

IN2120 Information Security

University of Oslo

Autumn 2018

Lecture 2

Cryptography



University of Oslo, Autumn 2018

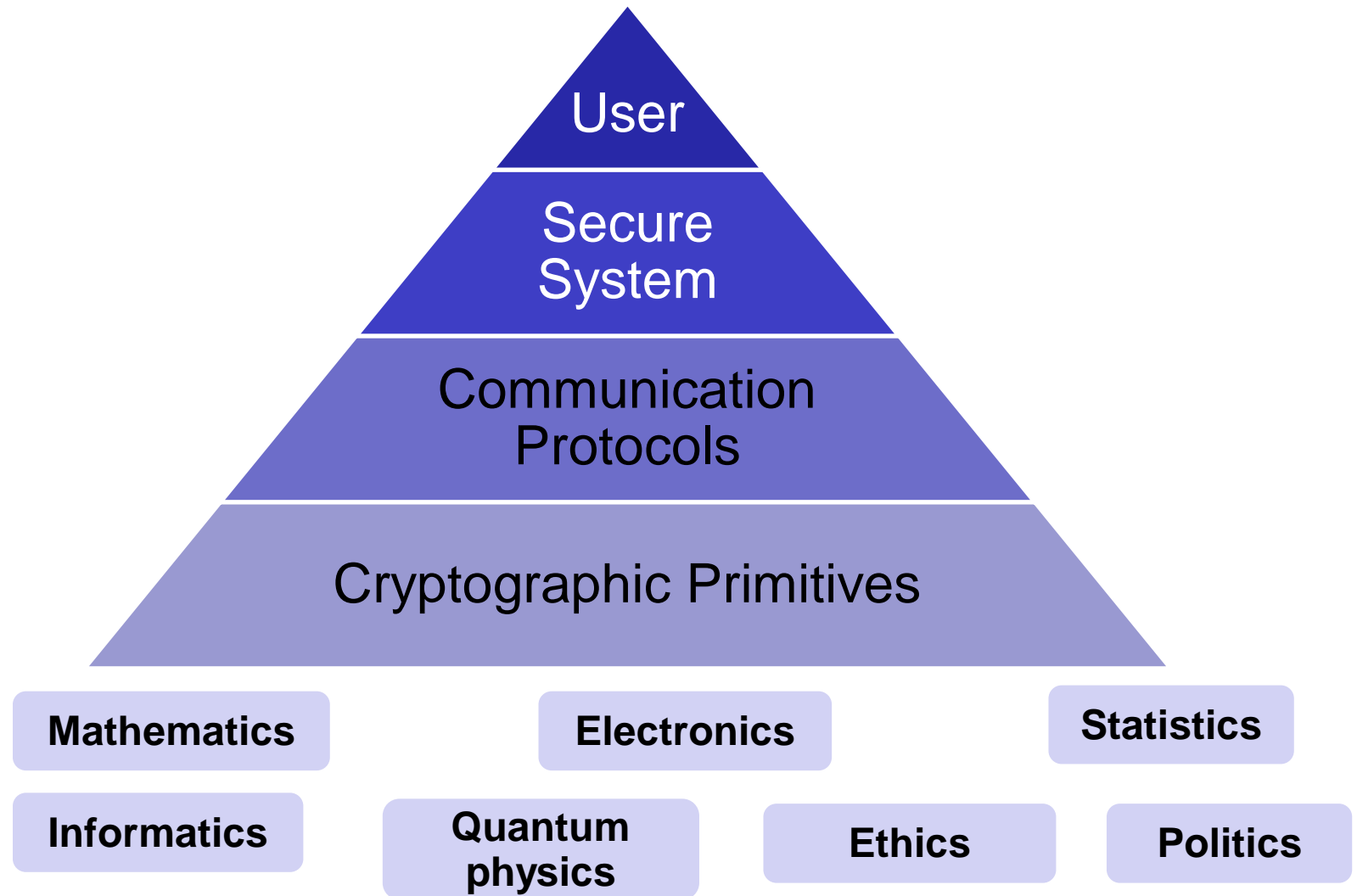
Nils Gruschka

Outline

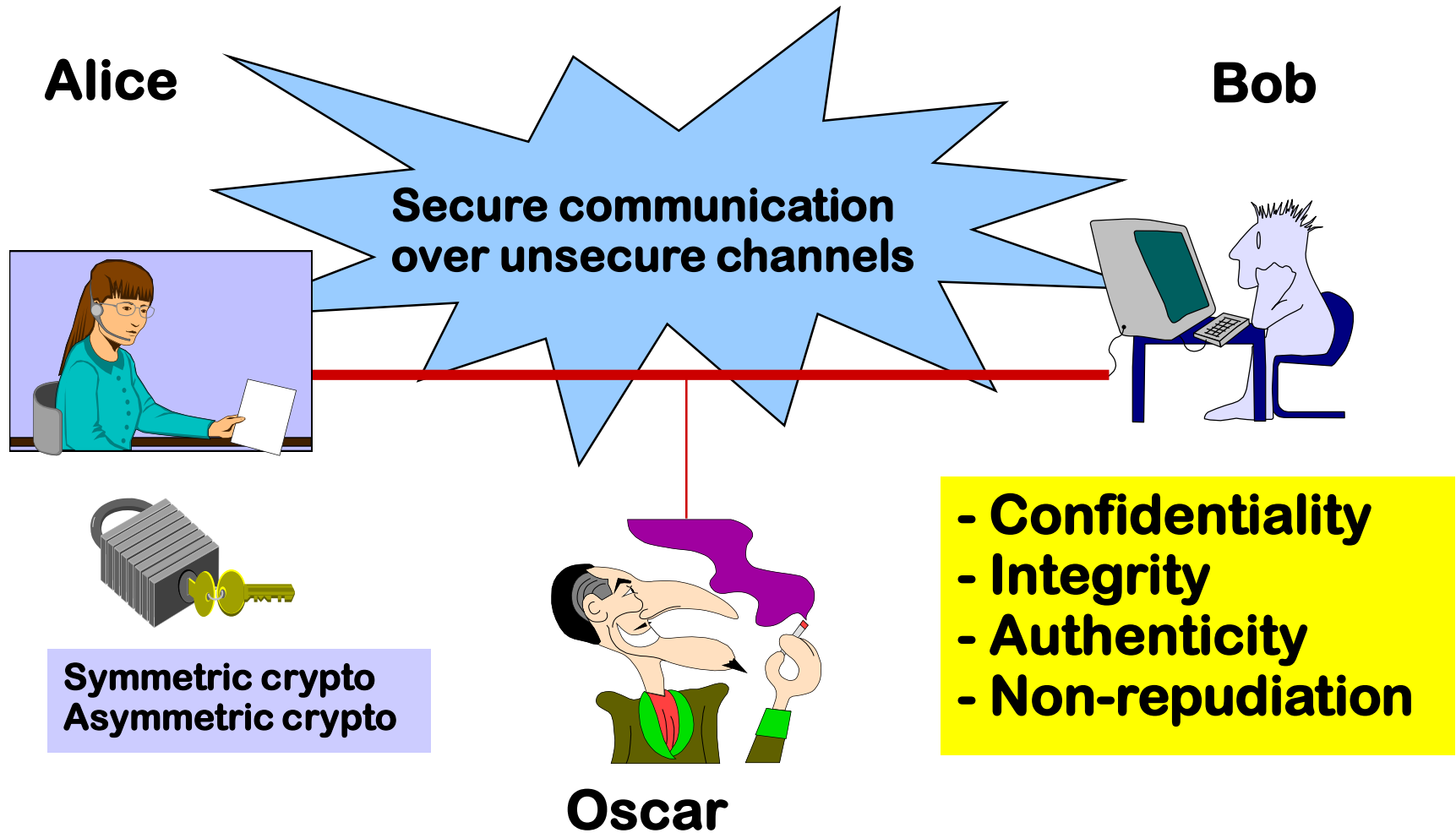
- What is cryptography?
- Brief crypto history
- Security issues
- Symmetric cryptography
 - Stream ciphers
 - Block ciphers
 - Hash functions
- Asymmetric cryptography
 - Factoring based mechanisms
 - Discrete Logarithms
 - Digital signatures
 - Quantum Resistant Crypto

Want to learn more?
Look up UNIK 4220

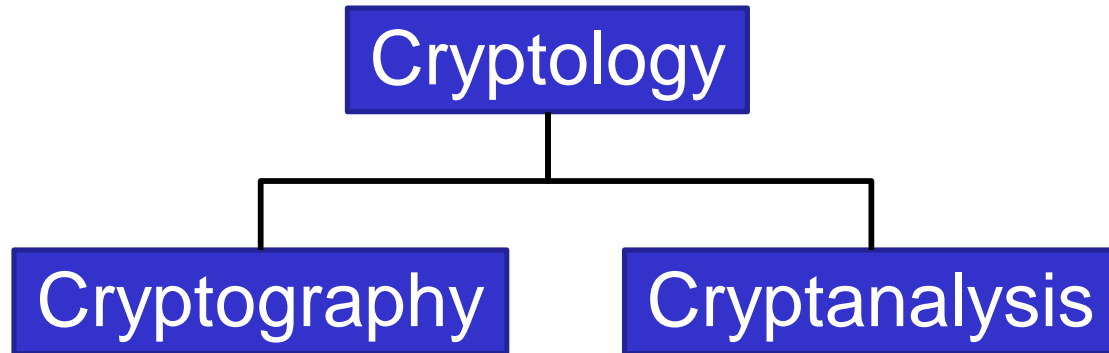
The security pyramid



What is cryptology?

