

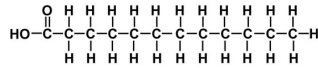
# Lecture 2

FYS4715 2021

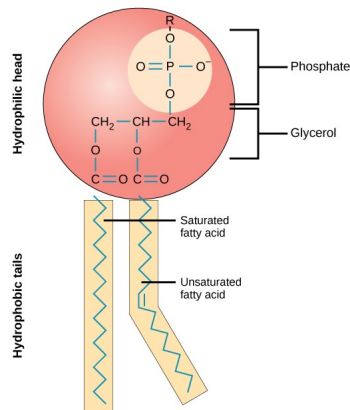
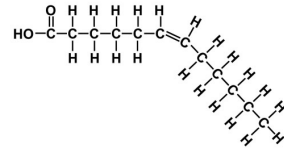
Whats inside cells, contd, statistical mechanics, diffusion, random walks

# fatty acids -> phospholipid -> membranes

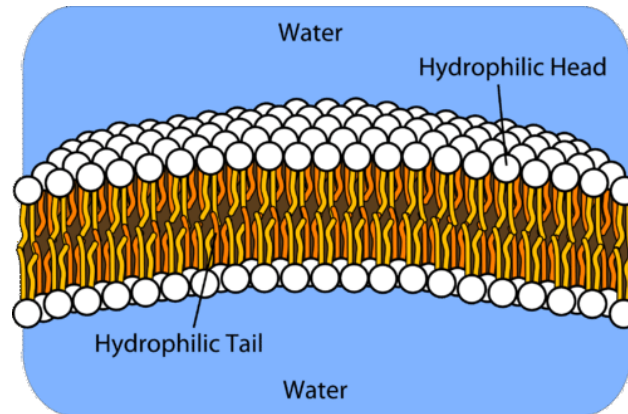
Saturated Fatty Acid



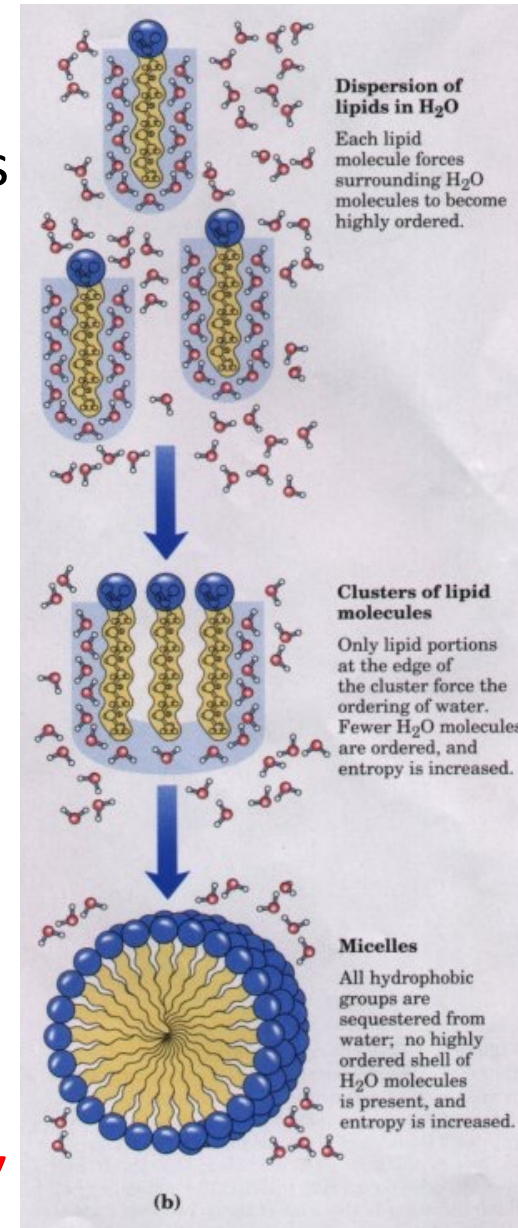
Unsaturated Fatty Acid



lipid:  
macromolecule that is  
soluble in nonpolar solvents

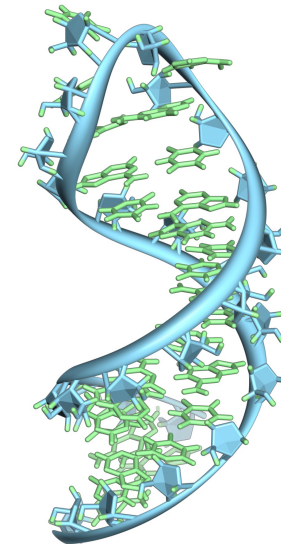
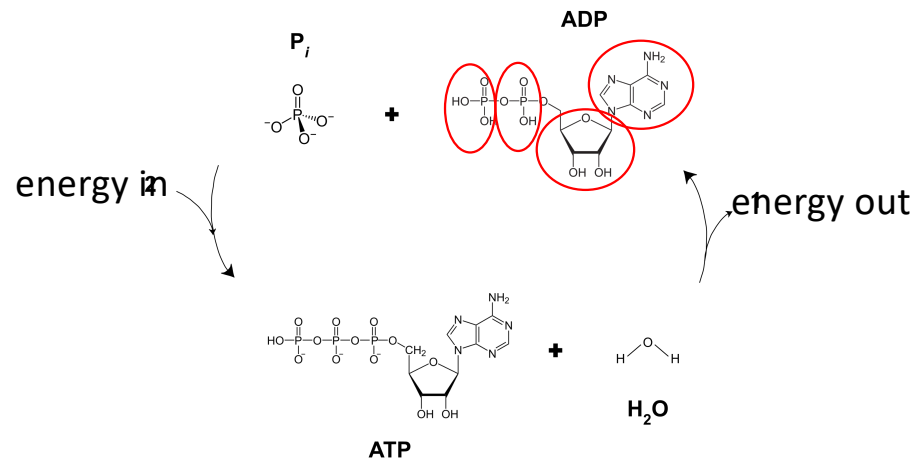
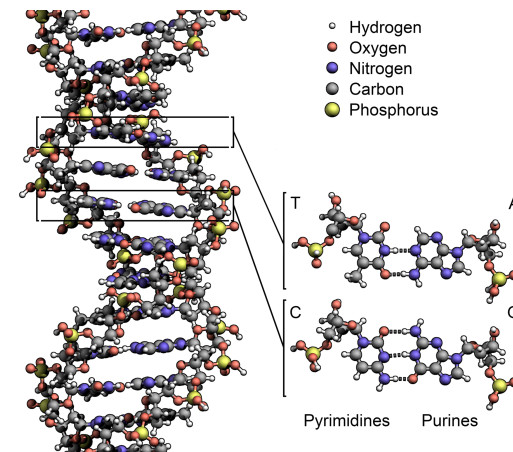


