

**AST5770**  
**Solar and stellar physics**

University of Oslo, 2022

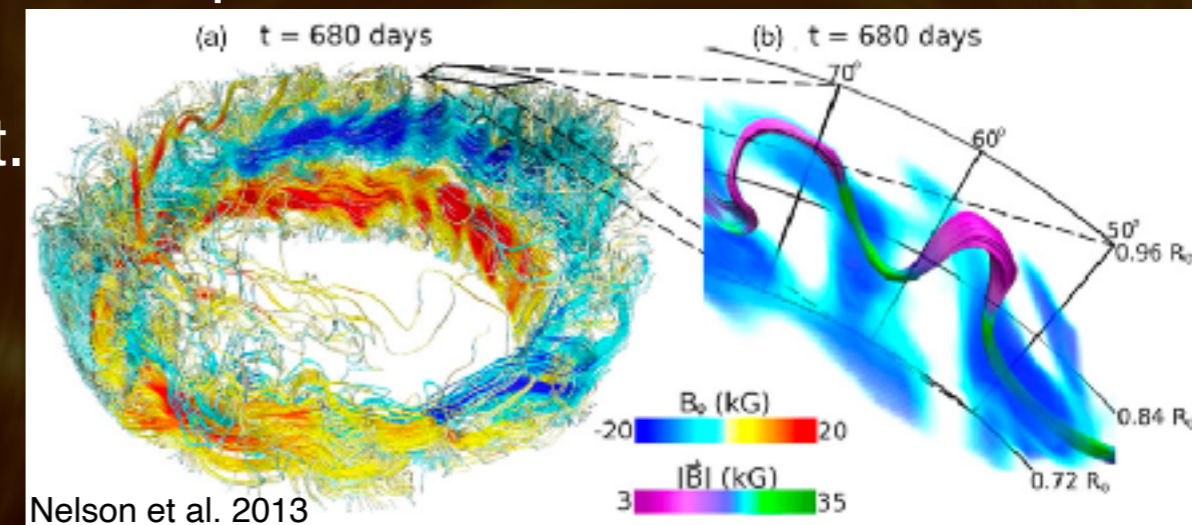
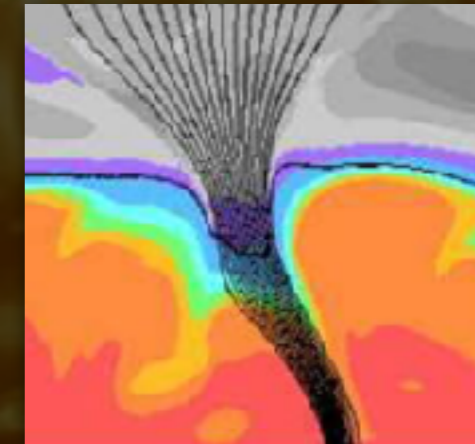
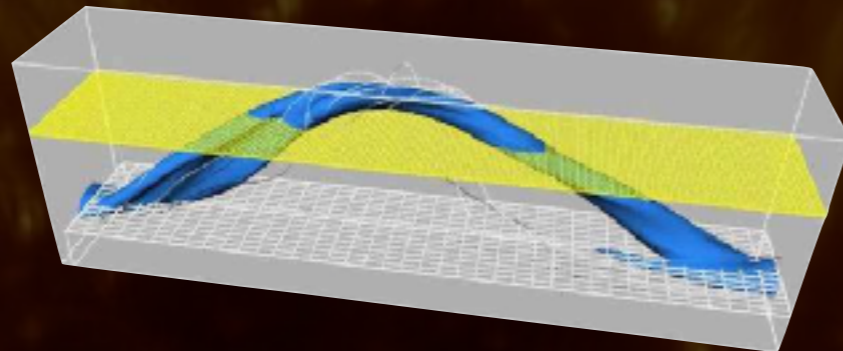
Sven Wedemeyer

# Magnetism and Dynamo Recap

# Magnetism

## Recap

- Ionised gas (plasma) in motion — electric and magnetic fields need to be considered
- **Magnetic pressure**  $P_m = B^2 / 8\pi$ 
  - Affects structure and dynamics of the plasma by “competing” with thermal pressure.
    - Magnetic flux structures funnel out in the atmosphere.
    - Magnetic flux bundles in the convection zone become buoyant.

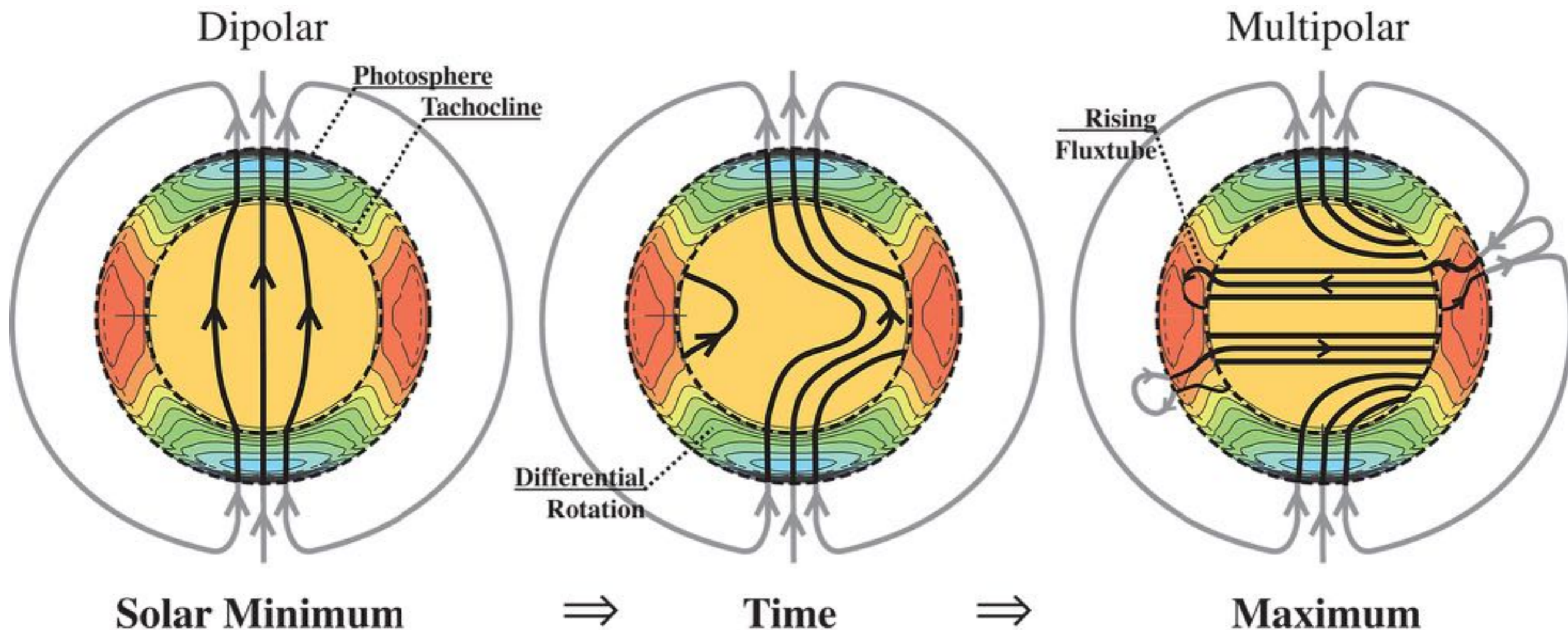


- **Plasma- $\beta$  parameter** = ratio of thermal to magnetic pressure
  - $\beta < 1$ : Magnetic field dominates and dictates the dynamics of the gas
  - $\beta > 1$ : Thermal gas dynamics dominate and forces the field to follow
    - The magnetic field is **frozen-in**.

# Dynamo

## Solar cycle — change of magnetic field configuration

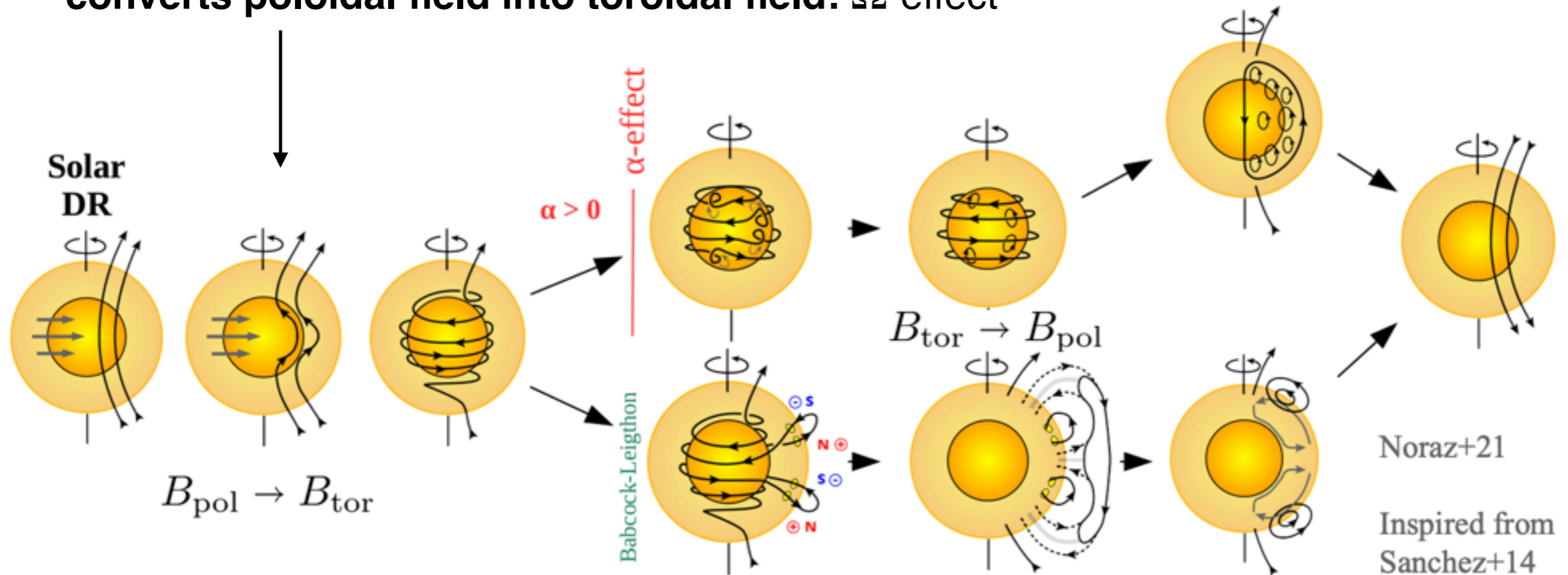
- Below **tachocline**: Rotation as solid body
- Above tachocline: **differential rotation** — faster rotation near equator, slower at poles
- Magnetic dipole field (poloidal) at solar minimum



# Dynamo

## Solar cycle — change of magnetic field configuration

- Over time: differential rotation shears magnetic field (mostly at the tachocline), converts poloidal field into toroidal field:  $\Omega$ -effect

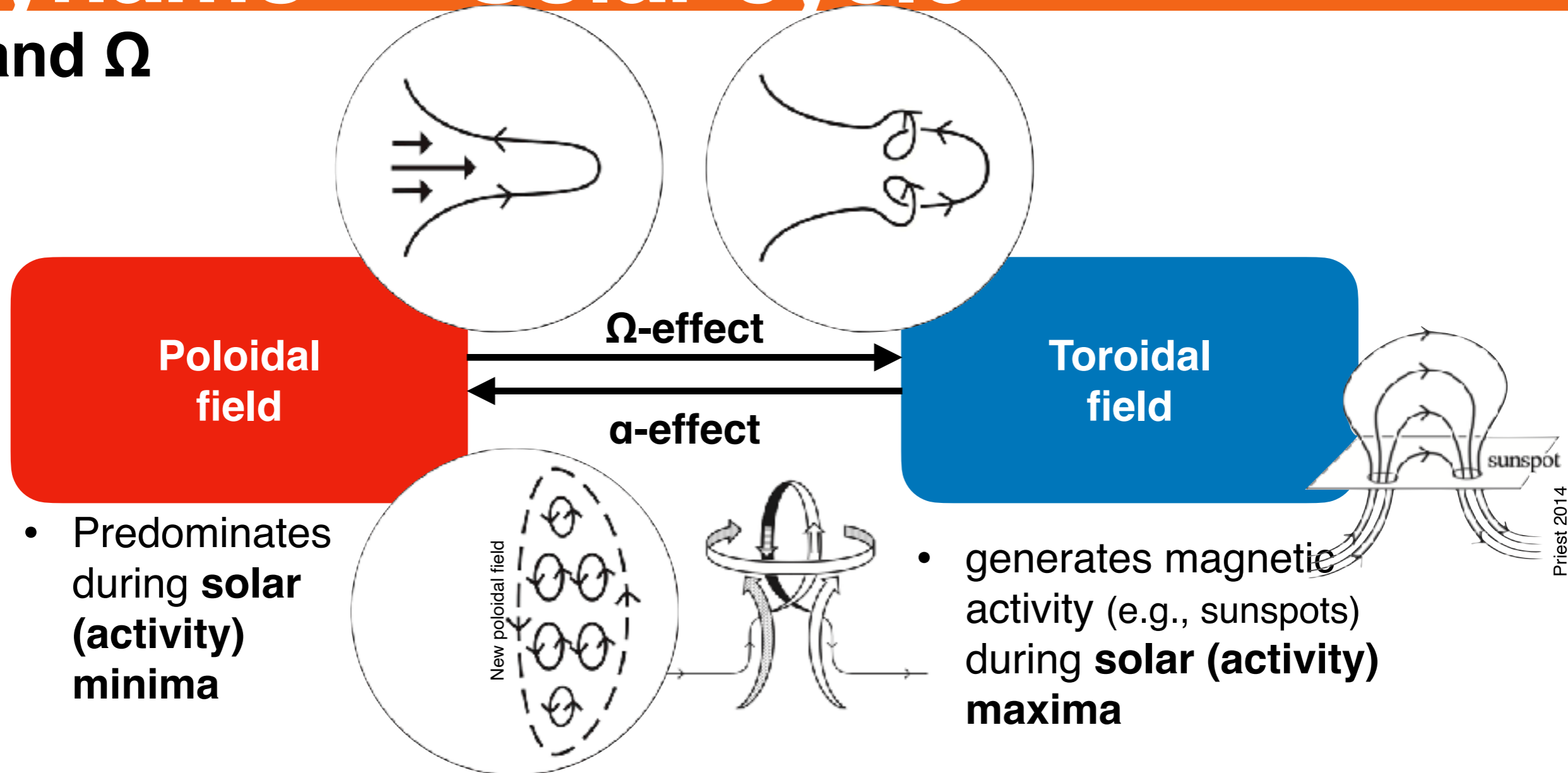


**NB :**

- Poloidal generation is likely to be a **combination of both processes  $\alpha$  and BL**
- The  $\alpha$ -effect can also take part in toroidal generation aside with the  $\Omega$ -effect

# Dynamo — Solar cycle

$\alpha$  and  $\Omega$



- Predominates during **solar (activity) minima**

- generates magnetic activity (e.g., sunspots) during **solar (activity) maxima**

- **Solar cycle:** Changes back and forth between these extreme configurations, forming a solar activity cycle with  $\sim 11$  year period
  - Global polarity of the Sun's magnetic field (N-S) swaps during that period
  - Complete cycle back to the same polarity =  $2 \times 11 \text{ yr} = 22 \text{ yr} = \text{Hale cycle}$ . -> How this process has been observed?

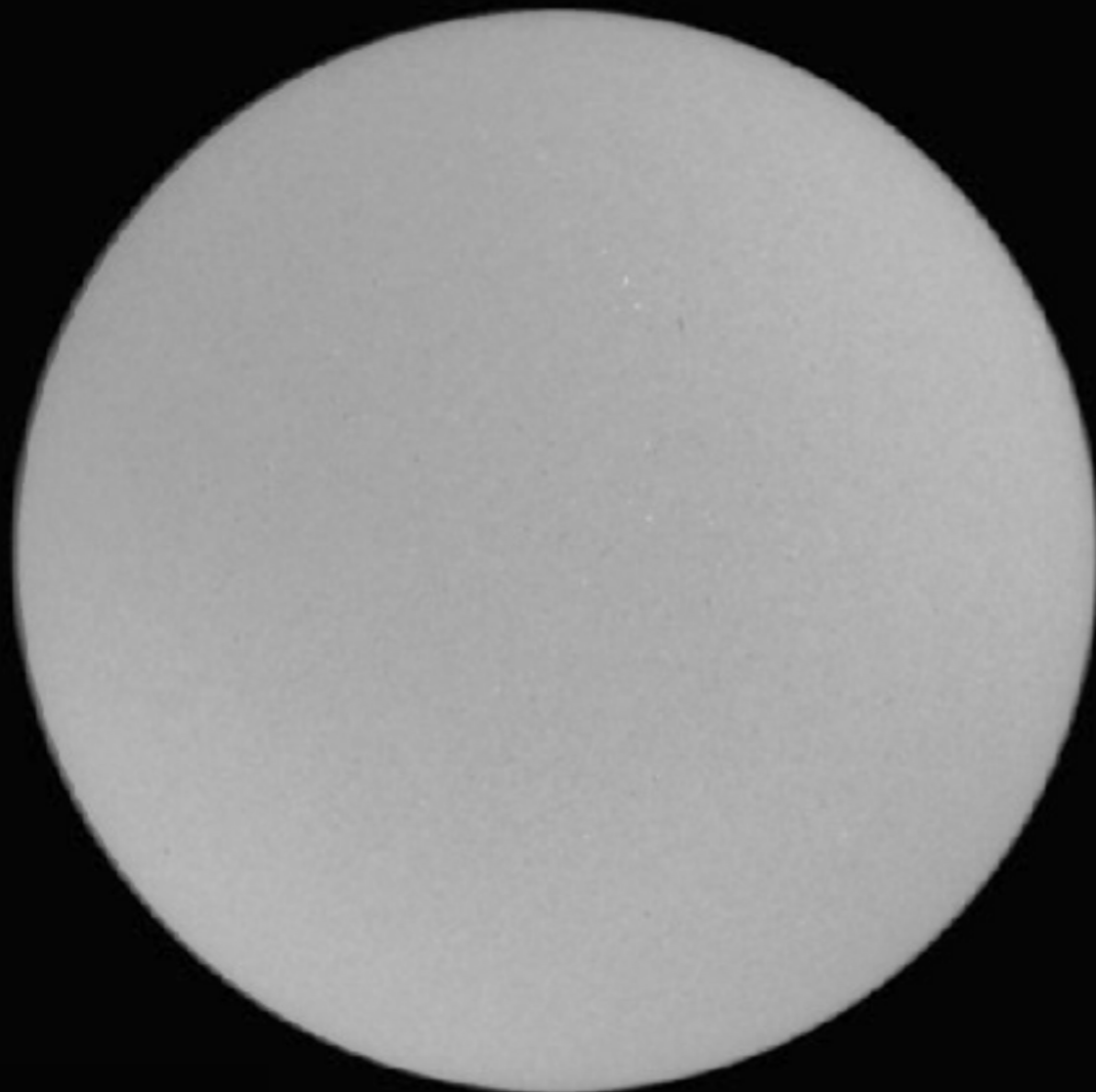
# Dynamo And Solar cycle

# Dynamo — Solar cycle

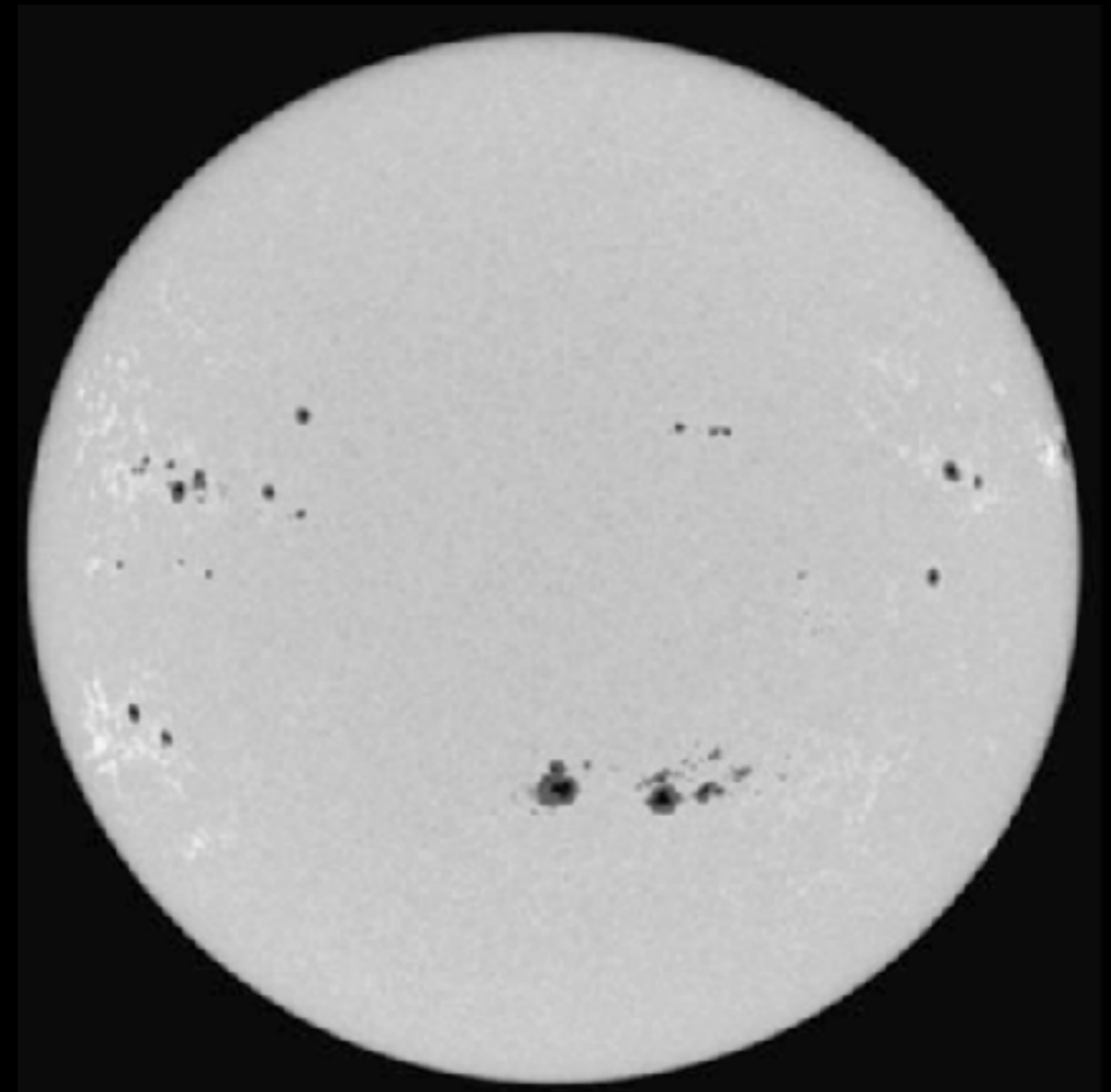
## Continuum intensity

- How to quantify solar cycles ?
- Relatively small area covered by sunspots — Overall variation in brightness?