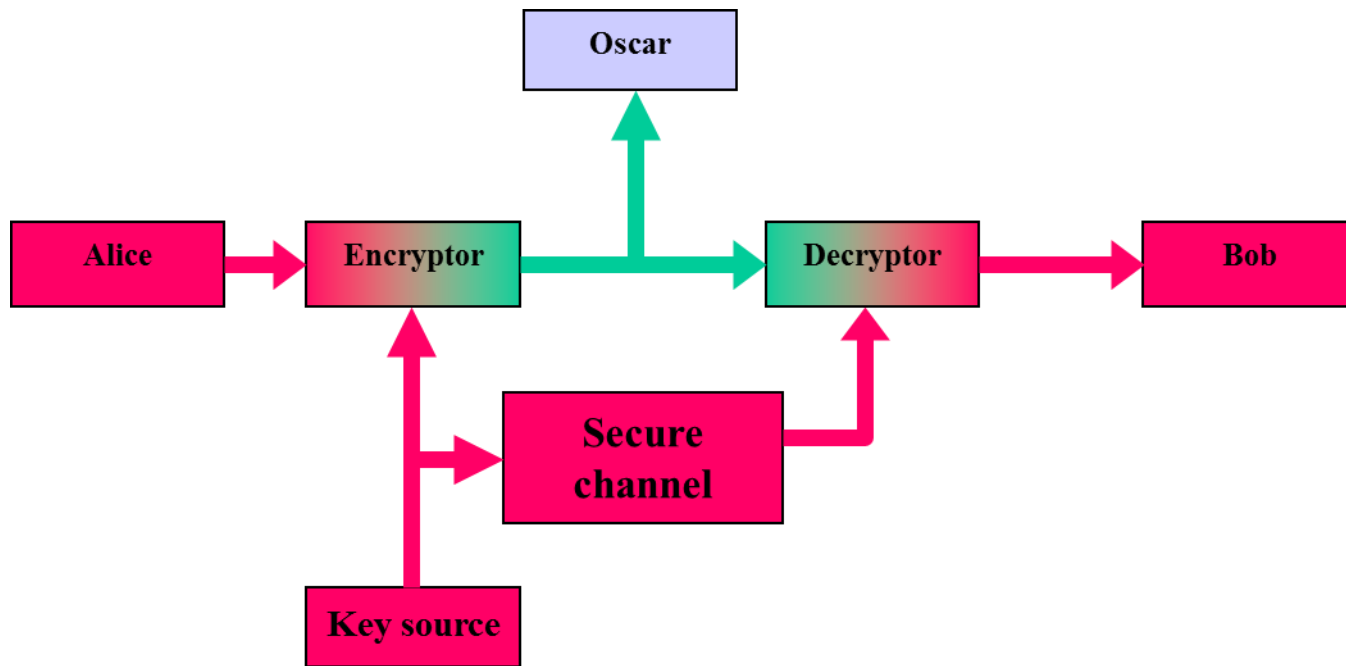


Terminology



- **Cryptography** is the science of secret writing with the goal of hiding the meaning of a message.
- **Cryptanalysis** is the science and sometimes art of *breaking* cryptosystems.

Model of symmetric cryptosystem



Confidential Communication

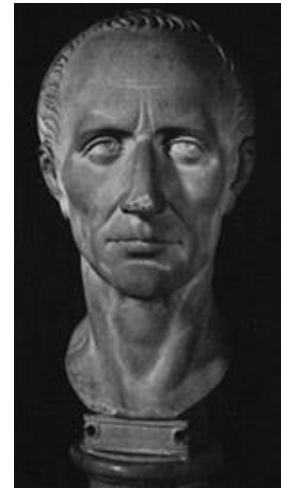
A



B



Caesar cipher



Encryption: Move all characters by K positions “to the right”

Decryption: Move all characters by K positions “to the left”

Example: $K = 5$

Plaintext: kryptologi er et spennende fag

Chiphertext: pwduytqtln jw jy xujssjsij kfl

(Note: In the original Caesar cipher K was set fix to 3.)

Numerical encoding of the alphabet

a	b	c	d	e	f	g	h	i	j	k	l	m	n	o
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14

p	q	r	s	t	u	v	w	x	y	z	æ	ø	å	
14	16	17	18	19	20	21	22	23	24	25	26	27	28	

Using this encoding many classical crypto systems can be expressed as algebraic functions over \mathbb{Z}_{26} (English alphabet) or \mathbb{Z}_{29} (Norwegian alphabet)

Shift cipher

Let $\mathcal{P} = \mathcal{C} = \mathbb{Z}_{26}$. For $0 \leq K \leq 25$, we define

$$E(x, K) = x + K \pmod{26}$$

and

$$D(y, K) = y - K \pmod{26}$$

$$(x, y \in \mathbb{Z}_{26})$$

Question: What is the size of the key space?

Puzzle: ct =

LAHYCXPAJYQHRBWNNMNMOMXABNLDANLXVVDWRLJCRXWB

Find the plaintext!

Exhaustive search

For[i=0, i<26, i++, Print["Key = ", i, " Plain = ", decrypt[ct,1,i]]]

Key = 0 Plain = LAHYCXPAJYQHRBWNNMNMOMOXABNLDANLXVVDWRLJCRXWB

Key = 1 Plain = KZGXBWOZIXPGQAVMMLMLNWZAMKCMKWUUCVQKIBQWVA

Key = 2 Plain = JYFWAVNYHWOFZULLKLMVYZLJBYLJVTTBUPJHAPVUZ

Key = 3 Plain = IXEVZUMXGVNEOYTKKJKJLUXYKIAXKIUSSATOIGZOUTY

Key = 4 Plain = HWDUYTLWFUMDNXSJJIIKJTWXJHZWJHTRRZSNH FYNTSX

Key = 5 Plain = GVCTXSKVETLCMWRIIHHJJSVWIGYVIGSQQYRMGEXMSRW

Key = 6 Plain = FUBSWRJUDSKBLVQHHGHGIRUVHFXUHFRPPXQLFDWLRQV

Key = 7 Plain = ETARVQITCRJAKUPGGFGFHQTUGEWGTGEQOOWPKECVKQPU

Key = 8 Plain = DSZQUPHSBQIZJTOFFEFEGPSTFDVSFDPNNVOJDBUJPOT

Key = 9 Plain = CRYPTOGRAPHYISNEEDEDFORSECURECOMMUNICATIONS

Key = 10 Plain = BQXOSNFQZOGXHRMDDCDCENQRDBTQDBNLLTMHBZSHNMR

Key = 11 Plain = APWNRMEPYNFWGQLCCBCBDMPQCASPCAMKKSLGAYRGMLQ

Key = 12 Plain = ZOVMQLDOXMEVFPKBBABACLOPBZROBZLJJRKFXZQFLKP

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-

Exhaustive search

For[i=0, i<26, i++, Print["Key = ", i, " Plain = ", decrypt[ct,1,i]]]

Key = 0 Plain = LAHYCXPAJYQHRBWNNMNMOMOXABNLDANLXVVDWRLJCRXWB

Key = 1 Plain = KZGXBWOZIXPGQAVMMLMLNWZAMKCMKWUUCVQKIBQWVA

Key = 2 Plain = JYFWAVNYHWOFZULLKLMVYZLJBYLJVTTBUPJHAPVUZ

Key = 3 Plain = IXEVZUMXGVNEOYTKKJKJLUXYKIAXKIUSSATOIGZOUTY

Key = 4 Plain = HWDUYTLWFUMDNXSJJIIKJTWXJHZWJHTRRZSNH FYNTSX

Key = 5 Plain = GVCTXSKVETLCMWRIIHHJJSVWIGYVIGSQQYRMGEXMSRW

Key = 6 Plain = FUBSWRJUDSKBLVQHHGHGIRUVHFXUHFRPPXQLFDWLRQV

Key = 7 Plain = ETARVQITCRJAKUPGGFGFHQTUGEWGTGEQOOWPKECVKQPU

Key = 8 Plain = DSZQUPHSBQIZJTOFFEFEGPSTFDVSFDPNNVOJDBUJPOT

Key = 9 Plain = CRYPTOGRAPHYISNEEDEDFORSECURECOMMUNICATIONS

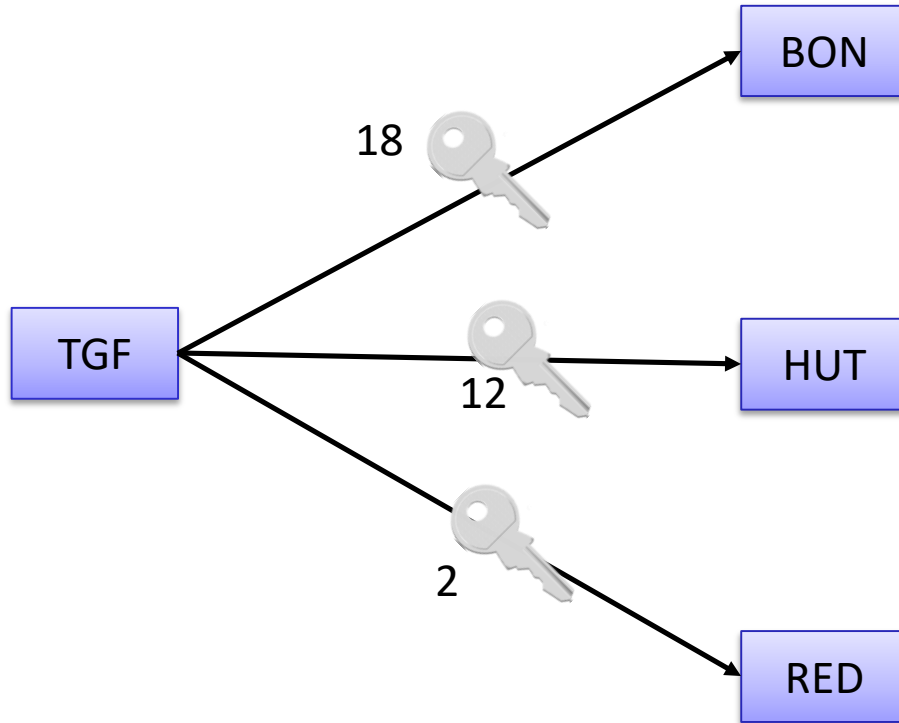
Key = 10 Plain = BQXOSNFQZOGXHRMDDCDCENQRDBTQDBNLLTMHBZSHNMR

