Monte Carlo simulations

Lesson FYSKJM4710

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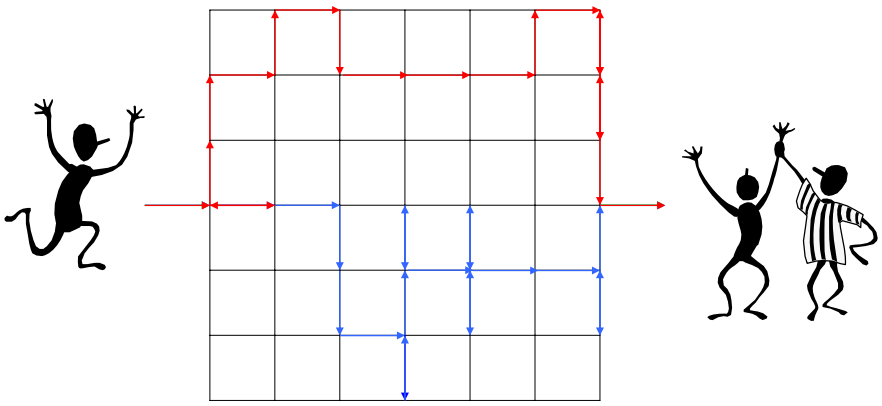
MC simulations 1

- Simulations of stochastic processes
- Interactions are stochastic: the path of a single ionizing particle may not be predicted
- Interactions are quantified by probabilities (cross sections)
- Random numbers and cross sections may be used to simulate single events
- Better than analytical methods, but requires CPU-time

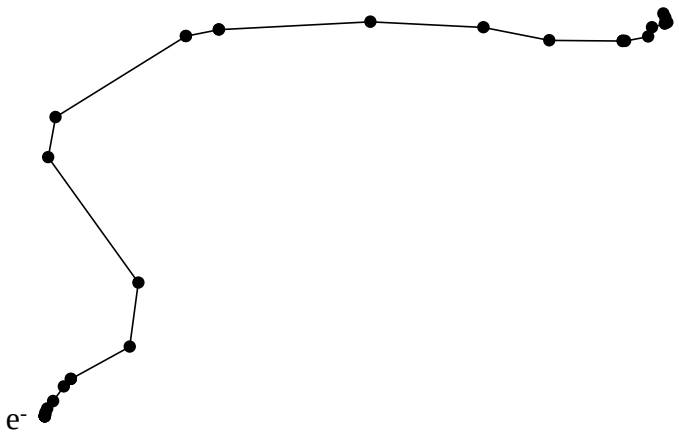
MC simulations 2

- Photons give rise to electrons and vice versa; coupled energy transport
- Analytic methods are suboptimal for:
  - Modeling of scatter
  - Generating electron- and photon spectra
  - Modeling interface effects
  - Calculating energy dependence of dosimeter response

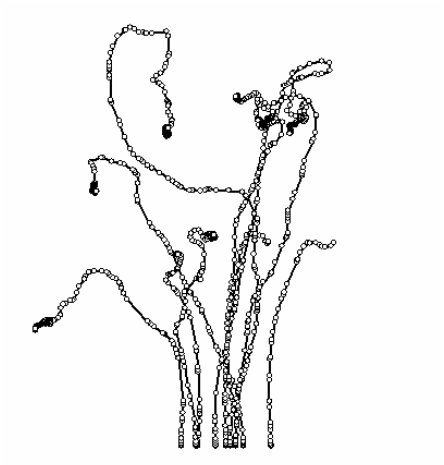
Random walk



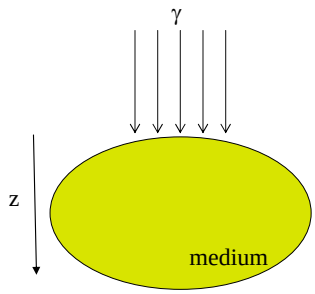
Electron ’walk’



Electron ’tree’



