

1.4. PROBLEMS

1. Given that the acceleration due to gravity decays with height from the centre of the Earth following an inverse square law, what is the percentage change in g from the Earth's surface to an altitude of 100 km? (See also Problem 6 of Chapter 3.)
2. Compute the mean pressure at the Earth's surface given the total mass of the atmosphere, M_a (Table 1.3), the acceleration due to gravity, g , and the radius of the Earth, a (Table 1.1).
3. Express your answer to Problem 2 in terms of the number of apples per square meter required to exert the same pressure. You may assume that a typical apple weighs 0.2 kg. If the average density of air is 5 apples per m^3 (in apple units), calculate how high the apples would have to be stacked at this density to exert a surface pressure equal to 1000 hPa. Compare your estimate to the scale height, H , given by Eq. 3.6 in Section 3.3.
4. Using (i) Eq. 1-4, which relates the saturation vapor pressure of H_2O to temperature T , and (ii) the equation of state of water vapor, $e = \rho_v R_v T$ (see discussion in Section 1.3.2), compute the maximum amount of water vapor per unit volume that air can hold at the surface, where $T_s = 288 \text{ K}$, and at a height of 10 km where (from Fig. 3.1) $T_{10 \text{ km}} = 220 \text{ K}$. Express your answer in kg m^{-3} . What are the implications of your results for the distribution of water vapor in the atmosphere?