Key = 11 Plain = APWNRMEPYNFWGQLCCBCBDMPQCASPCAMKKSLGAYRGMLQ

Key = 12 Plain = ZOVMQLDOXMEVFPKBBABACLOPBZROBZLJJRKZFZXQFLKP

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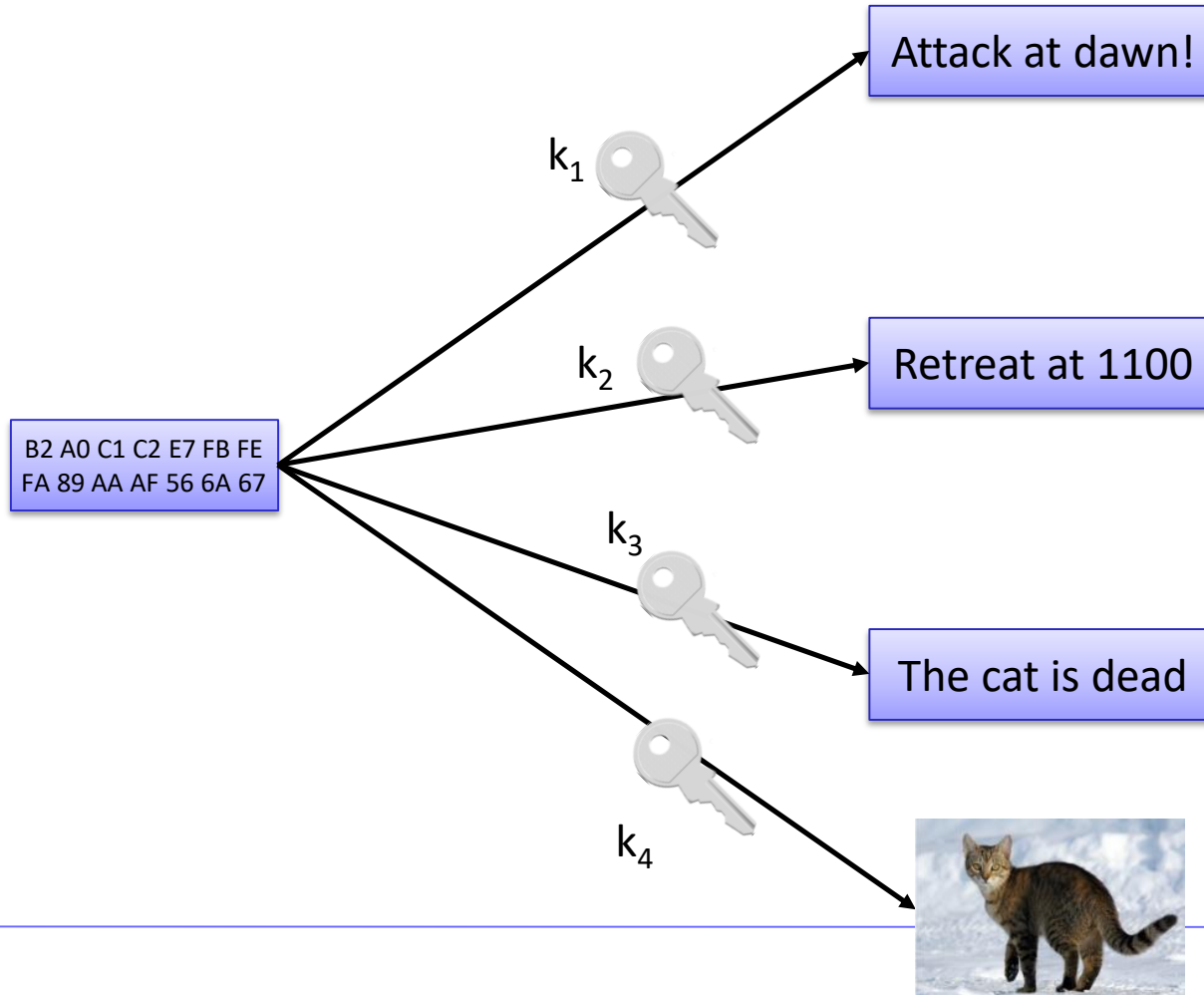
Exhaustive search



Finding the correct key is hard, without knowledge of the plaintext.

One-Time Pad Encryption

Exhaustive search



Brute-Force Attack (or Exhaustive Key Search)

- Treats the cipher as a black box
- Requires (at least) one plaintext-ciphertext pair (x_0, y_0)
- Check all possible keys K until condition is fulfilled:

$$d_K(y_0) = x_0$$

- How many keys do we need to test?

Substitution cipher - example

a	b	c	d	e	f	g	h	i	j	k	l	m	n	o
U	D	M	I	P	Y	Æ	K	O	X	S	N	Å	F	A
p	q	r	s	t	u	v	w	x	y	z	æ	ø	å	
E	R	T	Z	B	Ø	C	Q	G	W	H	L	V	J	

Plaintext: fermatssisteteorem

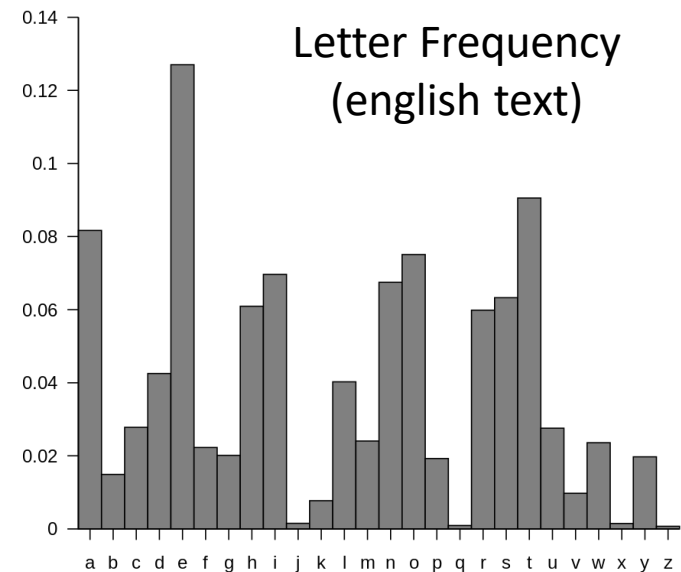
Ciphertext: YPTÅUBZZOZBPBPATPÅ

What is the size of the key space?

$$29! \approx 2^{103}$$

Breaking (monoalphabetic) Substitution ciphers

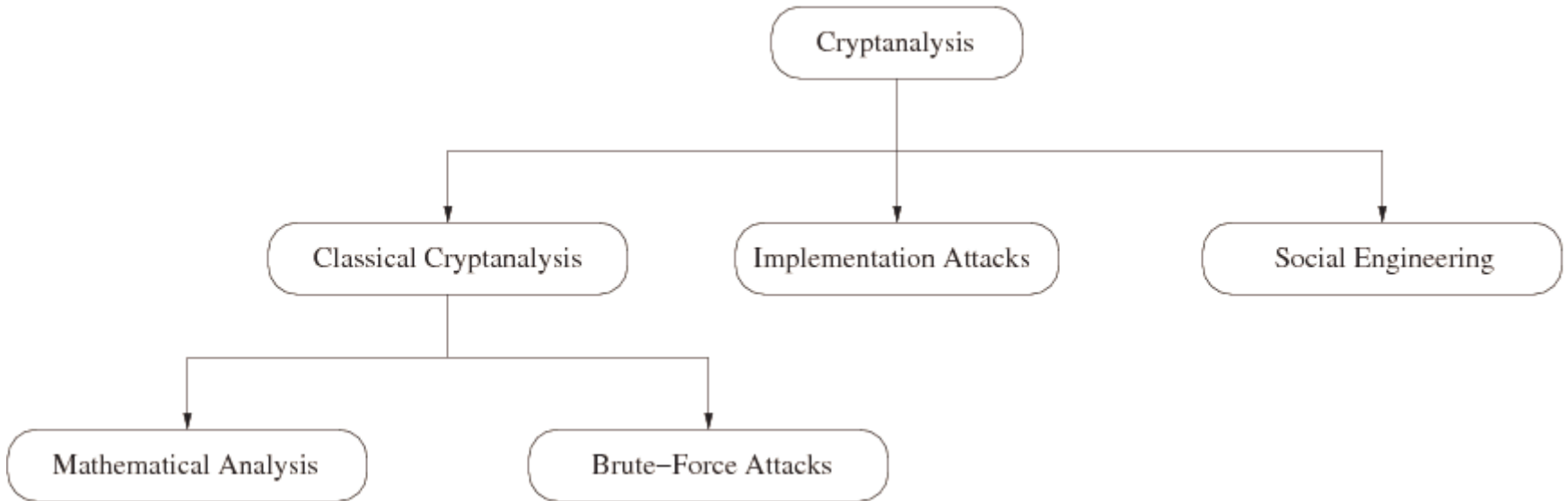
- How to break a message like this?
 - Tvctujuvujpo djqixs jt b nxuipe pg xodszqujoh cz fijdi vojut pg qmbjouxyu bsx sxqmbdxe fjui djqixsuxyu; bddpsejoh up b gjyxe tztuxn- uix vojut nbz cx tjohmx mxuuxst uix nptu dpnnpo; qbjst pg mxuuxst; usjqmxut pg mxuuxst; njyuvst pg uix bcpwx; boe tp gpsui, Uix sxdxjwxs exdjqixst uix uxyu cz qxsgpsnjoh uix jowxstx tvctujuvujpo,



Lessons learned

- A cipher with a small key space can easily be attacked by *exhaustive search*
- A *large key space* is necessary for a secure cipher, but it **is by itself not sufficient**
- *Monoalphabetical substitution* ciphers can easily be broken

