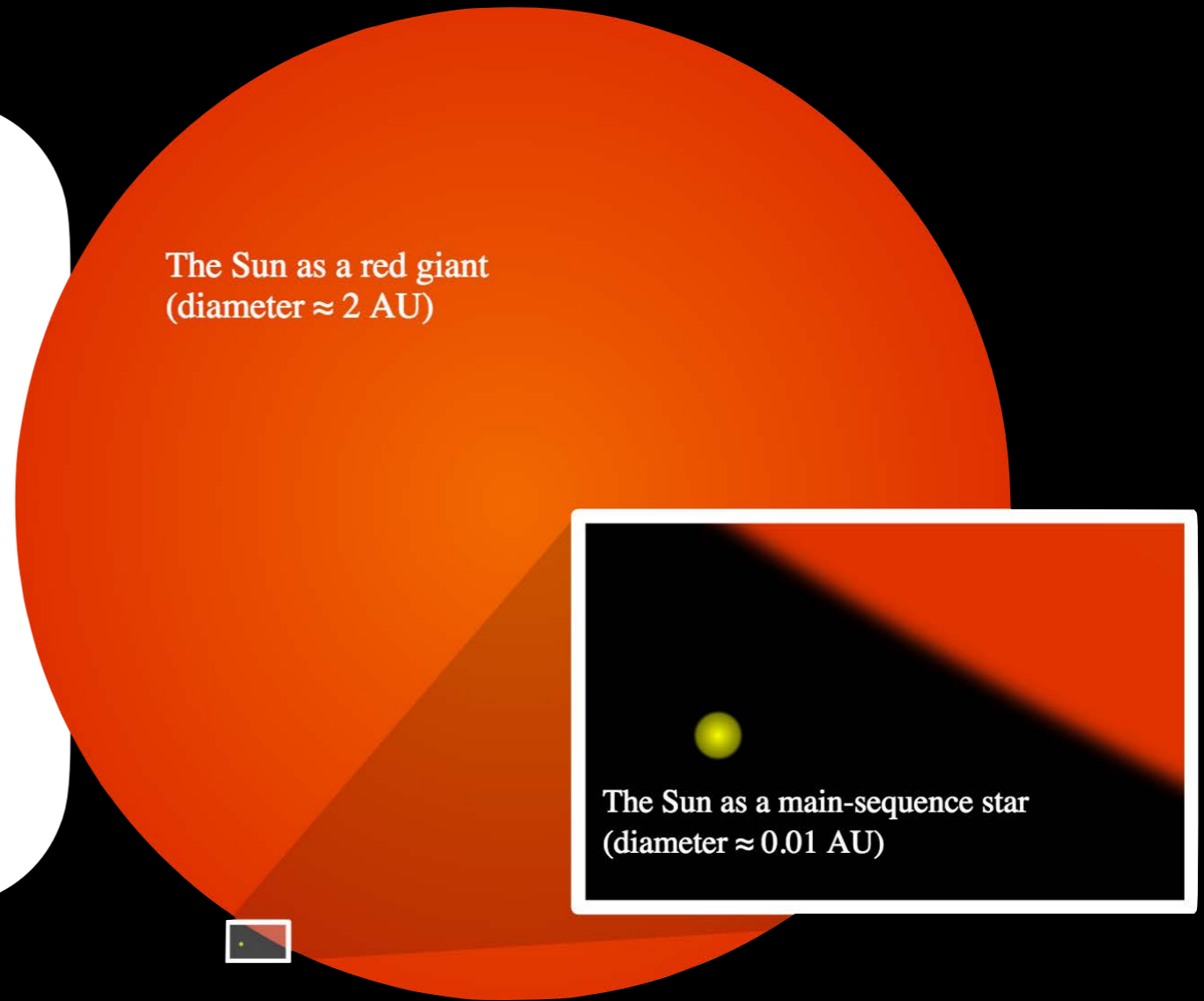
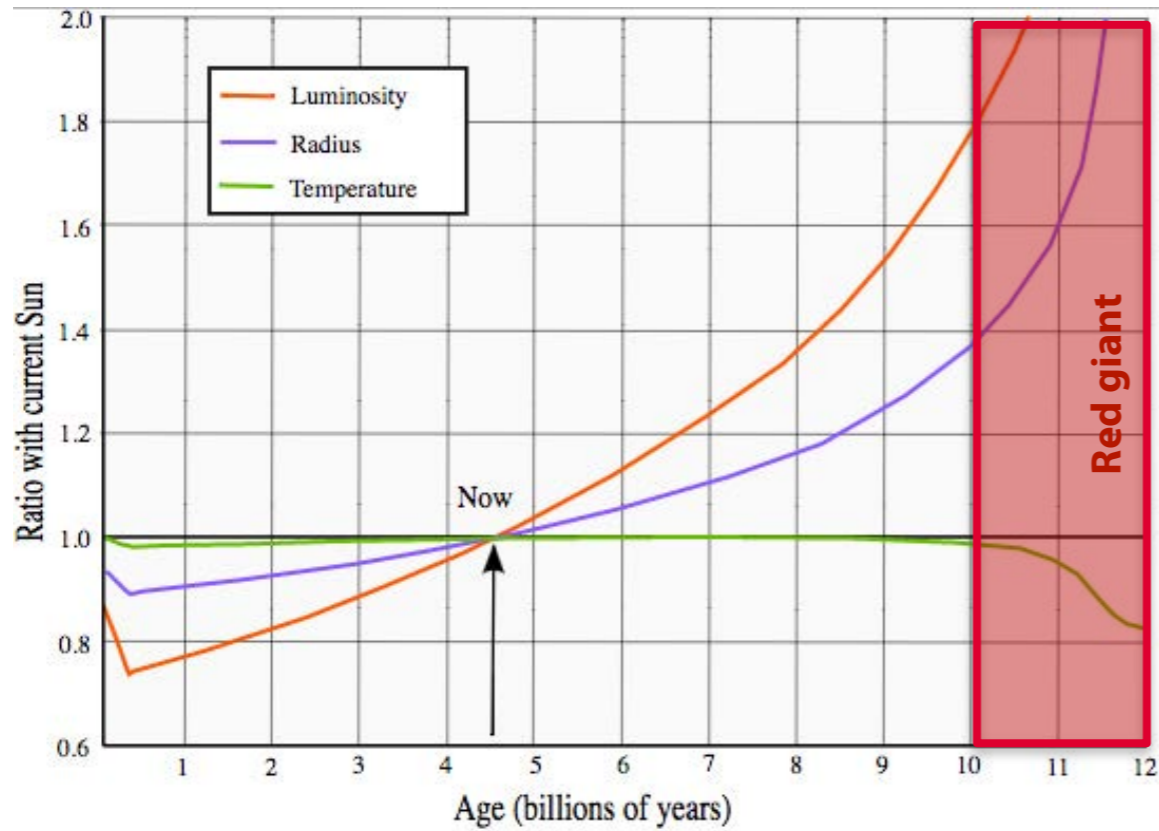
- When reaching $T_{\text{eff}} > 30\,000\text{ K}$:
 - weak but fast wind develops
 - strong **UV** flux
- ➔ Destroys the dust grains in CSE, dissociates molecules, ionises gas
- ➔ Part of CSE turns into an HII region, appears as **planetary nebula**
 - (Emission: fluorescence from recombination)
- H-burning shell finally extinguishes once envelope mass down to $\sim 10^{-5} M_{\odot}$ (at $T_{\text{eff}} \approx 10^5\text{ K}$)
- Exposed stellar core = White Dwarf



