

FYS4630/FYS9630

Assignment #6 Tuesday October 10, 2017

- 1) The two-stream equations for a homogeneous atmosphere and isotropic scattering phase function is:

$$\bar{\mu} \frac{dI^+(\tau)}{d\tau} = I^+(\tau) - \frac{\bar{\omega}}{2} I^+(\tau) - \frac{\bar{\omega}}{2} I^-(\tau) - (1 - \bar{\omega})B$$

$$-\bar{\mu} \frac{dI^-(\tau)}{d\tau} = I^-(\tau) - \frac{\bar{\omega}}{2} I^+(\tau) - \frac{\bar{\omega}}{2} I^-(\tau) - (1 - \bar{\omega})B$$

We assume uniform illumination at the top of the atmosphere: $I^-(\tau = 0) = \mathfrak{S} = \text{constant}$ and a non-reflecting lower boundary, $I^+(\tau = \tau^*) = 0$. (This is prototype problem 1)

Solve the two-stream equations above for $\bar{\omega} = 1$ (conservative scattering) and show that:

$$I^+(\tau) = \frac{\mathfrak{S} \cdot (\tau^* - \tau)}{2\bar{\mu} + \tau^*}$$

$$I^-(\tau) = \frac{\mathfrak{S} \cdot [2\bar{\mu} + (\tau^* - \tau)]}{2\bar{\mu} + \tau^*}$$

$$S(\tau) = \frac{\mathfrak{S} \cdot [\bar{\mu} + (\tau^* - \tau)]}{2\bar{\mu} + \tau^*}$$

$$F(\tau) = - \frac{4\pi\bar{\mu}^2\mathfrak{S}}{2\bar{\mu} + \tau^*}$$

$$H(\tau) = 0$$

- 2) Derive Eq.(7.7) on page 229. Specifically find $I_a^-(\tau, \mu = \mu_0, \varphi)$. Also derive Eq.(7.8) on page 230.