Cryptanalysis: Attacking Cryptosystems



- **Classical Attacks**

- Mathematical Analysis
- Brute-Force Attack

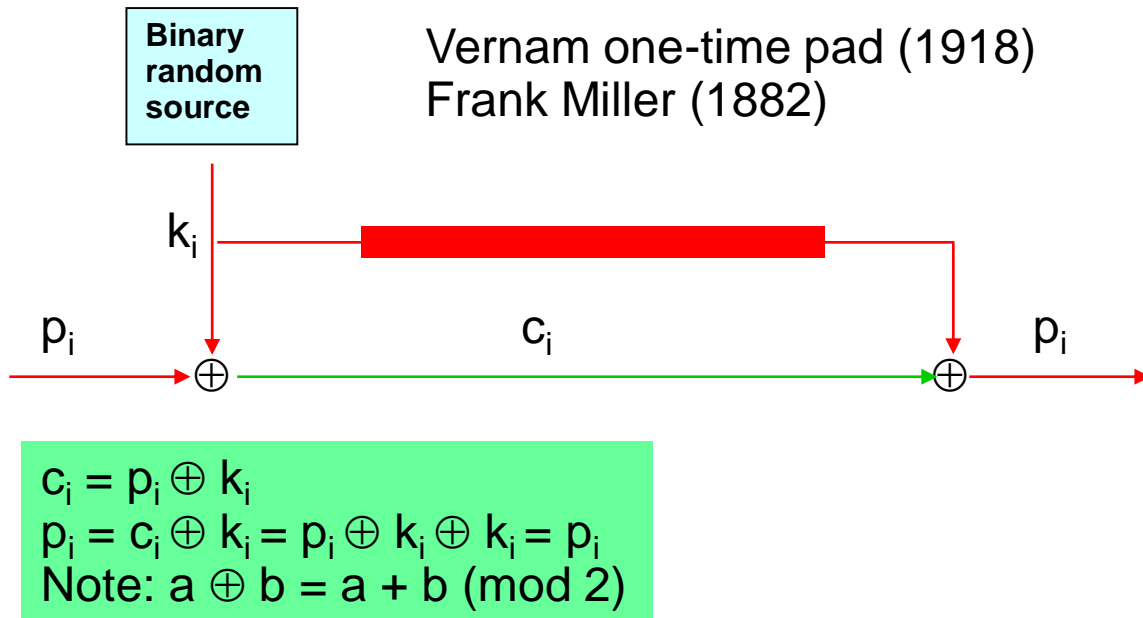
- **Implementation Attack:** Try to extract the key through reverse engineering or power measurement, e.g., for a banking smart card.

- **Social Engineering:** E.g., trick a user into giving up her password

Does secure ciphers exist?

- What is a secure cipher?
 - Perfect security
 - Computational security
 - Provable security

A perfect secure crypto system



Offers perfect security assuming the key is perfectly random, of same length as The Message; and only used once. Proved by Claude E. Shannon in 1949.

ETCRRM

- Electronic Teleprinter Cryptographic Regenerative Repeater Mixer (ETCRRM)
- Invented by the Norwegian Army Signal Corps in 1950
- Bjørn Rørholt, Kåre Mesingseth
- Produced by STK
- Used for "Hot-line" between Moskva and Washington
- About 2000 devices produced



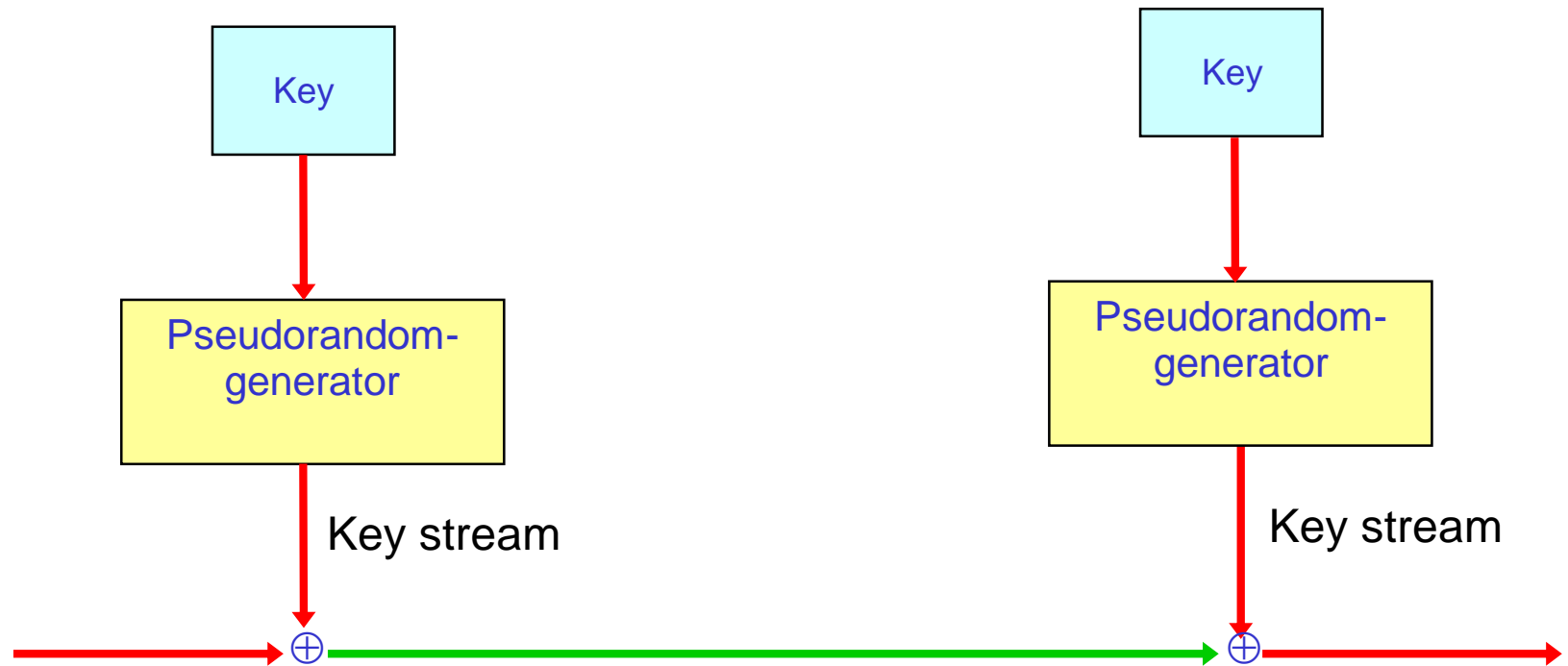
White House Crypto Room 1960s



Symmetric encryption

- Is it possible to design secure and practical crypto?

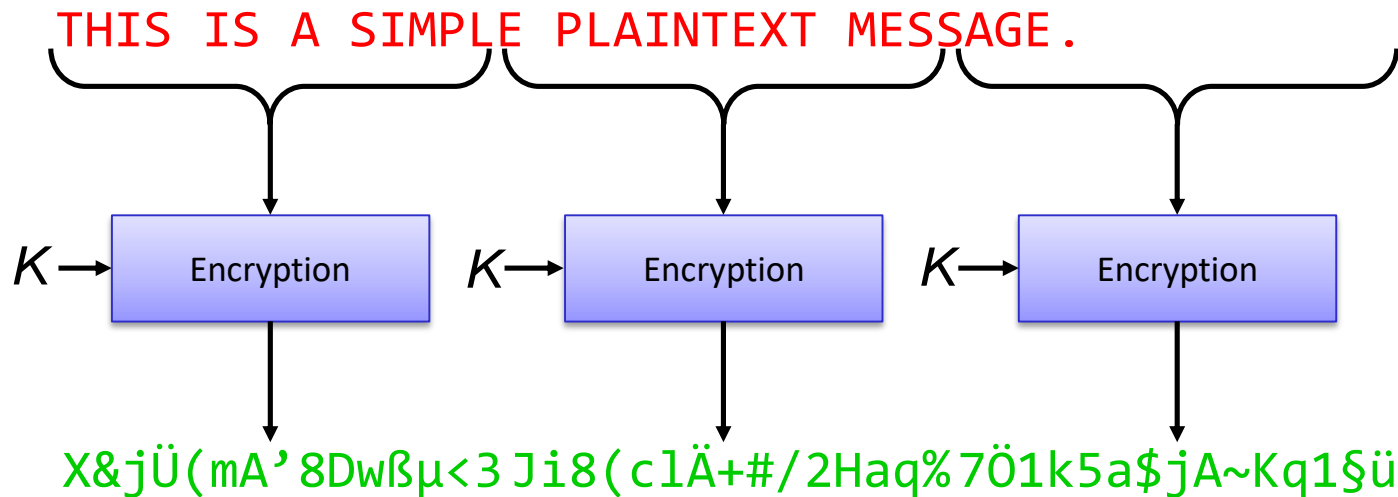
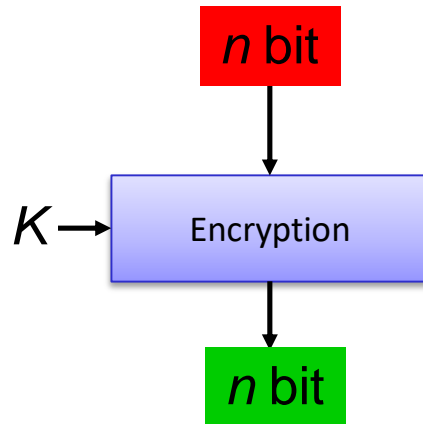
Symmetric stream cipher



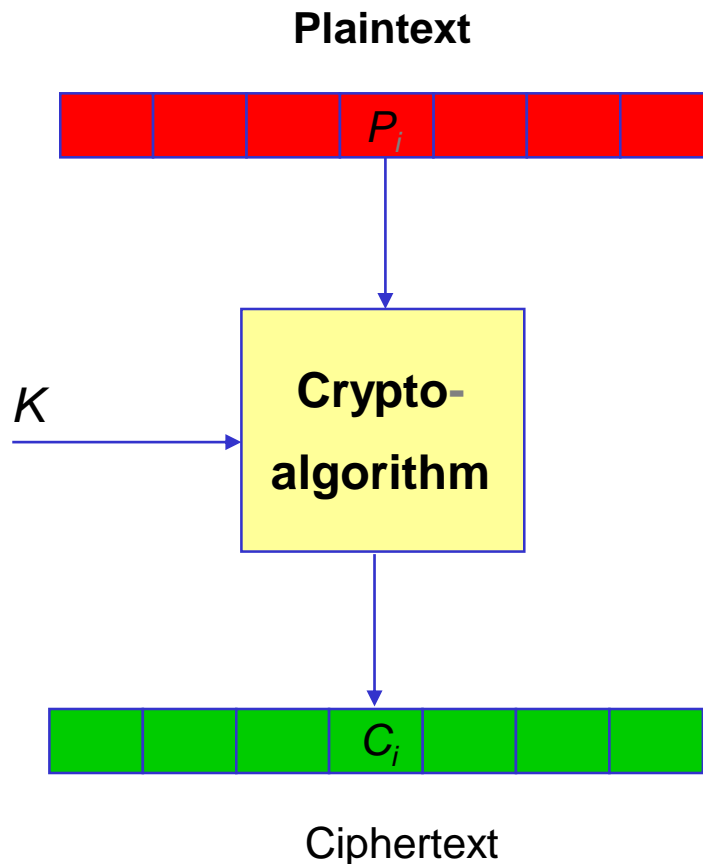
Symmetric stream cipher

- Examples:
 - A5/1 and A5/2 (1989; used in GSM) → broken
 - RC4 (1987) → broken
 - Salsa20 (2005)
 - ChaCha20 (2008)

Symmetric Block Cipher



Symmetric block cipher



- The algorithm represents a family of permutations of the message space
- Normally designed by iterating a less secure round function
- May be applied in different operational modes
- Must be impossible to derive K based on knowledge of P and C

Data Encryption Standard

- Published in 1977 by the US National Bureau of Standards for use in unclassified government applications with a 15 year life time.
- 16 round Feistel cipher with 64-bit data blocks, 56-bit keys.
- 56-bit keys were controversial in 1977; today, exhaustive search on 56-bit keys is very feasible.
- Controversial because of classified design criteria, however no loop hole was ever found.