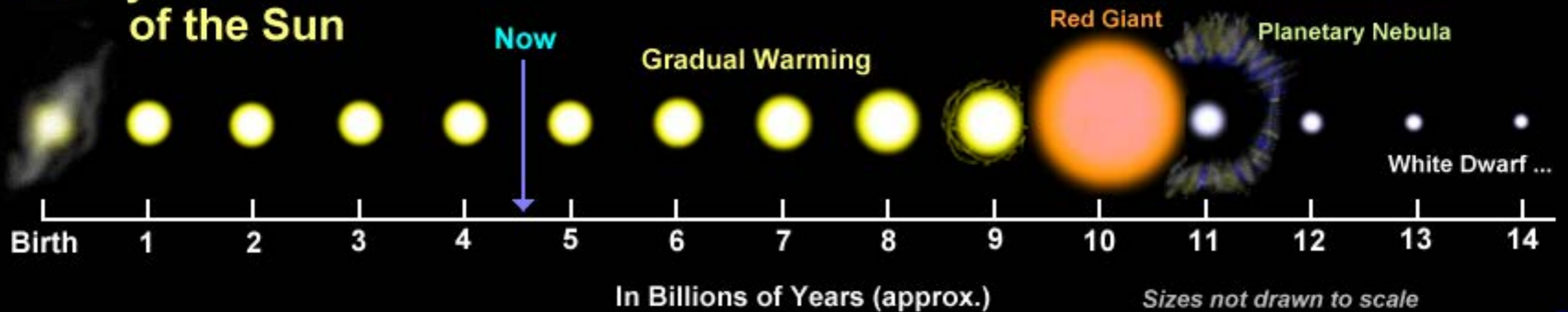
Exposed stellar core
(White Dwarf)