Photon MC

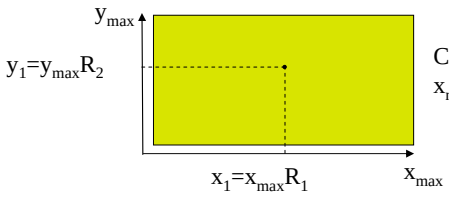


Description of photons and their energy depositions:

1. Position
2. Pathlength
3. Interaction
4. Secondary photon?

} Depends on photon energy

1: Draw two random numbers; $0<R<1$



Cross section of field: $x_{max} \times y_{max}$

Photon pathlength

- Photon attenuation:

$$N = N_0 e^{-\mu z}$$

- Describes the number of photons at depth z – is a type of *frequency distribution*:

$$f(z) = Ce^{-\mu z} \quad , \quad \int_0^\infty f(z)dz \overset{!}{=} 1 \Rightarrow C = \mu$$

$$\Rightarrow \langle z \rangle = \int_0^\infty z f(z)dz = \frac{1}{\mu}$$

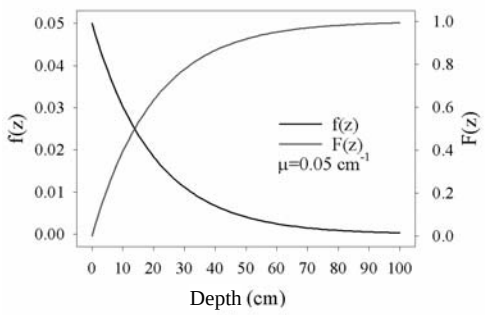
- Expected pathlength: $1/\mu$

Photon interaction point 1

- At what depth does an event (interaction) take place?
- Need a cumulative distribution with respect to depth:

$$F(z) = \int_0^z f(z')dz' = \int_0^z \mu e^{-\mu z'} dz' = 1 - e^{-\mu z}$$

F(z): probability that a photon has interacted between 0 and z



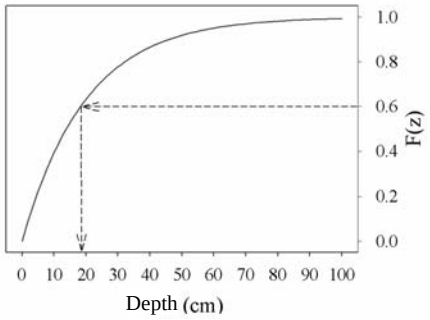
Photon interaction point 2

- Draw a random number R_1 – what is the corresponding pathlenght for this photon?

$$F(z_1) = R_1 = 1 - e^{-\mu z_1} \quad \Rightarrow \quad e^{-\mu z_1} = 1 - R_1$$

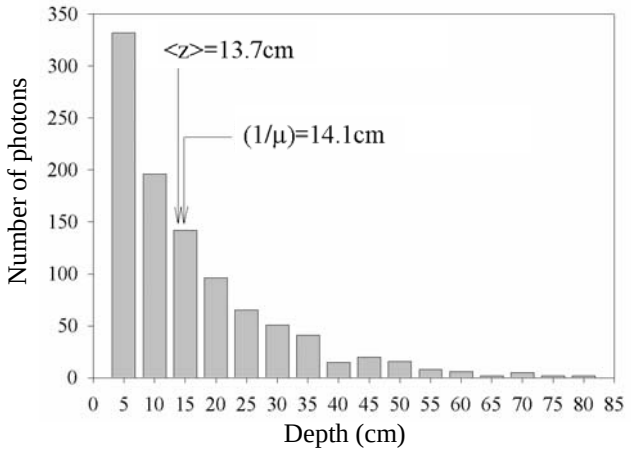
$$z_1 = -\frac{\ln(1 - R_1)}{\mu}$$

Example: R_1=0.6 → z_1=18.3 cm



Pathlength sampling

- Sampled pathlength of 1000 photons (1 MeV):