**Minimum**



**Maximum**





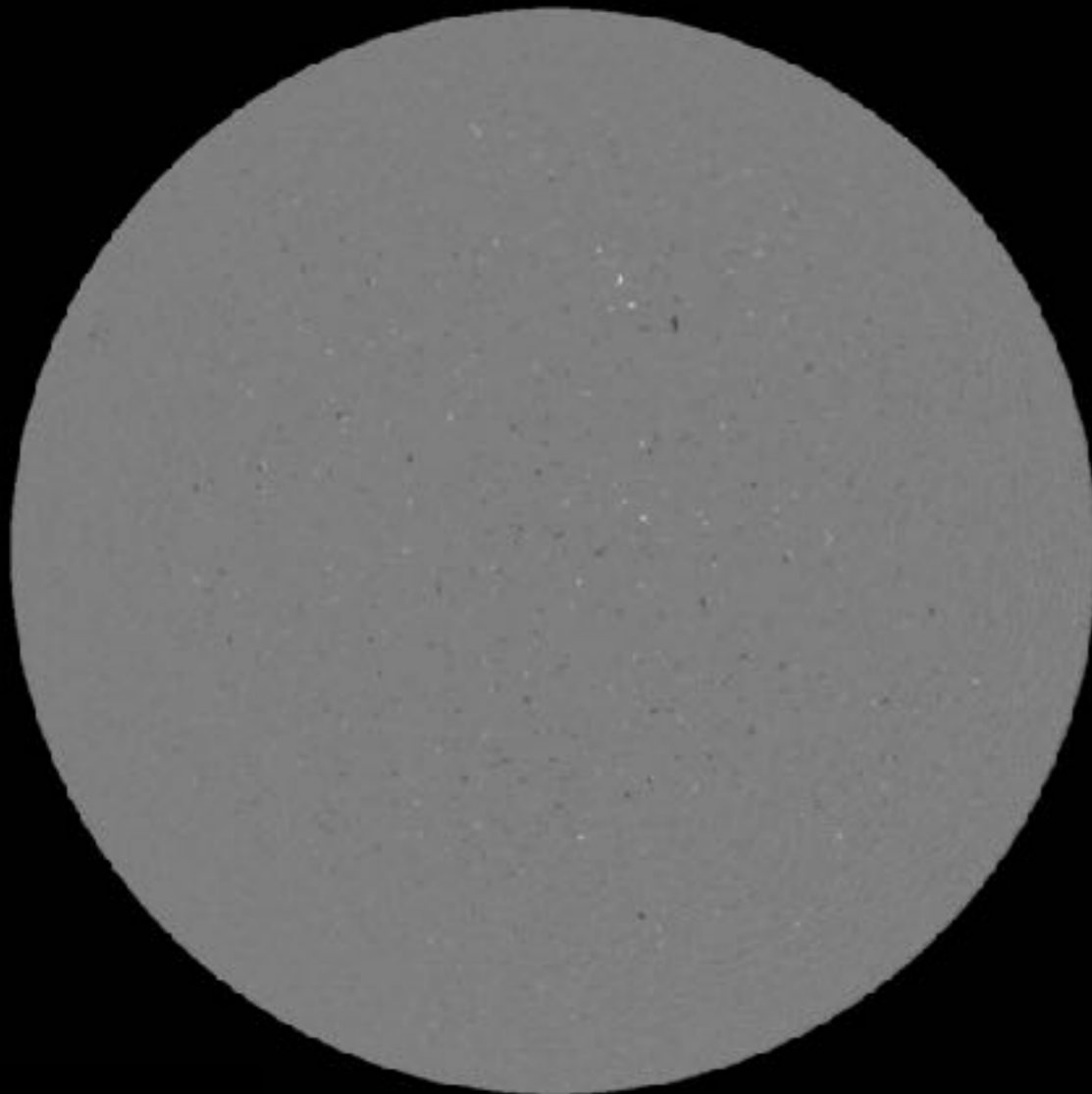
# Dynamo — Solar cycle

## Magnetograms

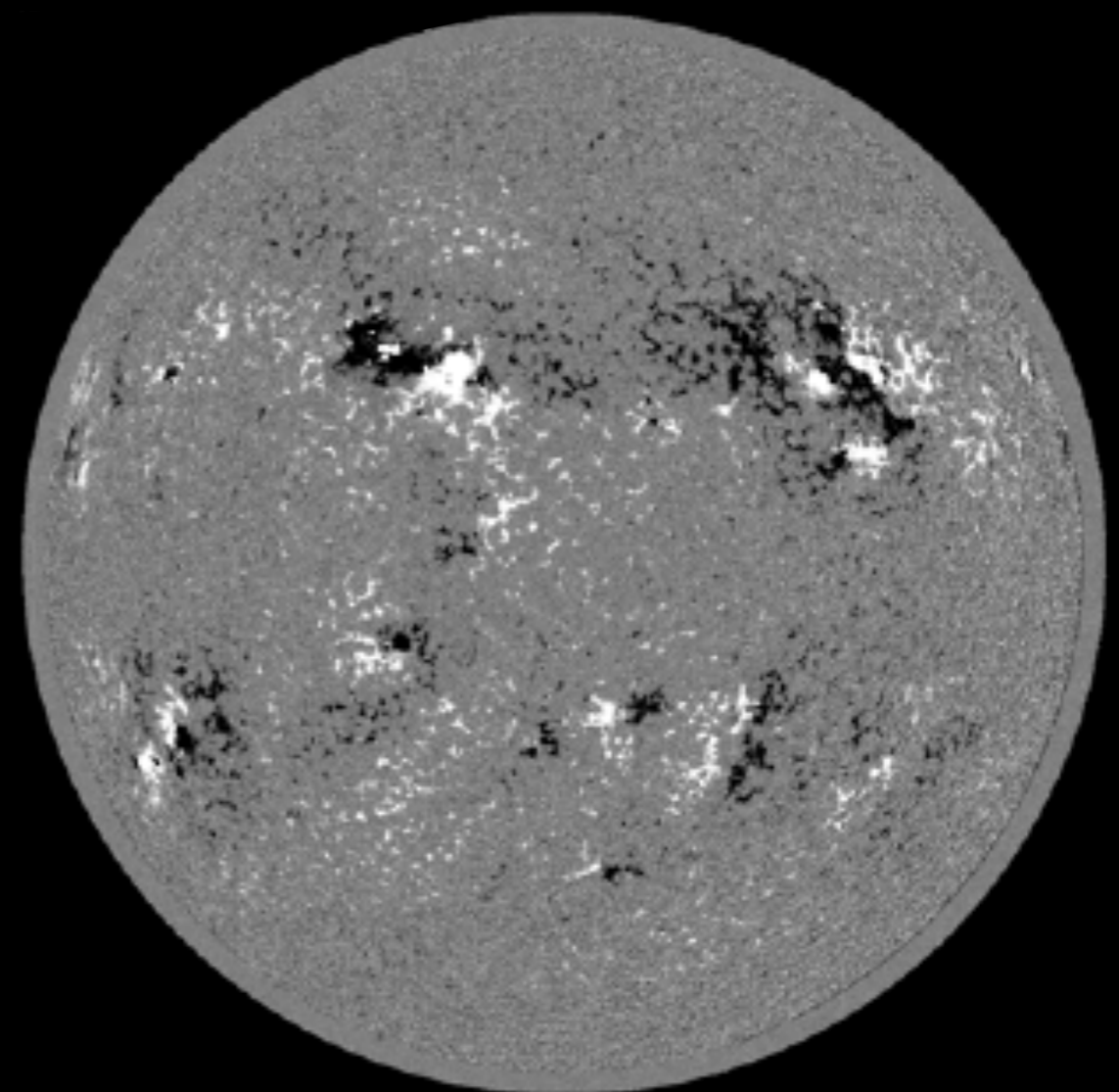
- Changes are more drastic when looking at magnetograms

Solar magnetograms:  
Line of sight B-field from  
circularly polarized light

Minimum



Maximum

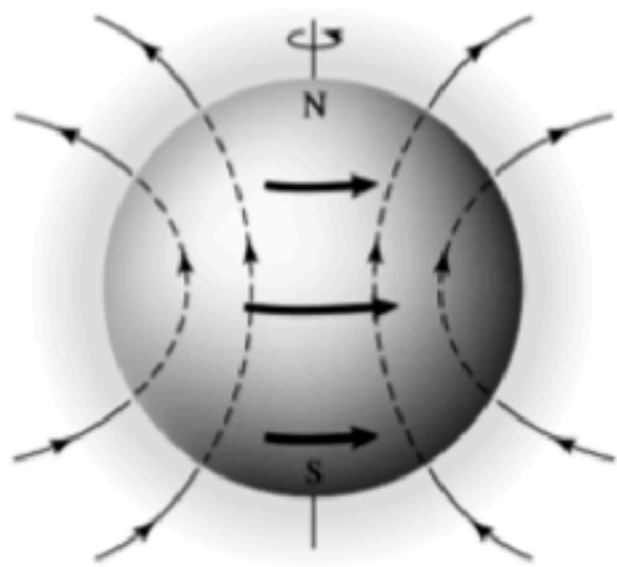


- Hemispheric inversion of polarities

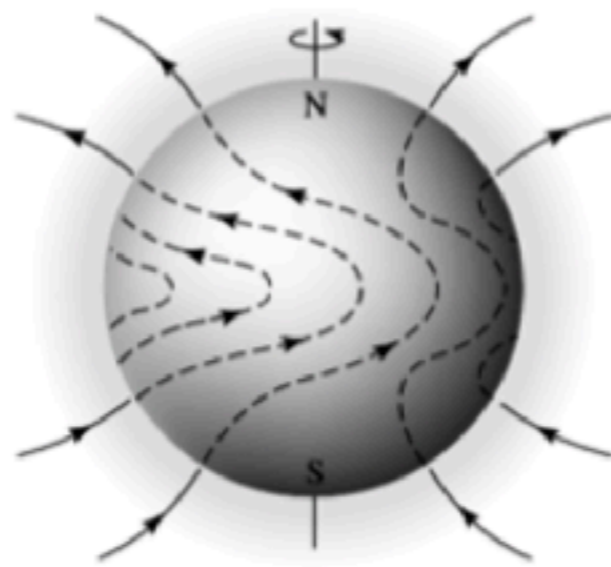
# Dynamo — Solar cycle

## Sunspots — latitude

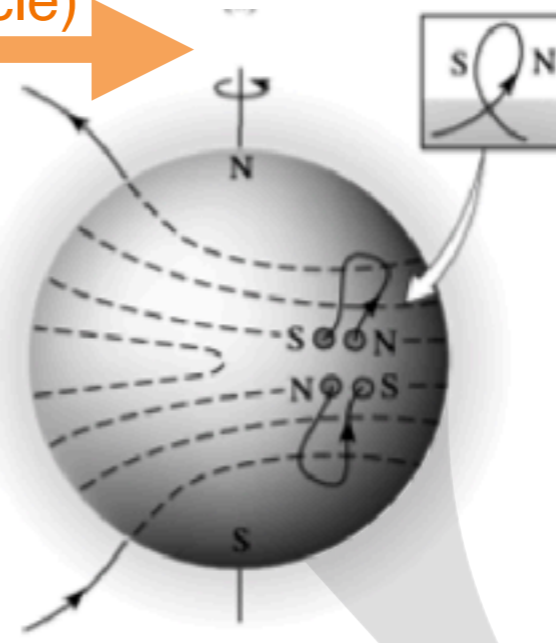
Time (solar cycle) →



Poloidal

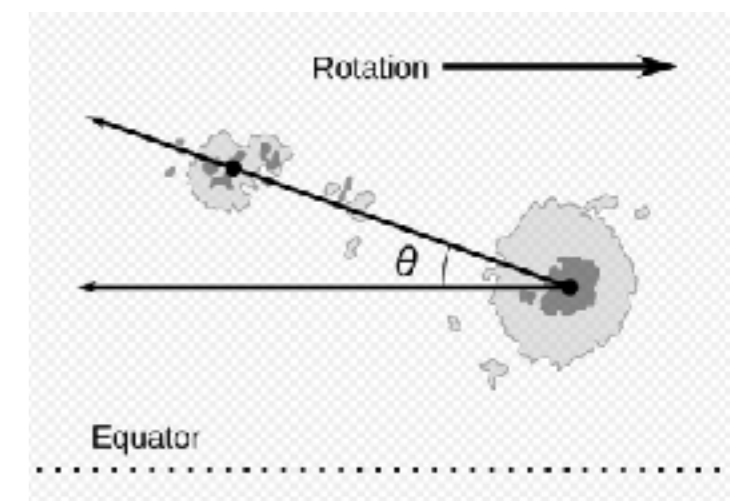
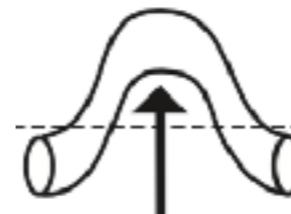


Toroidal



Poloidal but N/S poles flipped

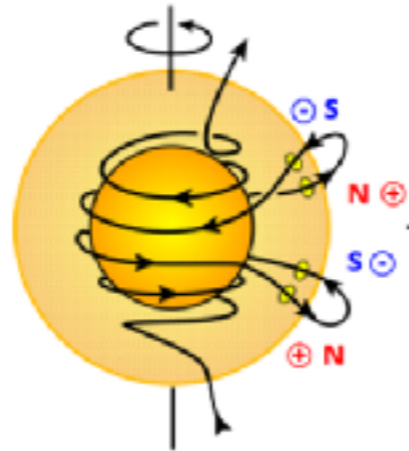
- Coriolis force depends on latitude  $\lambda$   
 -> tilt angle  $\theta$  stronger at high latitudes (Joy's law)
- Polarities of the northern and southern hemispheres cancel out at the equator!
- ➔ **Cancellation** of magnetic field at the equator
- ➔ More sunspots develop at **intermediate latitudes**
- With time, the poloidal field will be re-established (but with opposite polarity)



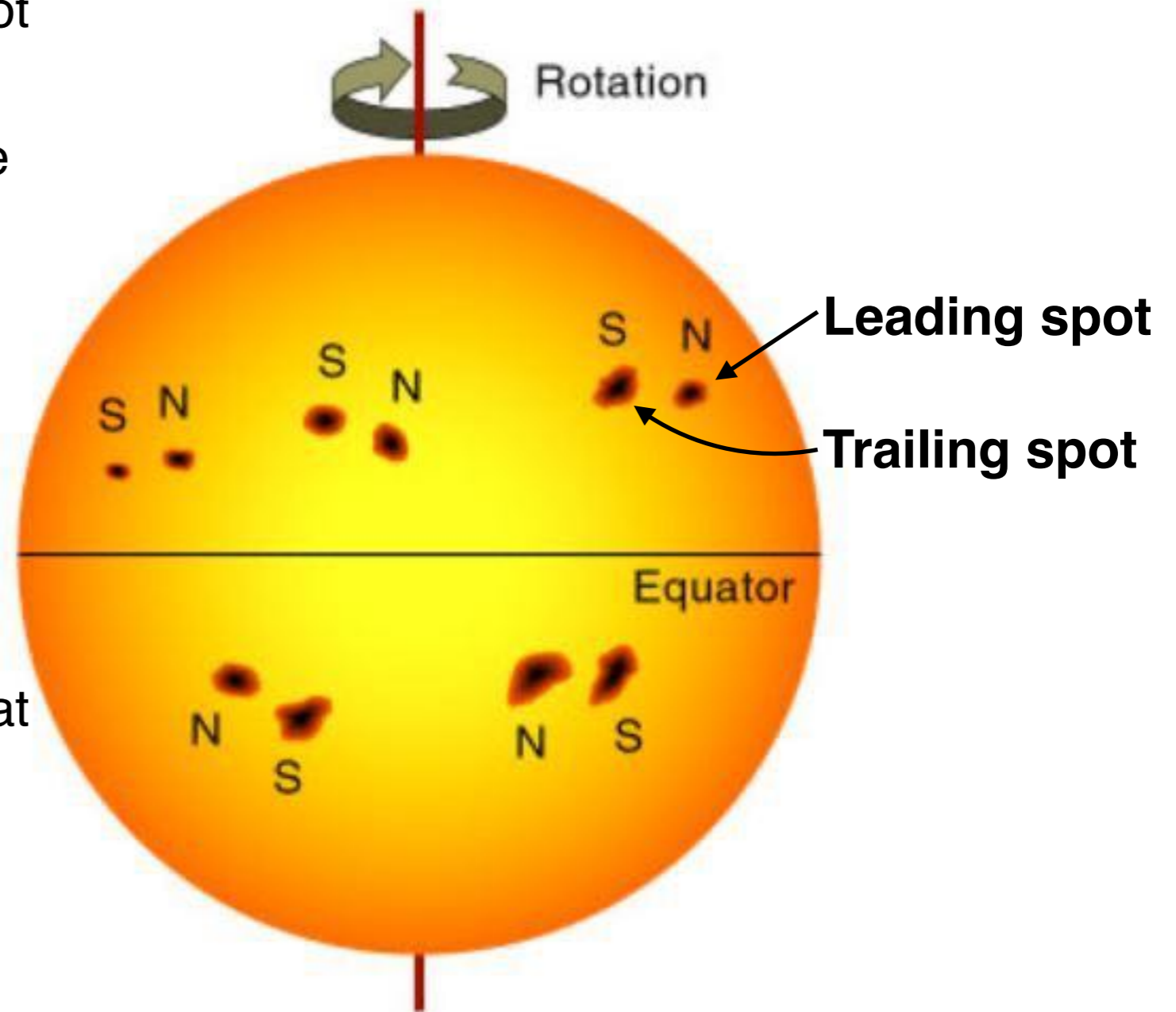
# Dynamo — Solar cycle

## Sunspots — latitude and orientation

- Active Regions with a leading spot and a trailing spot
- Order of polarities reversed in the two hemispheres



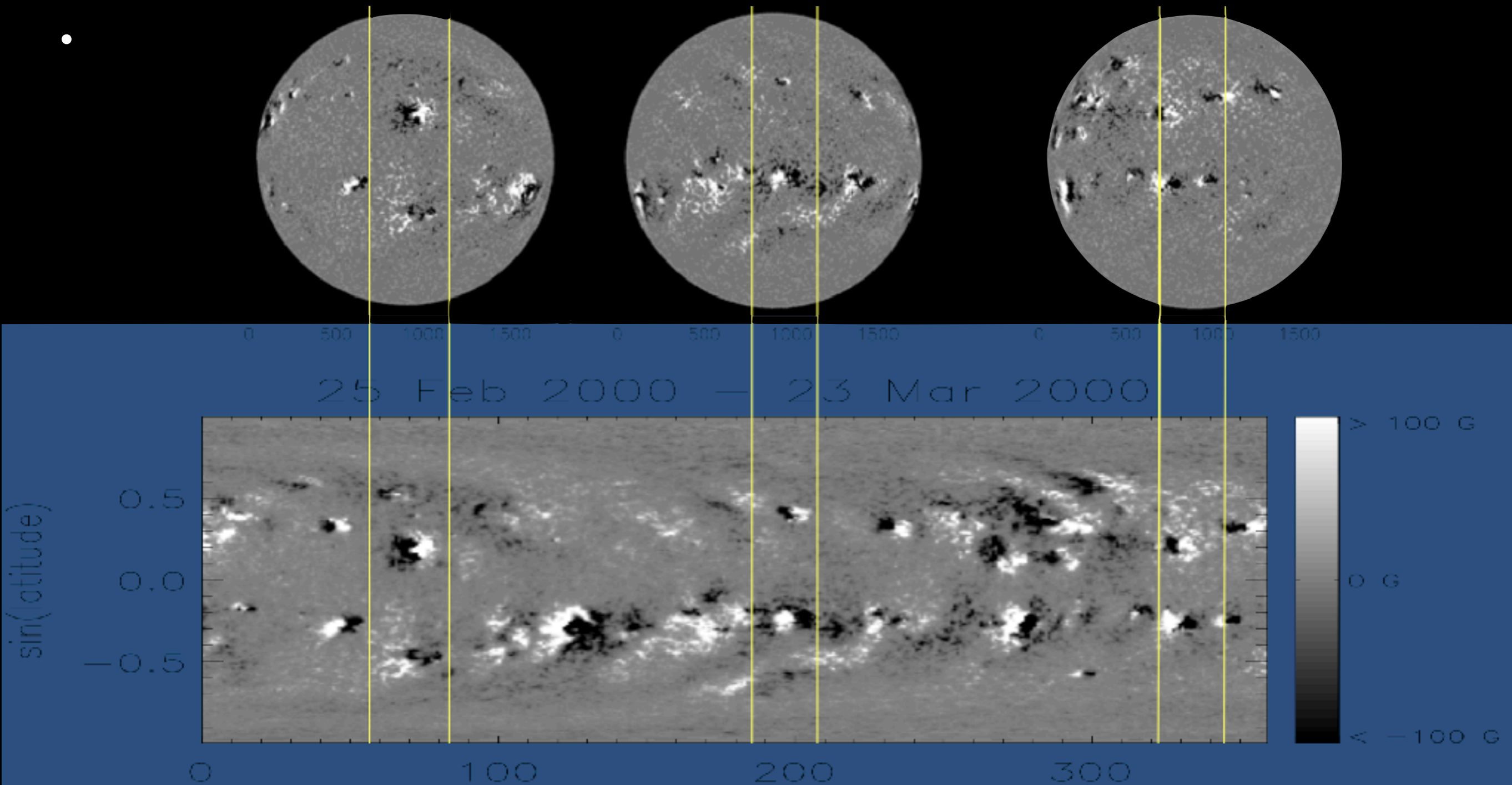
- Flips with global magnetic field orientation every 11yr
- New cycle begins with sunspots at latitudes of 30-45 degrees on both hemispheres
- During a solar cycle: Sunspots appear gradually more towards equator (Spörer's law)
- Cycle ends with sunspots at low latitudes (~7 degrees)



# Dynamo — Solar cycle

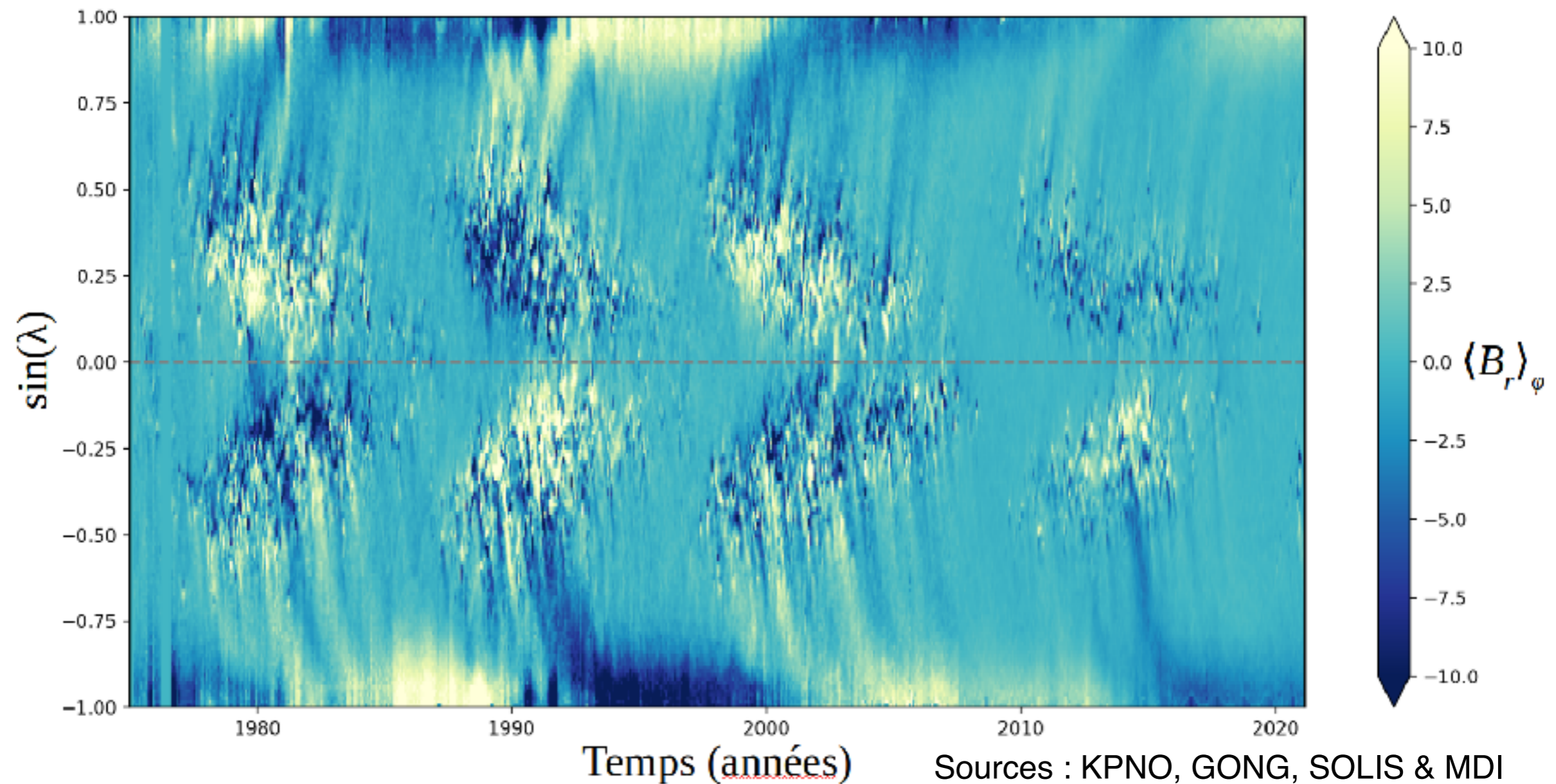
## Magnetic field configuration at surface