Solar evolution

RJHall/Ribas, Ignasi; DOI:10.1017/S1743921309992298, CC BY-SA 3.0, <https://commons.wikimedia.org/w/index.php?curid=16799327>



Life Cycle of the Sun



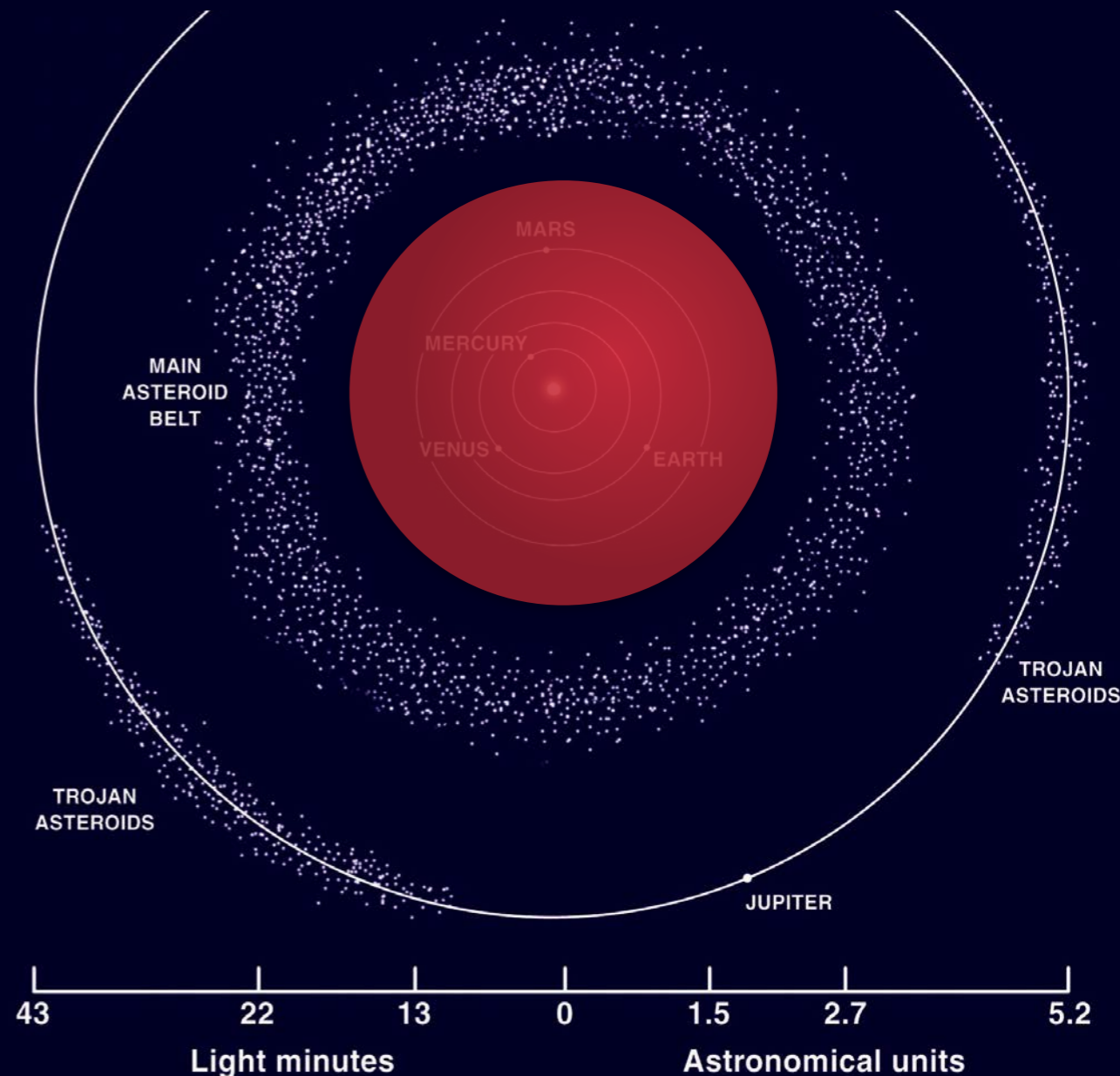
By Oona Räisänen (User:Mysid), User:Misanitazier. - Vectorized in Inkscape by Mysid on a JPEG by Misanitazier (en:Image:Sun Red Giant2.jpg), CC BY-SA 3.0, <https://commons.wikimedia.org/w/index.php?curid=2585107>