Breaking DES

- Brute force attack on a 56 bit DES key:
 - 1998: EFF DES Cracker (ASICs), 4.5 days, 250.000\$
 - 2006: COPACOBANA (FPGA), 6.4 days, 10.000\$
 - 2012: Pico Computing (FPGA), 0.5 days

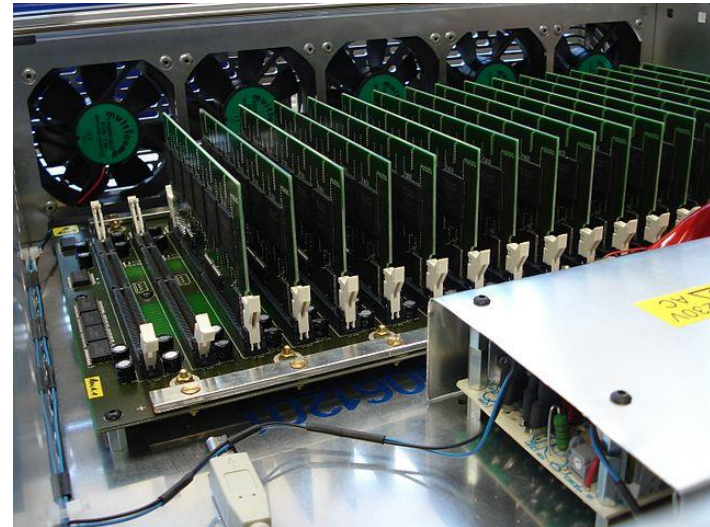
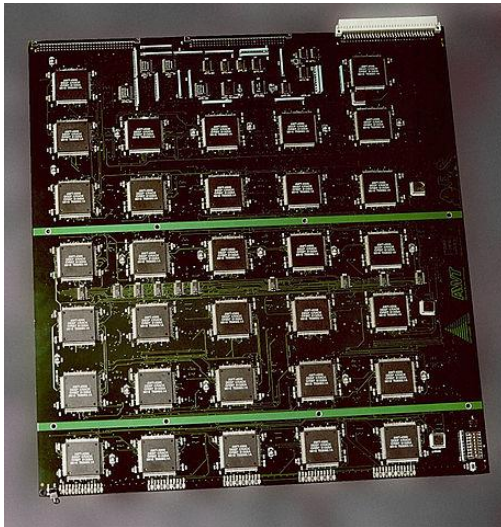


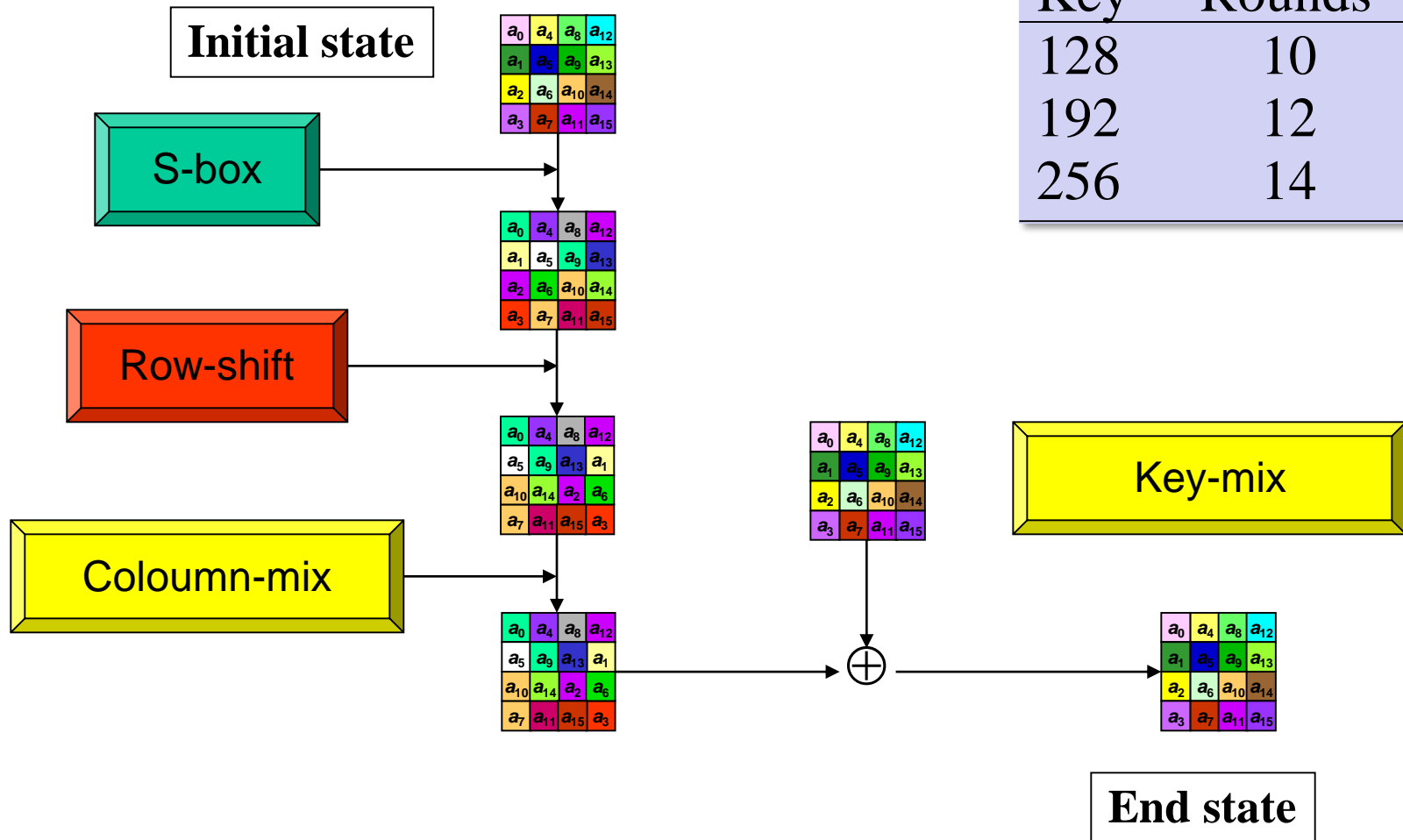
Image Source: Wikipedia, Gerd Pfeiffer, EFF

Advanced Encryption Standard

- Public competition to replace DES: because 56-bit keys and 64-bit data blocks no longer adequate.
- Rijndael nominated as the new Advanced Encryption Standard (AES) in 2001 [FIPS-197].
- Rijndael (pronounce as “Rhine-doll”) designed by Vincent Rijmen and Joan Daemen.
- 128-bit block size (**Note error in Harris p. 809**)
- 128-bit, 192-bit, and 256-bit key sizes.

Rijndael round function

Key	Rounds
128	10
192	12
256	14



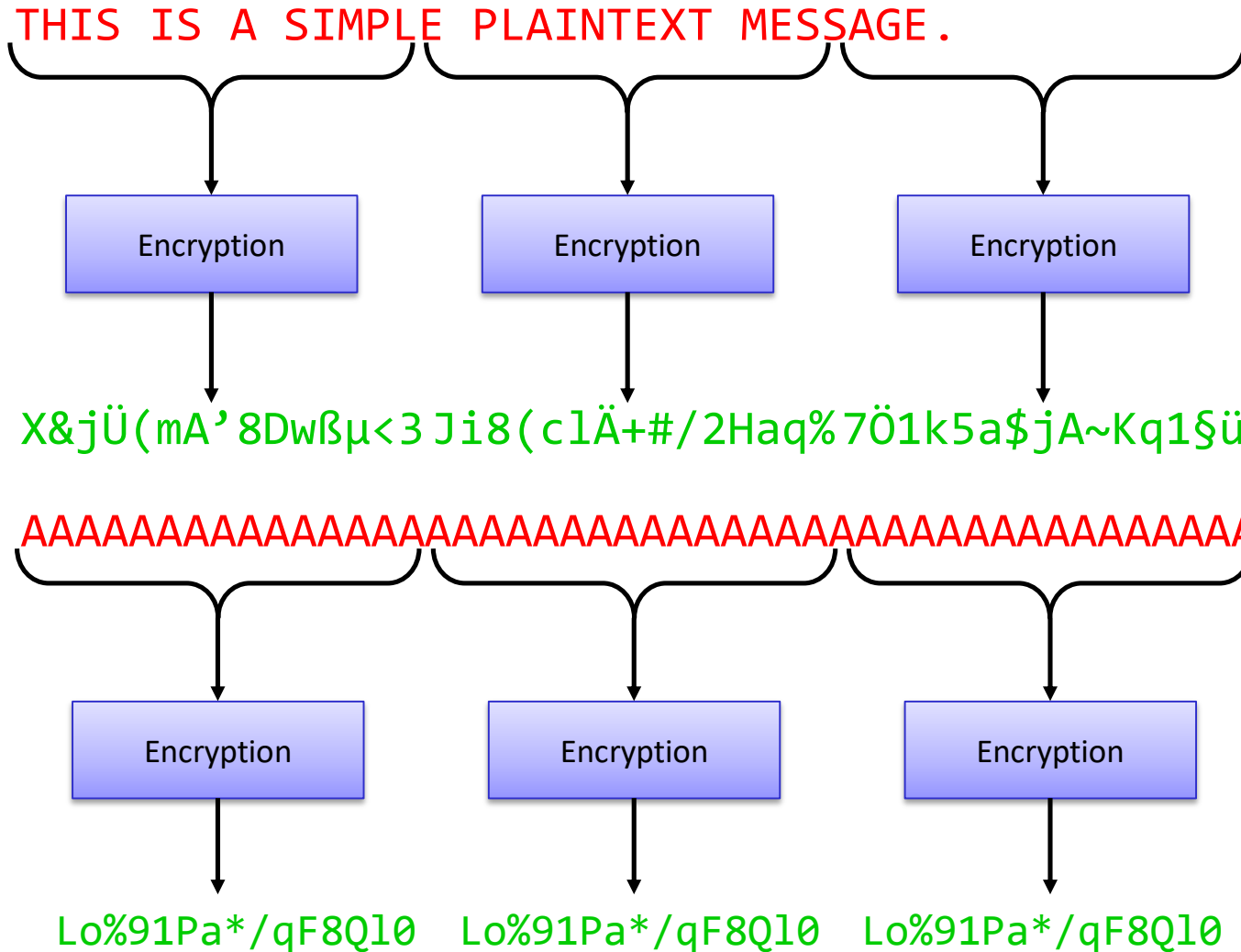
Breaking AES

- How long does a brute force attack on a 128 or 256 bit AES key take?
- Assumption: breaking 56 bit in 1 second

