

Plan → ongoing Ex 10 Gault

Hoffmeyer ex 9 Gault

Ute 40 + 41 forbesed Cellular Polfs

Ute 42 Cellular Polfs

Why cells are microscopic!

$$\text{MSD } \langle r^2 \rangle = \langle x^2 + y^2 + z^2 \rangle = 3 \langle x^2 \rangle = 6Dt$$

$$\Rightarrow \tau = \frac{L^2}{6D}$$

$N$  - # macromolecules in a cell ( $\approx 10^{10}$ )

- viscosity
- hydrophobic interactions
- contact / crowding

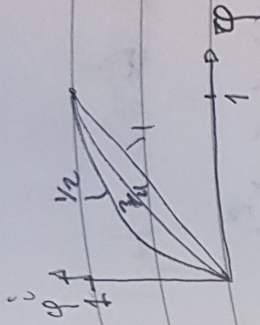
$$V \approx 4R^3$$

Packing fraction  $\phi = \frac{NV}{V} = N \left( \frac{V}{R} \right)^3$

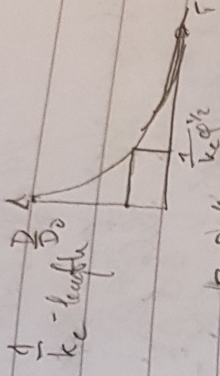
$$\phi \ll 1 \quad D_0 = \frac{kT}{6\pi\eta R}$$

Crowding  $D = D_0 e^{-\gamma R}$ ,  $R = k_c \phi^\delta$ ,  $\gamma = \left\{ \frac{1}{\phi_1}, \frac{1}{\phi_2}, \frac{1}{\phi_3} \right\}$

in cell  $\delta = 1/2$



$$\frac{D_0}{D} = e^{-k_c R \phi^\delta}$$



$$D = e^{-\left(\frac{k_c R}{\tau} \right)^{1/2} \phi}$$

Obstruction theory

(Experimentalists theory)

$$\phi^{1/2} = N \left( \frac{V}{R} \right)^{3/2}$$

$$\zeta(R) = \frac{R^2}{6D_0 e^{-\left(\frac{k_c R}{\tau} \right)^{1/2} \phi}}$$

minimum:  $R_{min} = \left( \frac{3}{2} \right)^{2/3} N \tau \Rightarrow \phi_{min} = 0.4$

Eutargote:  $2R_{min} = 2 \cdot 6 \cdot 10^{10} \cdot 3 \text{ (nm)} = 157 \mu\text{m}$

$$\phi \sim 8 \cdot 10^{-9} \left( \frac{3 \cdot 2}{15700} \right)^3 \approx 0.45$$

Eushog theory  $\phi_{min} \approx 0.25$ ,  $2R_{min} \approx 20 \mu\text{m}$

Simple idea

$$N \approx 10 \cdot 4 \cdot (4 \cdot 10^{-9})^3 = 4 \cdot 10^{-17} = 260$$

packed radius  $\phi = 1$

$$R = \sqrt[3]{\phi} \tau = 2 \cdot 10^{-9} \tau = 8 \mu\text{m}$$

Thus, necessary conclusion.