Solar evolution

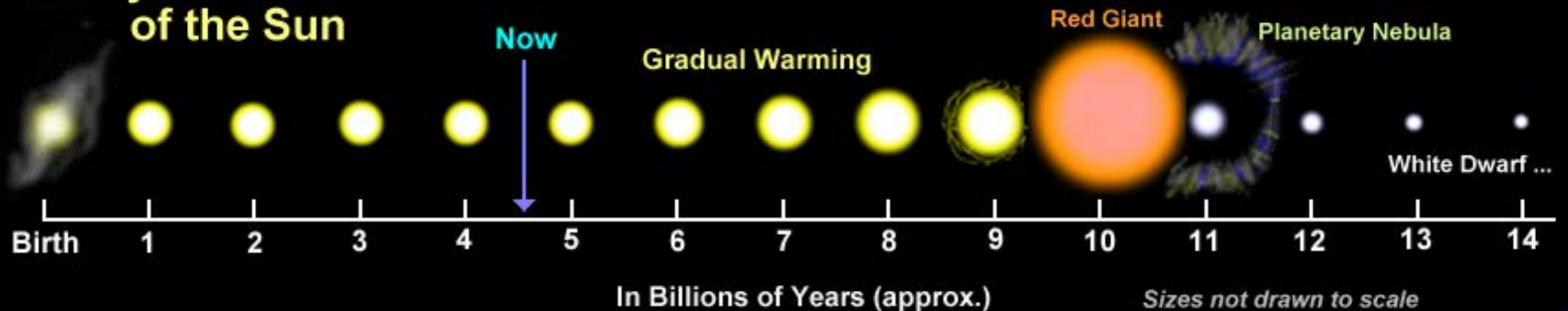
Late evolution stages

- **Red giant star**
- High radiation pressure in the star's interior makes the radius large
- The surface becomes large.
- Radiation is spread over a large area:
 - ➔ Low surface temperature
 - ➔ Low surface gravity