*energy and entropy*



# Important molecules

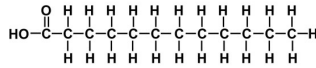
- Important nitrogenous bases: Adenine, Thymine, Guanine, Cytosine, Uracil
- Nucleic acids
  - DNA (DeoxyriboNucleic Acid): base **pairs** T-A, C-G
  - RNA (RiboNucleic Acid): single strands of G,U,A,C
- Nucleotide = (nitrogenous) base + sugar + phosphate
  - Adenine (base) + ribose (sugar) = Adenosine
  - ATP (Adenosine TriPhosphate)
  - ADP (Adenosine DiPhosphate)



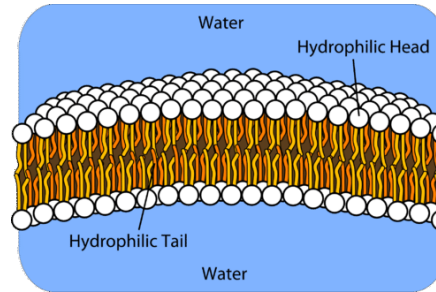
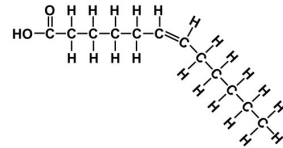
# Important molecules

- fatty acids -> phospholipid -> membranes

Saturated Fatty Acid



Unsaturated Fatty Acid

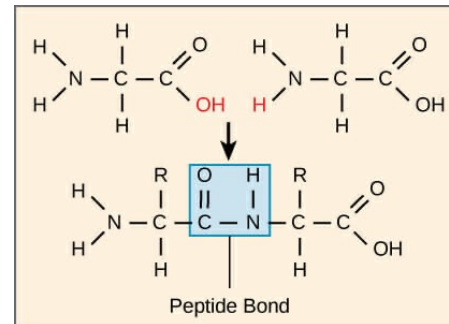


- amino acids -> polypeptides - proteins

<chem>NC(=O)O</chem> Glycine	<chem>CC(N)C(=O)O</chem> Alanine	<chem>CC(C)C(N)C(=O)O</chem> Valine	<chem>C1CCNC1C(=O)O</chem> Proline	<chem>OC(C)C(N)C(=O)O</chem> Serine	<chem>CCC(N)C(=O)O</chem> Asparagine
<chem>CC1=CC=CC=C1CC(N)C(=O)O</chem> Phenylalanine	<chem>CC1=CC=C(O)C=C1CC(N)C(=O)O</chem> Tyrosine	<chem>C1=CN=C(N1)CC(N)C(=O)O</chem> Histidine	<chem>SCC(N)C(=O)O</chem> Cysteine	<chem>CC(O)C(N)C(=O)O</chem> Threonine	
<chem>CSCC(N)C(=O)O</chem> Methionine	<chem>CC(C)C(C)C(N)C(=O)O</chem> Leucine	<chem>C1=CC=C2C(=C1)C(=CN2)C3=CC=CC=C3CC(N)C(=O)O</chem> Tryptophan	<chem>CCC(N)C(N)C(=O)O</chem> Glutamine	<chem>CCC(N)C(O)C(=O)O</chem> Aspartate	
<chem>CC(C)C(N)C(=O)O</chem> Isoleucine	<chem>CCC(N)C(=O)O</chem> Glutamate	<chem>CCC(N)C(N)C(=O)O</chem> Arginine	<chem>CCCC(N)C(=O)O</chem> Lysine		