Interaction sampling

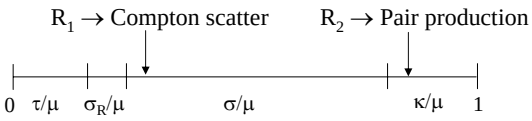
- What interaction occur at given depth?
- Total probability:

$$\mu = \tau + \sigma_R + \sigma + \kappa$$

- Probability for e.g. Compton scatter:

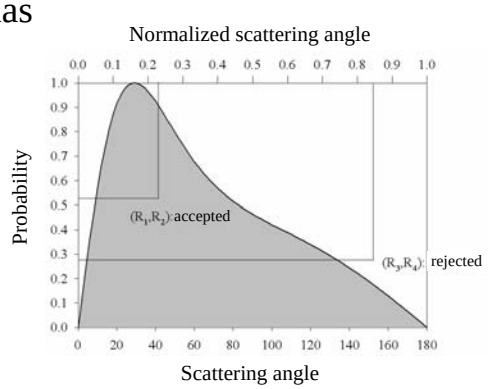
$$p_{Compton} = \frac{\sigma}{\mu}$$

- Draw random number:

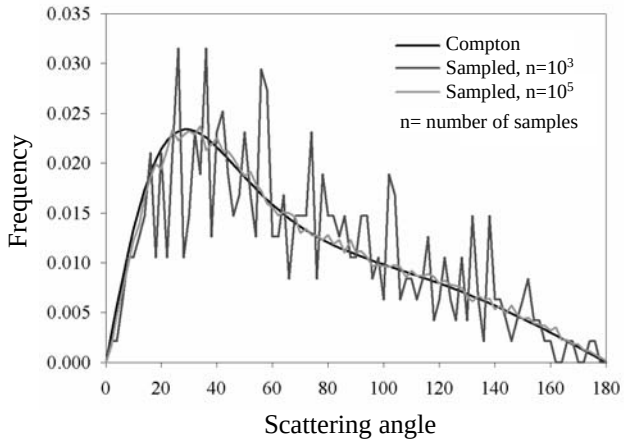


Sampling of scattered photons

- Is the photon scattered? In what direction?
- Angular distribution follows Compton cross section:
- Compton distribution has no analytic cumulative
- Must draw *two* random numbers

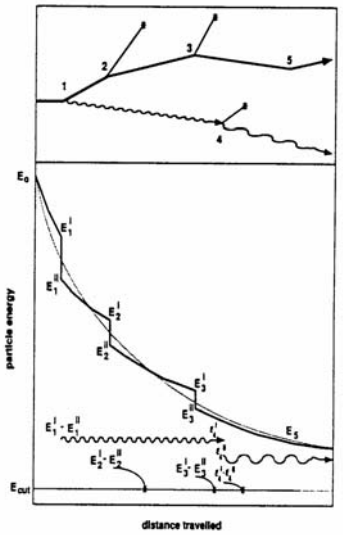


Sampling Compton scatter



Electron MC 1

- Simulations of electrons and positrons are more complicated
- A 0.5 MeV electron interacts ~10000 times when slowing down to 1 keV in aluminium!
- Number of calculations $\rightarrow \infty$
- *Macroscopic* Monte Carlo: Evaluate the electron after a given steplength – several interactions included in one step (simulations of every interaction: *microscopic* Monte Carlo)