Key length	Duration
56 bit	1 s
64 bit	4 m
80 bit	194 d
112 bit	10^9 a
128 bit	10^{14} a
192 bit	10^{33} a
256 bit	10^{52} a

Key length in bit	Key space	Security life time (assuming brute-force as best possible attack)
64	2^{64}	Short term (few days or less)
128	2^{128}	Long-term (several decades in the absence of quantum computers)
256	2^{256}	Long-term (also resistant against quantum computers – note that QC do not exist at the moment and might never exist)

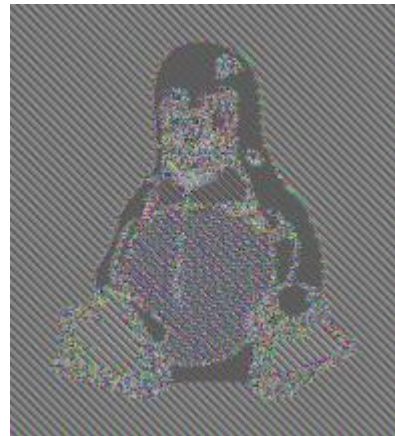
Block Cipher: Electronic Code Book



Modes in Block Ciphers



Plaintext



Ciphertext using
ECB mode



Ciphertext using
CBC mode

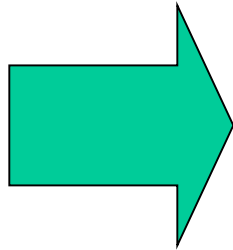
Block Ciphers: Modes of Operation

- Block ciphers can be used in different modes in order to provide different security services.
- Common modes include:
 - **E**lectronic **C**ode **B**ook (ECB)
 - **C**ipher **B**lock **C**haining (CBC)
 - **G**alois **C**ounter **M**ode (GCM)
{Authenticated encryption}

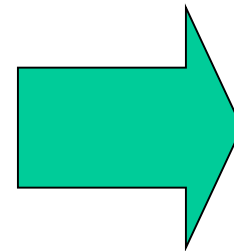
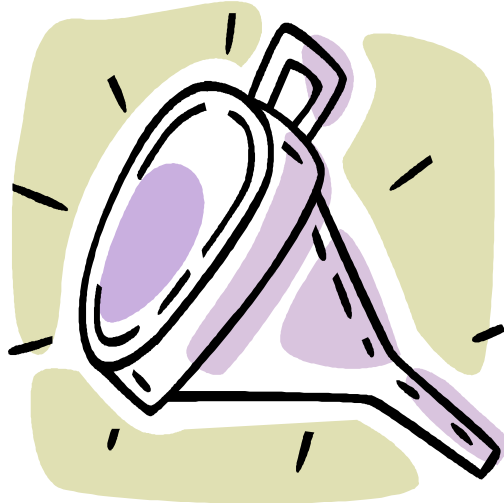
Integrity Check Functions

Hash functions

Data



Hash function



Hash value

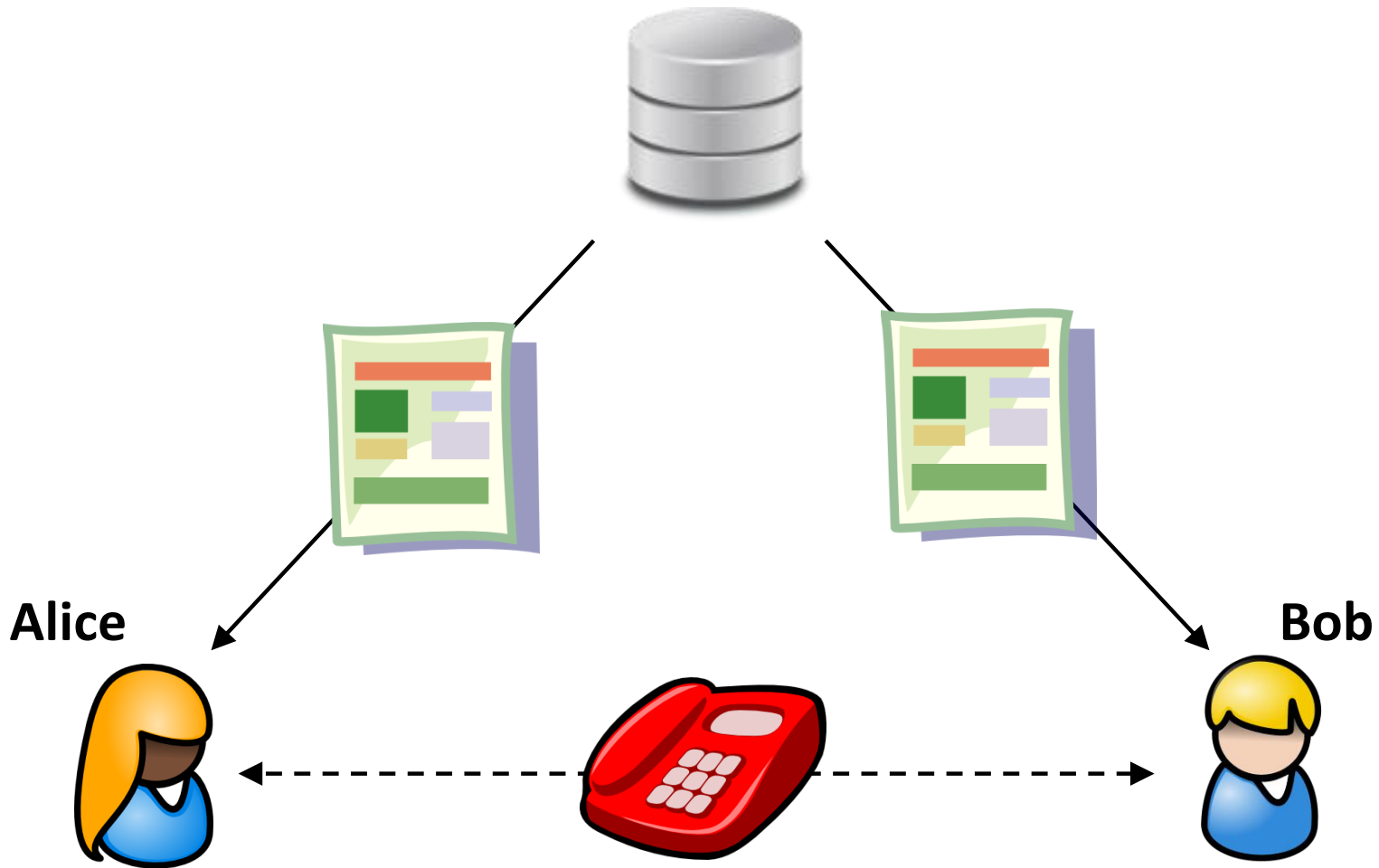


ISBN-13 Number



- 978-0-306-40615-r
$$r = (10 - (x_1 + 3x_2 + x_3 + 3x_4 + \dots + x_{11} + 3x_{12}) \bmod 10)$$
- $r = 7 \rightarrow 978-0-306-40615-7$
- (Weak) integrity protection:
 - Transmit ISBN number (just the first 12 digits)
 - Transmit check digit on a secure channel
 - Receiver compares calculated r_1 and received check digit r_2
 - If any one of the 12 digits is changed during transmission $\rightarrow r_1 \neq r_2$

Applications of hash functions

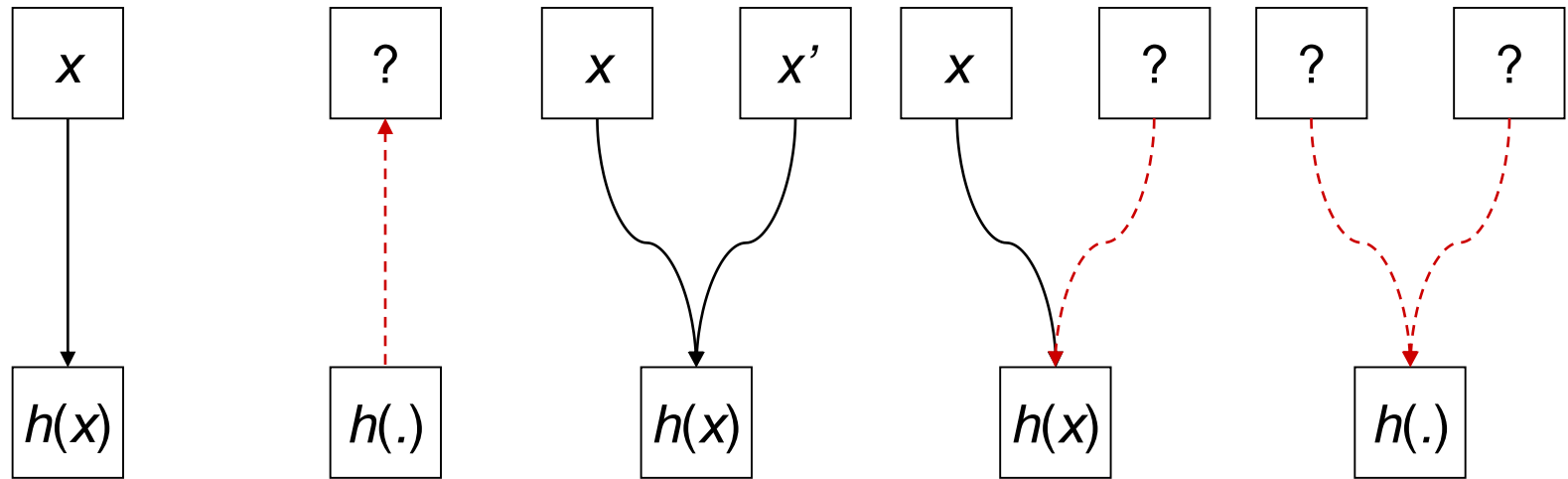


Hash functions (message digest functions)

