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## Partial solutions to problems: Part 3C

## Exercise 3C.1

1. We use supplied formula for pp-chain:

$$\epsilon_{pp} \approx \epsilon_{0,pp} X_H^2 \rho T_6^4 \approx 0.001$$

where  $\epsilon_{0,pp} = 1.08 \cdot 10^{-12}, \ X_H = 0.33, \ \rho = 1.5 \cdot 10^5$  and T = 15.7. Similarly,a

$$\epsilon_{cno} \approx 3.4 \cdot 10^{-4}$$

and

$$\epsilon_{3\alpha} \approx 0$$

as  $0.157^{41} \approx 0$ .

- 2. We see that  $\epsilon_{pp}/\epsilon_{cno} \approx 3$ , which is way off the 1% expectation. This answer is wrong because we assumed that the temperature is constant in the core, which is not true: the high temperatures are only evident in the center of the core. This means that most of the energy is created at lower temperatures, where the pp chain dominates. The  $3\alpha$  is practically non-existing.
- 3. With  $T=13\cdot 10^6 K$ , we obtain a ratio  $\epsilon_{pp}/\epsilon_{cno}\approx 65$ , which is more closer to reality (that is, pp dominates CNO by approx 1.5%).
- 4. At what temperature T is  $\epsilon_{pp} = \epsilon_{CNO}$ ? We equate:

$$\epsilon_{0,pp} X_H^2 \rho T_6^4 = \epsilon_{0,CNO} X_H X_{CNO} \rho T_6^{20}$$

Solving for  $T_6$ :

$$T = \left(\frac{\epsilon_{0,pp} X_H}{\epsilon_{0,CNO} X_{CNO}}\right)^{\frac{1}{16}} \approx 17$$

such that CNO dominates from 17 million K (assuming the temperature in the core is homogeneous).

5. The total energy  $L_{sun}$  emmitted from the sun must equal the total mass inside the core of the sun multiplied with the reaction rate:

$$L_{sun} = \frac{4}{3}\pi R^3 \cdot \rho \cdot \epsilon$$

Solving for R:

$$R = \left(\frac{3L_{sun}}{4\pi\rho\epsilon}\right)^{1/3} \approx 0.15R_{sun}$$

when the values have been inserted.

6. Using the same equation as in the previous question, we obtain that  $R \approx 0.6 R_{sun}$ .