- Synoptic maps approximate the radial magnetic flux observed near the central meridian over a period of 27.27 days (= 1 Carrington rotation)



# Dynamo - Solar cycle

## Butterfly diagram

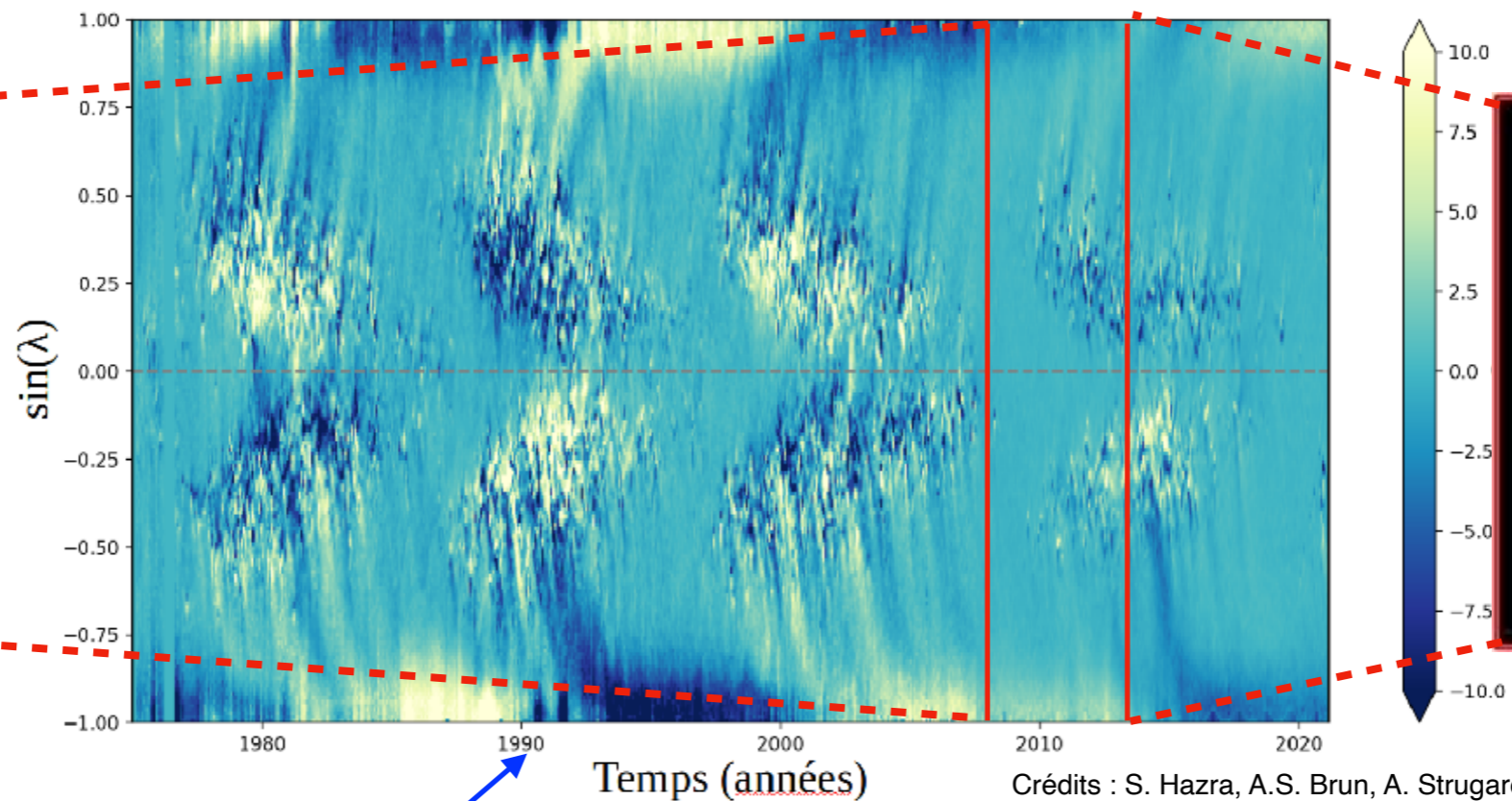
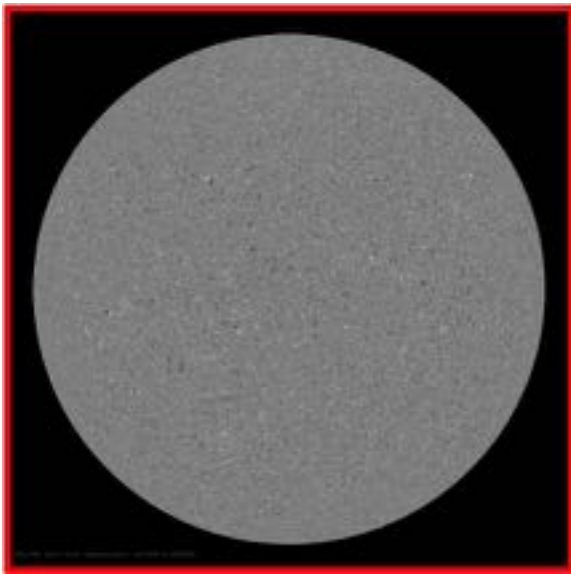


Sources : KPNO, GONG, SOLIS & MDI  
Crédits : S. Hazra, A.S. Brun, A. Strugarek

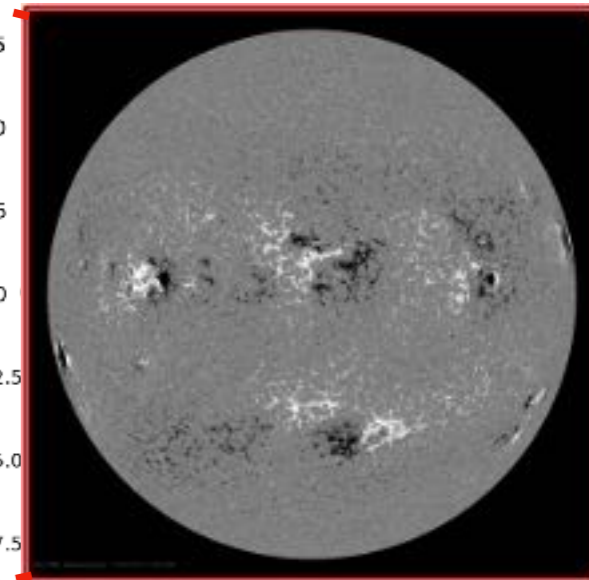
# Dynamo - Solar cycle

## Butterfly diagram

Activity Minimum

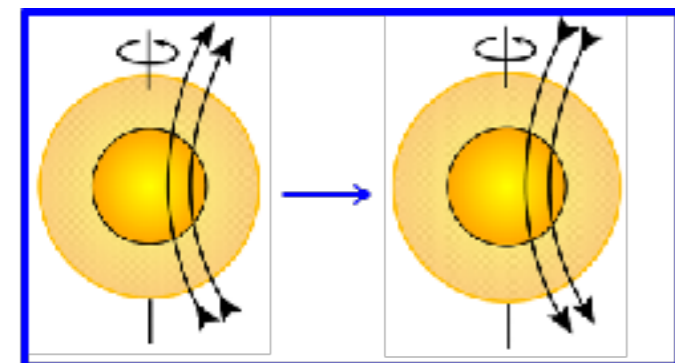


Activity Maximum



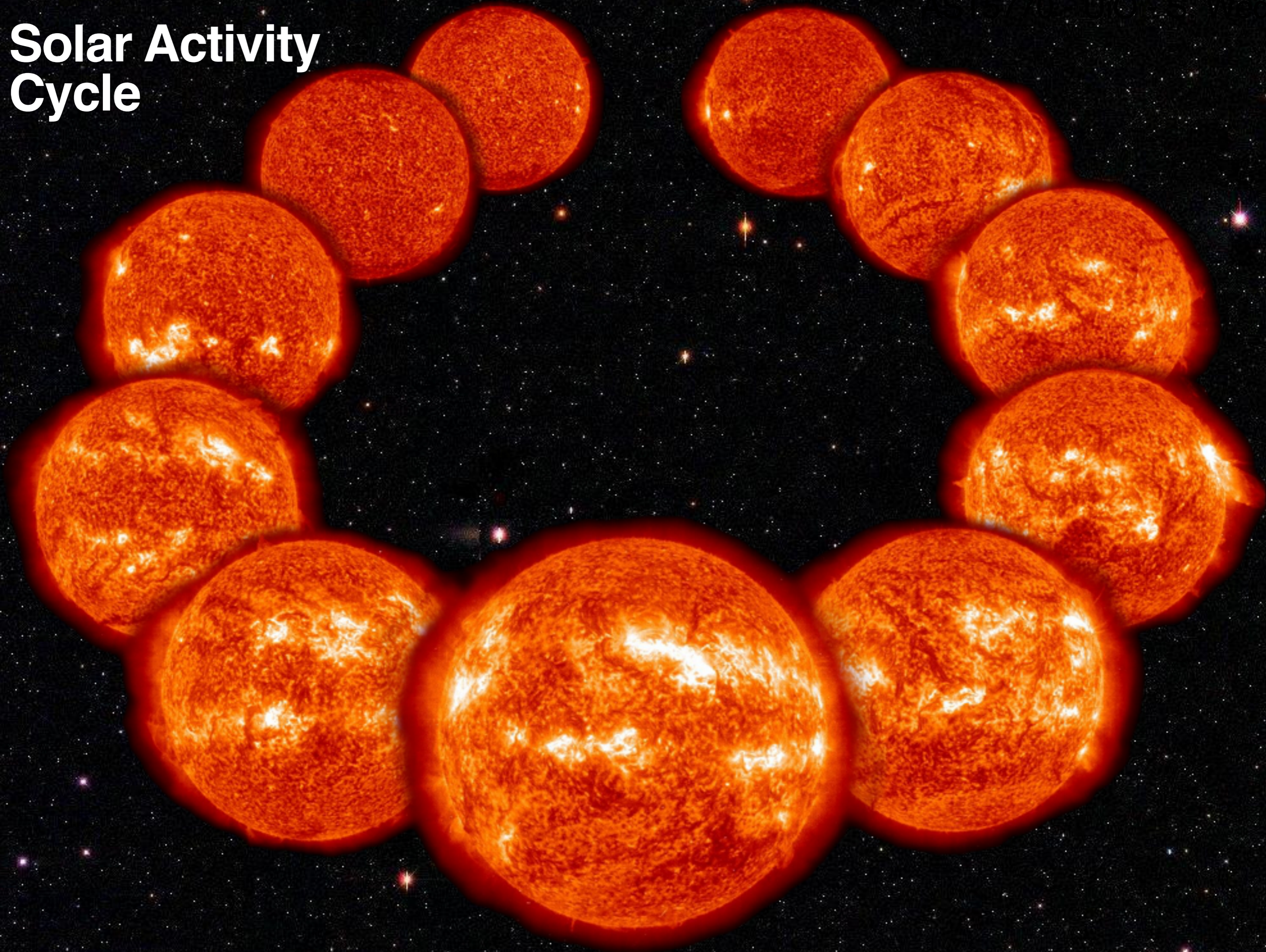
Crédits : S. Hazra, A.S. Brun, A. Strugarek

**Global  
polarity  
reversal**



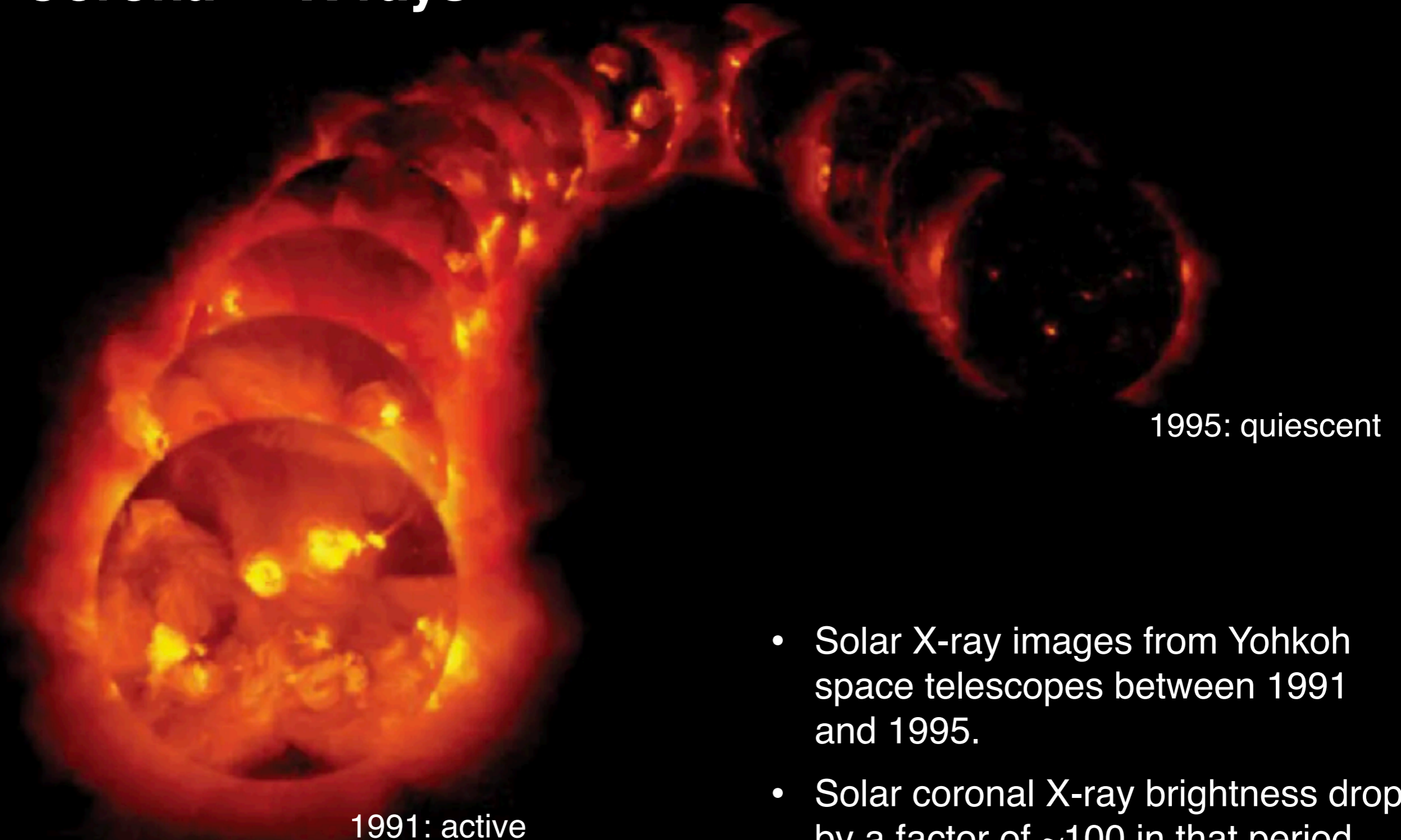
- **11-years activity cycle**
- Migration of structures toward equator
- Opposite hemisphere polarities
- **22-years magnetic cycle**

# Solar Activity Cycle



# Dynamo — Solar cycle

## Corona — X-rays



- Solar X-ray images from Yohkoh space telescopes between 1991 and 1995.
- Solar coronal X-ray brightness drops by a factor of  $\sim 100$  in that period



# Dynamo — Solar cycle

## Corona

- Solar cycle clearly visible in the change of the coronal magnetic field
- The solar disk can be hidden using a “coronagraph”
- Topology changes are then visible with eclipse

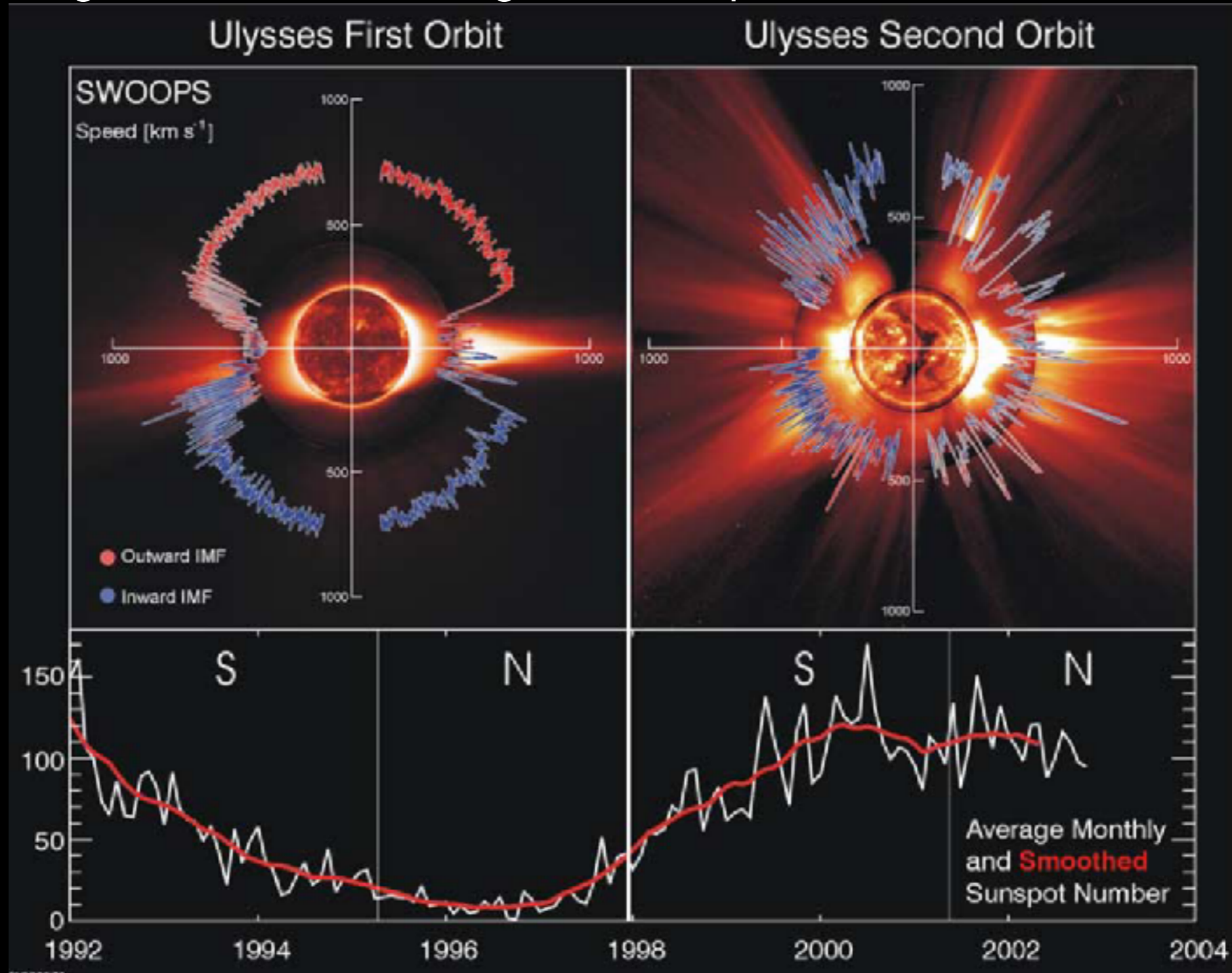


*Corona visible — brighter solar disk is blocked out*

# Dynamo — Solar cycle

## From corona to wind formation

- Cyclic changes of the coronal magnetism shape the solar wind

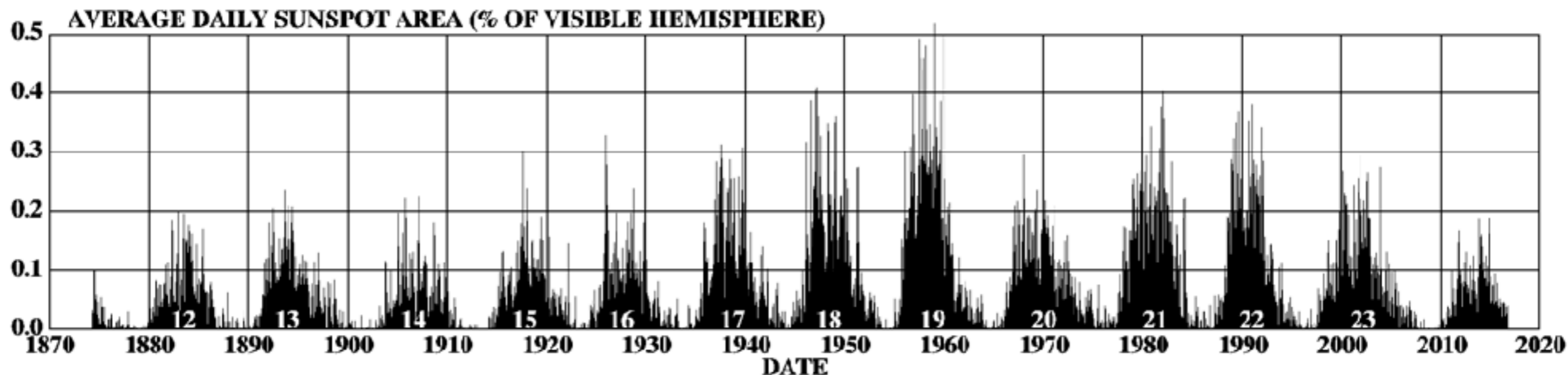
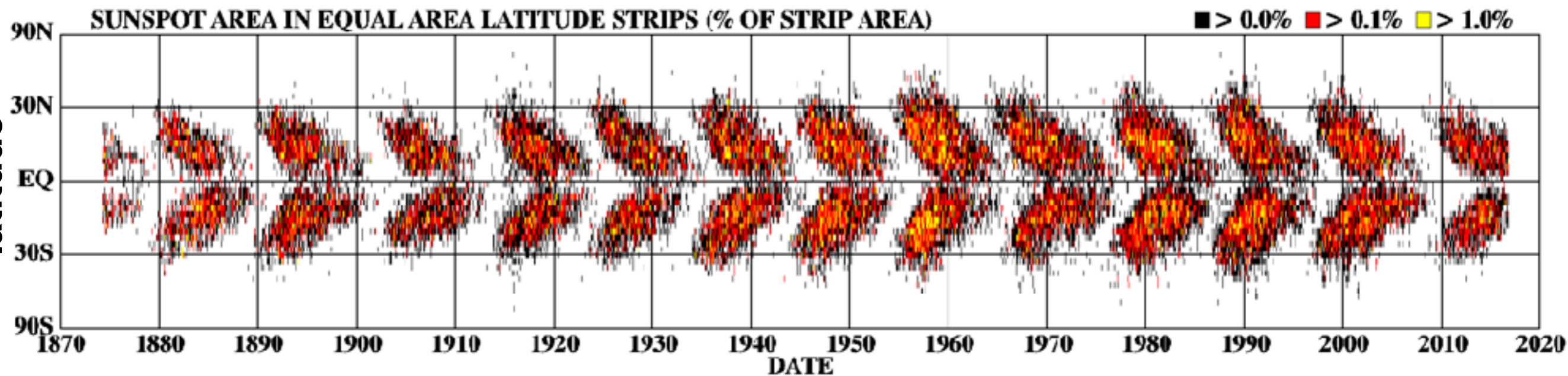