**Hydrophobic** (left column)      **Polar** (right column)

Amino: NH<sub>2</sub>, Acid: OOH



Peptides: 2-50 amino acids  
Proteins: >50 amino acids

# Proteins

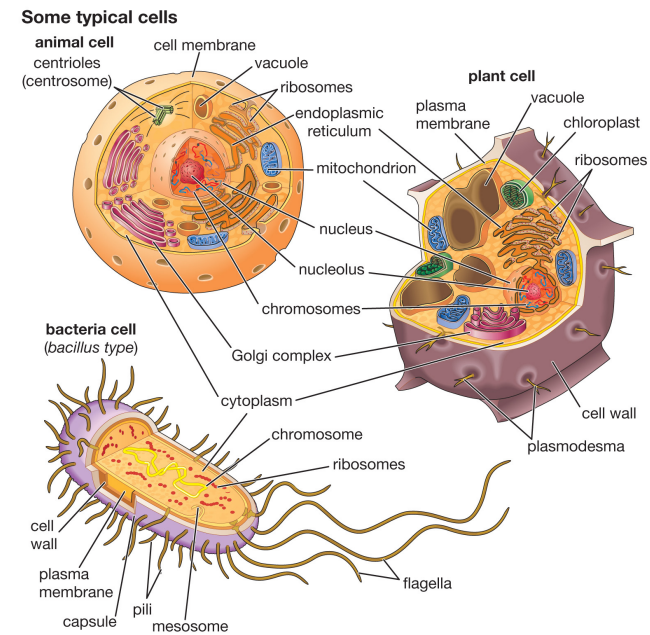
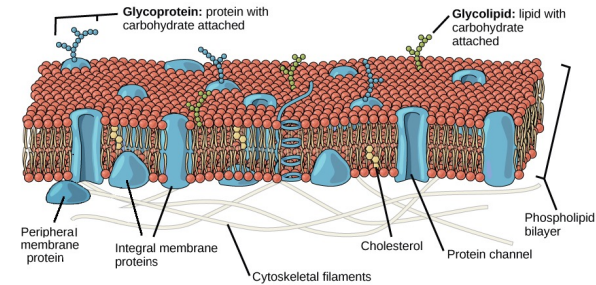
- Proteins perform a vast array of functions
  - catalysing metabolic reactions
  - DNA replication
  - responding to stimuli
  - providing structure to cells, and organisms
  - transporting molecules from one location to another
- <https://www.rcsb.org> protein data bank
  - 1aoi
  - 1tau
  - 1mbn
- Proteins are folded: <https://youtu.be/SMNIfNJKdRc>
- peptide in water: atomify

# Cells – fundamental functional units of life

- enclosed by **plasma membrane**
- interior «soup» called **cytoplasm**
- organized in **organelles** = specialized compartments surrounded by membrane
  - **nucleus**: contains the genetic information necessary for cell growth and reproduction
  - **mitochondria**: responsible for the energy transactions necessary for cell survival
  - **lysosomes**: digest unwanted materials within the cell
  - **endoplasmic reticulum & Golgi apparatus**: organization of the cell by synthesizing selected molecules and then processing, sorting, and directing them to their proper locations

