

(b)

```
counter1 = 10
counter2 = counter1
counter1 = 11
counter2 += 2 + counter1
print counter2
```

(c)

```
A = [1, 2, 3, -1]
if A[2] < 3:
    A[2] = 0
else:
    A[2] = 10
if A[-1] <= 0:
    A.append(4)
print A
```

(d)

```
B = [2*x+1 for x in range(5)]
print B[1:-1]
```

(e)

```
from numpy import linspace
x = linspace(0, 2, 3)
v = x + 2
for x_, v_ in zip(x, v):
    print '%.1f %.1f' % (x_, v_)
```

(f)

```
def Q(y):
    r = 4*y
    r = r + 1
    return r

x = 2
print 'Q(%g)=%g' % (x, Q(x))
```

(g)

```
x = range(1, 17, 5)
y = x
for x_ in x[1:-1]:
    for y_ in y[1:-1]:
        if x_ != y_ and x_ > y_ + 1:
            print x_, y_
```

(Continued on page 3.)

(h) The following program, called `prog.py`,

```
import sys

try:
    r1 = float(sys.argv[1])
    print r1
    r2 = float(sys.argv[2])
    print r2
    r3 = float(sys.argv[3])
    print r3
except IndexError:
    print 'Not enough command-line arguments!', sys.argv[1:]
except ValueError:
    print 'Illegal conversion to float!'
```

is run as

```
Terminal> python prog.py 3 6 hello world
```

(i)

```
u = [-1, -2]
v = [1, 2]
print u + v
from numpy import array
u = array(u)
v = array(v)
print u + v
```

(j)

```
def equal(a, b, eps=1E-14):
    """Test if a==b with tolerance eps."""
    return abs(a - b) < eps

def some_function(Q):
    if Q < 0:
        raise ValueError('Q<0 is not allowed')

    if equal(Q, 0):
        return 0, None
    else:
        return 1, 2

def run_some_function():
```

(Continued on page 4.)

```
try:
    r1, r2 = some_function(-1)
    print 'Something is wrong with some_function(-1)!'
    ok = False
except:
    ok = True
r1, r2 = some_function(0)
if not equal(r1, 0) or not r2 == None:
    print 'Something is wrong with some_function(0)!'
    ok = False
r1, r2 = some_function(2)
if not equal(r1, 1) or not equal(r2, 2):
    print 'Something is wrong with some_function(2)!'
    ok = False
if ok:
    print 'All tests passed!'
else:
    print 'Some test(s) failed!'

run_some_function()
```

Exercise 2 (3 points)

We want to write a program that can compute values of the function $g(t) = e^{-at}$ and its derivative $g'(t) = -ae^{-at}$, where a is some known parameter. Write a Python function `g(t)` that evaluates and returns the values of $g(t)$ and $g'(t)$. The parameter a can be a global variable. Demonstrate how the function is called and how the returned result can be stored in variables. Write out the computed value of $g'(t)$ to the screen.

Exercise 3 (3 points)

Extend the program in Exercise 2 such that the t and a values are read from the command line. Add a `try-except` block to handle the cases that the user has failed to provide enough command-line arguments or when the command-line arguments cannot be interpreted as real numbers. Stop the program in those cases.

Hint: You may get inspired by code snippets elsewhere in this exam. Even if you did not succeed in writing the function in Exercise 2, you can just assume that it is available as described.

Exercise 4 (3 points)

Assume that you have the function that evaluates $g(t)$ and $g'(t)$ as specified in Exercise 2. Make a code snippet for creating a plot with the two curves $g(t)$ and $g'(t)$, for $0 \leq t \leq 5/a$. Add a label τ on the x axis in the plot and include a legend for each curve. Save the plot to a file.

Exercise 5 (3 points)

The quadratic equation

$$ax^2 + bx + c = 0$$

has two solutions

$$x_1 = \frac{-b + \sqrt{q}}{2a}, \quad x_2 = \frac{-b - \sqrt{q}}{2a},$$

where $q = b^2 - 4ac$. The two solutions coincide if $q = 0$. Write a Python function that takes a , b , and c as arguments and returns the two solutions x_1 and x_2 . Require $q \geq 0$ so that x_1 and x_2 are real numbers. Raise a `ValueError` exception if $q < 0$. Return x_1 and `None` if $x_1 = x_2$.

Write a main program with necessary code for demonstrating how the function can be used to solve the particular quadratic equation $x^2 + 3x = -1$.

Exercise 6 (3 points)

The purpose of this exercise is to test the function developed in the previous exercise. Even if you have not succeeded in writing the function, you can just assume that it is available as specified in Exercise 5.

Write a test function that calls the function from the previous exercise and checks that the results are correct in three test cases: $q > 0$, $q = 0$, and $q < 0$. Write a message to the screen when a test fails, and write OK if all tests succeed. Remember to test equality of real numbers with a tolerance.

Hint: You may get inspired by code snippets elsewhere in this exam.

END