# Dynamo — Solar cycle

## Sunspots — latitude and time

- Solar cycle — sunspots first at 30deg N/S, then gradually towards equator

### Butterfly diagram DAILY SUNSPOT AREA AVERAGED OVER INDIVIDUAL SOLAR ROTATIONS



# Solar cycle

## Sunspot number (Wolf number/Zürich sunspot number )

- Numerical measure for the “spottedness” of the Sun and thus its magnetic activity level

$$R = k (10 g + s)$$

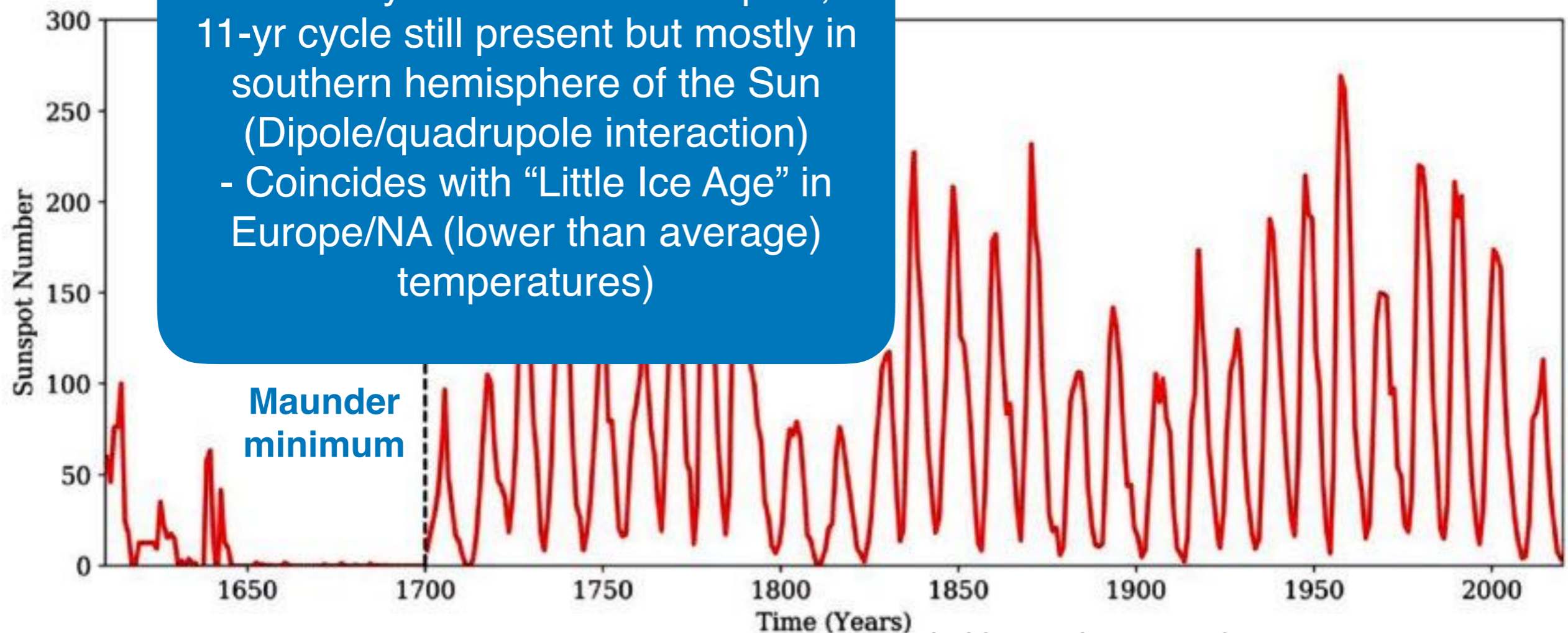
$s$ : number of individual sunspots

$g$ : number of sunspot groups

$k$ : calibration factor (instrument, personal bias)

- Captured by telescope (Gleissberg)
- Correlation of screening from cosmic rays

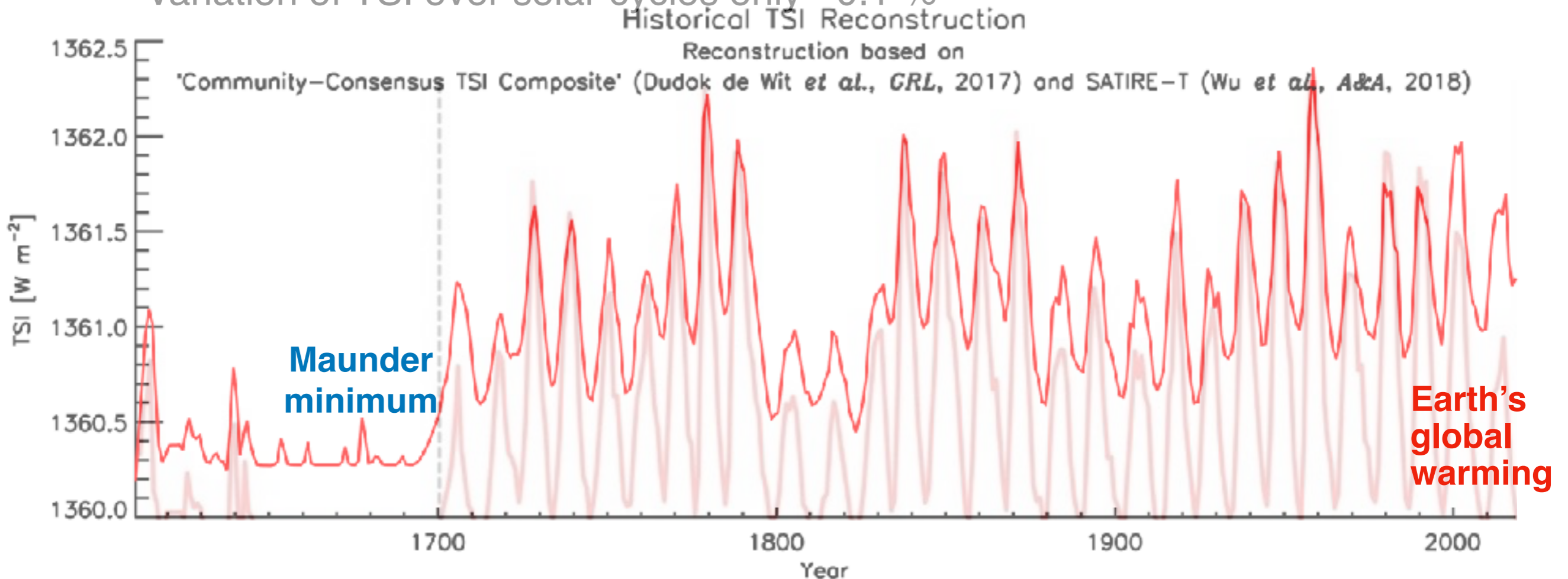
- Maunder Minimum 1645 - 1715  
Unusually small number of spots,  
11-yr cycle still present but mostly in  
southern hemisphere of the Sun  
(Dipole/quadrupole interaction)  
- Coincides with “Little Ice Age” in  
Europe/NA (lower than average)  
temperatures)



# Solar cycle

## Variation of the Sun's total irradiance

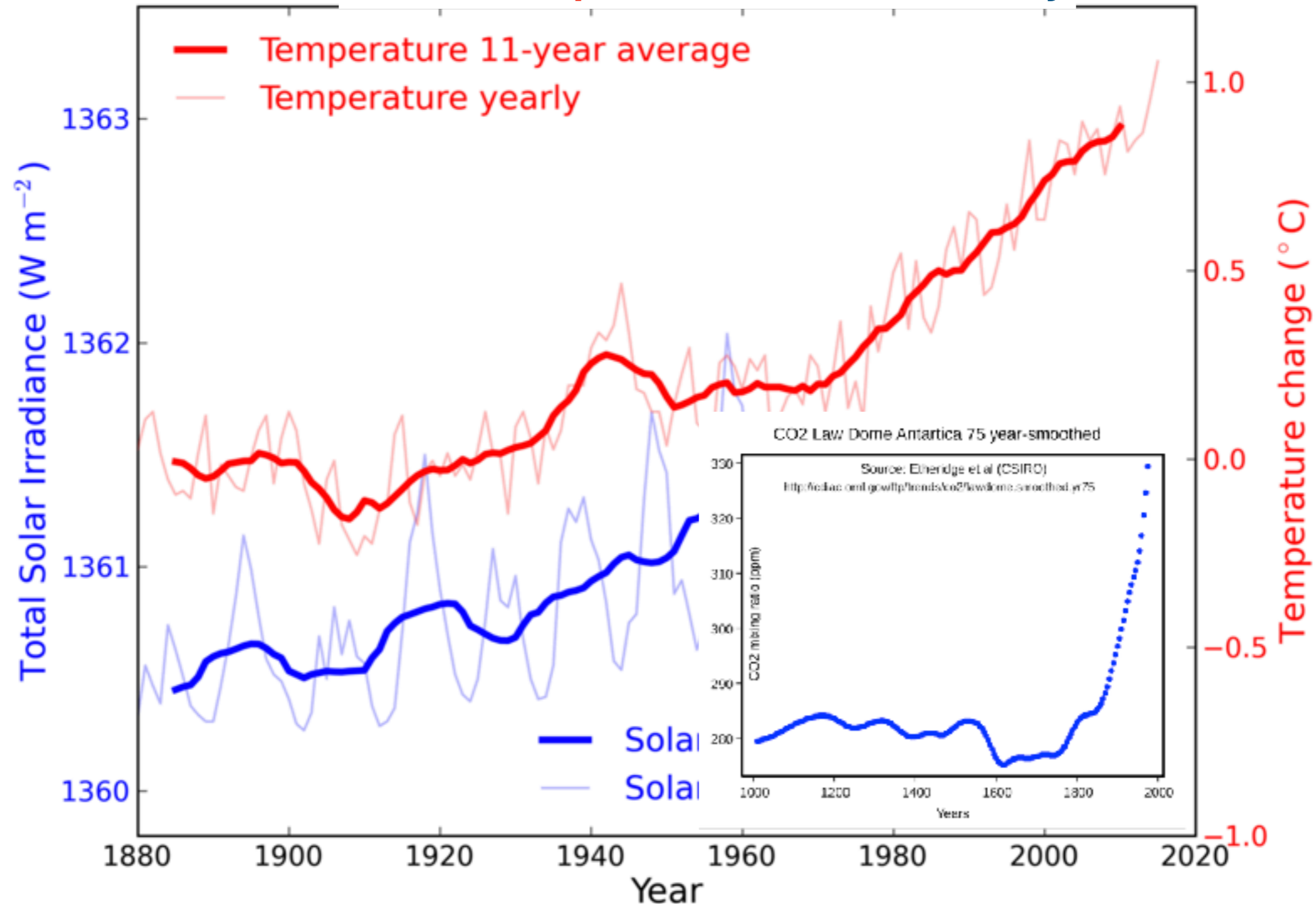
- Magnetic fields produce sunspots and faculae (to be discussed later) at the surface
  - Visible brightness changes of Sun correlated with number of sunspots but only a few milli-mags!
- **Total Solar Irradiance** (TSI, measure of the radiation flux from the Sun that is received at Earth)
  - Variation of TSI over solar cycles only  $\sim 0.1\%$



# Solar cycle

## Variation of the Sun's total irradiance

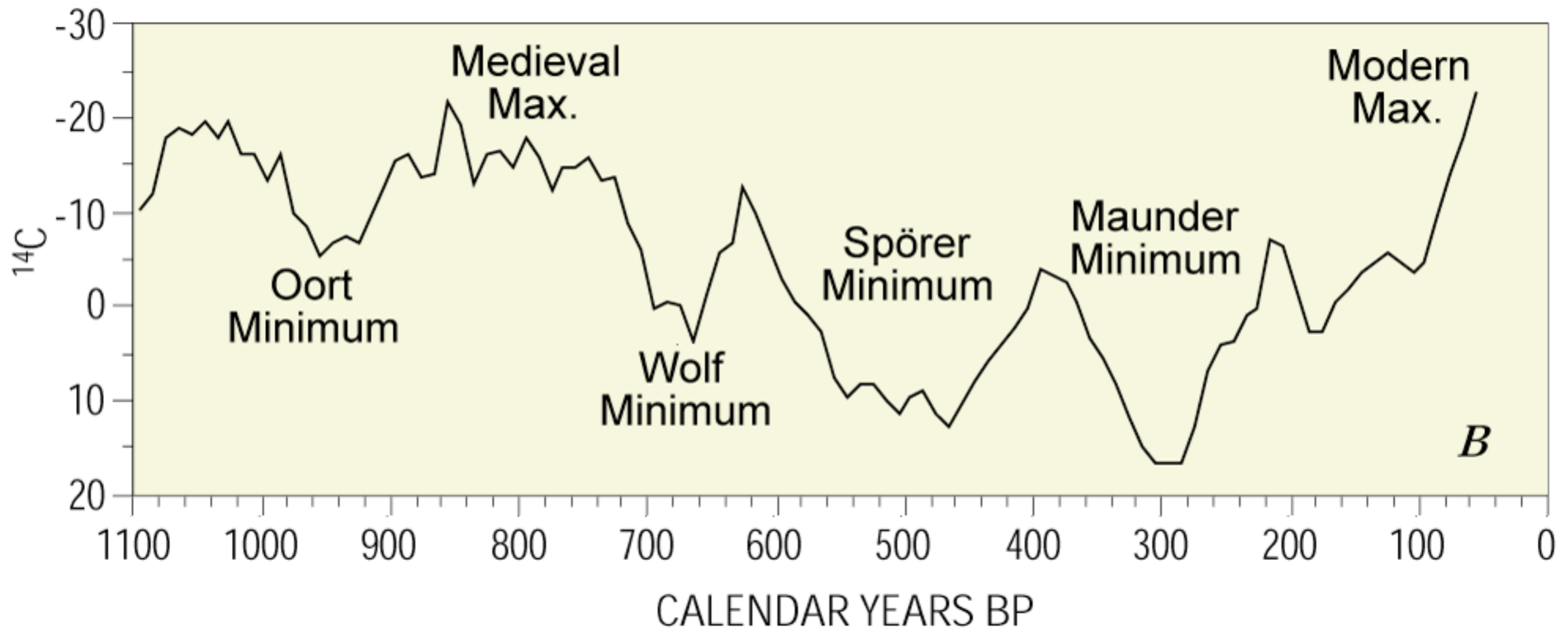
Earth's temperature vs solar activity



# Solar cycle

## Long-term variation of solar activity

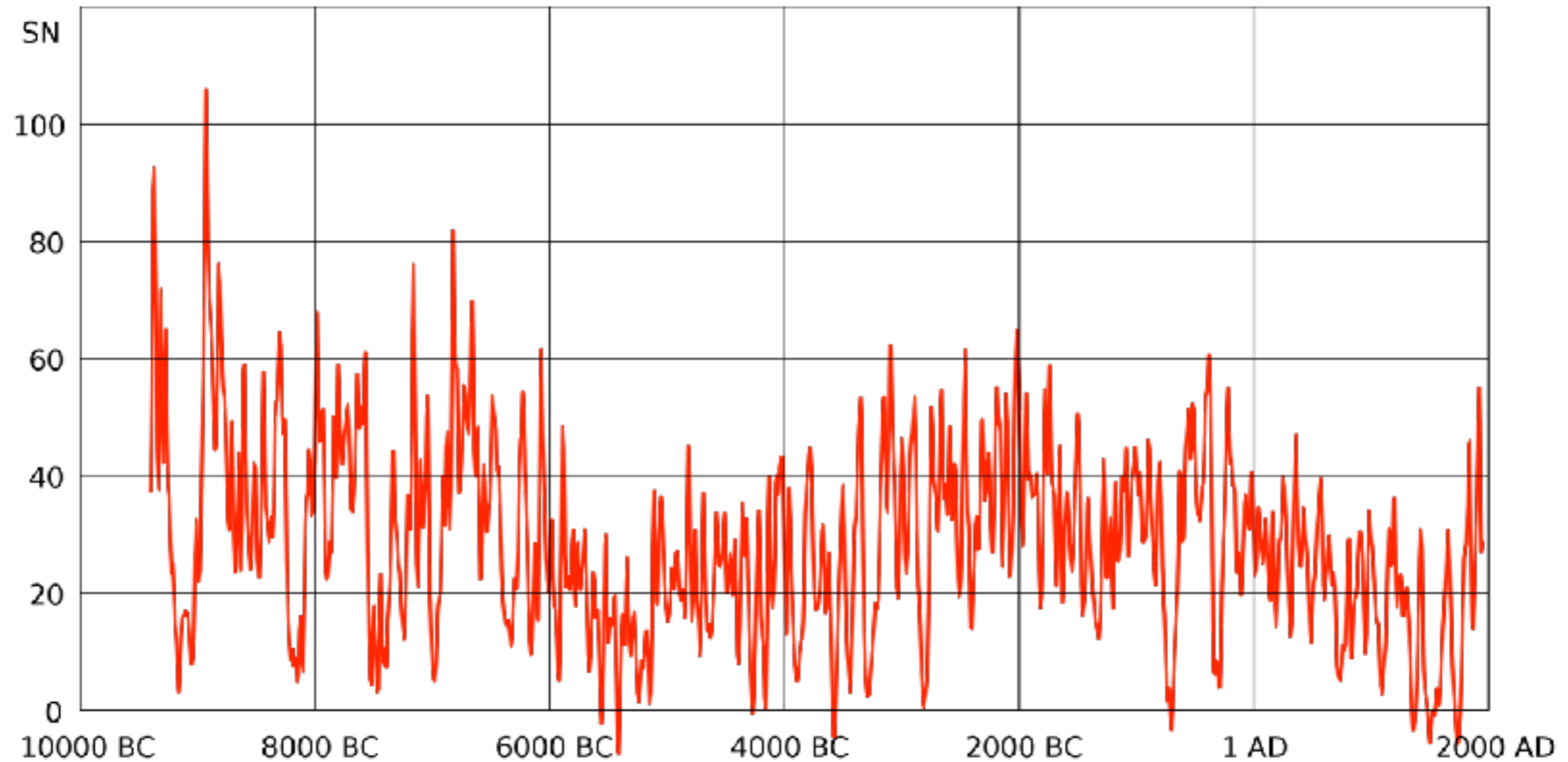
Changes in **carbon-14** concentration in the Earth's atmosphere, which serves as a long term **proxy of solar activity**.



# Solar cycle

## Long-term variation of solar activity (2)

11,000 Year Sunspot Number Reconstruction

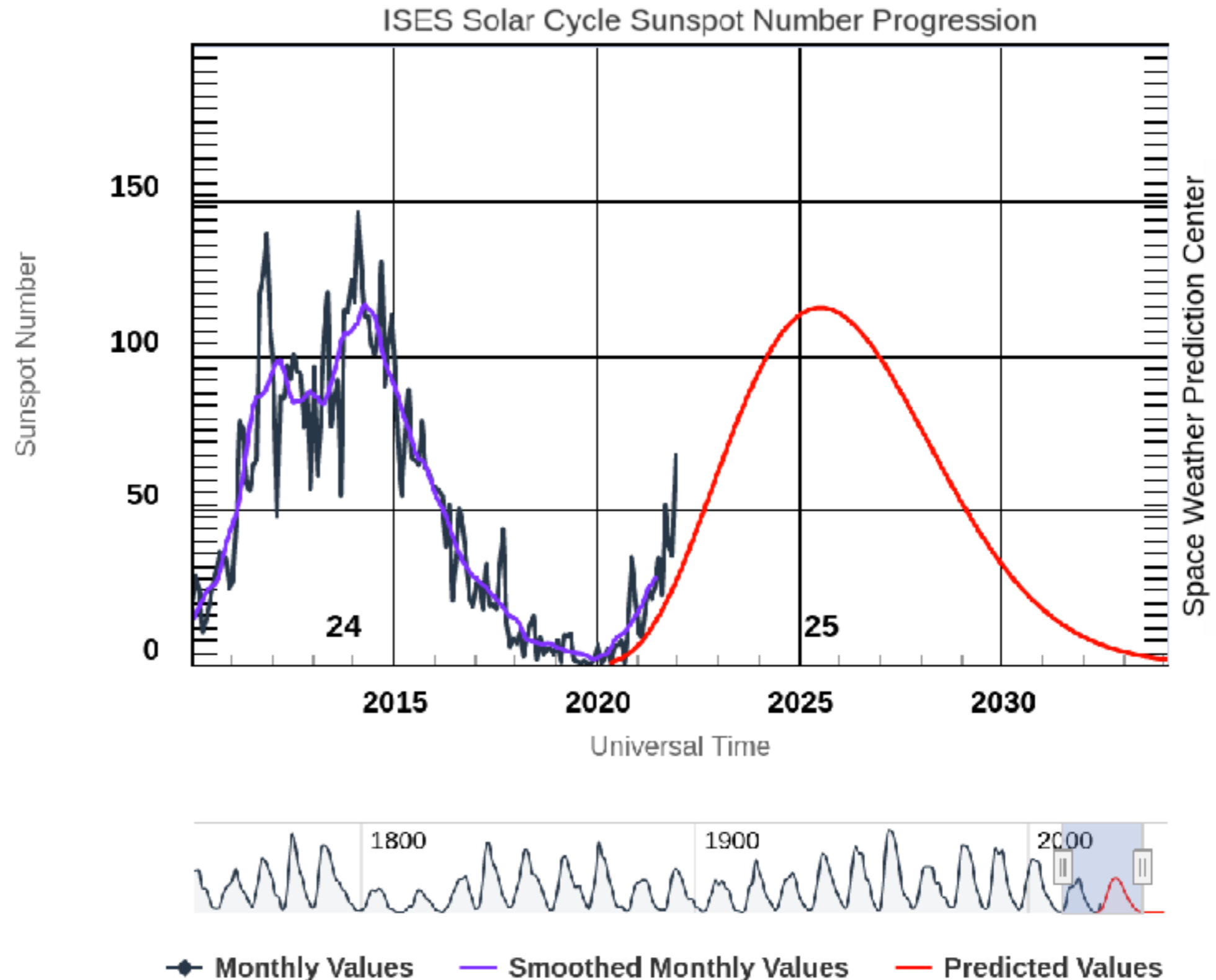




# Solar cycle

## Current and future cycle (prediction)

- Models of the solar dynamo allow for prediction of the next cycle
- Comparison of actual sunspot number (as they occur) as a crucial test of the model



# Dynamo — Solar cycle

## Global dynamo simulations

# Stellar Magnetism

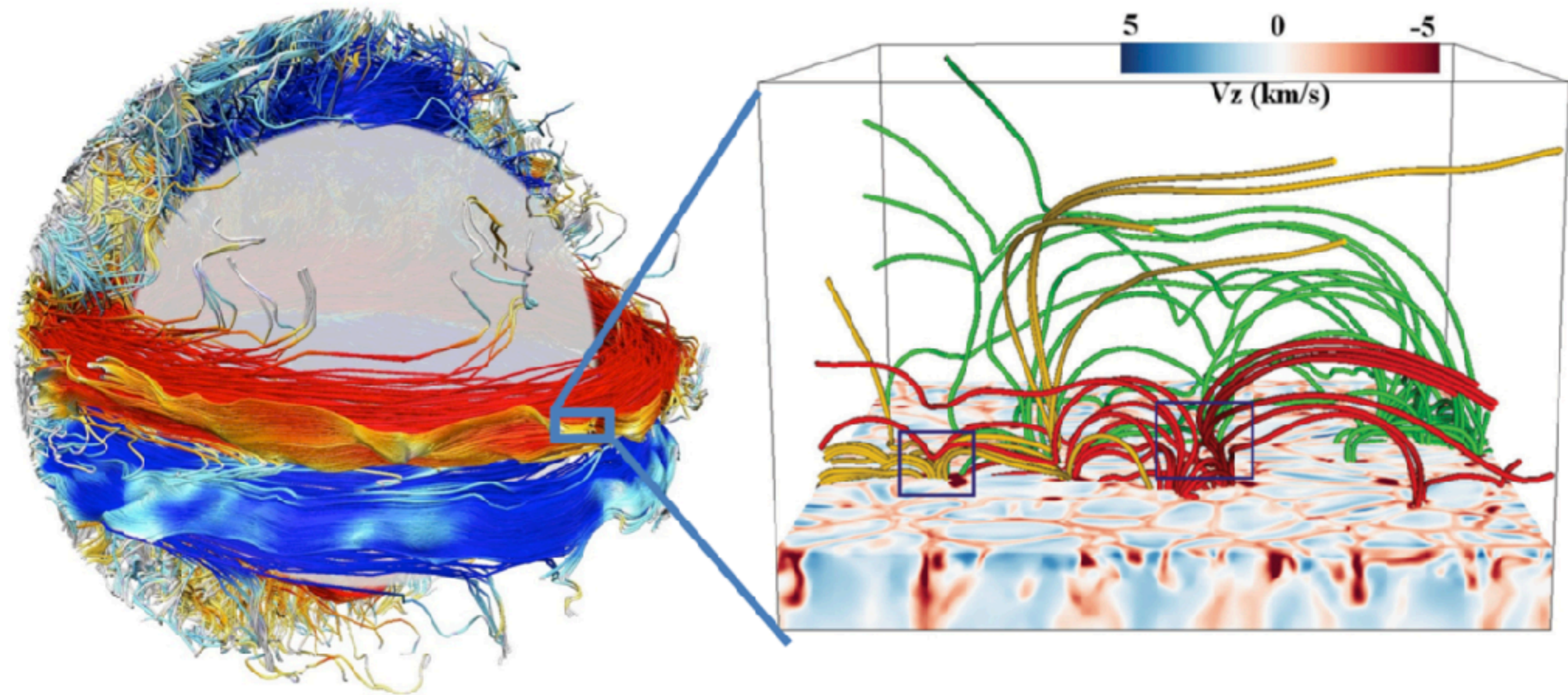
Scientific Computing and Imaging Institute  
UNIVERSITY OF UTAH