Increase of the Sun's diameter from 0.01 AU to 2 AU



Life Cycle of the Sun

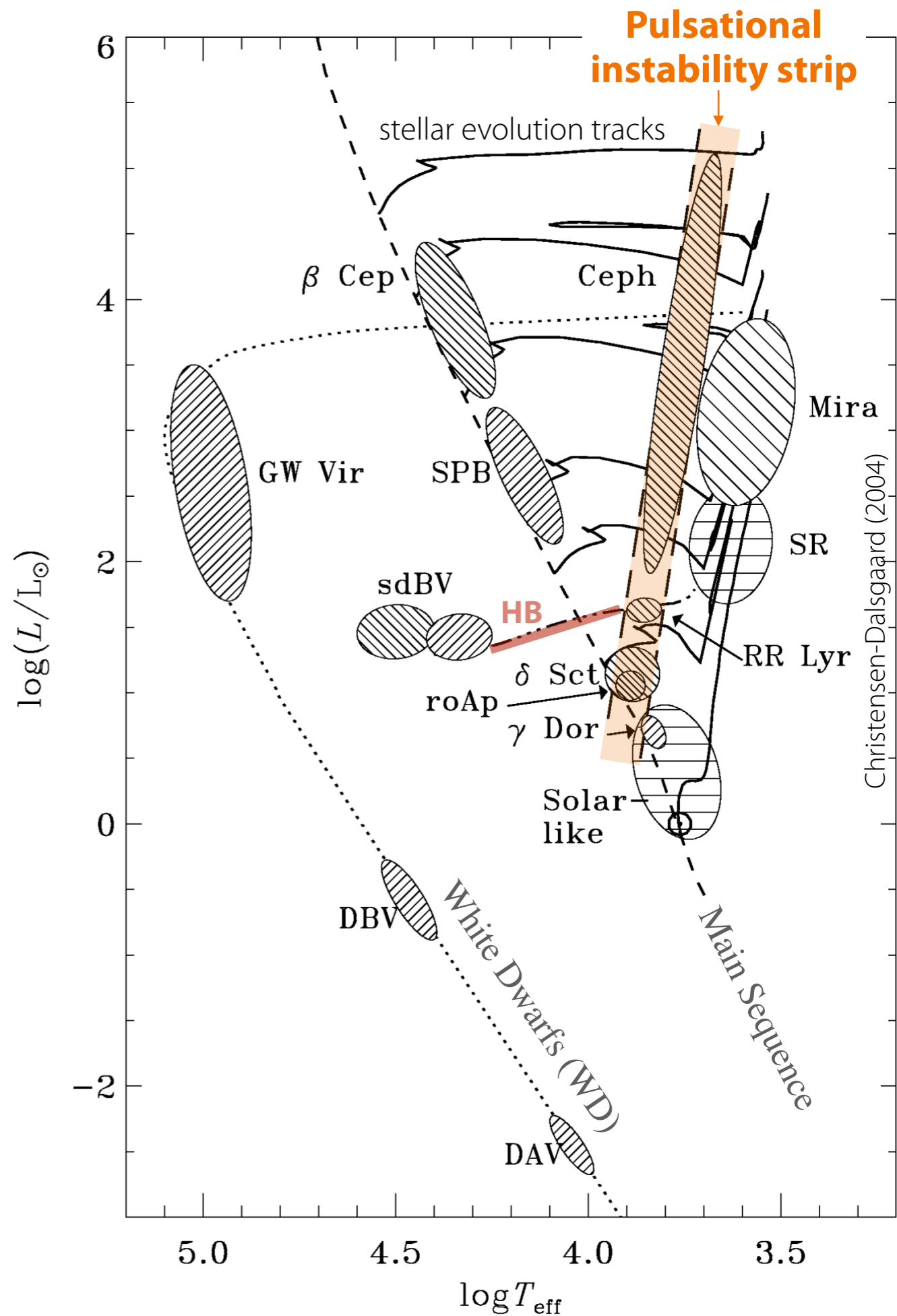


Pulsating and Variable stars

Pulsating and Variable stars

Classes

- Different classes of variables within the **pulsational instability strip**:
 - Cepheid variables: He-burning stars during blue loop (3 - 18 M_{\odot})
 - RR Lyrae variables (0.5 - 0.7 M_{\odot} , on horizontal branch, HB)
 - δ Scuti stars on main-sequence
 - Mira variables: luminous red giants
 - β Cep variables and slowly pulsating B (SPB) stars: massive main-sequence stars
 - Subdwarf B stars (sdBV) on extreme end of HB
 - White dwarfs
- Intermediate-mass stars cross instability strip up to three times during evolution: once during H-shell burning, twice during blue loop phase