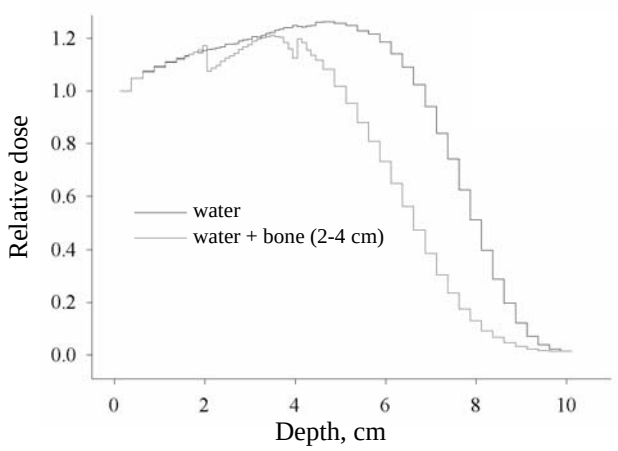


Electron MC 2

- Relative energy loss per step, η:
$$\eta = \frac{T_{k+1} - T_k}{T_k} = \frac{\Delta T}{T_k}$$
- T_k: electron energy in interaction point k
- η is set by user – may be sampled: $\eta' = \eta R$
- Step length: $\Delta s = \eta \frac{T_k}{\left(\frac{dT}{dx}\right)_{k,k+1}}$

Electron MC, example

- 18 MeV electrons in water/bone



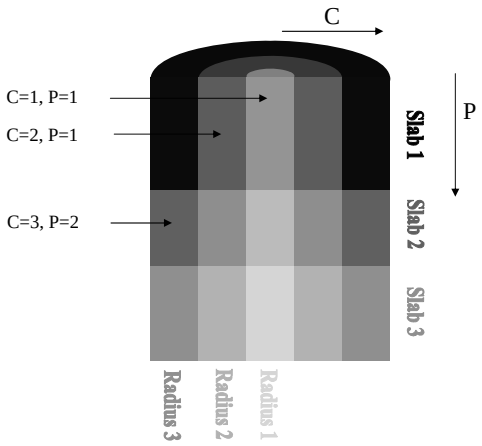
EGSnrc

- EGSnrc is a widely used MC code for e.g. simulations of photon- and electron beams
- Complicated programming, but simplified, user-friendly interface available: egs_inprz

http://www.irs.inms.nrc.ca/inms/irs/EGSnrc/EGSnrc.html

EGSnrc/DOSRZ

- DOSRZ: MC in cylindrical geometry



DOSRZ

- The user sets:
  - Phantom geometry
  - Radiation type- and energy (or spectrum)
  - Source (parallel beam, point source, ...)
  - Number of ”histories”, i.e. number of particles
  - Some MC parameters

DOSRZ

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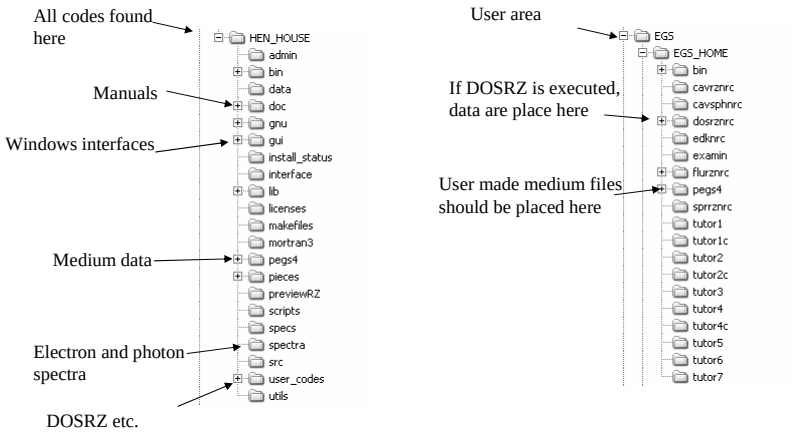
  - Some MC parameters