Niklas Jansson

# Dynamo

## WholeSun project

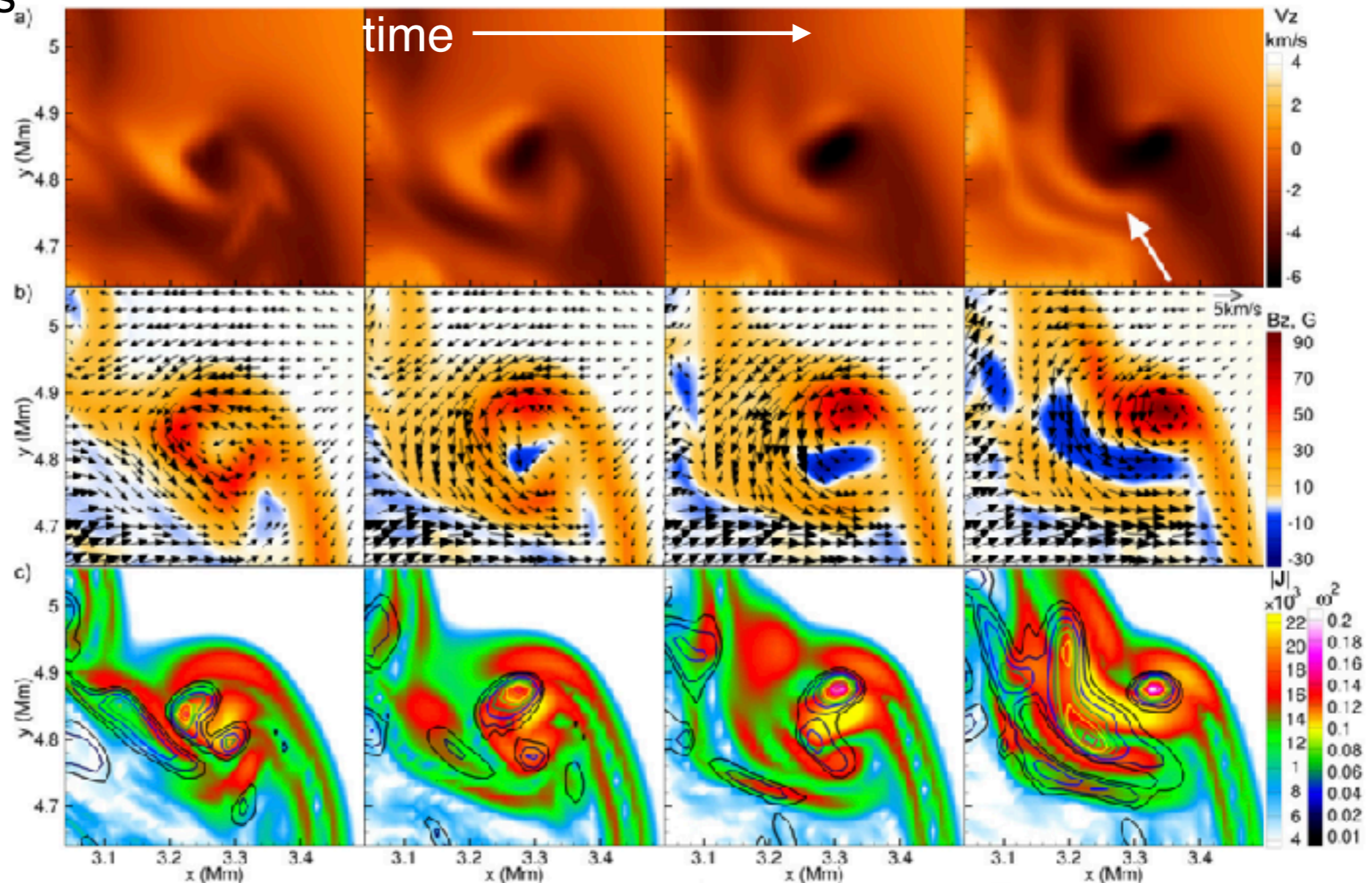


# Dynamo

## Local dynamo

- In addition to the global solar dynamo: local dynamo action near the solar surface
- Dynamo action will occur in a turbulent medium even in the absence of rotation (Emonet and Cattaneo 2001)
- ➔ Strong enough surface convection can lead to magnetic field generation due to a local dynamo process

Magnetic field is generated by swirling turbulent flows  
(Kitiashvili et al. 2015)

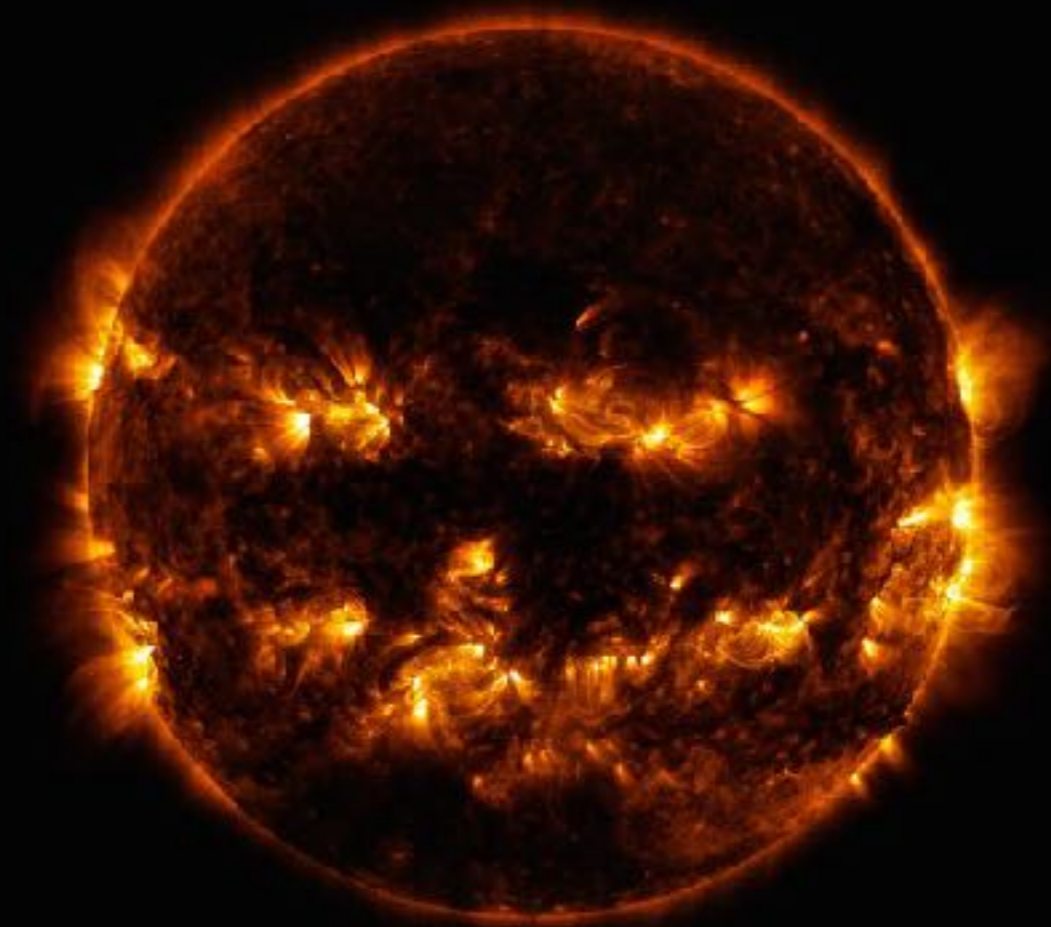


# Stellar activity

# Stellar activity

## What is stellar activity?

- **Stellar activity** refers to all phenomena in a stellar atmosphere that result in
  - **Variability** of the emitted radiation  
(on different timescales, except for pulsations, or influences of accompanying objects/disks)
  - **Heating** of the outer atmosphere  
(existence of a chromosphere, temperatures above radiative equilibrium)
- Mostly found for **cool late-type stars** due to the presence of surface convection and the resulting highly structured magnetic fields in their atmospheres
  - Initially activity thought to be produced by the dissipation of acoustic waves in the atmosphere (acoustic heating; Biermann 1948; Schwarzschild 1948).
  - Today understood that dissipation of magnetic energy is essential.
- ➔ **Magnetic activity** is synonym of stellar activity

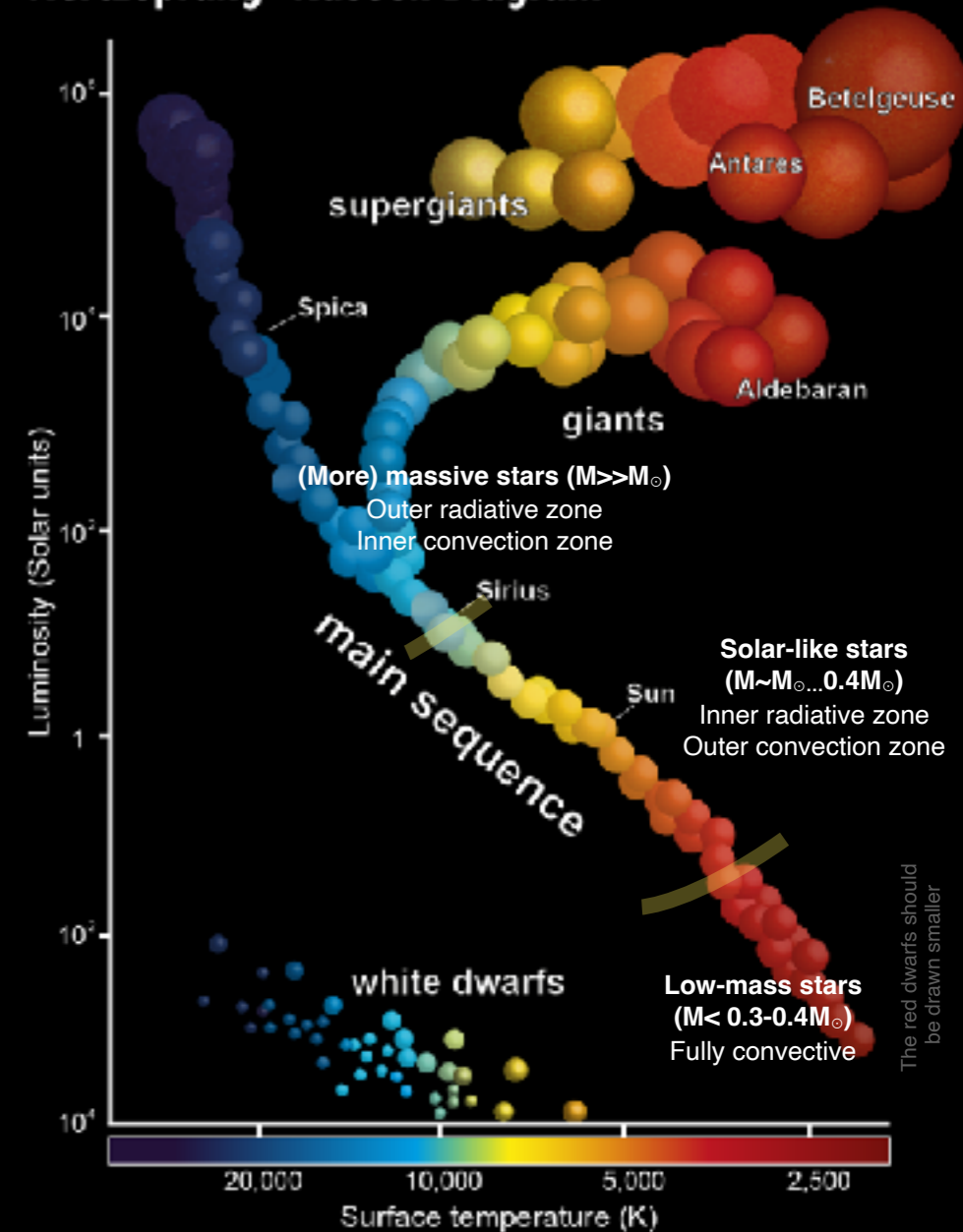


# Stellar activity

## What is stellar activity?

- We have learned so far about...
  - ... **main-sequence stars**:
    - Differences of global properties (mass, radius,  $T_{\text{eff}}$ , ...)
    - Differences in their inner structure incl. extent and location of convection zones
  - ... **the Sun**:
    - generation of magnetic via a dynamo
    - resulting solar activity cycle
  - ... radiative zone? (Tayler-Spruit / Zahn+07)
- **What do we now expect to see in terms of activity cycles for other main sequence solar-type stars?**

Hertzsprung–Russell Diagram



# Stellar activity

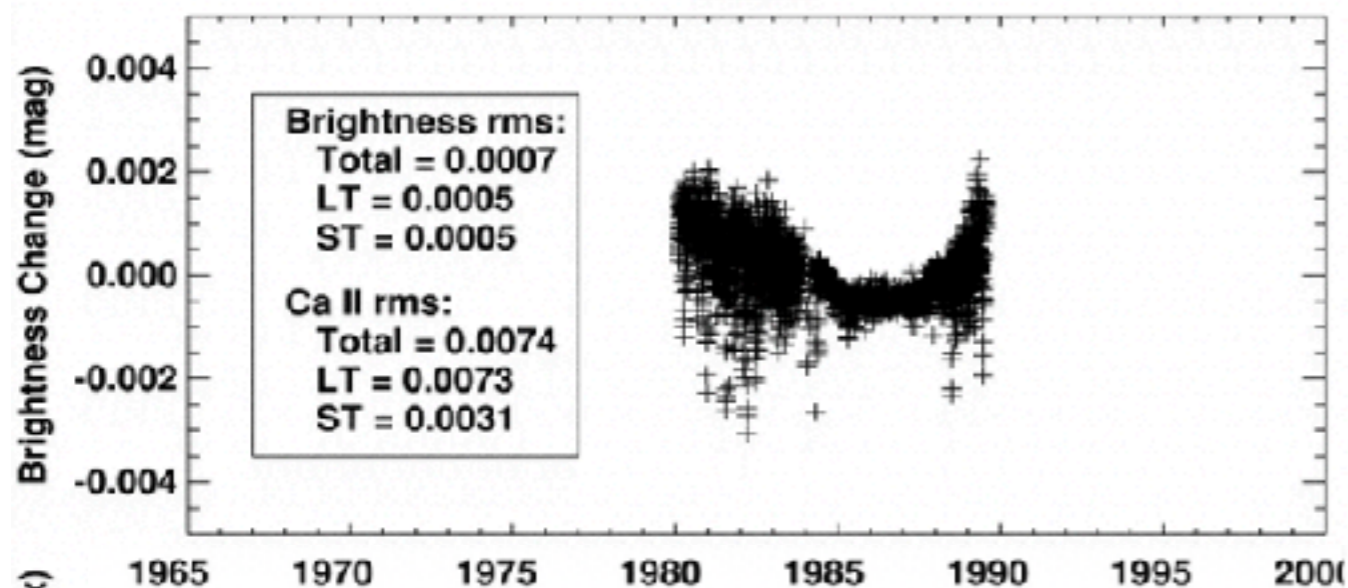
## How to detect activity cycles?

- The usual problem: Stellar observations are **spatially not resolved**, starspots not observed directly\* — no “starspot number” can be derived directly \*except for a few interferometric observations
- Visible brightness changes of Sun only few milli-mags anyway

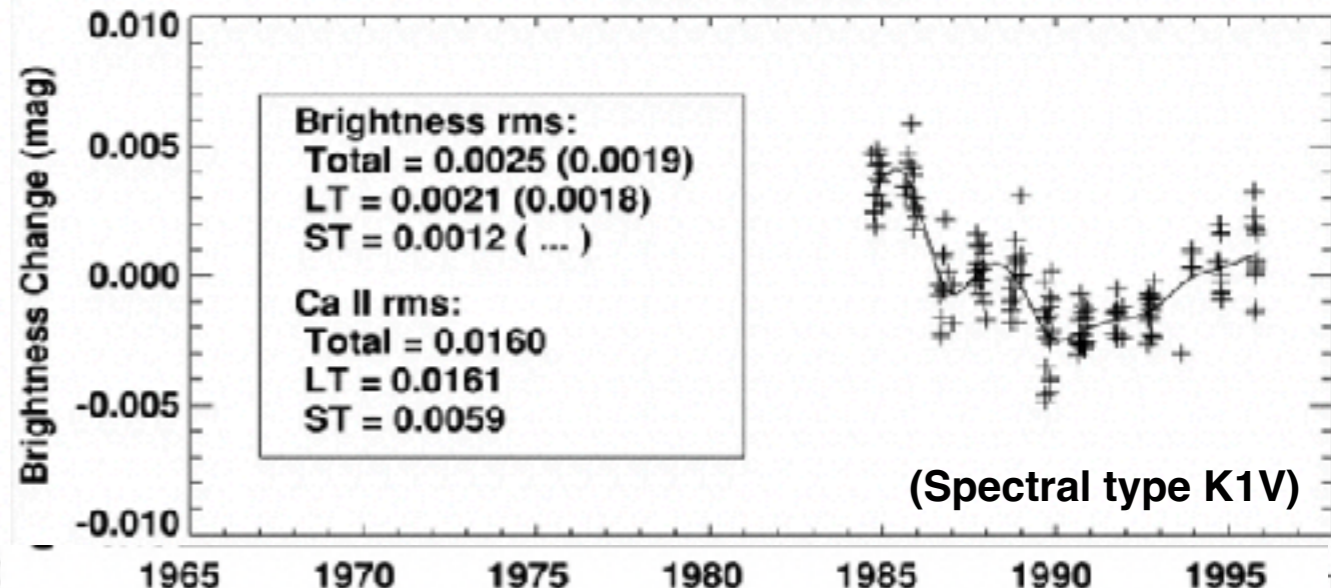
➔ More **sensitive indicators**?

➔ indicators based on spectral lines! (Example below: Ca II)

Sun



HD 10476





# Stellar activity

## Activity indicators

- Other activity indicators use impact of magnetic field on the cores of the Ca II H and K spectral lines (integrated across the (unresolved) stellar disk) : **chromosphere**
  - ➔ Measures of the overall magnetic activity level of the star, for instance:  
<https://pyastronomy.readthedocs.io/en/latest/pyasIDoc/asIDoc/sindex.html>

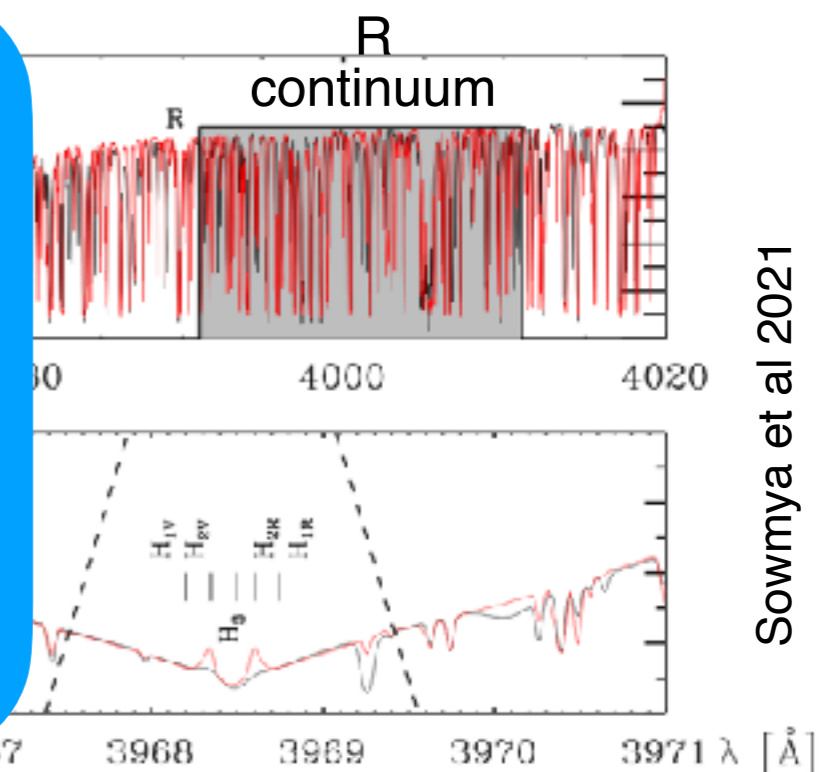
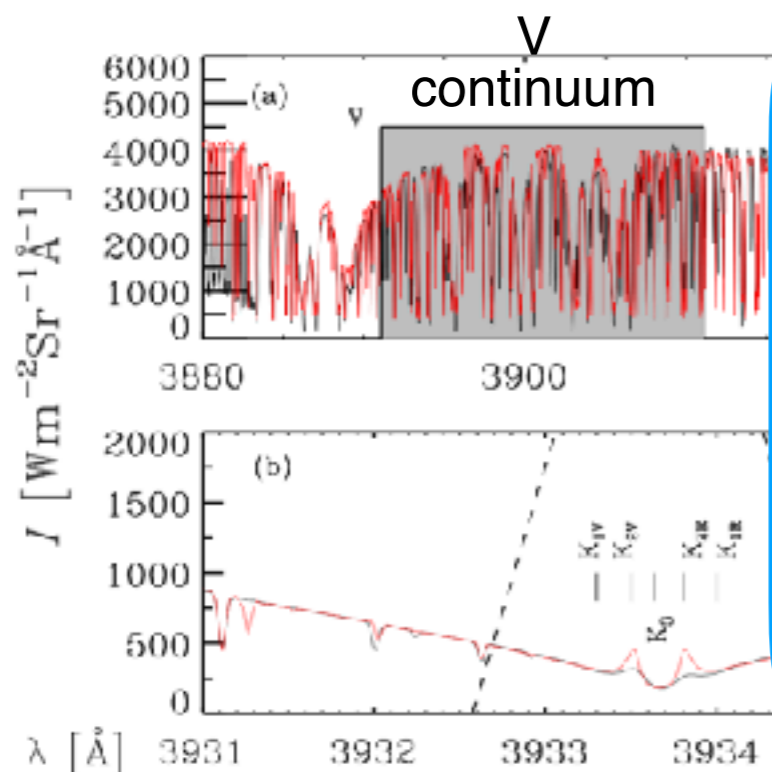
**R<sub>HK</sub>-index.** 
$$R_{HK} = \frac{F_H + F_K}{\sigma T_{eff}^4}$$

$F_{HK}$ : flux in H and K band ;  $\sigma T_{eff}^4$ : bolometric flux

**S-index** 
$$S(t) \propto \frac{N_H(t) + N_K(t)}{N_R(t) + N_V(t)}$$

$N$ : Counts (flux) in the passbands

• **Wilson-Bappu Effect (1957):** Linear relation between the **absolute magnitude** and log of **Ca II K line widths** for G-type and later stars (dwarfs and giants)  
 $M_v = 27.59 - 14.94 \log W_o$



# Stellar activity

## Activity indicators

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- When  $R_{HK}$  and the S-index are absolute measure of emitted light, they exist similar indicator looking at the variability of these emissions :

➔ 
$$R'_{HK} = \frac{F_{HK} - F_{phot}}{\sigma T_{eff}^4}$$
  $F_{HK}$ : flux,  $F_{phot}$ : flux, photospheric contributions

➔  $S_{ph}$  is a measure of the variability of the **photometric** light-curve (Santos et al. 2014)