Pulsating and Variable stars

Prominent classes

Cepheid variables:

luminous pulsating stars with periods ~ 2 -100 days

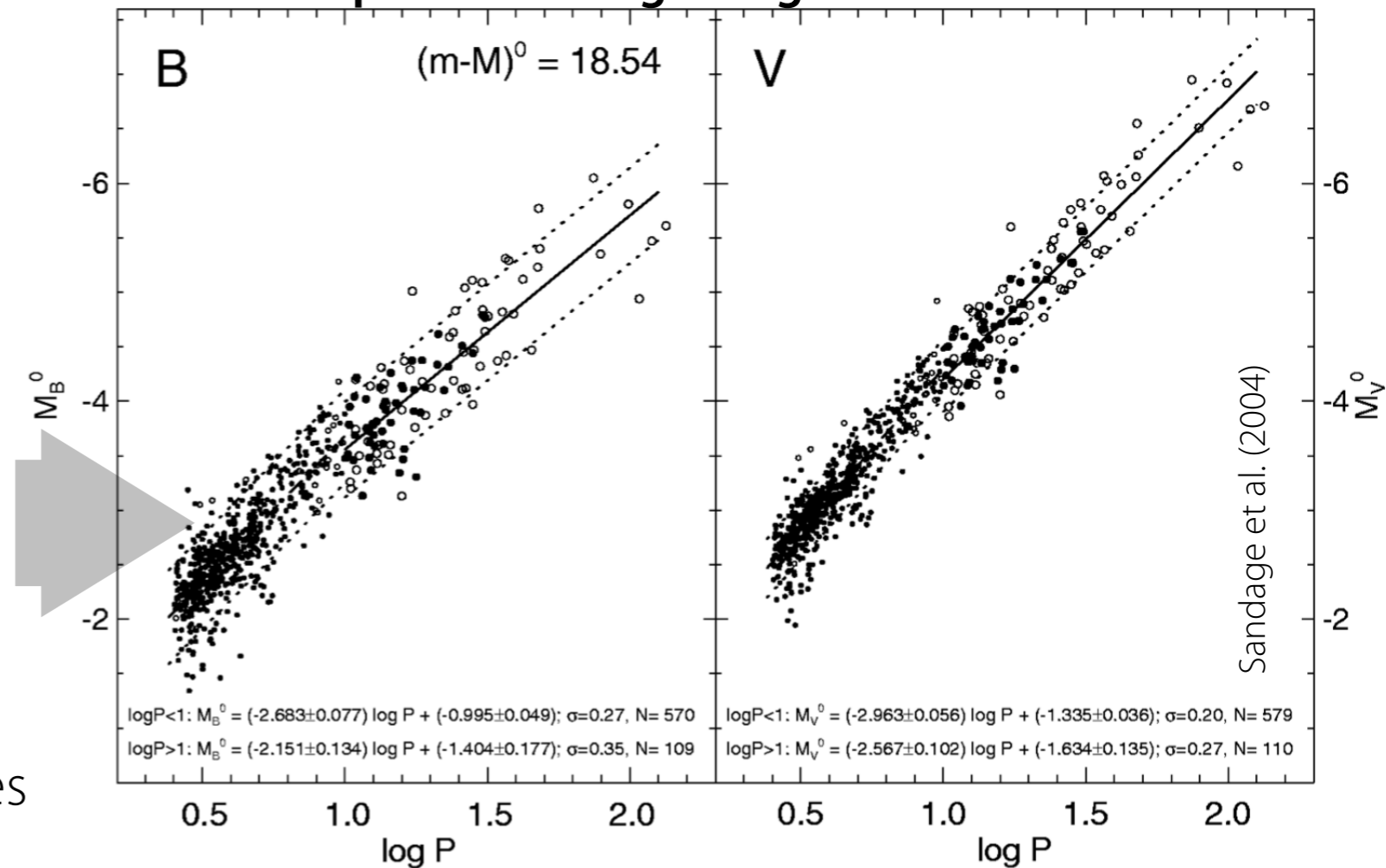
- Well-defined correlation between pulsation period and luminosity
 - Can be seen in other galaxies
 - Measured period gives luminosity / absolute brightness
 - Absolute vs. apparent brightness (distance modulus!) gives distance
- ➔ Cepheids important standard candles for the extragalactic distance scale.