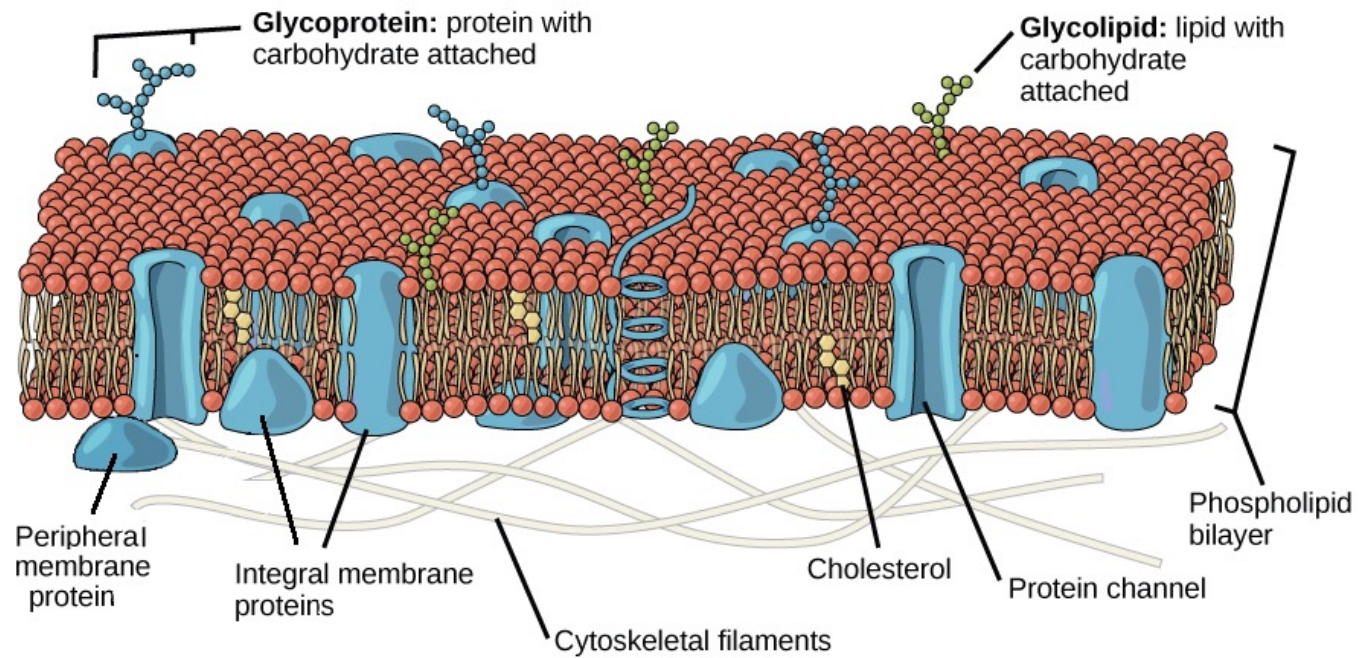
• <https://www.allencell.org/>

cyto- = cell

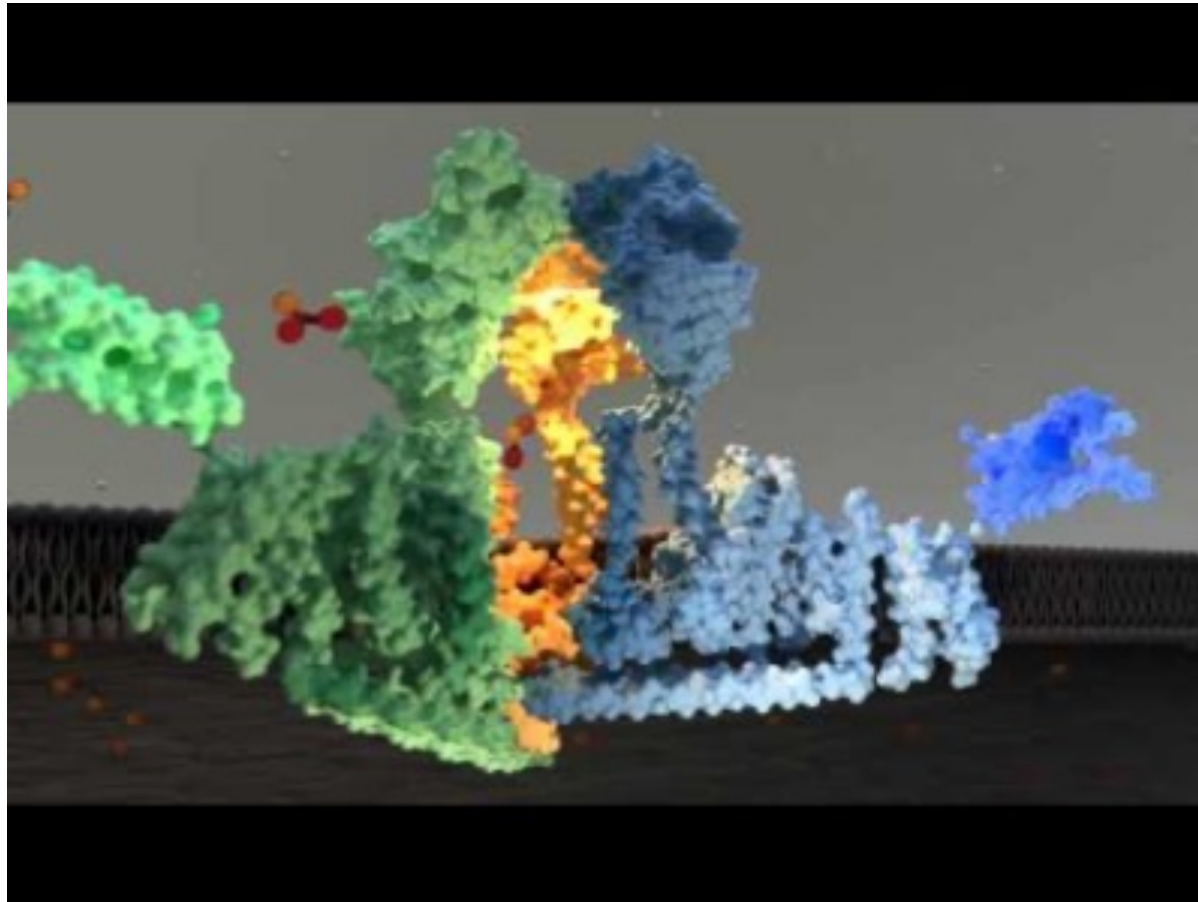


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# Plasma membrane



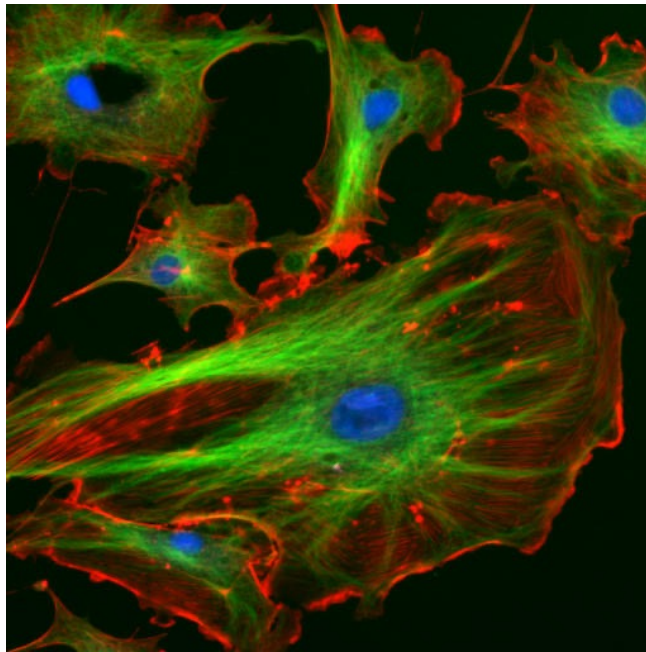
# Ion channels





# Cytoskeleton

- actin filaments (7 nm  $\emptyset$ )
- microtubules (25 nm  $\emptyset$ )
- intermediate filaments (10  $\emptyset$ )



The eukaryotic cytoskeleton. Actin filaments are shown in red, and microtubules composed of beta tubulin are in green.