# Stellar activity cycles

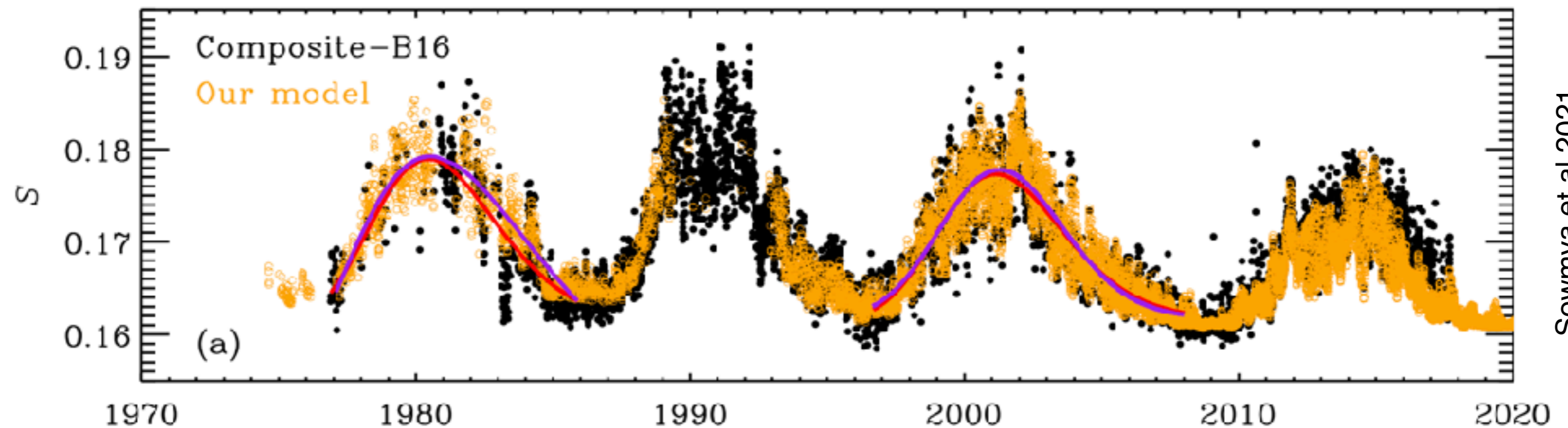
## Activity indicators

S-index

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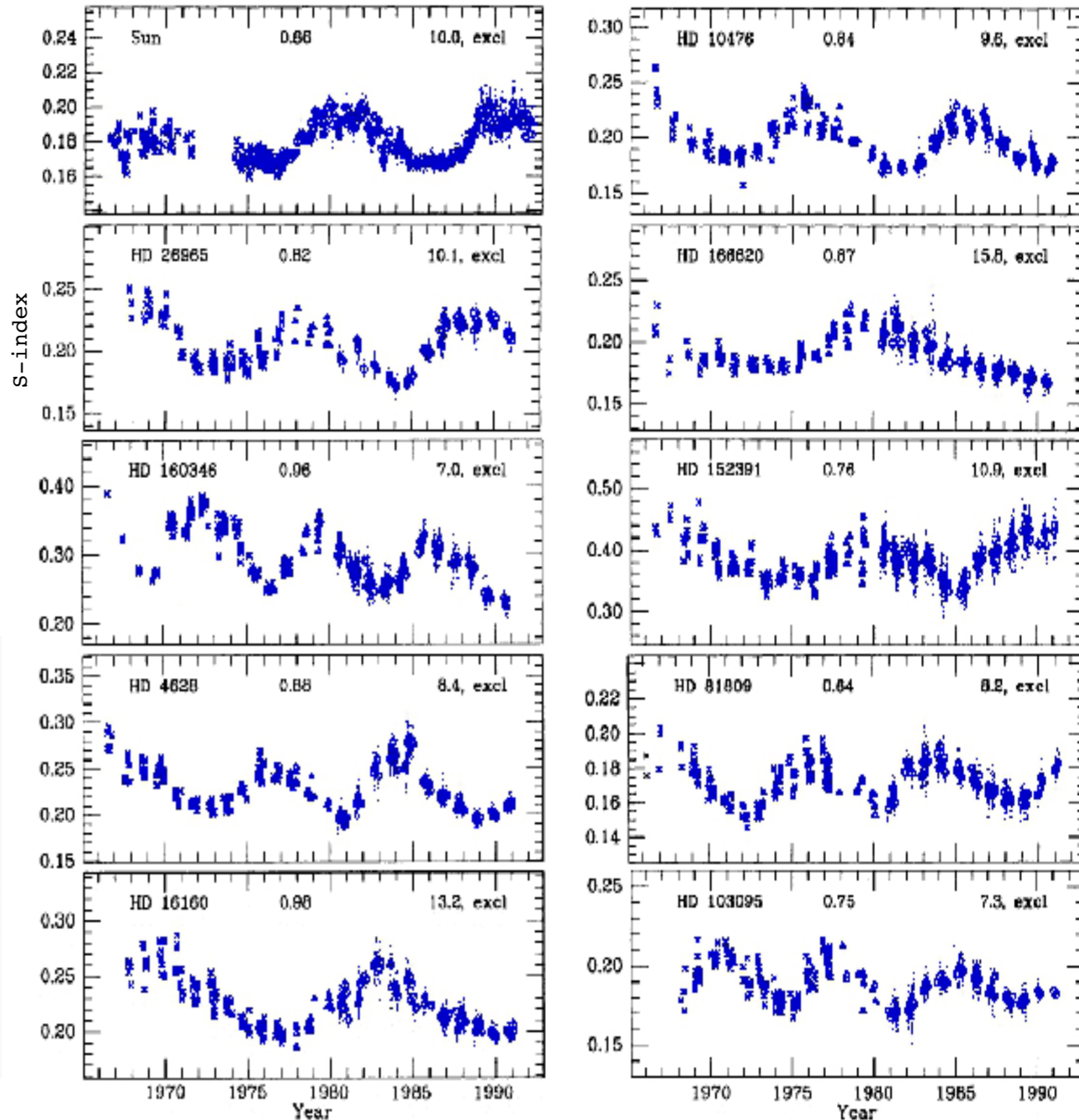
- S-index over several solar cycles (photo):



# Stellar activity cycles

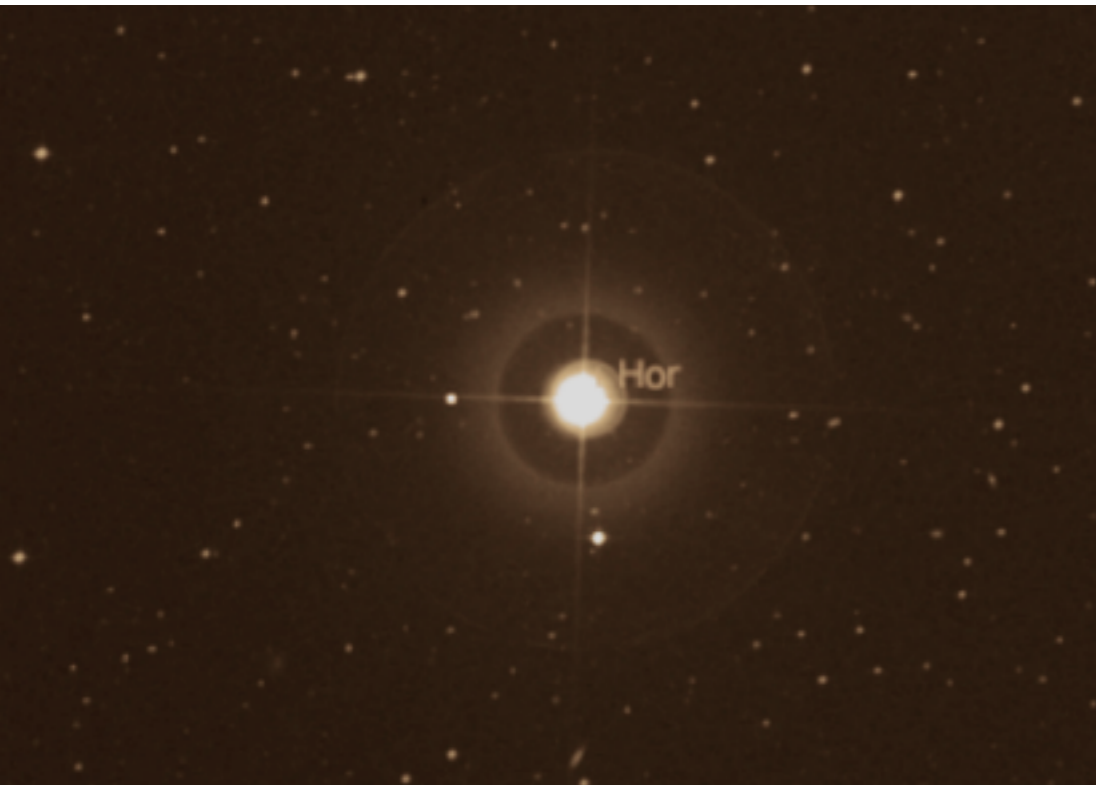
## Ca II observations

- Magnetic activity cycles found for many stars (survey at **Mount Wilson Observatory**)
- Survey ended in 2000's after more than 30 years of Ca II HK observations

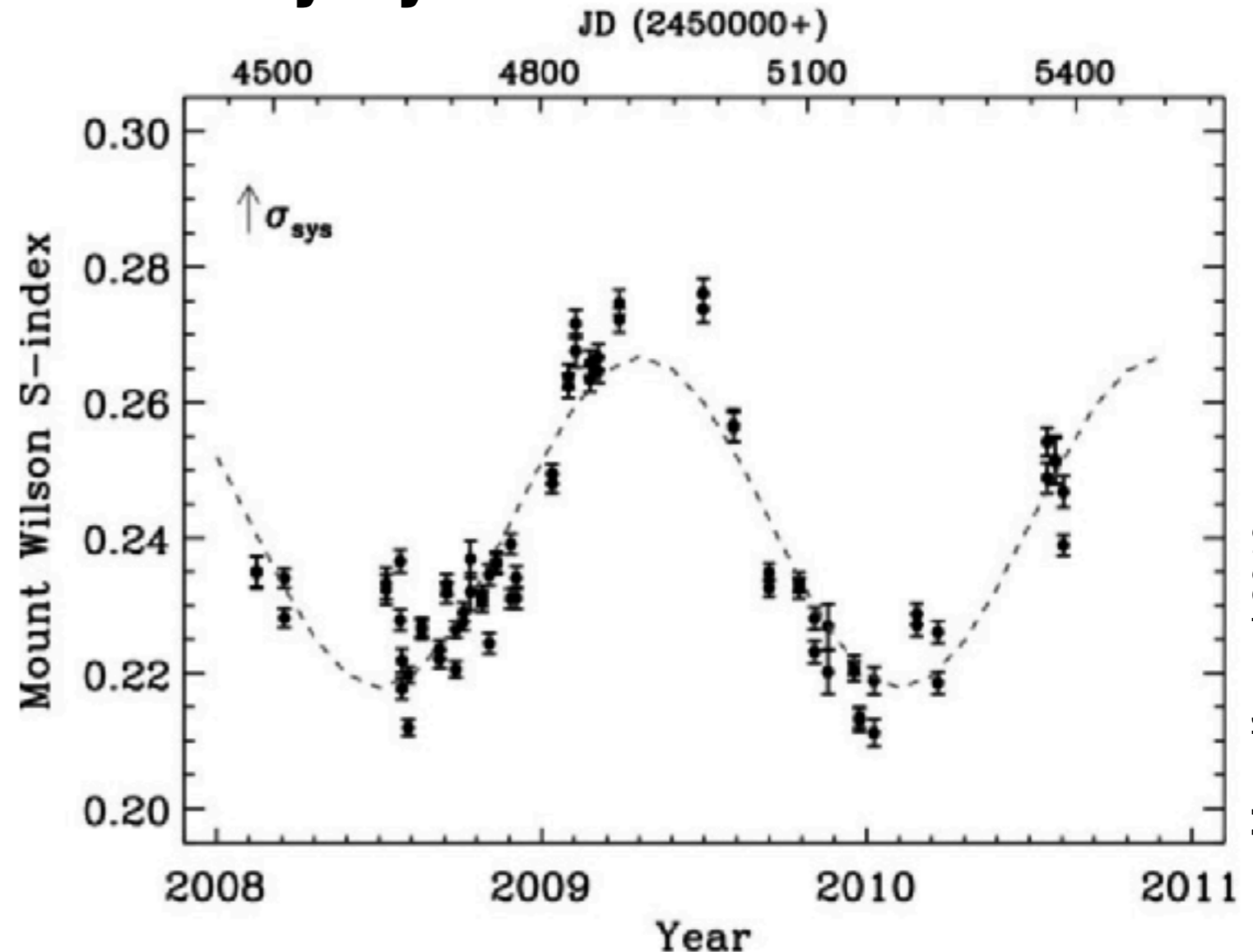


# Stellar activity cycles

## Shortest measured stellar activity cycle in a solar-like star



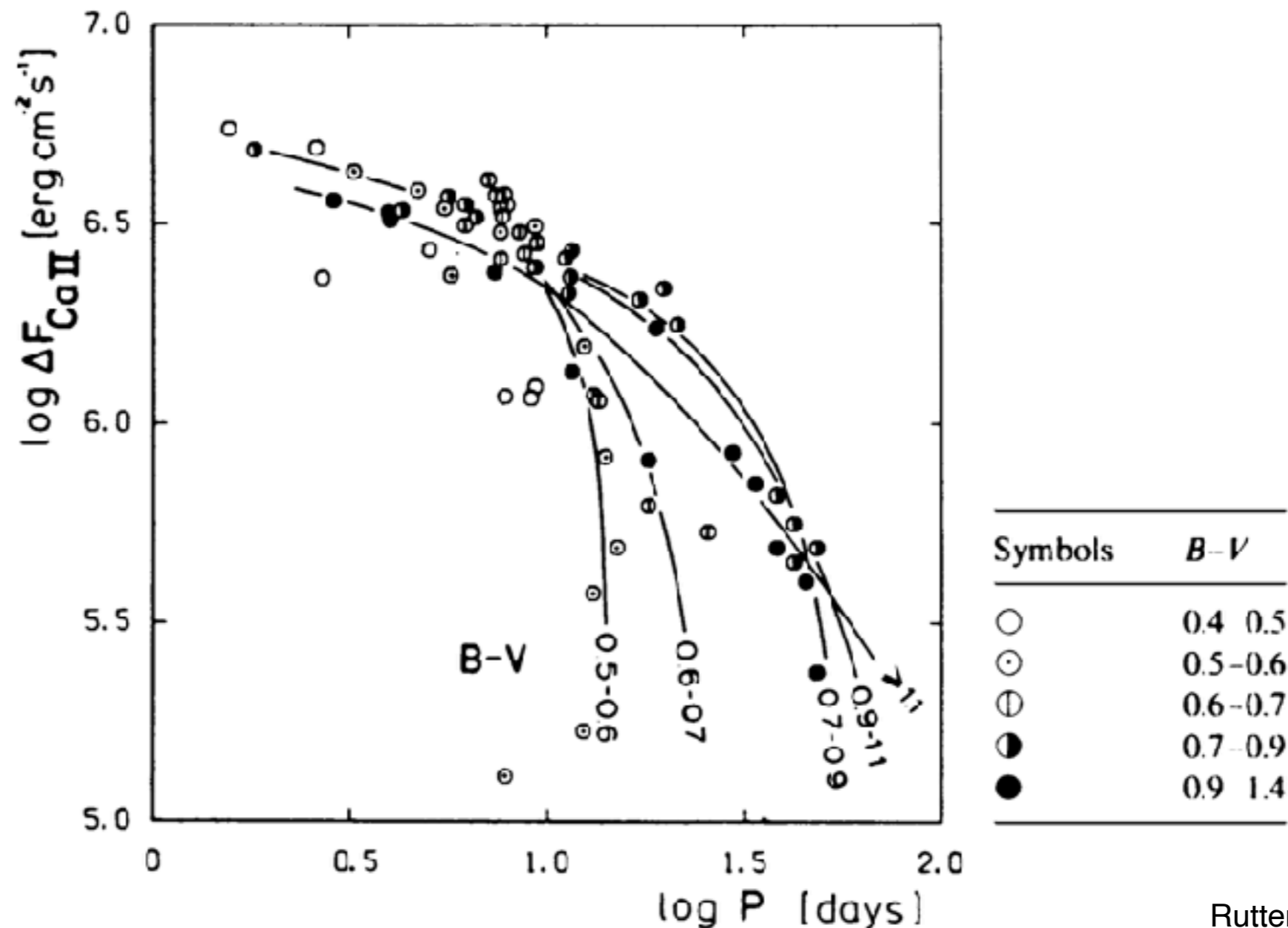
- G0V star  $\iota$  Horologii (*iota*)
- **Magnetic activity cycle of 1.6 yr**
- $M = 1.25 M_{\odot}$
- $R = 1.18 R_{\odot}$
- Rotation period 8.5 d
- Rotation speed  $v \sin i \sim 7 \text{ km s}^{-1}$ 
  - ➔ 3 times faster than the Sun, among the faster rotating stars of that spectral type
- Consistent with coronal activity cycle found from XMM x-ray measurements



# Stellar activity cycles

## Ca II observations

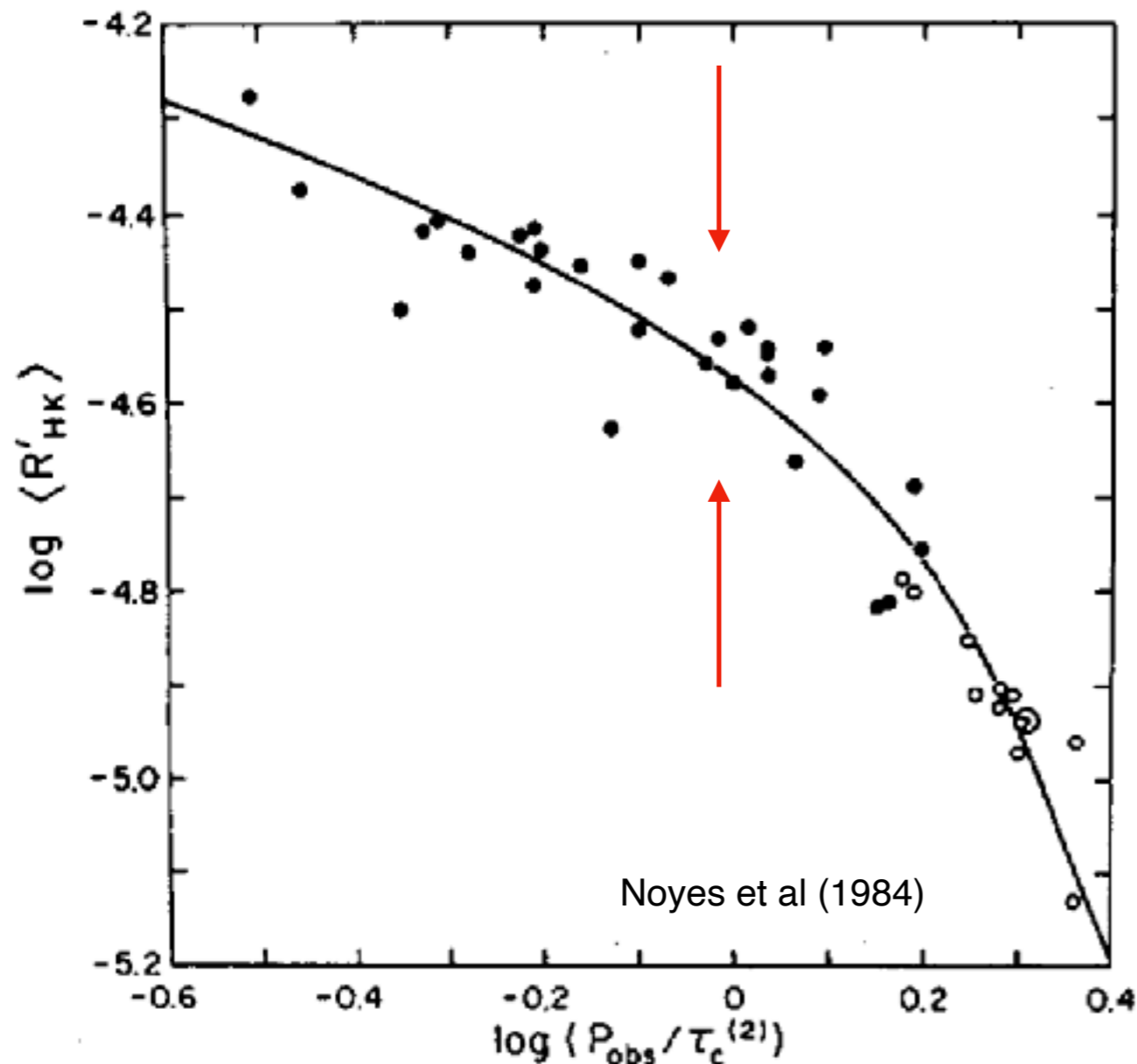
- Statistical analysis of many (cool) stars: Ca II flux vs. rotation period
- Increase of Ca II flux with decreasing rotation period
- ➔ Faster rotators have higher activity — generation of stronger magnetic field via a dynamo



# Stellar activity cycles

## Ca II observations

- Similar: Ca II activity indicator ( $R'_{\text{HK}}$ ) vs. Rossby number  
(Rossby number: ratio of observed rotation period to convective turnover time)
- Clear indication of the **importance of stellar rotation and convection** for the efficiency of stellar dynamos and the resulting (magnetic) activity level



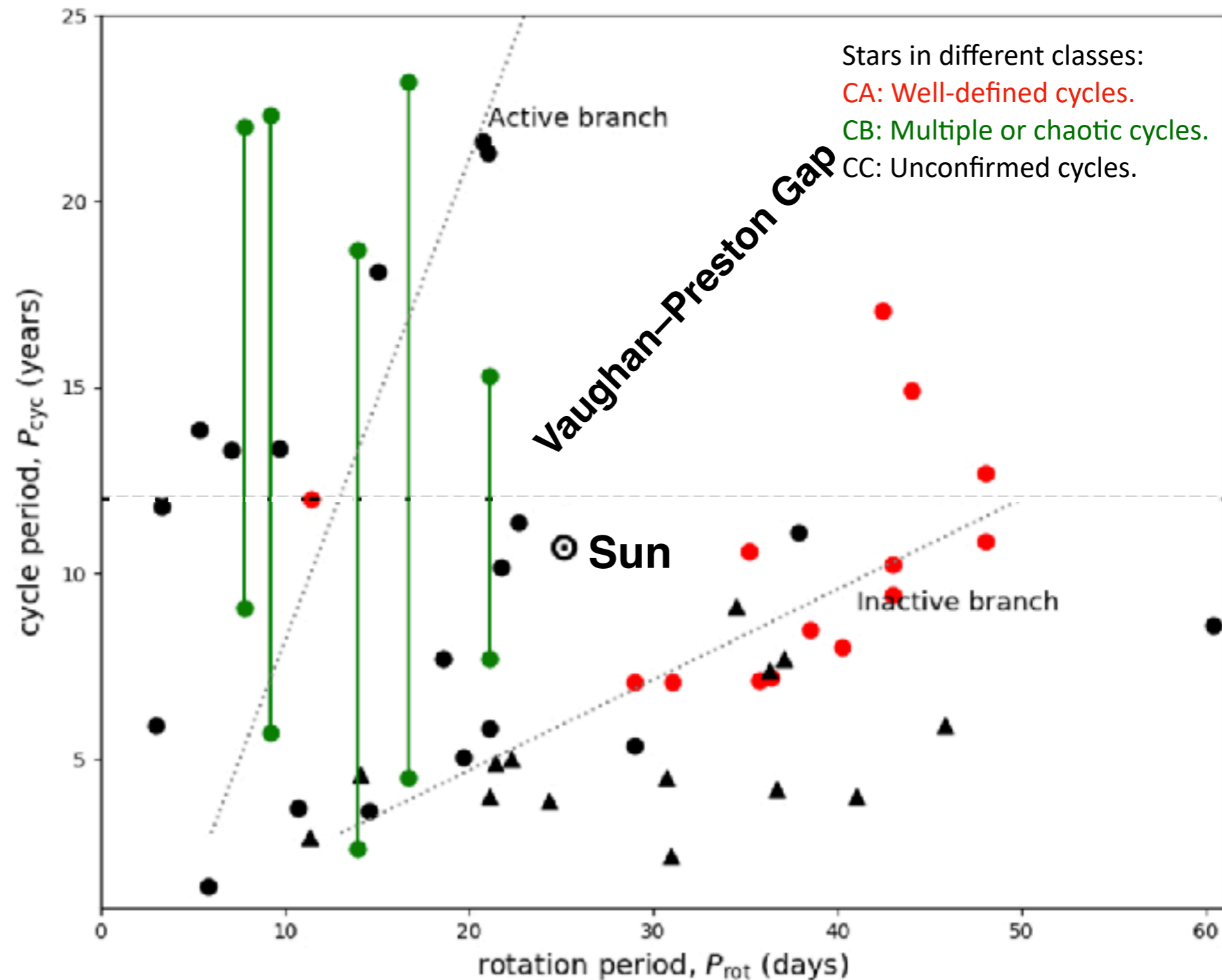
$$Ro = \frac{\text{Advection}}{\text{Coriolis}} = \frac{\text{Convection}}{\text{Rotation}} \propto \frac{M_*^{1.7}}{\Omega_*}$$