$$m * M = 5 \log r [\text{pc}] * 5 + A$$

RR Lyrae stars: Short periods of 1.5 - 2.4 h

- $L \sim 100 L_{\odot}$ ($M_V = 0.5 = \text{const}$) independent of period.
- Fainter, seen in globular clusters, but not in other galaxies

Period-luminosity relation for Cepheids in Large Magellanic Cloud



Mira variables: Periods ~ 100 -700 days

- Large, irregular brightness variations
- Cool stars (2000 K) (He-shell burning)
- Strong absorption by dust + molecules
- Local T enhancements dissociate molecules, lead to increased L

Pulsating and Variable stars

Pulsational instability

- **Pulsation = radial oscillation** = standing sound wave (pressure!) resonating in stellar interior
- Radial pulsation modes:
 - Fundamental mode (one node at the centre, open end at stellar surface)
 - Overtone modes (additional nodes between the centre and surface)
 - Most radially pulsating stars, such as Cepheids, oscillate in fundamental mode.



Pulsating and Variable stars

Pulsational instability

- Two possible mechanisms that can drive pulsations:
 - **ϵ -mechanism**: Compression of region with nuclear burning results in temperature increase and thus increased energy generation rate ϵ_{nuc} .
 - ➔ Instability
 - In principle always present but amplitudes of induced oscillations usually too small to drive significant pulsations (potentially relevant for very massive stars though)
 - **κ -mechanism**: Layer is compressed so that density and opacity increases
 - Energy flux through this layer impeded, heating of the layer locally
 - Pressure increases and expands / pushes the layer outward.
 - Gas becomes more transparent again and releases trapped heat.
 - Can drive radial pulsations.
- Note: Some layers absorb heat and do work to drive the pulsation, while other layers may lose heat and thus damp pulsations

Pulsating and Variable stars

Pulsational instability

- Condition for κ -mechanism: opacity must increase when gas is compressed.
 - ➔ Depends on the temperature dependence of opacity sources in driving layer
 - ➔ Interior stratification (temperature, density)
 - ➔ Partial ionisation zones inside star
 1. At $T \approx 1.5 \cdot 10^4$ K: ionisation and recombination of H and He (singly ionised)
 2. At $T \approx 4 \cdot 10^4$ K: ionisation and recombination of He (fully ionised, He III)
 - ➔ location of instability strip in H-R diagram!

$T_{\text{eff}} > 7500$ K — 'blue edge'	Instability strip	$T_{\text{eff}} < 5500$ K — 'red edge'
Both ionisation zones near surface (very low density!)	Ionisation zones located deeper in interior	Partial ionisation zones lie at very high density
Region non-adiabatic, mass and heat capacity too small to drive pulsations effectively	Mass and heat larger but still non-adiabatic enough to absorb sufficient heat to drive pulsations	Gas near adiabatic. Cannot absorb enough heat to drive pulsation.