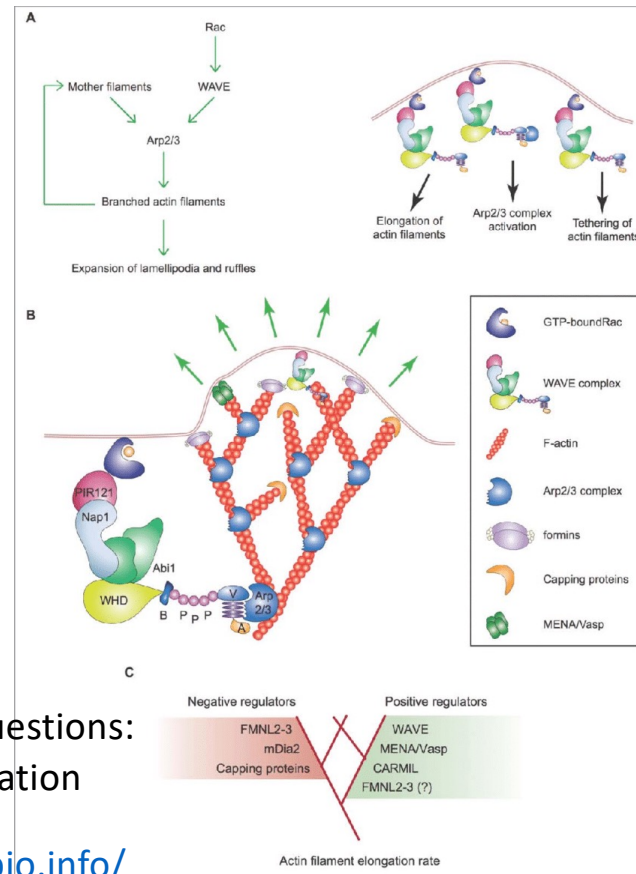
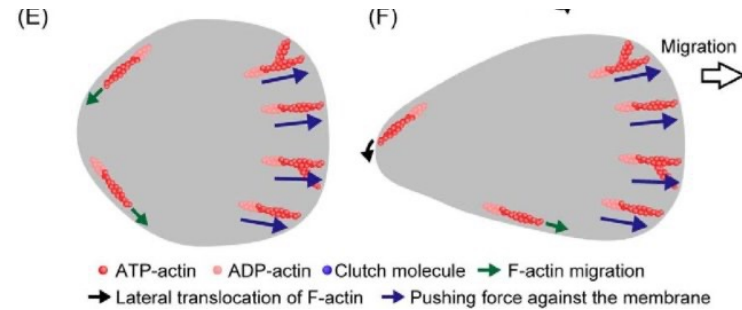
G-actin monomer

F-actin polymer

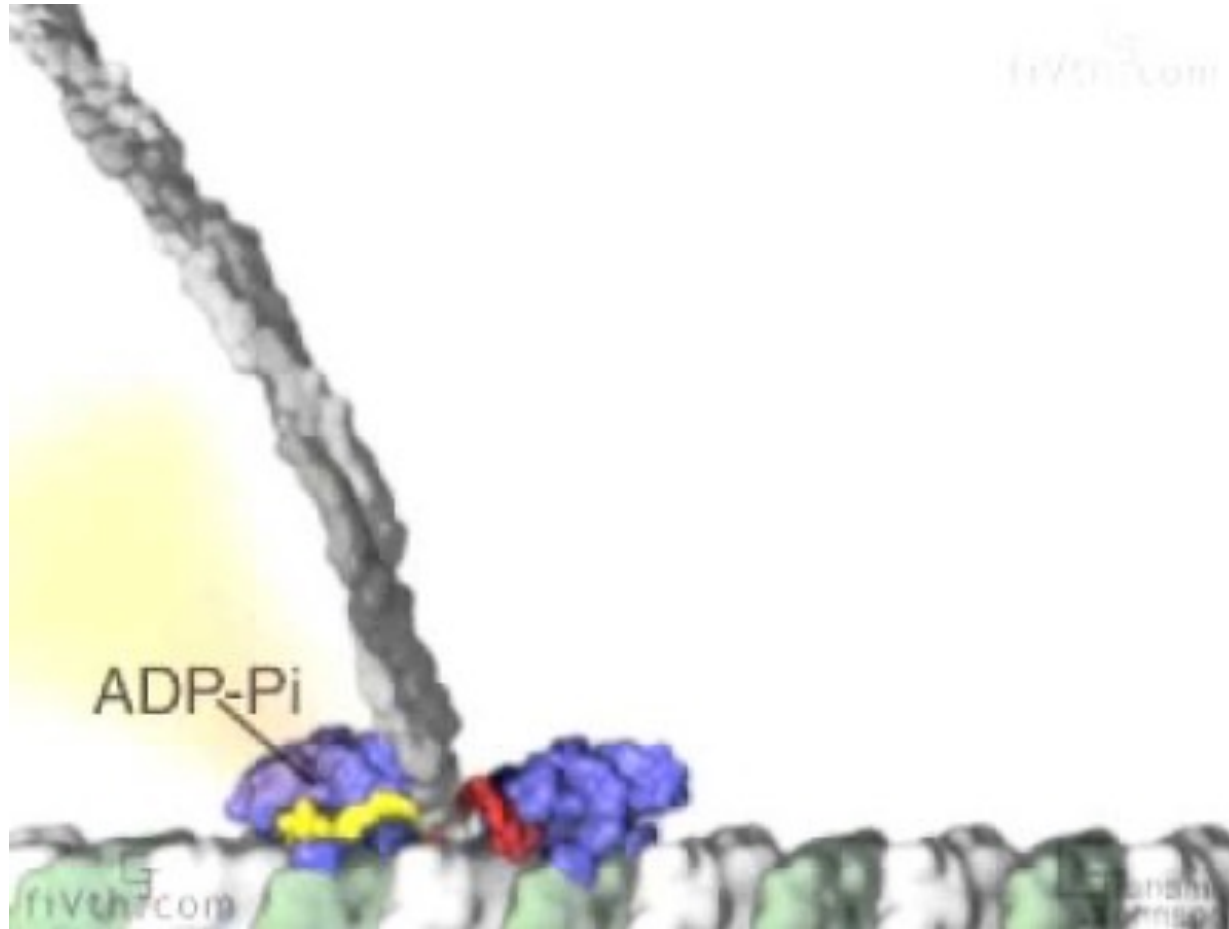
physics questions:

- polarization
- force

<https://www.mechanobio.info/>



# Microtubules & kinesin motors



Crash course in greek and latin:

Angio-		Vessel	
-atomy, -otomy		cutting	Angiogenesis
Auto-		self	=production
Brachy		short	of vessels
Cata- (katalysis)		dissolving	
Carcino-		tumor (crab-like)	
Centro-, -centric		centre	Carcinogenesis
-ceptor, ceptive		capere, to take	
Chromo-		color	Production
Chrono-		time	(development) of
-cyte, cyto-			f cancer
Diplo	hollow	double	
e-, ec-		out of	
Endo-		within, inside	
Exo-		outside	
Extra-		beyond	
Erythro-		red	
-gen, genous	descent		
-genic, -genous		birth, descent, origin	
-genic, -genous		to produce	

Crash course in greek and latin:

Glia-	glue
Haem-	blood
Histo-	tissue
Homeo-	alike
Homo-	the same
Hyper-	above
Hypo-	under
Infero-	beneath
Infra-	below
Inter-	between
Intra-	within
Iso-	equal
-kinesis, -kinetic	kinesis=movement
Leuko-	white
Lipo-	fat
-lysis, -lysin	dissolving
Macro-	large
Medi-	middle

Crash course in greek and latin:

-mere, mero-	a part		
Meta-		after	
Metabolism	change		Centromere= middle part
Micro-		small	
Mito- (mitosis)		a tread	
Mono-		single	
Muta-		mutare=to change	telomere= end part
Necro-		dead	
Neuro-		nerve	
-nomics		law	
Oligo-		few	
Onco-		bulk, mass	
Ortho-		straight	
Para-		beside	
Per-		through	
Peri-		around	
-phage, -phagous		phagein=to eat	
-phil		to love	

Crash course in greek and latin:

-phobe		to fear
Photo-		light
Plasma-, -plasm		form
-plicate		to fold
Post-		after
Pre-		before
Pro-		before
Proto-		first
Re-		back
Retro-		backwards
Serum		whey (myse)
-some, soma-		body
Stereo-, -stERIC		solid
Sub-		under
Super-		over
Supra-		above
Sym-, syn-	with	

Crash course in greek and latin:

-synthesis

Tauto-

Tele-

Teleo-

Telo-, telio-

Trans-

Ultra-

composition

the same

far

complete

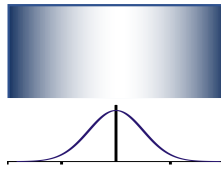
end

across

beyond

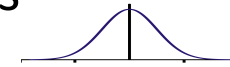
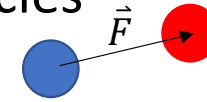
## Thermodynamics

- Macroscopic
- Continuum matter
- Differentiable
- Necessary relations based on some axioms
  - Always true for all matter
  - Necessary tool for theory
  - Always present in applications (engineering, chemistry, geoscience...)
- All properties of matter ( $\Delta H_m$ ,  $\Delta S_v$ ,  $c_v$ ,  $\lambda$ ,  $D$ ) must be measured



## Statistical physics

- Microscopic
- Discrete particles
- Mechanics
- Statistical behaviour of simplified models
- Bottom up explanation of thermodynamics
- Properties of model matter ( $\Delta H_m$ ,  $\Delta S_v$ ,  $c_v$ ,  $\lambda$ ,  $D$ ) can be calculated and measured in simulation







How do cows move and interact in a meadow?

Theoretical physicist:

ASUME A  
SPHERICAL  
COW  
IN A VACUUM



Model: Representation of a real phenomenon that is simple enough that you may do calculations.

# Phenomenon: Diffusion



- Observations
  - Dissolved matter moves from high concentration to low concentration. (sugar in tea, smell of fart, ink in water).
    - After a long time: concentration is the same everywhere
    - What is diffused? “matter”, sugar, smelly molecules, ink
  - Hot metal in contact with cold metal: Temperature evens out.
    - After a long time: temperature is the same everywhere
    - What is diffused? **Heat**
    - **What is heat?**
- “After a long time” = notion of equilibrium
- Only one direction of development -> equilibrium
- Irreversibility, arrow of time

A small detour...

## Heat, first physics definition

- **Heat** is **energy** in **transfer** to or from a system, by mechanisms other than work.
- Amount of heat transferred: J (Joule)
- Rate of heat transfer:  $W=J/s$  (Watt)
- Heat flux,  $Q$ ,  $[Q]=W/m^2$



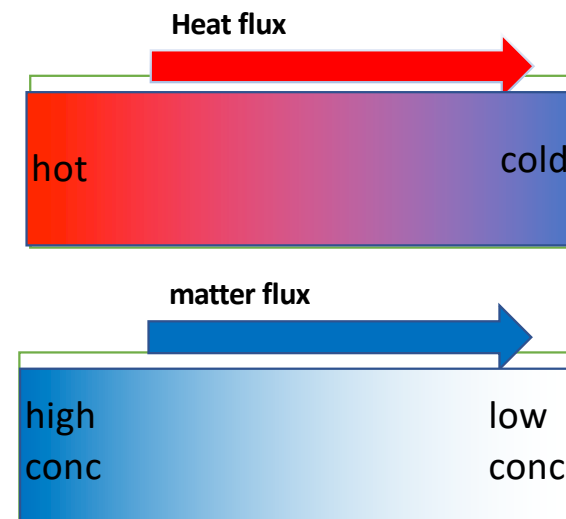
# Theory:

## Relaxation to equilibrium by diffusion

### Macroscopic explanation of diffusion:

Net transport of *energy* or *particles* until thermodynamic equilibrium is reached

- $\vec{J} = -D\nabla c$  Matter flux is proportional to gradient of concentration
- $\vec{Q} = -\lambda\nabla T$  Heat flux is proportional to gradient of temperature
- What are «matter» and »heat»?



