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Monte Carlo simulations

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MC simulations 2

- Photons give rise to electrons and vice versa; coupled energy transport
- Analytic methods are suboptimal for:
 - Modeling of scatter
 - Generating electron- and photon spectra
 - Modeling interface effects
 - Calculating energy dependence of dosimeter response

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MC simulations 1

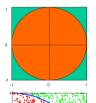
- Simulations of stochastic processes
- Interactions are stochastic: the path of a single ionizing particle may not be predicted
- Interactions are quantified by probabilities (cross sections)
- Random numbers and cross sections may be used to simulate single events
- Better than analytical methods, but requires CPU-time

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MC simulation - example

• Use random numbers to estimate π



Ratio of areas: $\pi/4$

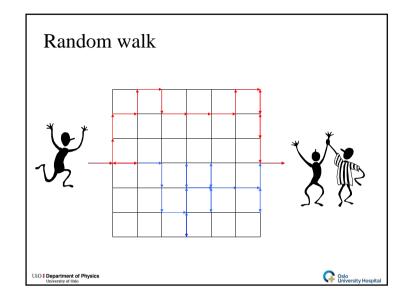
Sample points so that $x^2 + y^2 \le 1$

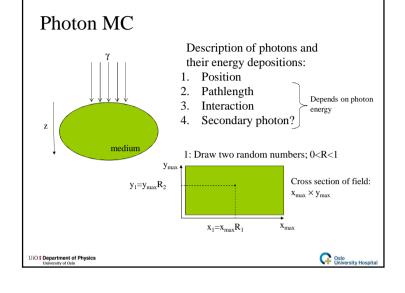
Here, Ratio = 787/1000 = 0.787

 $\rightarrow \pi \approx 4 \times 0.787 = 3.148$

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Photon pathlength

• Photon attenuation:

$$N = N_0 e^{-\mu z}$$

• Describes the number of photons at depth z - is a type of *frequency distribution*:

$$f(z) = Ce^{-\mu z}$$
, $\int_{0}^{\infty} f(z)dz = 1 \Rightarrow C = \mu$

$$\Rightarrow \langle z \rangle = \int_{0}^{\infty} z f(z) dz = \frac{1}{\mu}$$

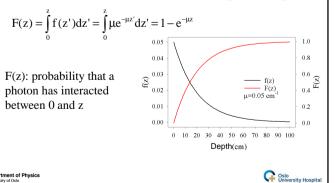
• Expected pathlength: 1/μ

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Photon interaction point 1

- At what depth does an event (interaction) take place?
- Need a cumulative distribution with respect to depth:



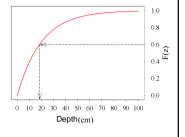
Photon interaction point 2

• Draw a random number R₁ – what is the corresponding pathlenght for this photon?

$$F(z_1) = R_1 = 1 - e^{-\mu z_1} \implies e^{-\mu z_1} = 1 - R_1$$

$$z_1 = -\frac{\ln(1 - R_1)}{\mu}$$

Example: $R_1=0.6 \rightarrow z_1=18.3$ cm



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Interaction sampling

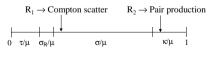
- What interaction occur at given depth?
- Total probability:

$$\mu = \tau + \sigma_{_R} + \sigma + \kappa$$

• Probability for e.g. Compton scatter:

$$p_{Compton} = \frac{\sigma}{\mu}$$

• Draw random number:

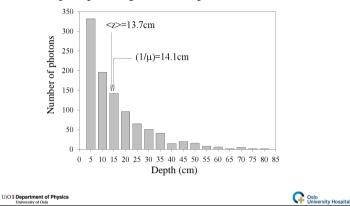


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Pathlength sampling

• Sampled pathlength of 1000 photons (1 MeV):

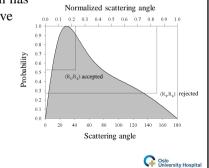


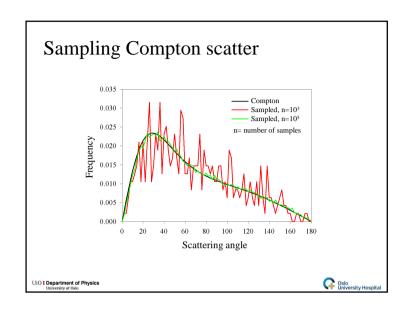
Sampling of scattered photons

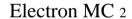
- Is the photon scattered? In what direction?
- Angular distribution follows Compton cross section:

• Compton distribution has no analytic cumulative

• Must draw *two* random numbers







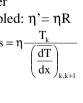
• Relative energy loss per step, η:

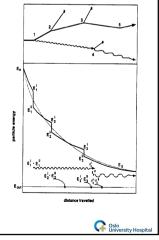
$$\eta = \frac{T_{k+1} - T_k}{T_k} = \frac{\Delta T}{T_k}$$

• T_k: electron energy in interaction point k

• η is set by user - may be sampled: $\eta' = \eta R$

• Step length: $\Delta s = \eta \frac{T_k}{\left(\frac{dT}{dx}\right)_{k,k+}}$



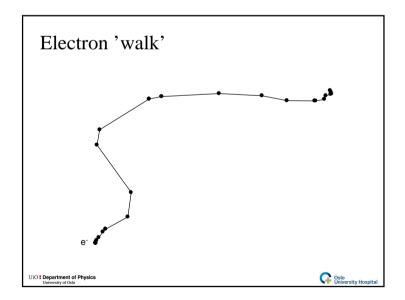


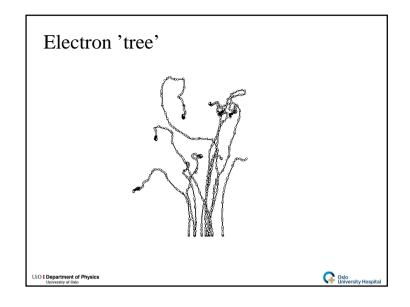
Electron MC 1

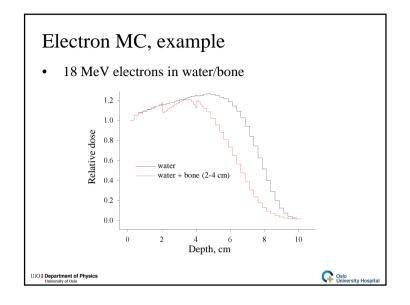
- Simulations of electrons and positrons are more complicated
- A 0.5 MeV electron interacts ~10000 times when slowing down to 1 keV in aluminium!
- Number of calculations $\rightarrow \infty$
- *Macroscopic* Monte Carlo: Evaluate the electron after a given steplength several interactions included in one step (simulations of every interaction: *microscopic* Monte Carlo)

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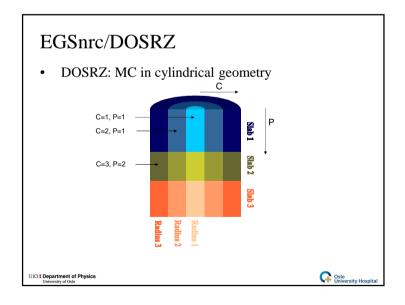


EGSnrc

- EGSnrc is a widely used MC code for e.g. simulations of photon- and electron beams
- Complicated programming, but simplified, user-friendly interface available: egs_inprz

www.nrc-nrc.gc.ca/eng/solutions/advisory/egsnrc_index.html





DOSRZ

- The user sets:
 - Phantom geometry
 - Radiation type- and energy (or spectrum)
 - Source (parallel beam, point source, ...)
 - Number of "histories", i.e. number of particles
 - Some MC parameters

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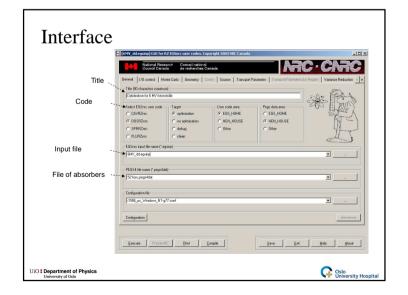
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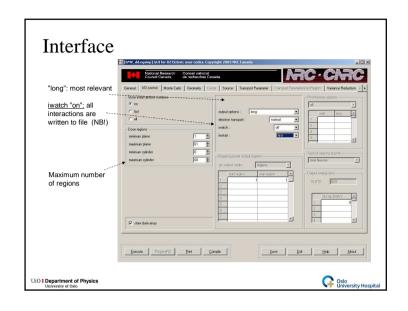
Some important parameters