Some important parameters

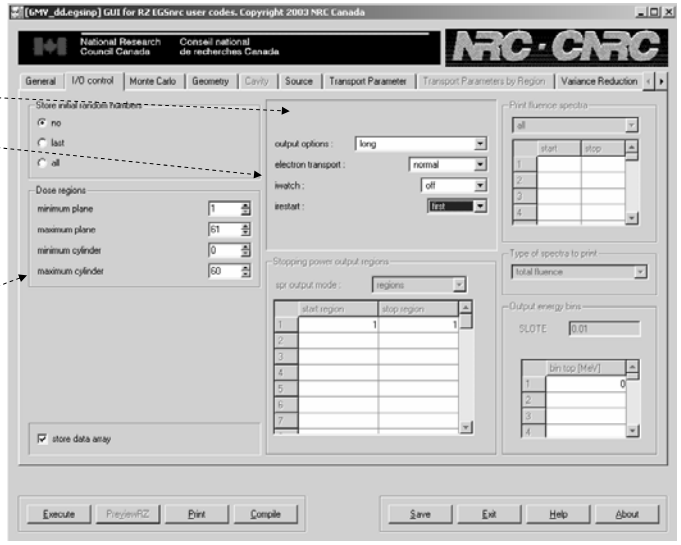
- ECUT: lower limit for electron transport (includes rest mass of 0.511 MeV)
- PCUT: lower limit for photon transport
- AE: lower limit for generation of electrons
- AP: lower limit for generation of photons
- AE and AP is medium specific and must be set in PEGS (see below)

Directories



Interface

Interface

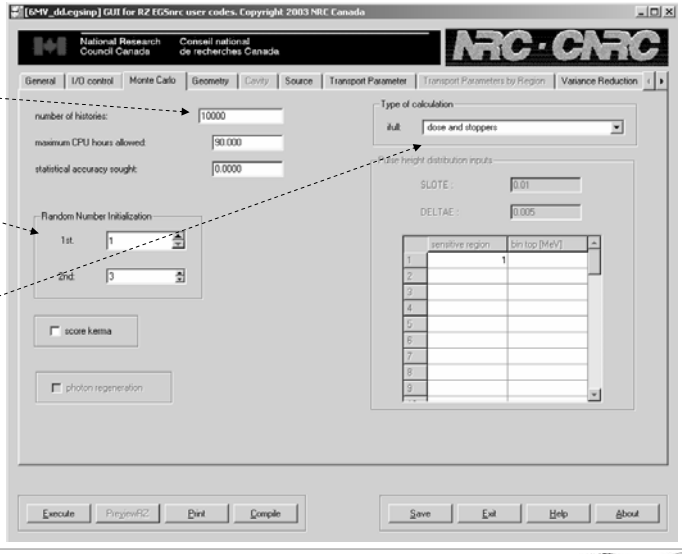


"long": most relevant

iwatch "on": all interactions are written to file (NB!)