## I. DIFFUSION AS A MIXING PROCESS

Diffusion equation:

$$J = -D_{12} \frac{\partial \rho}{\partial y} \quad (1)$$

Divergence theorem (continuity equation)

$$\frac{\partial \rho}{\partial t} + \nabla J = 0 \quad (2)$$

Combine the two to get the partial differential equation for diffusion:

$$\frac{\partial \rho}{\partial t} + D_{12} \frac{\partial^2 \rho}{\partial y^2} = 0 \quad (3)$$

Starting with particles in  $y = 0$  at time  $t = 0$ :  $\rho(t = 0, y) = \delta(y)$ , where  $\delta$  is the Kroeneker delta function the diffusion equation has solution (you may easily verify this):

$$\rho(t, y) = \frac{1}{\sqrt{4\pi D_{12}t}} \exp\left(-\frac{y^2}{4D_{12}t}\right) \quad (4)$$

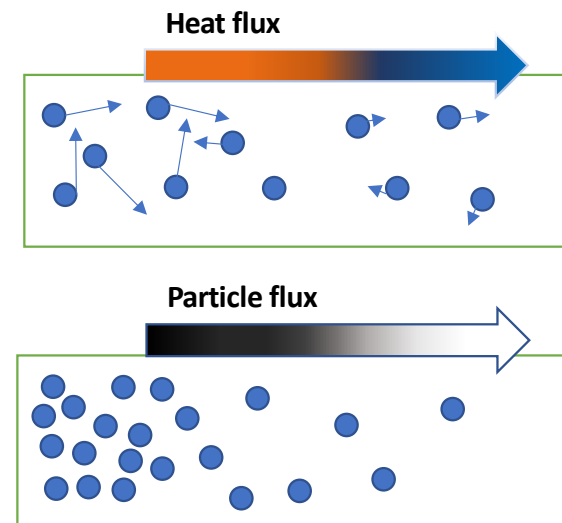
# Theory:

## Relaxation to equilibrium by diffusion

### Microscopic explanation of diffusion:

Net transport of *energy* or *particles* through **random thermal motion and particle collisions** until thermodynamic equilibrium is reached

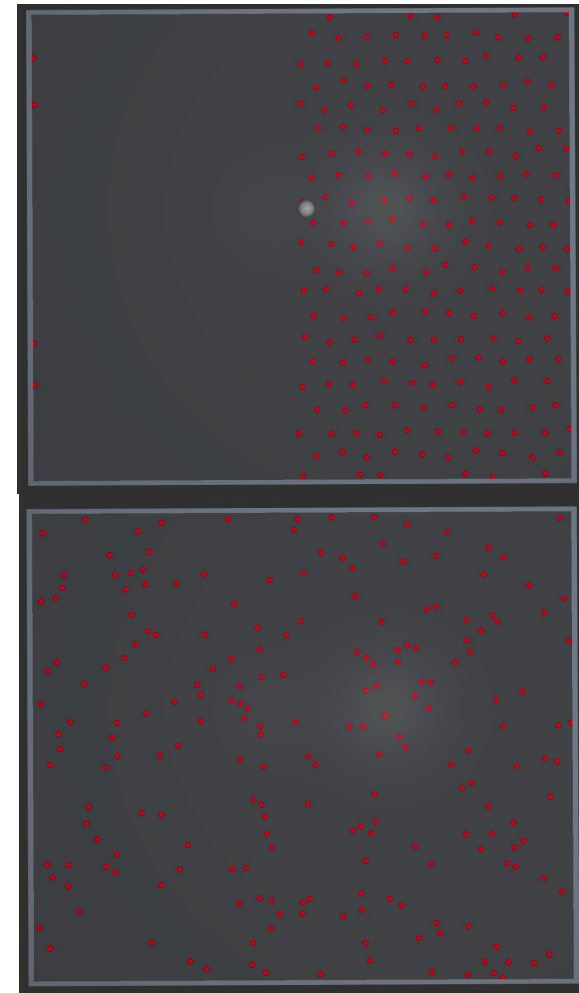
- At any  $T > 0\text{K}$ , particles are in *thermal motion*
- Collisions between particles  $\rightarrow$  particle trajectory is a zigzag -- random (*diffusive particle*)



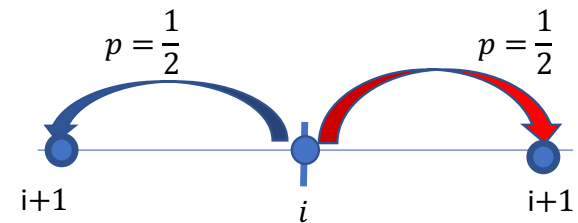
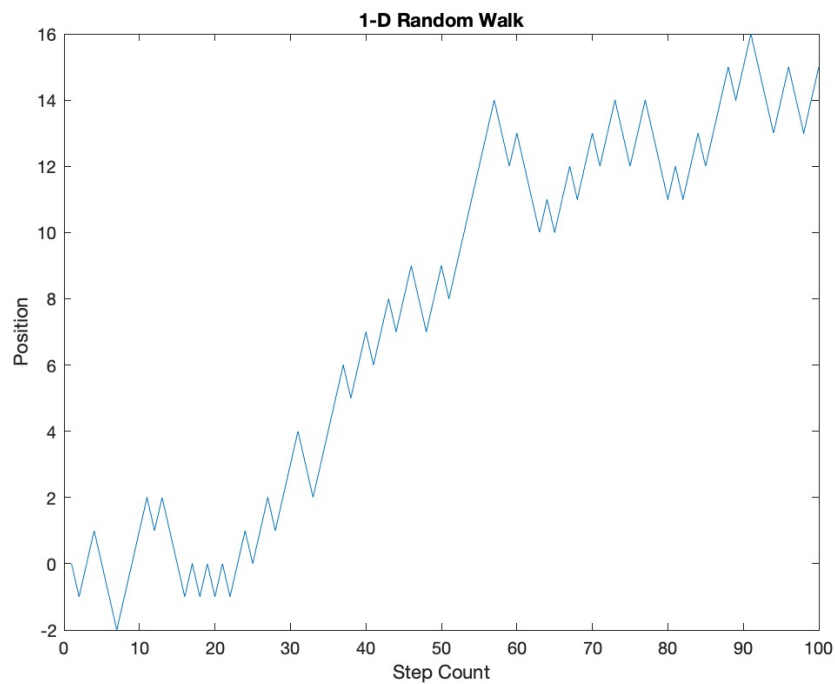
# Models of diffusion

- Molecular dynamics: `gas_2_sections_lammps.in`
  - Random walk: `rw1d_vector.m`, `rw1d.m`
  - Algorithmic: `gasboxalgo.m`
  - Ideal gas
- 
- Reversible laws of motion
  - Irreversible development: arrow of time
  - Measure average property: distribution in box

Gas particles moving randomly starting at one side.