Pulsating and Variable stars

Non-pulsating Variables

- **T Tauri stars:** PMS objects of $0.2 - 2 M_{\odot}$: Young objects with rapid rotation, fully convective, strong magnetic fields, flares, stellar wind; circumstellar absorbing clouds
- **Flare stars:** "solar-like" stars, rapid rotation + deep convection, magnetic fields — can exhibit super/megaflares
- **Magnetic variables - Ap stars** (spectral type A, peculiar): strong magnetic fields, relatively small brightness changes possibly due to star spots.
- **RS CVn (Canum Venaticorum) stars:** very close double stars (orbital periods of 0.5 day to several months), starspots. probably magnetically interacting, resulting in strong flares
 - Components of different luminosity classes (V + IV, i.e. main-sequence + sub-giant)
- **Luminous blue variable (P Cygni):** Very massive stars (hypergiant, $>50 M_{\odot}$) with irregular outbursts, possibly due to mass inflow from binary companion
- **Eclipsing binaries**

Pulsating and Variable stars

Overview over classes of pulsating variables

Type	Prototype	M_V	Spectral Class	Pulsation Period Range	Characteristic Period
Classical Cepheids	d Cephei	-0.5 to -6	F6 to K2	1d to 50d	5d to 10d
Population II Cepheids	W Virginis	0 to -3	F2 to G6	2d to 45d	12d to 28d
RR Lyrae stars	RR Lyrae	0.5 to 1	A2 to F6	1.5h to 24h	0.5d
Long-Period variables	o Ceti (Mira)	1 to -2	M1 to M6	130d to 500d	270d
RV Tauri stars	RV Tauri	-3	G, K	20d to 150d	75d
Beta Canis Majoris stars	b Canis Majoris	-3	B1, B2	4h to 6h	5h
Semiregular red variables	a Herculis	-1 to -3	K, M, R, N, S	100d to 200d	100d
Dwarf Cepheids	d Scuti	4 to 2	A to F	1h to 3h	2h

Pulsating and Variable stars

Overview over classes of cataclysmic variable stars

Type	Time	Example	M_{\max}	Dm	Energy per Outburst (J)	Cycle	Mass Ejected per Cycle (M_{\odot})	Velocity of Ejection (km/s)	Mass of Star (M_{\odot})
Supernova I		Tycho's	-20	>20	10^{44}		< 1	10,000	1
Supernova II			-18	>20	10^{43}		?	10,000	>4
Novae	Fast	GK Per = Nova Per	-8.5 to -9.2	11 to 13	6×10^{37}	10^6 y ?	10^{-5} to 10^{-3}	500 to 4000	1 to 5
	Slow	DQ Her	-5.5 to -7.4	9 to 11				100 to 1500	0.02 to 0.3
	Recurrent	T Cr B	-7.8	8	10^{37}	18 to 80 y	5×10^{-6}	60 to 400	2
Dwarf Novae		U Gem SS Cyg	+5.5	4	6×10^{31}	40 to 100 d	10^{-9}		~0.4

Variable stars / Binary stars

- List of common types of variable and binary stars

Name	Definition
Algol	Semi-detached binary system with a cool subgiant and an early-type companion, with mass transfer from the Roche-lobe filling secondary to the primary star, which has resulted in the more evolved star being the least massive.
ζ Aur	Eclipsing binary consisting of a bright K (super) giant and a hot B star.
BY Dra	The most active main-sequence emission-line stars of type dKe or dMe; many are binary systems.
FK Com	Very active, rapidly rotating, late-type single giants, possibly coalesced binaries.
RS CVn	In the strict definition, a close binary with stars of nearly equal masses, with the hotter component of spectral type F, G, or K, and luminosity class V or IV (but with the subgiant not filling its Roche lobe), with orbital periods between 1 day and 2 weeks. In the expanded definition, any tidally interacting binary system with at least a single cool star. RS CVn stars have negligible mass exchange.
UV Ceti	Red-dwarf flare stars, variable, either single or members of binaries.
T Tau	Irregularly variable pre-main-sequence stars.
W UMa	In the strict definition: eclipsing contact binaries of main-sequence stars. In the relaxed definition, semidetached systems are sometimes included.