Maximum number of regions

Interface

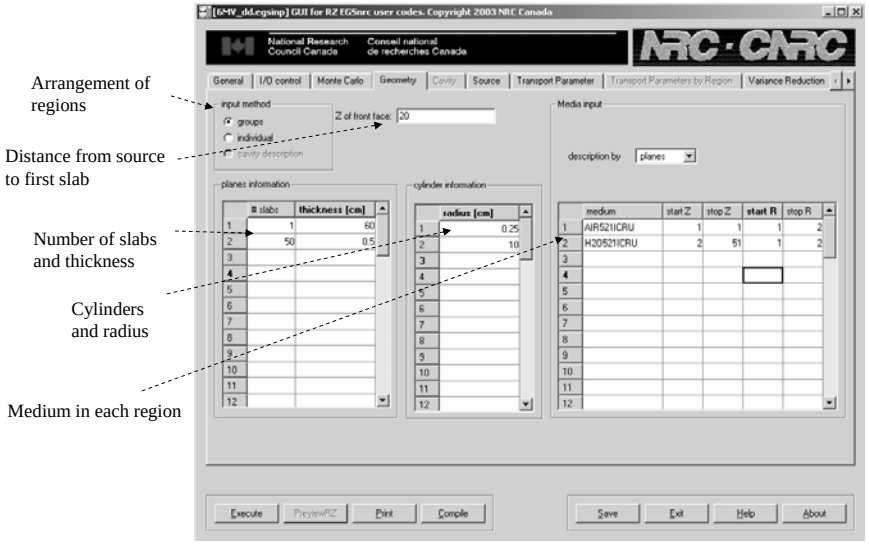


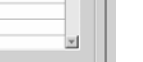
Number of histories

Initial random numbers

What should be calculated

Interface





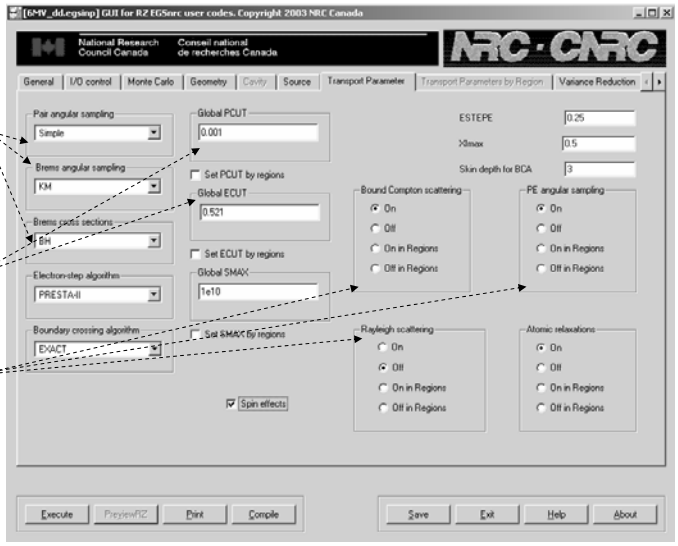
Interface

Interface

Methods for calulating pair production and brehmsstrahlung

PCUT and ECUT

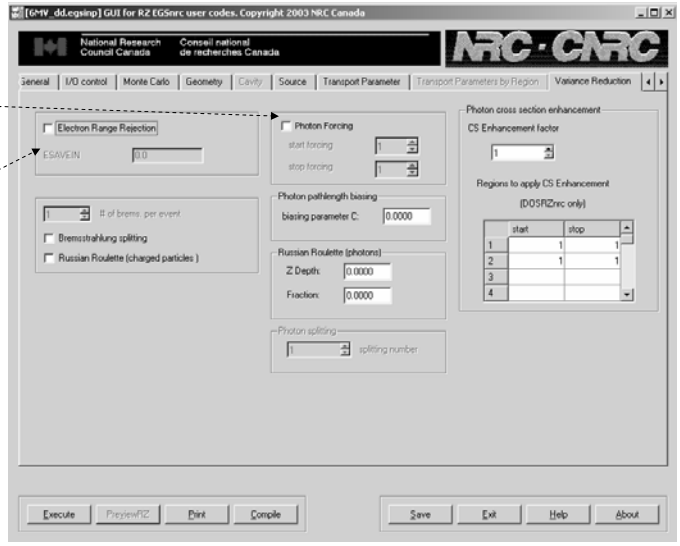
Photon interactions



Interface

Force photon to interact

Stop electron transport if range is short



Output - *.egsgph (with IWATCH=graph)