Brun et al. 2017

# Stellar activity cycles

## Activity cycle vs. rotation

- Statistics for many stars shows trend:
- Longer activity cycles for longer rotation periods
- Range between **active branch** (stars with strong activity) and **inactive branch** (stars with weak chromospheric activity)
- Branches divided by Vaughan–Preston Gap
  - *Due to properties of stellar dynamos?*
  - *Or a statistical artefact?*





# Stellar activity cycles

## Activity cycle vs. rotation

- For same stars: ratio of cycle frequency  $\omega_{\text{cyc}}$  and rotation rate  $\Omega$  vs. Rossby number

$Ro$

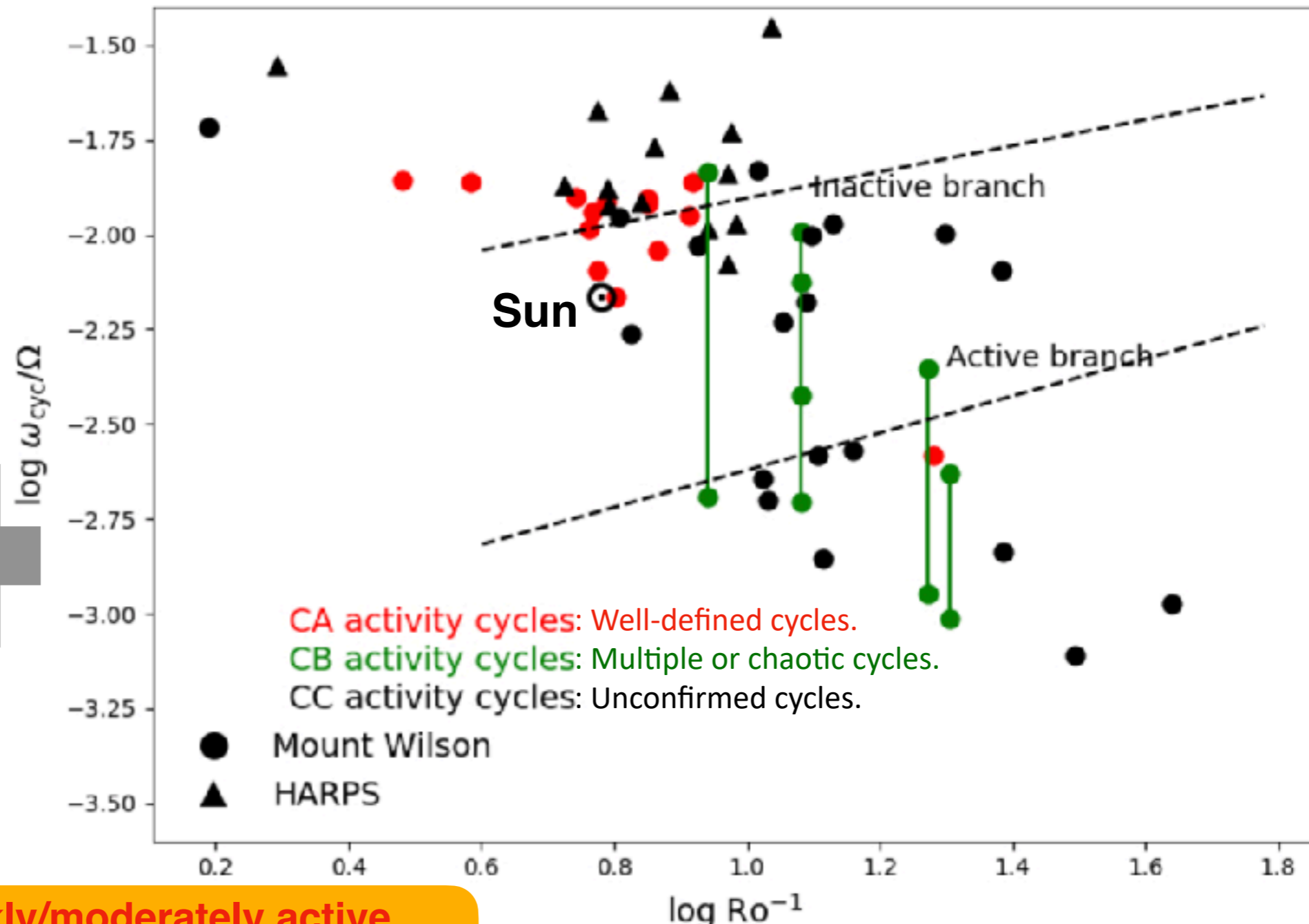
- Remember:

**Rossby number =**

ratio of inertial to Coriolis forces  
(Ratio of rotation period to convective turnover time)

- Dependence of activity cycle and Rossby number

➔ Properties of the global dynamo of stars and thus their activity cycles depend on Rossby number and

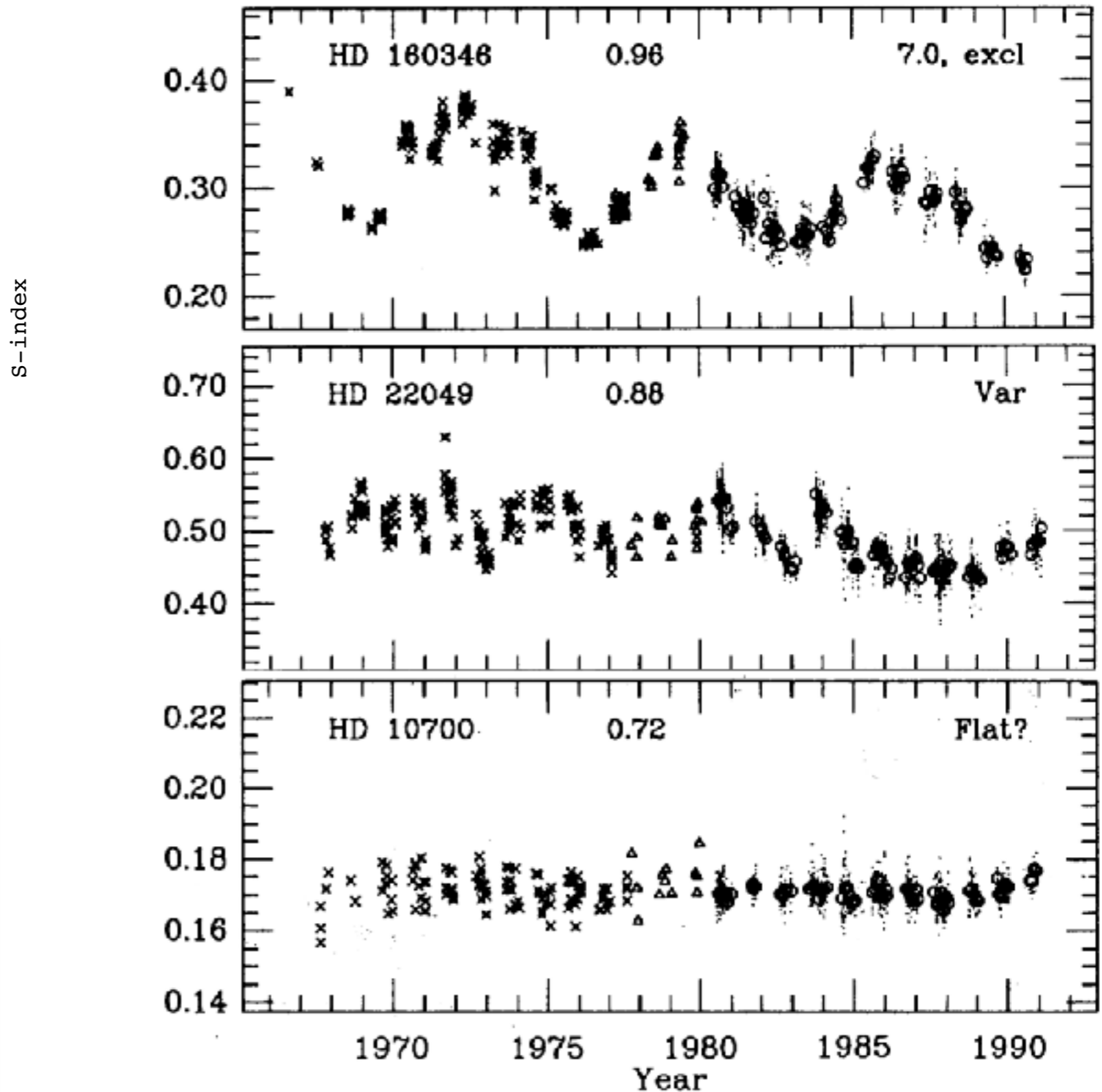


➔ The Sun is only a weakly/moderately active

# Stellar activity cycles

## Ca II observations

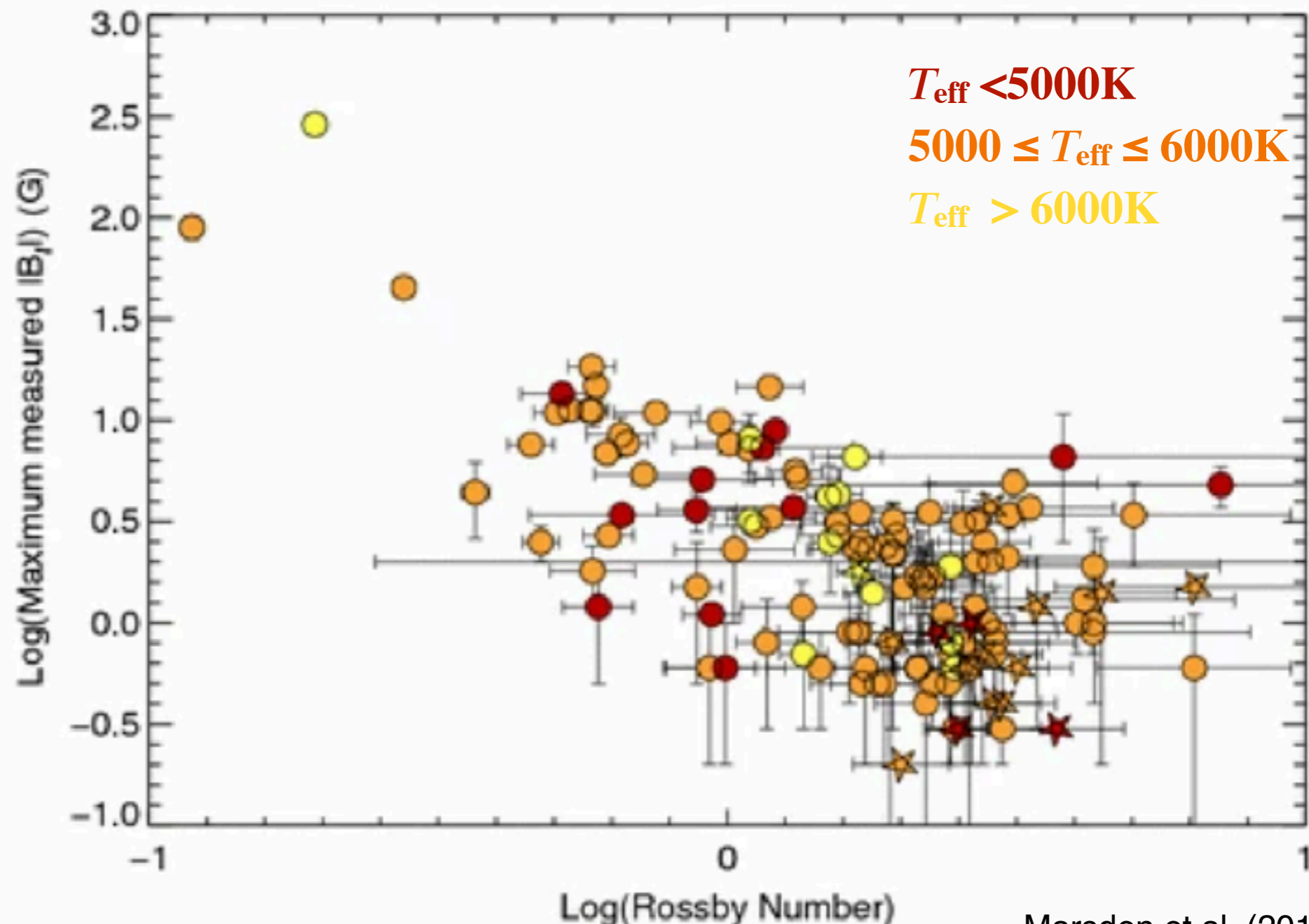
- Magnetic activity cycles found for many stars (survey at **Mount Wilson Observatory**)
- Not all stars have clear magnetic cycle, some may have none
  - ➔ **Stationary dynamo?**
  - ➔ **Observational biases?**



# Stellar activity cycles

## Stellar dynamos

- BCOOL survey: Magnetic field strength correlates with Rossby number in solar-like stars and subgiants.
- Trend: Stronger magnetic fields for smaller Rossby numbers
- Supports rotation being important for global stellar dynamos and thus the generation of magnetic field

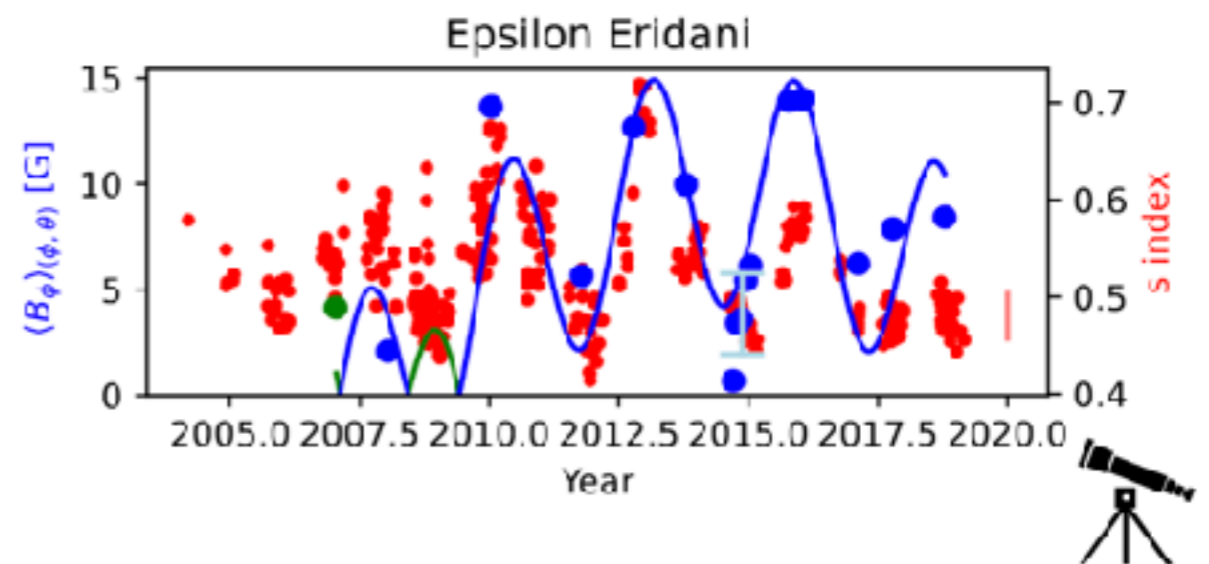
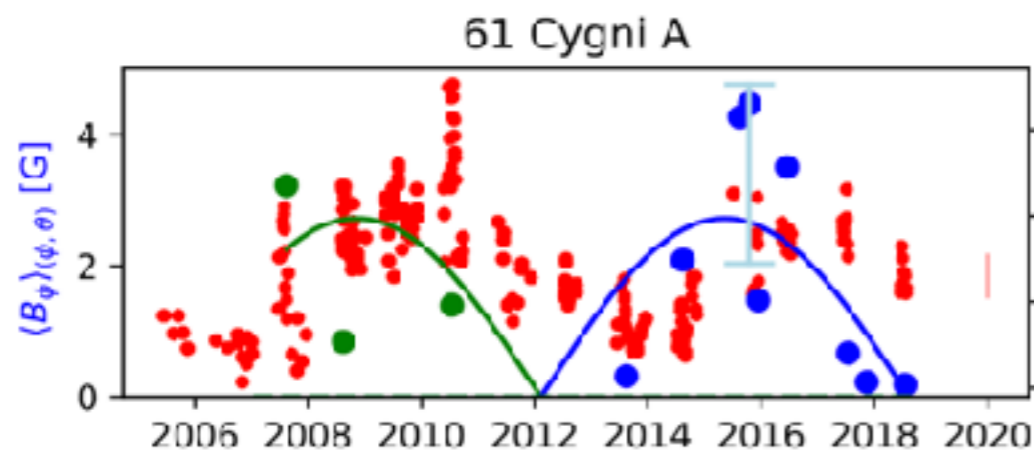


# Stellar activity cycles

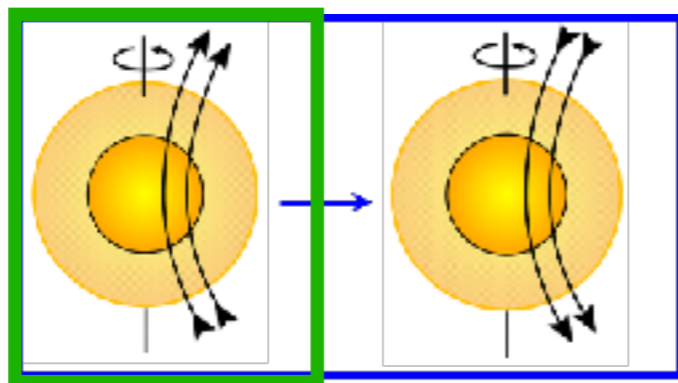
## Stellar dynamos

- BCOOL survey: **different nature of magnetic cycle can be found**

Jeffers et al. (2022)



- Cyclic global polarity reversal



No cyclic global reversal

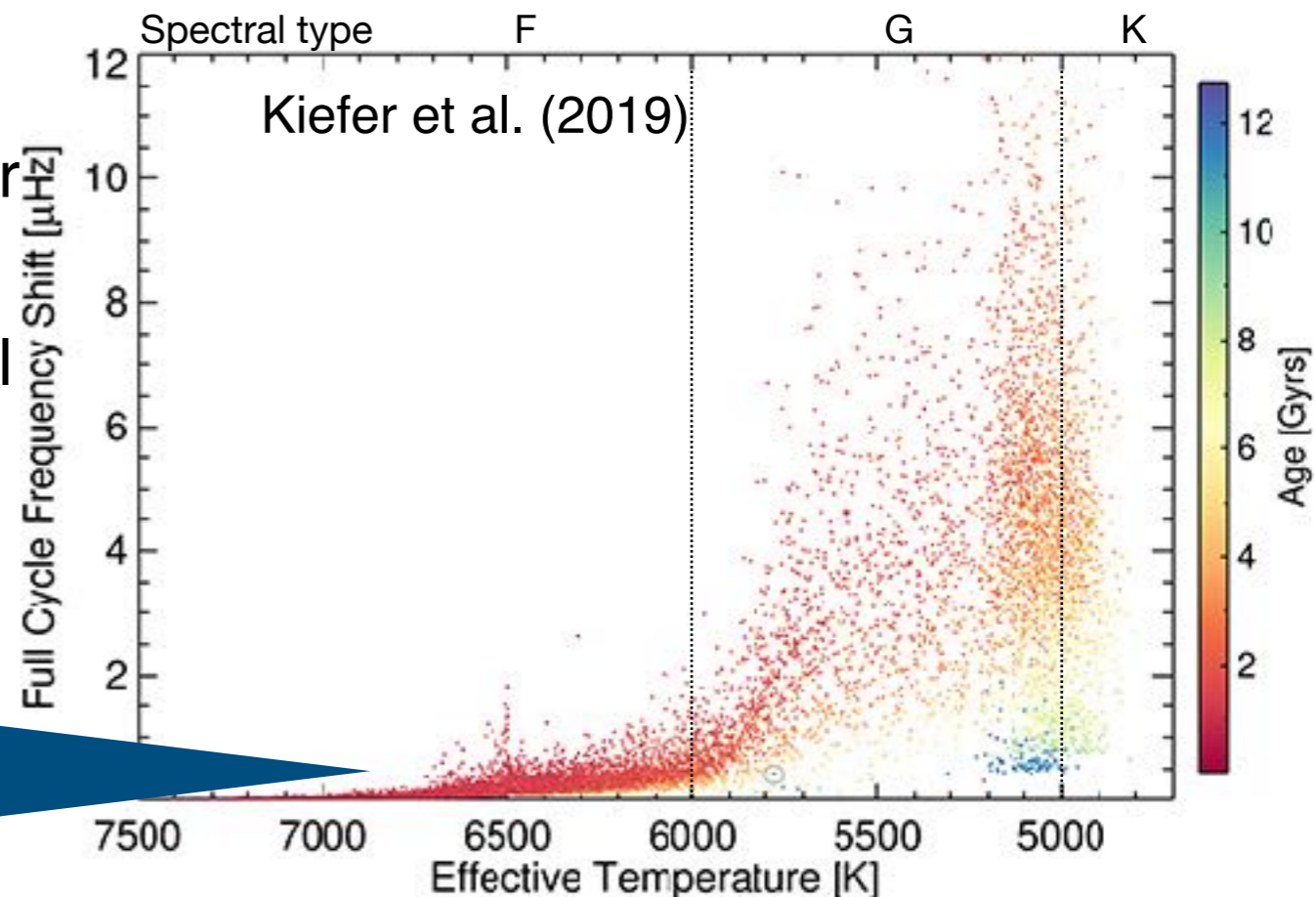
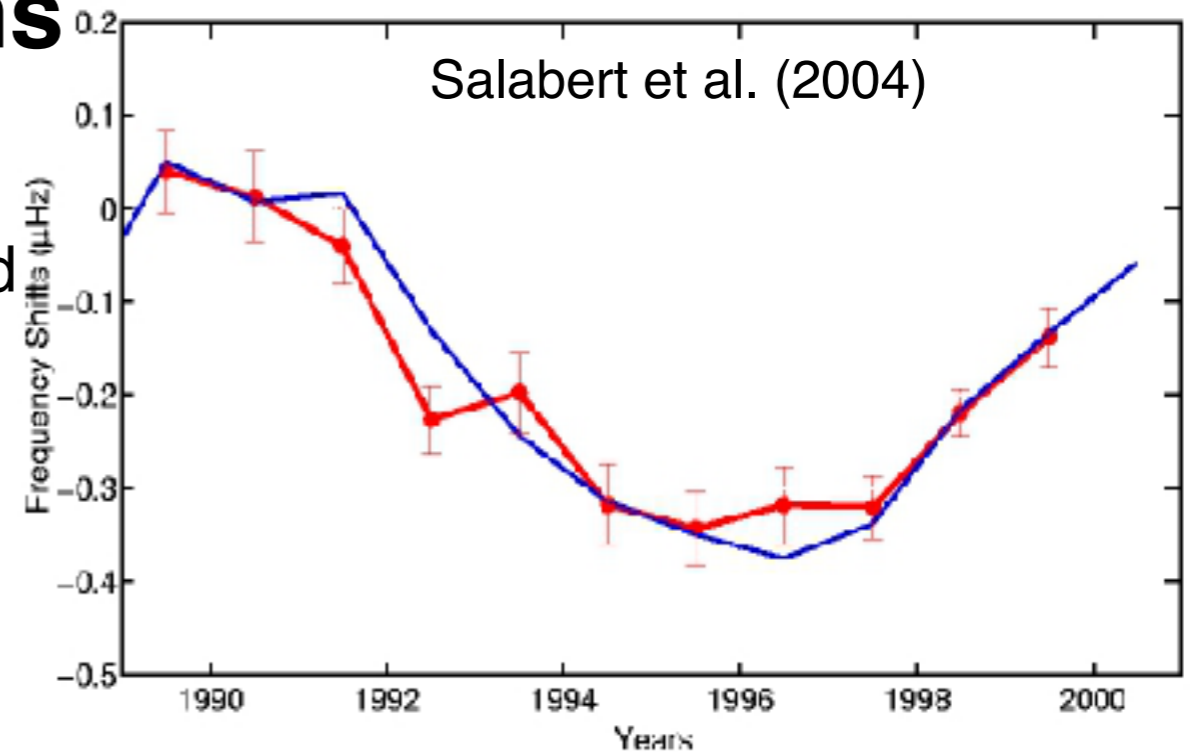
- Hard to characterized, global reversals only found for **5 stars** :  
61 Cigny A ;  $\epsilon$  - Eridani ;  $\kappa$  Ceti ; AF Lep & V1358 Ori

