

Initial laboratory course in FYS-KJM4740

The NMR data obtained and discussed in this tutorial are acquired on a Maran Ultra NMR instrument, operating at 23 MHz proton frequency. All data are available on the home page of the course. All students must write up a report based on the experimental findings. Relevant raw data and model fits must be included in the report.

Exercise 1

- a) The ^1H -NMR FID of water confined between glass beads was acquired after applying an rf-pulse for a time t_p ($= 0.5, 1.0, 1.5, 2.00, 2.50, 3.0, 3.50, 4.00, 4.50$ and $5.00 \mu\text{s}$). The observed signal intensity $I(t_p)$ is found on the home page of the course: *Exp1/Results I(t_p)*. Discuss the results and calculate the strength B_1 (gauss) of the rf-pulse?

- b) The ^1H -NMR FID (real/imaginary) of water confined between glass beads was acquired with an apparent rf-offset denoted O1. The results are found on the home page of the course: *O1 nnnnnn.0001.Dat*.

It is known that the actual frequency offset $\Delta\nu$ (or the frequency in the rotating frame of reference) is related to O1 by the formula:

$$\Delta\nu = \nu_{\text{rf}} - \nu_0 = \text{O1} + \text{constant (Hz)} \quad (1)$$

With ν_0 being the Larmor frequency of the nucleus and ν_{rf} is the frequency of the radio pulse. Hence, the real part $R(t)$ of the FID reads:

$$R(t) = I_0 \cos(2\pi\Delta\nu \cdot t + \theta) \quad (2)$$

where θ represents the phase shift. Determine the period length P (in seconds) from the real part $R(t)$ of the FID and calculate:

$$\Delta\nu = 1/P \quad (3)$$

for each O1. Plot $\Delta\nu$ (Eq 3) against O1 and discuss your results. Are your results in agreement with Eq 1?

- c) The FID is acquired on-resonance. For a liquid, the FID or $F(t)$ is theoretically expected to be described by a single exponential function. Hence, fit $F(t)$ to a single exponential function: $\exp(-R_2 t)$ as well as to a single Gaussian function: $\exp(-(R_2 t)^2)$ and try to explain your results
(Hint: inhomogeneous magnetic field).
- d) A 90° rf-pulse followed by a repetition delay time t_{RD} and a subsequent 90° rf-pulse (measuring pulse) is applied on water confined between glass beads for four (4) different repetition delays t_{RD} ($= 3\text{s}, 2\text{s}, 1\text{s}$ and 0.5s). The observed FID is denoted $F(t; t_{\text{RD}})$ with t being time. Show that:

$$F(0, t_{RD}) = F(0, \infty)[1 - \exp(-t_{RD}/T_1)] = F_0[1 - \exp(-t_{RD}/T_1)] \quad (4)$$

where $F(0; t_{RD})$ represents the signal intensity at $t = 0$ for a given delay time t_{RD} . Measure $F(0; t_{RD})$ (File: Exp1/RD ns) for all t_{RD} and determine F_0 and T_1 from Eq 4 by model fitting.

Exercise 2

Inversion Recovery experiments are performed on a series of CuSO₄-solutions (concentration $C = 20\text{mM}$, 10mM , 5mM , 2.5mM , 1.25mM and 0mM). The data are available on the homepage of the course, file: *Exp2/nn mM-CuSO4-T1*.

Show that:

$$F(\tau) = F_0[1 - \alpha \cdot \exp(-\tau/T_1)] \quad (5)$$

Where F_0 is the equilibrium magnetization ($F_0 \approx F(\tau = 5T_1)$) and α equals 2.00. The experimental parameter τ represents the time between the initial 180° -rf pulse and the subsequent 90° rf-pulse (measuring pulse). Determine T_1 by model fitting Eq 5 to the observed relaxation data. Use α as an adjustable parameter. Plot the spin-lattice relaxation rate $R_1 (= 1/T_1)$ as a function of the CuSO₄ concentration $C(\text{CuSO}_4)$. Present all data/fits in one Figure and discuss your results.

Exercise 3

CPMG experiments are performed on a series of CuSO₄-solutions (concentration $C = 20\text{mM}$, 10mM , 5mM , 2.5mM , 1.25mM and 0mM) and the data are available on the homepage of the course, file: *Exp3/CPMG nn MM*. It is known that the signal intensity of the CPMG envelope can be written:

$$I(2\tau) = I_0 \cdot \exp(-2\tau/T_2) \quad (5)$$

where I_0 is the equilibrium magnetization and T_2 defines the spin-spin relaxation time. Determine T_2 by model fitting Eq 5 to the observed relaxation data. Plot the spin-spin relaxation rate $R_2 (= 1/T_2)$ against $C(\text{CuSO}_4)$. Show all data/fits in one Figure and discuss your results.