Requirements for a one-way hash function h :

1. **Ease of computation**: given x , it is easy to compute $h(x)$.
2. **Compression**: h maps inputs x of arbitrary bitlength to outputs $h(x)$ of a fixed bitlength n .
3. **One-way**: given a value y , it is computationally infeasible to find an input x so that $h(x)=y$.
4. **Collision resistance**: it is computationally infeasible to find x and x' , where $x \neq x'$, with $h(x)=h(x')$ (note: two variants of this property).

Properties of hash functions



Ease of computation

Pre-image resistance

Collision resistance

Weak collision resistance

(2nd pre-image resistance)

Strong collision resistance

Further applications of hash functions

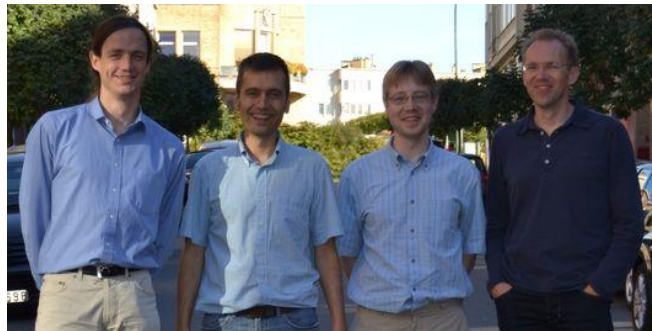
- Comparing files
- Protection of password
- Authentication of SW distributions
- Bitcoin
- Generation of Message Authentication Codes (MAC)
- Digital signatures
- Pseudo number generation/Mask generation functions
- Key derivation

Frequently used hash functions

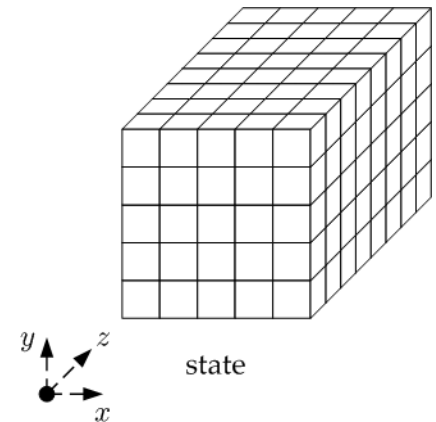
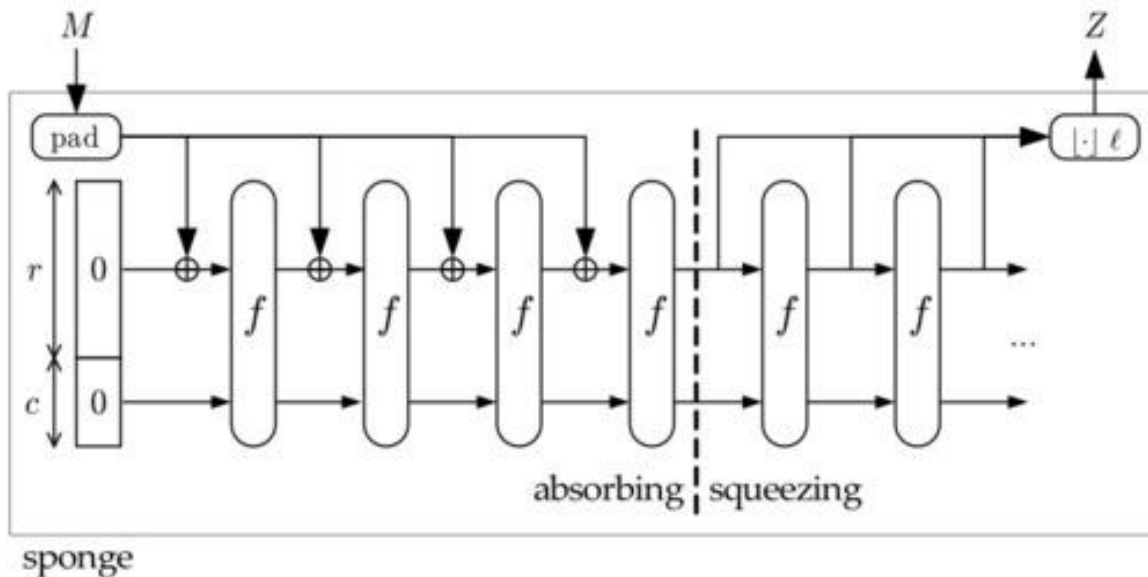
- MD5: 128 bit digest. Broken. Often used in Internet protocols but no longer recommended.
- SHA-1 (Secure Hash Algorithm): 160 bit digest. Potential attacks exist.
- SHA-2: Replacement for SHA-1. 256, 384 or 512 bit digest (called SHA-256, SHA-384, SHA-512). Still secure.
- RIPEMD-160: 160 bit digest. Still secure. Hash function frequently used by European cryptographic service providers.
- NIST competition for new secure hash algorithm (SHA-3), closed in 2012

And the winner is?

- [NIST announced Keccak as the winner](#) of the SHA-3 Cryptographic Hash Algorithm Competition on October 2, 2012, and ended the five-year competition.
- [Keccak](#) was designed by a team of cryptographers from Belgium and Italy, they are:
 - Guido Bertoni (Italy) of STMicroelectronics,
 - Joan Daemen (Belgium) of STMicroelectronics,
 - Michaël Peeters (Belgium) of NXP Semiconductors, and
 - Gilles Van Assche (Belgium) of STMicroelectronics.



