Introduction to numerical projects

Here follows a brief recipe and recommendation on how to write a report for each project.

- Give a short description of the nature of the problem and the eventual numerical methods you have used.
- Describe the algorithm you have used and/or developed. Here you may find it convenient to use pseudocoding. In many cases you can describe the algorithm in the program itself.
- Include the source code of your program. Comment your program properly.
- If possible, try to find analytic solutions, or known limits in order to test your program when developing the code.
- Include your results either in figure form or in a table. Remember to label your results. All tables and figures should have relevant captions and labels on the axes.
- Try to evaluate the reliabilty and numerical stability/precision of your results. If possible, include a qualitative and/or quantitative discussion of the numerical stability, eventual loss of precision etc.
- Try to give an interpretation of you results in your answers to the problems.
- Critique: if possible include your comments and reflections about the exercise, whether you felt you learnt something, ideas for improvements and other thoughts you've made when solving the exercise. We wish to keep this course at the interactive level and your comments can help us improve it.
- Try to establish a practice where you log your work at the computerlab. You may find such a logbook very handy at later stages in your work, especially when you don't properly remember what a previous test version of your program did. Here you could also record the time spent on solving the exercise, various algorithms you may have tested or other topics which you feel worthy of mentioning.

Format for electronic delivery of report and programs

The preferred format for the report is a PDF file. You can also use DOC or postscript formats. As programming language we prefer that you choose between C/C++ and Fortran90/95. You could also use Java or Python as programming languages. Matlab/Maple/Mathematica/IDL are not allowed as programming languages for the handins, but you can use them to check your results where possible. The following prescription should be followed when preparing the report:

- Use Classfronter to hand in your projects, log in at blyant.uio.no and choose 'fellesrom fys3150 og fys4150'. Thereafter you will see an icon to the left with 'hand in' or 'innlevering'. Click on that icon and go to the given project. There you can load up the files within the deadline.
- Upload **only** the report file and the source code file(s) you have developed. The report file should include all of your discussions and a list of the codes you have developed. Do not include library files which are available at the course homepage, unless you have made specific changes to them.
- Comments from us on your projects, approval or not, corrections to be made etc can be found under your Classfronter domain and are only visible to you and the teachers of the course.

Finally, we do prefer that you work two and two together. Optimal working groups consist of 2-3 students. You can then hand in a common report.

Project 2, deadline 3 october 12pm (midnight)

We assume that at $t = 0$ we have $N_X(0)$ nuclei of the type X which can decay radioactively. At a given time t we are left with $N_X(t)$ nuclei. With a transition rate ω_X, which is the probability that the system will make a transition to another state during a time step of one second, we get the following differential equation

$$dN_X(t) = -\omega_X N_X(t)dt, \tag{1}$$

whose solution is

$$N_X(t) = N_X(0)e^{-\omega_X t}, \tag{2}$$

and where the mean lifetime of the nucleus X is

$$\tau = \frac{1}{\omega_X}. \tag{3}$$

If the nucleus X decays to Y, which can also decay, we get the following coupled equations

$$\frac{dN_X(t)}{dt} = -\omega_X N_X(t), \tag{4}$$

and

$$\frac{dN_Y(t)}{dt} = -\omega_Y N_Y(t) + \omega_X N_X(t). \tag{5}$$

We assume that at $t = 0$ we have $N_Y(0) = 0$. In the beginning we will have an increase of N_Y nuclei, however, they will decay thereafter. In this project we let the nucleus ^{210}Bi represent X. It decays through β-decay to ^{210}Po, which is the Y nucleus in our case. The latter decays through emision of an α-particle to ^{206}Pb, which is a stable nucleus. ^{210}Bi has a mean lifetime of 7.2 days while ^{210}Po has a mean lifetime of 200 days.

a) Find analytic solutions for the above equations assuming continuous variables and setting the number of ^{210}Po nuclei equal zero at $t = 0$.

b) Make a program which solves the above equations. What is a reasonable choice of timestep Δt? You could use the program on radioactive decay from the web-page of the course as an example and make your own for the decay of two nuclei. Compare the results from your program with the exact answer as function of $N_X(0) = 10$, 100 and 1000. Make plots of your results.

c) When ^{210}Po decays it produces an α particle. At what time does the production of α particles reach its maximum? Compare your results with the analytic ones for $N_X(0) = 10$, 100 and 1000.