p	q	r	x	y	z	E	
1	0	2	-3.8381002	-2.2746158	0.0000000	0.10000000	
1	0	2	-3.8381002	-2.2746158	1.8895864	0.10000000	
2	-1	2	-3.8381002	-2.2746158	1.8895864	0.52920631	
2	-1	2	-3.8381002	-2.2746158	1.8895864	0.52920631	
2	-1	2	-3.8381002	-2.2746158	1.8895864	0.52920631	
1	0	2	-3.8381002	-2.2746158	1.8895864	0.81773069E-01	
1	0	2	-3.9120636	-3.2345552	1.8234146	0.81773069E-01	
2	-1	2	-3.9120636	-3.2345552	1.8234146	0.52306919	
2	-1	2	-3.9120636	-3.2345552	1.8234146	0.52306919	
2	-1	2	-3.9120636	-3.2345552	1.8234146	0.52306919	
1	0	2	-3.9120636	-3.2345552	1.8234146	0.69693251E-01	
1	0	2	-7.7017622	-3.0405600	2.4233341	0.69693251E-01	
2	-1	2	-7.7017622	-3.0405600	2.4233341	0.51507270	
2	-1	2	-7.7017622	-3.0405600	2.4233341	0.51507270	
2	-1	2	-7.7017622	-3.0405600	2.4233341	0.51507270	
1	0	2	-7.7017622	-3.0405600	2.4233341	0.65609927E-01	
1	0	2	-9.9838972	-0.41123173	0.71254671	0.65609927E-01	
1	0	2	-9.9838972	-0.41123173	0.71254671	0.65609927E-01	
1	0	2	-9.9838972	-0.41123173	0.71254671	0.65609927E-01	
1	0	1	-9.9919167	-0.40199202	0.70653480	0.65609927E-01	
0	0	0	0.0000000	0.0000000	0.0000000	0.0000000	1
1	0	2	-0.81262147	-1.4711231	0.0000000	0.10000000	
1	0	2	-0.81262147	-1.4711231	0.17595443	0.10000000	
2	-1	2	-0.81262147	-1.4711231	0.17595443	0.52714602	
2	-1	2	-0.81262147	-1.4711231	0.17595443	0.52714602	
2	-1	2	-0.81262147	-1.4711231	0.17595443	0.52714602	
1	0	2	-0.81262147	-1.4711231	0.17595443	0.83314356E-01	
1	0	1	-7.7556510	-6.3126755	0.52070326	0.83314356E-01	

p: particle q: charge r: region x: x-coord E=energy

Output - *.egslst

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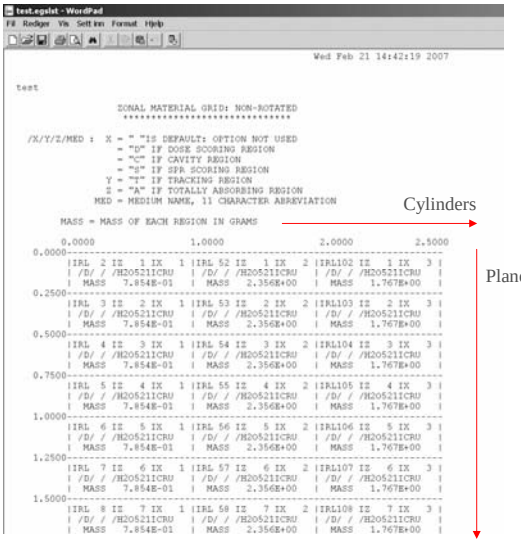
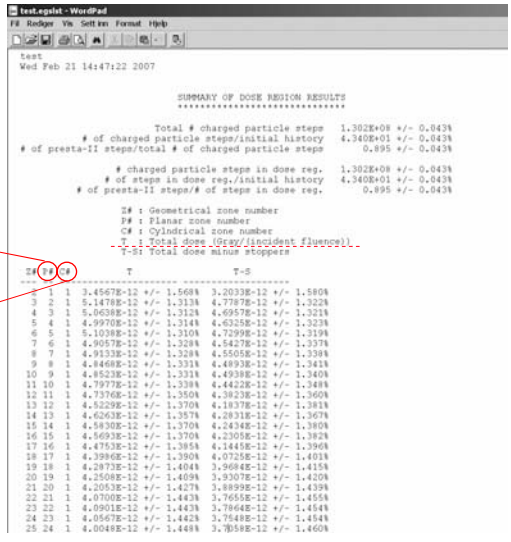


Output - *.egslst



PEGS

- Preprocessor for EGS
- Medium definition is performed in PEGS
- Have to set AE og AP, in addition to UE og UP (upper limit for for electron- and photon energy)

PEGS

Give medium composition

Provide name of subbstance

Density correction file

Lower limit for generation of secondary photons (AP) or electrons (AE)

File name