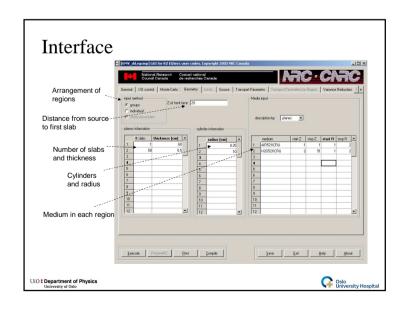
- ECUT: lower limit for electron transport (includes rest mass of 0.511 MeV)
- PCUT: lower limit for photon transport
- AE: lower limit for generation of electrons
- AP: lower limit for generation of photons
- AE and AP is medium specific and must be set in PEGS (see below)

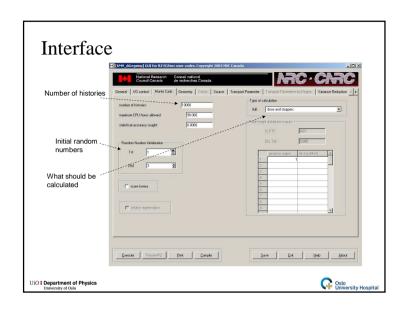
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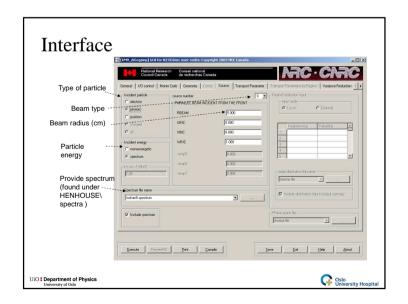


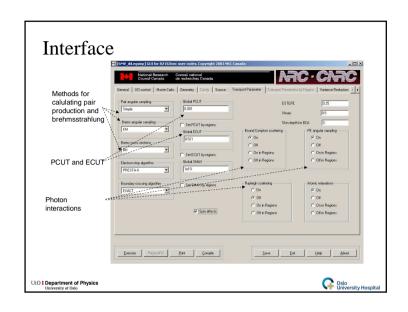


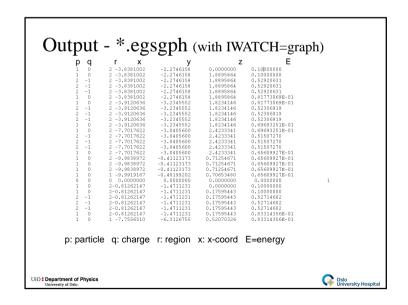


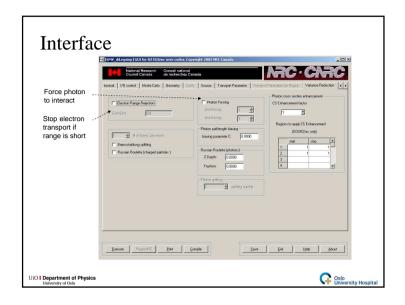


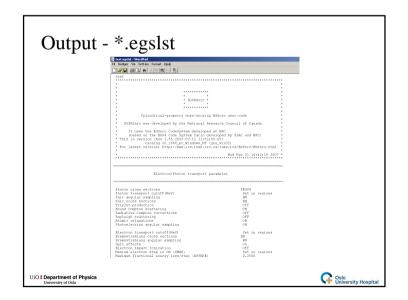


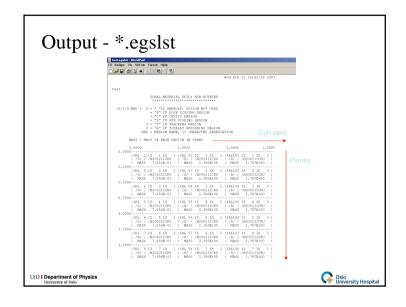


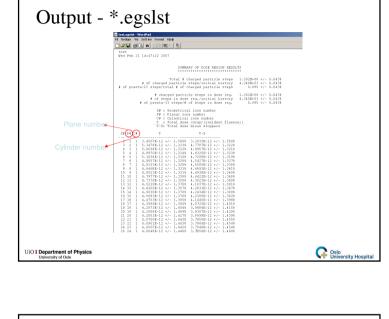












PEGS

- Preprocessor for EGS
- Medium definition is performed in PEGS
- Have to set AE og AP, in addition to UE og UP