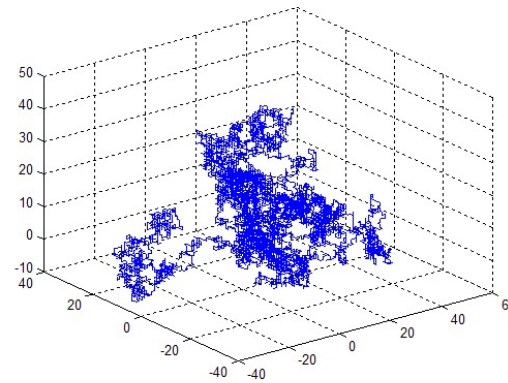
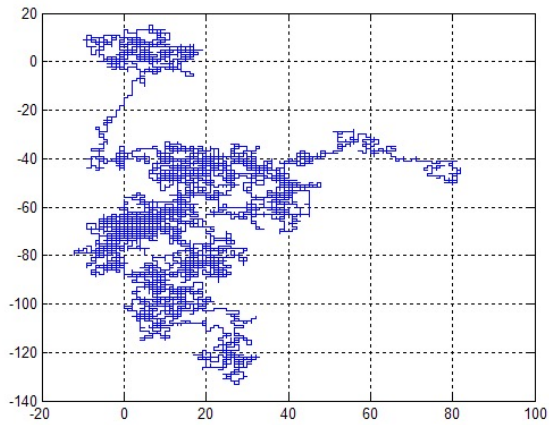
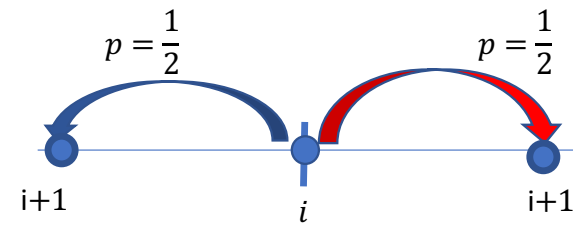
## Random walk (RW)



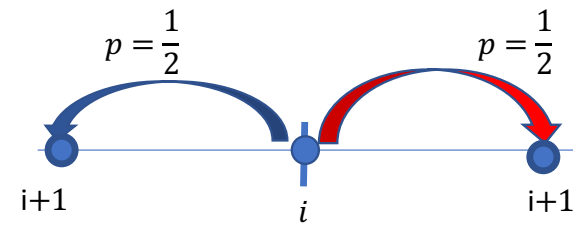
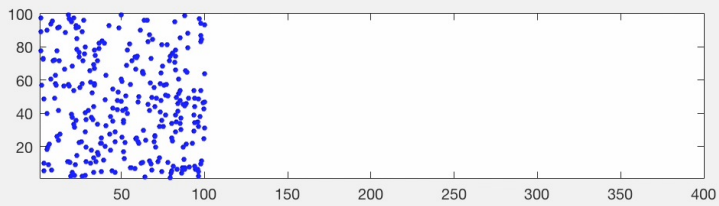
```
n = 100; % number of steps
P = zeros(n,1); %position(time)| vector
P(1) = 0; % Starting value
for i=2:n
    R = rand;
    if R < 0.5
        S = -1;
    elseif R > 0.5
        S = 1;
    end
    P(i) = S+P(i-1);
end
plot(1:n,P)
ylabel('Position')
xlabel('Step Count')
title('1-D Random Walk')
```



# Random walk (RW)



## Random walk and diffusion



# Exercises for next week

- 2D RW in Matlab or Python
  - (live script or Jupyter notebook)
- Your turn 1A
- Problems 1.3, 2.2, 2.5

# Ideal gas model

- Pressure = Force / Area

- $[P] = [F]/[A] = N/m^2$

- Newtonian mechanics

- $\vec{F} = m\vec{a} = \frac{d\vec{p}}{dt}$

- Used this to calculate pressure of ideal gas:

$$P_x = \frac{1}{A} \sum_i \frac{\Delta p_{x,i}}{\Delta t} = \frac{1}{A} N \frac{m\bar{v}_x^2}{2L} = \frac{Nk_B T}{V} = \rho k_B T$$

- When forces at distance:

- $P = \rho k_B T + \frac{1}{3V} \sum_{i < j} \vec{f}(\vec{r}_{ij}) \cdot \vec{r}_{ij}$

- second term: virial

# Statistical mechanics

- Model: MD (Atomify)
- micro  $x_i, m_i, v_i, f_{ij}, 10^{23}$ -> macro  $\rho, \langle v \rangle, \langle v^2 \rangle, E_k,$
- thermodynamics:  $P, T, c_p, H_v, \dots$  (stat + conservation laws)
- distributions: uniform, Gaussian, Poisson

$$P(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(x-x_0)^2}{2\sigma^2}}$$

- $x \rightarrow vx, x_0 \rightarrow 0, s$
- $\langle v \rangle, \langle v^2 \rangle$
- Model: ideal gas