(Bourrier et al. 2018, Jeffers et al. 2022, Boro Saikia et al. 2022, Marsden et al. 2021)

# Stellar activity cycles

## Impact on stellar oscillations

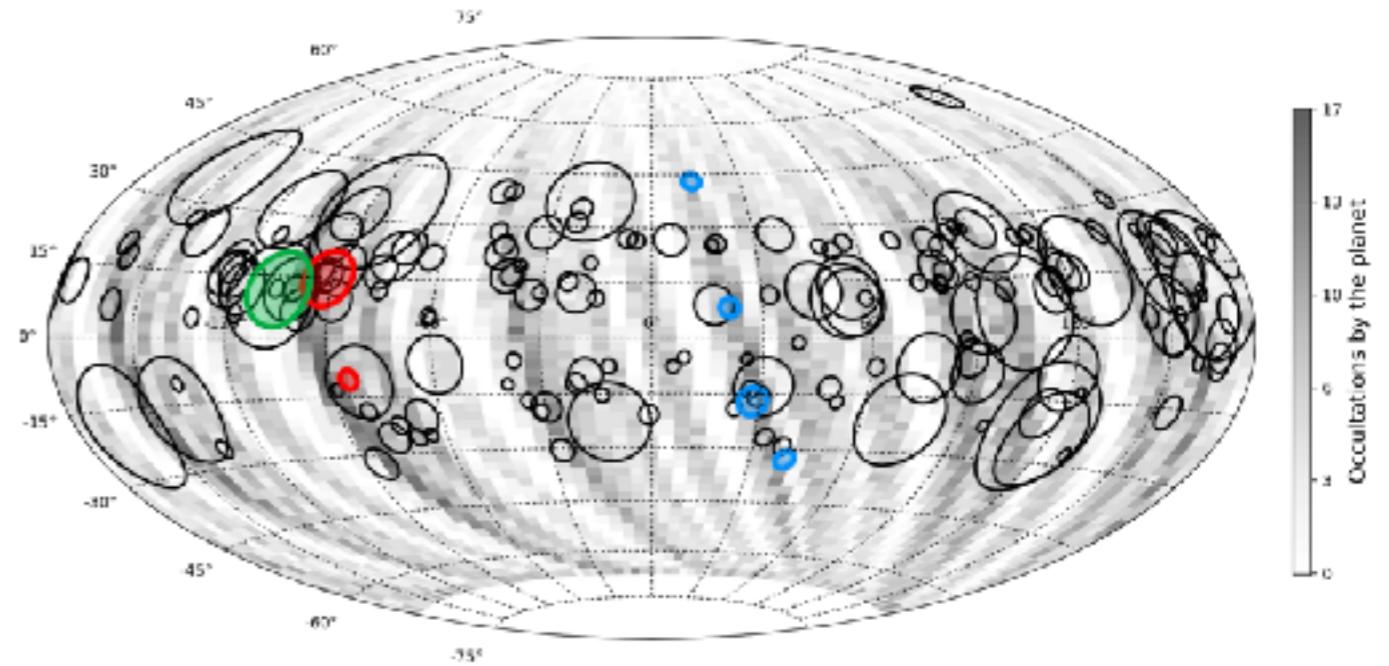
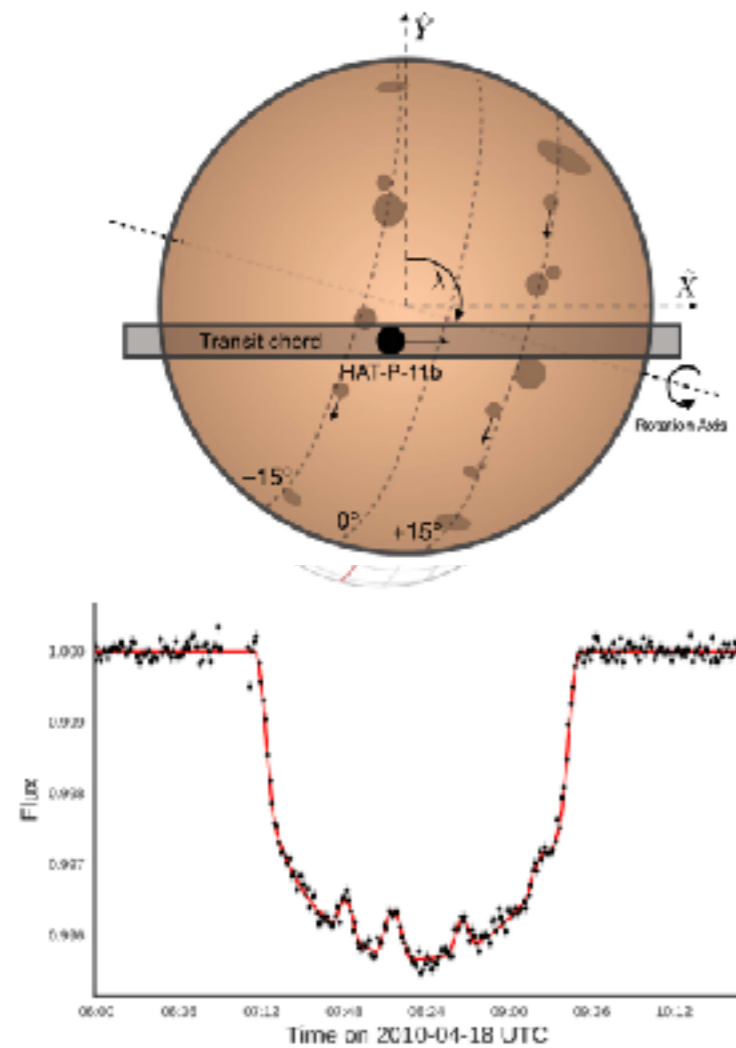
- Magnetic field modifies the near-surface propagation speed, convective velocity and interior stratification
  - ➔ Results in frequency shifts of p-modes!
- Solar p-mode shifts first detected in 1990, depend on frequency and degree
- Even the lowest degree solar p-modes are shifted by the magnetic cycle
- The amplitude of shifts depend on stellar properties (spectral type,  $T_{\text{eff}}$ , age...)
- ➔ Asteroseismology can provide additional constraints for stellar activity cycles



- Note the effect being much smaller for F-type stars
- ➔ Global dynamo needs surface convection

# Stellar activity cycles

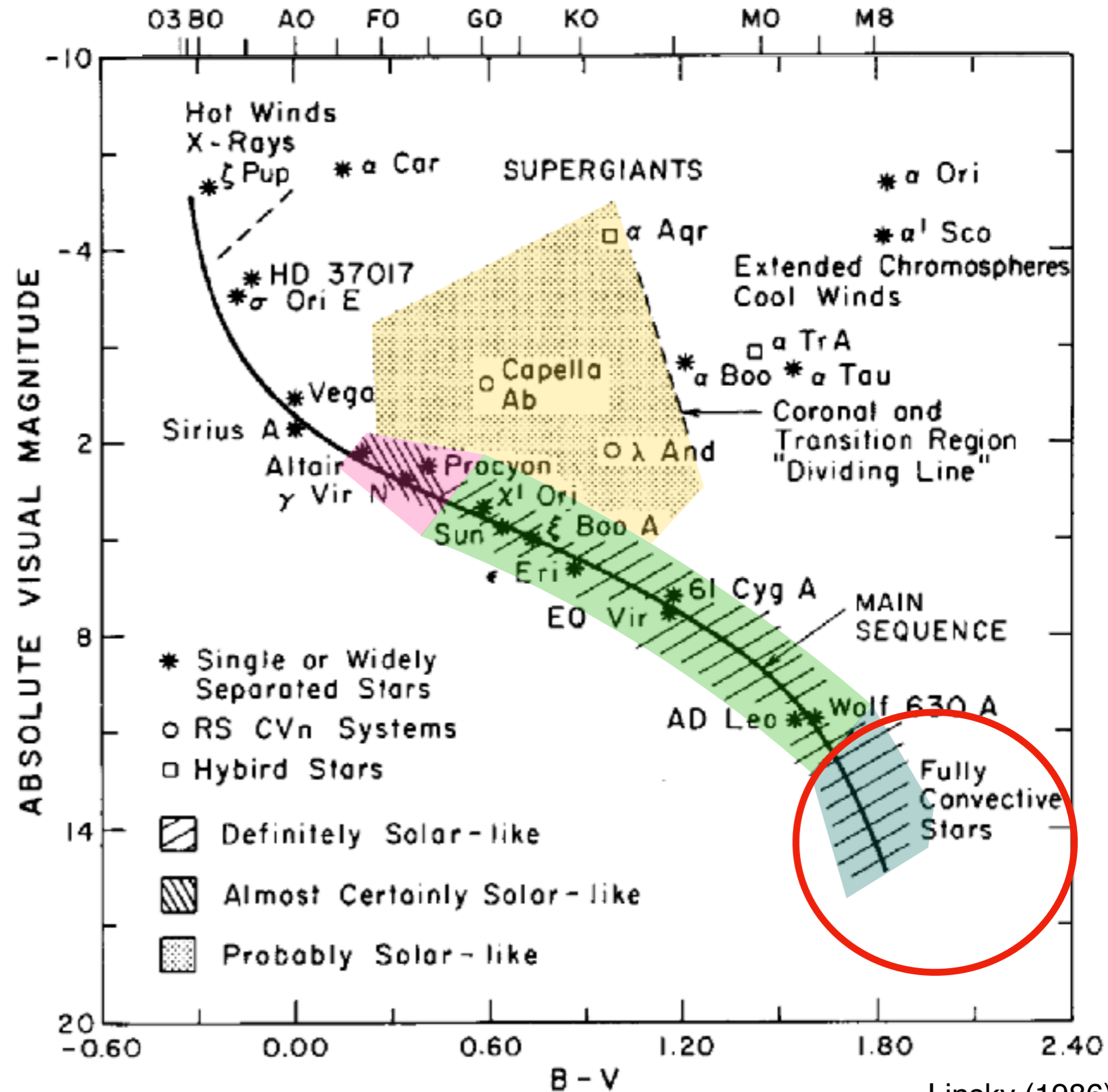
## “Photometric help” from transit



# Stellar activity

## Across the HRD

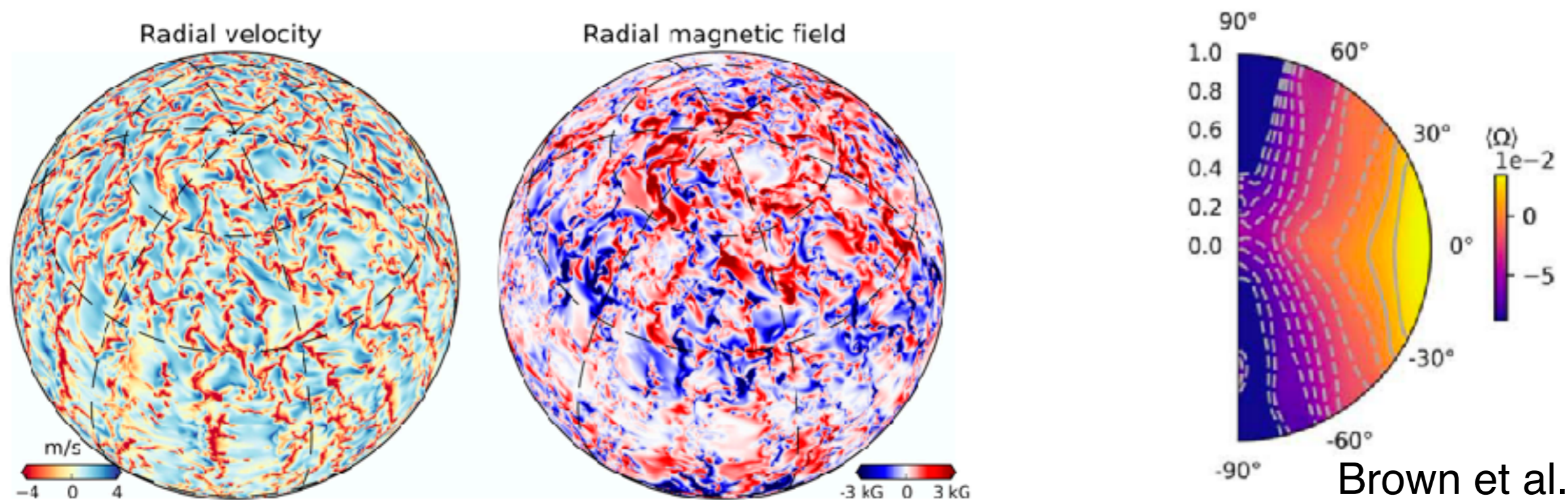
- Activity across the HRD as indicated by the existence of chromospheres (and coronae), resulting emission (e.g. Ca II), and (measurable) magnetic fields
- Clearly connected to presence of surface convection



# Stellar dynamos

## Fully convective stars

- **Example: Proxima Centauri** — representative of slowly rotating **fully convective** M-dwarfs (Stars with low mass  $M < 0.3-0.4M_{\odot}$ ) - **no tachocline**
- Numerical simulations (Yadav et al. 2016) show **rotating convection spontaneously generates differential rotation** in the convection zone (without the need of a tachocline)



Brown et al. 2020

Figure 4. Radial velocity and radial magnetic field on a layer close to the outer boundary ( $r = 0.97r_p$ ) of the simulation. Note that this snapshot is from a simulation segment that was run on a higher-resolution grid (2048 in longitude, 1024 in latitude, 161 in radius).

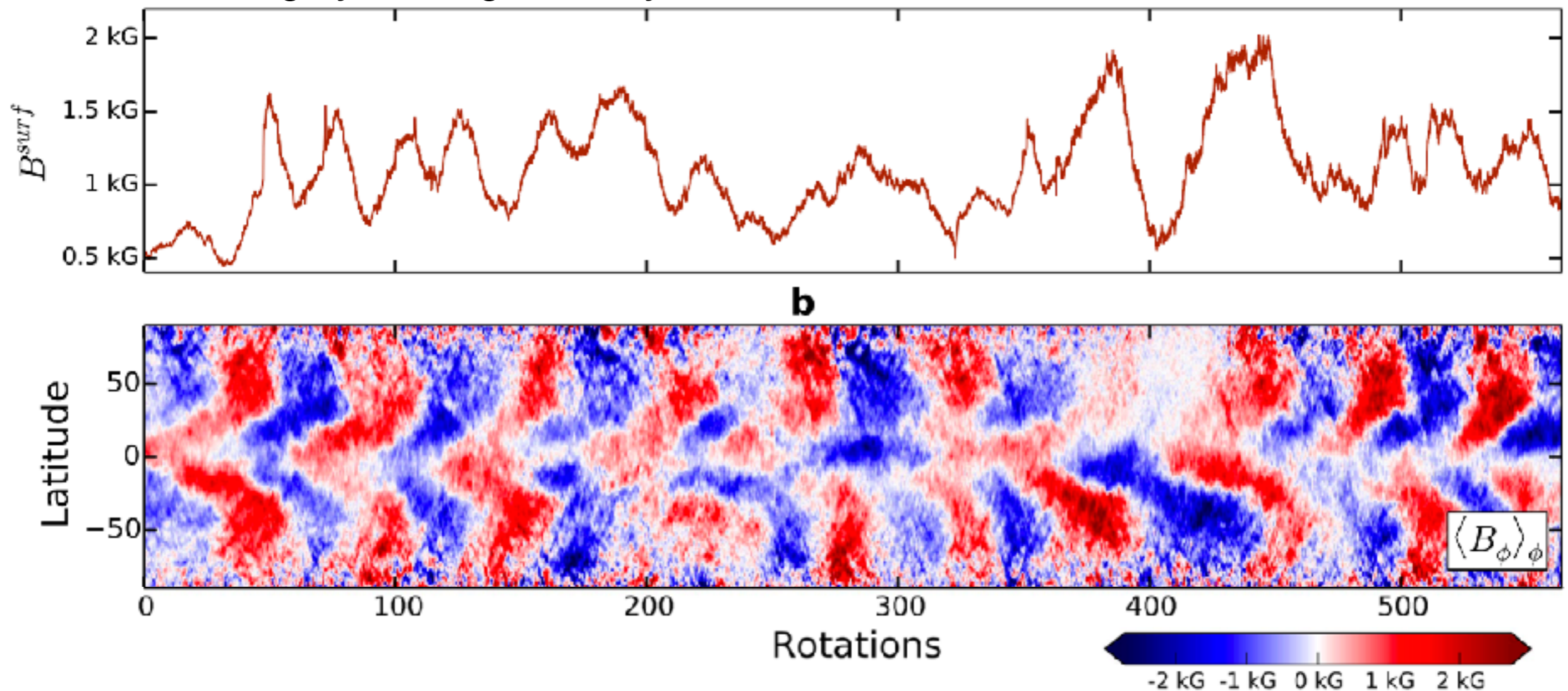
- Observational challenging: very faint objects, but active in  $H\alpha$
- Relationship rotation rate — activity level poorly known for M-type dwarf stars
- Many M-dwarfs relatively rapid rotators



# Stellar dynamos

## Fully convective stars

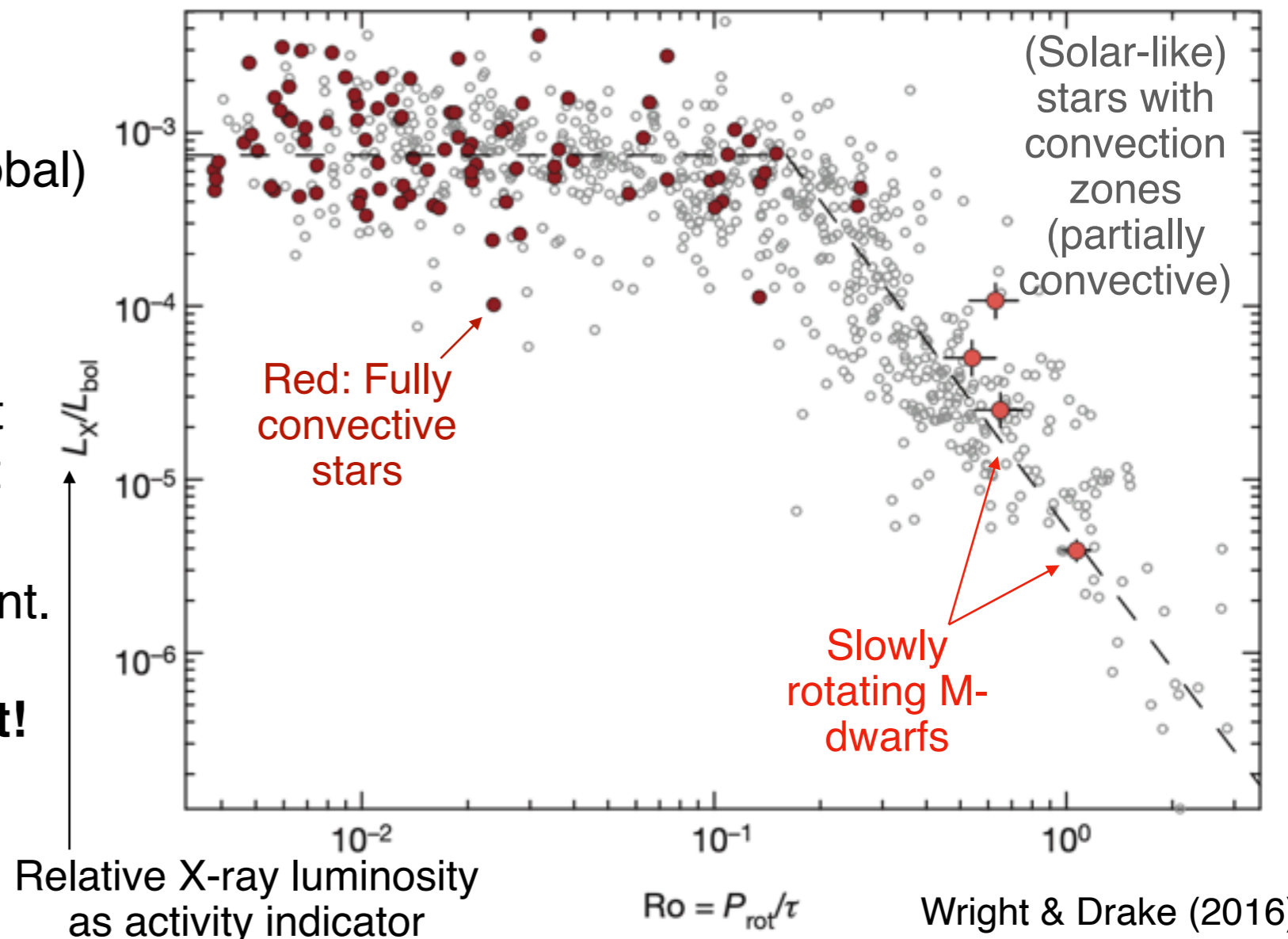
- **Example: Proxima Centauri** — representative of slowly rotating fully convective M-dwarfs
  - Drives magnetic cycles with axisymmetric magnetic field repeatedly changing polarity at all latitudes as time progress.
  - Resulting cycle length of  $\sim 9$ yr in line with observations of Proxima Centauri



# Stellar dynamos and activity

## Rotation-activity relation

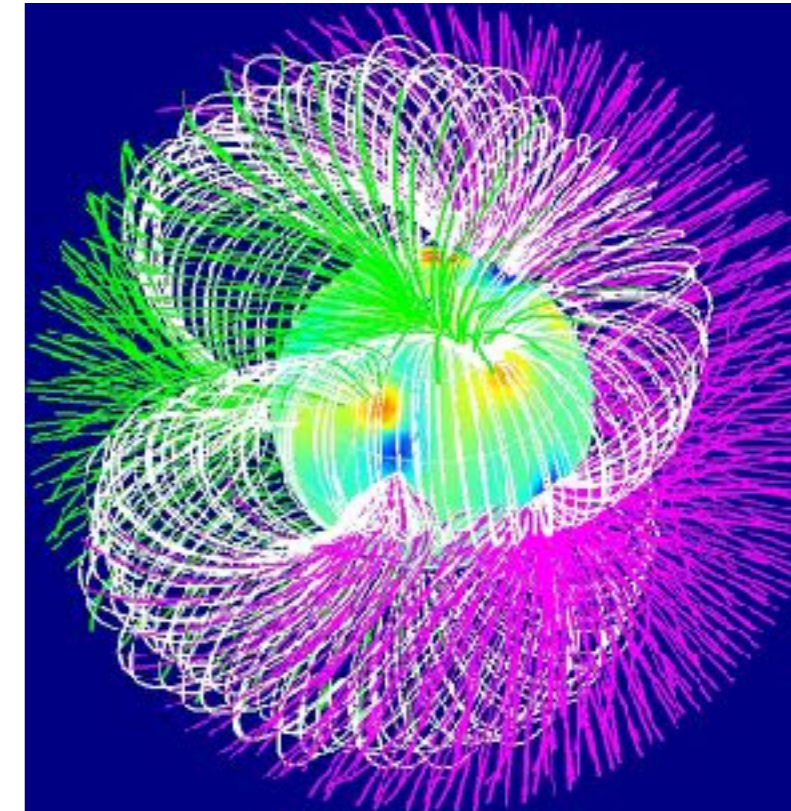
- Despite lack of a tachocline: Fully convective M-dwarfs fit the same rotation–activity sequence as solar-type stars with outer convection zones!
- Activity and magnetism of late-type stars increase with decreasing Rossby number, then saturate
- Most likely explanation (Wright & Drake 2016):
  - Both rotation and turbulence (convection) important for (global) dynamos in all late-type stars (Lehtinen et al 2020)
  - Fully and partially convective stars have rotation-dependent dynamos that share important properties
  - Tachocline not a vital ingredient. — **Differential rotation + Coriolis force is sufficient!**
  - **Still many open questions, active field of research!**



# Measuring magnetic fields

## Zeeman Doppler Imaging (ZDI)

- ZDI: observational constraints for dynamos in Sun-like stars
- Commonly used: Problem: Latitude degeneracy -
  - ZDI cannot always distinguish the hemisphere in which the starspots are located
  - Uncertain north–south distribution of starspot active latitudes
  - Limits constraints of dynamo theory !
- Alternative measurements via direct interferometric imaging



### Example: II Pegasi A (HD 224085)