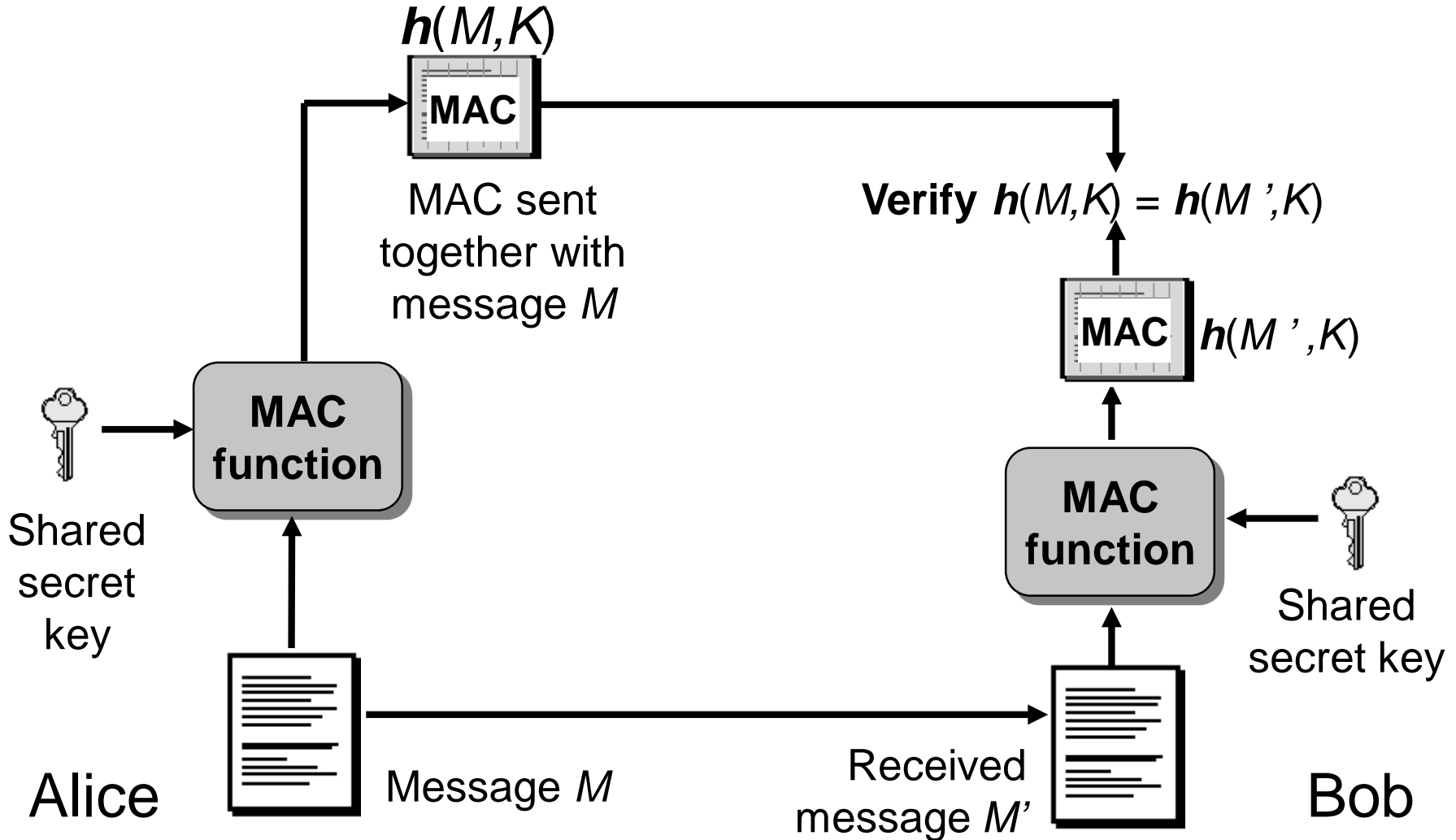
Keccak and sponge functions



MAC and MAC algorithms

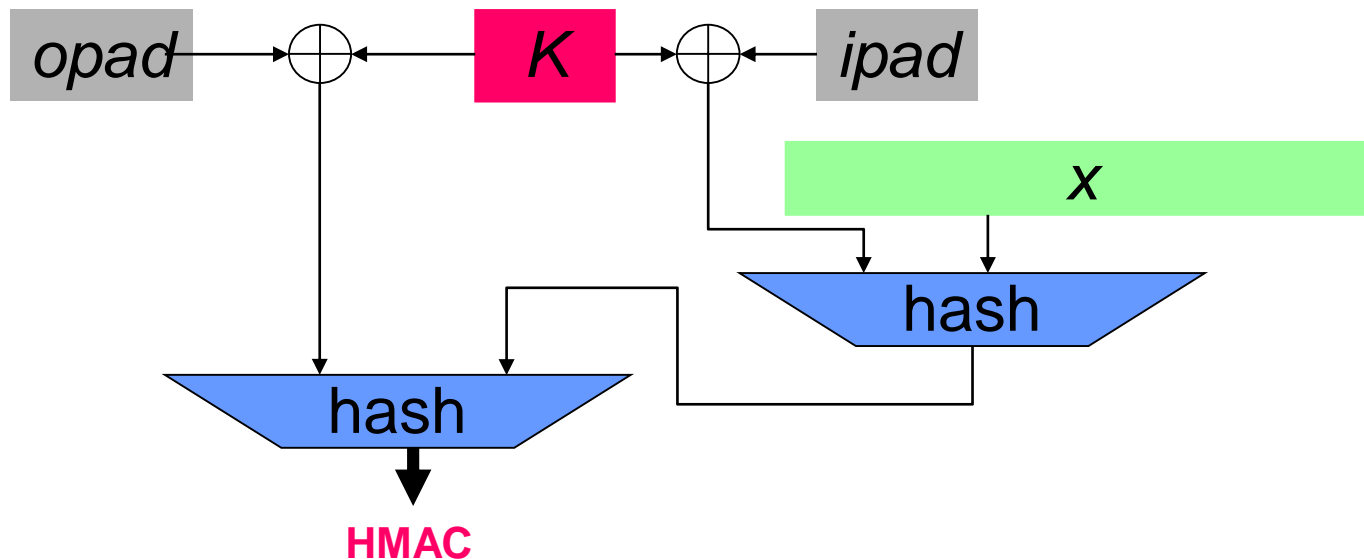
- MAC means two things:
 1. The computed message authentication code $h(M, k)$
 2. General name for algorithms used to compute a MAC
- In practice, the MAC algorithm is e.g.
 - HMAC (Hash-based MAC algorithm)
 - CBC-MAC (CBC based MAC algorithm)
 - CMAC (Cipher-based MAC algorithm)
- MAC algorithms, a.k.a. **keyed hash functions**, support data origin authentication services.

Practical message integrity with MAC



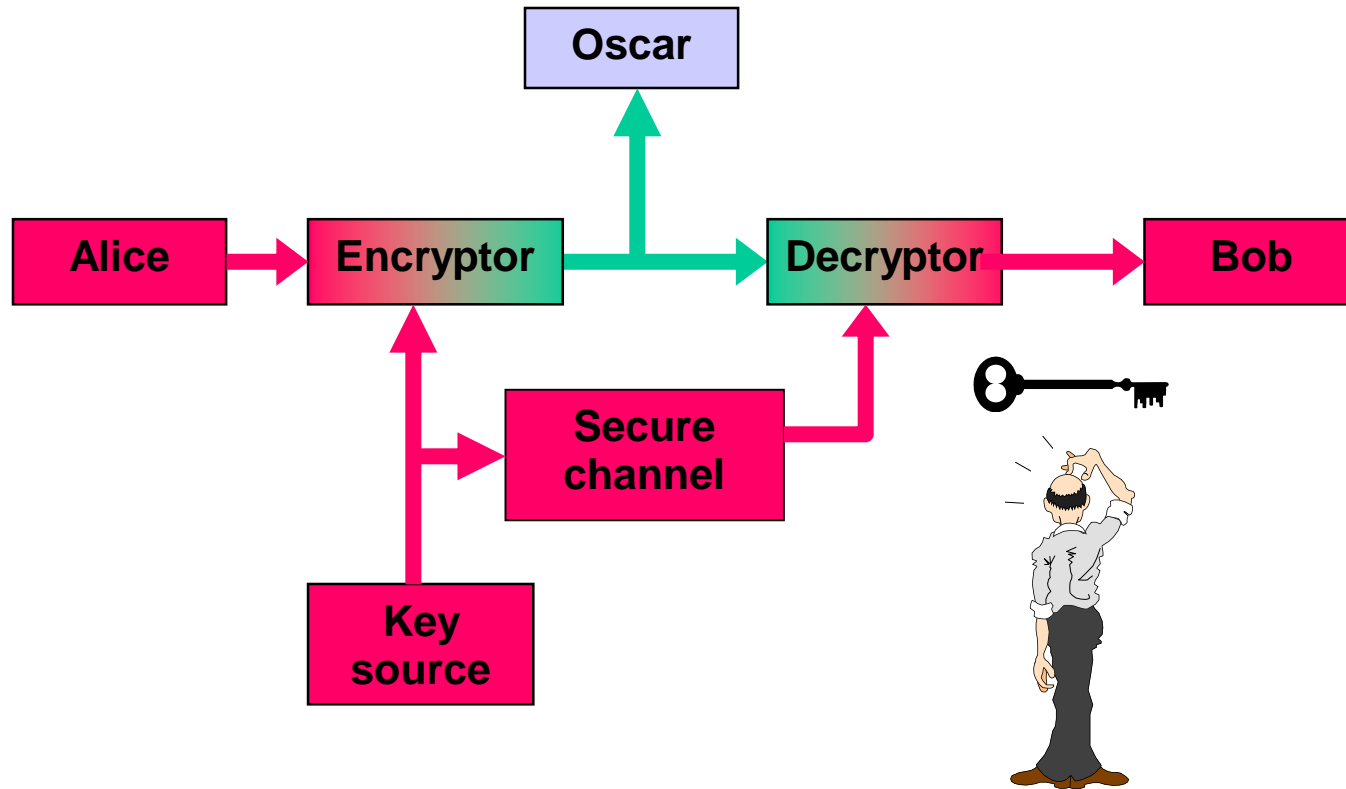
HMAC

- Define: $ipad = 3636\dots36$ (512 bit)
- $opad = 5C5C\dots5C$ (512 bit)
- $HMAC_K(x) = \text{hash}((K \oplus opad) \parallel \text{hash}((K \oplus ipad) \parallel x))$

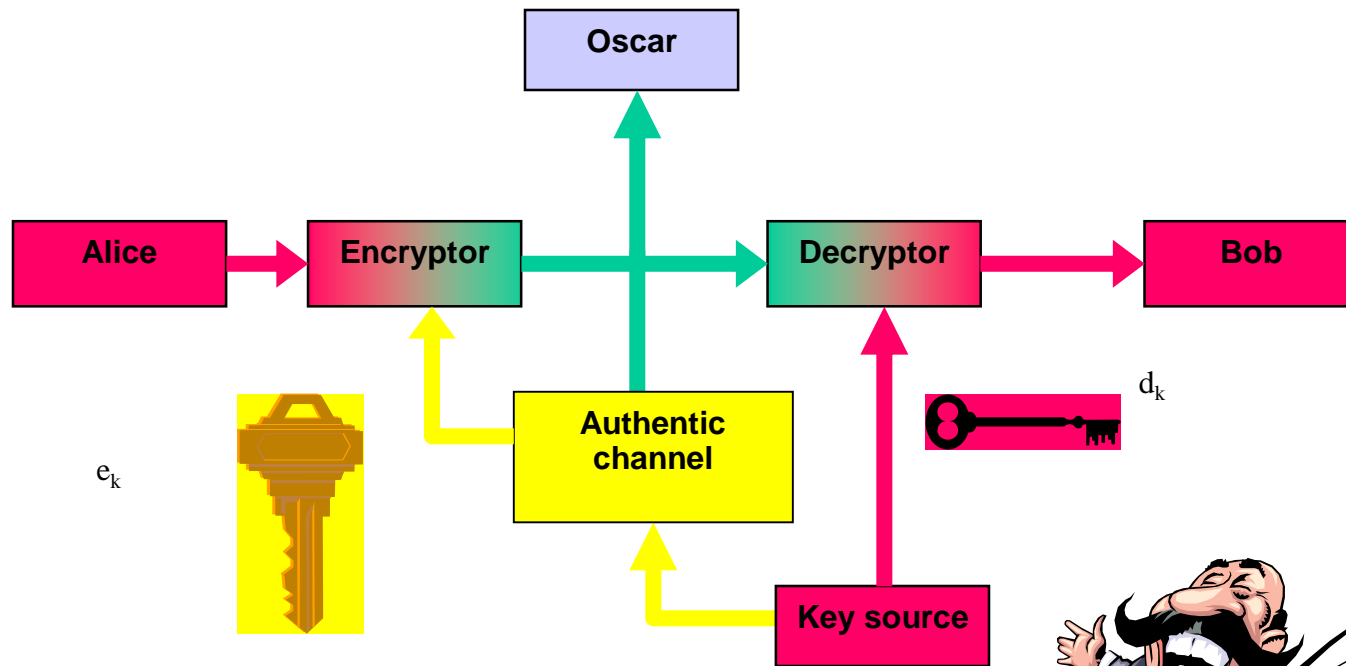


Public-Key Cryptography

Symmetric cryptosystem



Asymmetric crypto system



Public key inventors?

Marty Hellman and Whitfield Diffie, Stanford 1976



R. Rivest, A. Shamir and L. Adleman, MIT 1978



James Ellis, CESG 1970

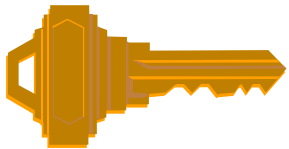


C. Cocks, M. Williamson, CESG 1973-1974

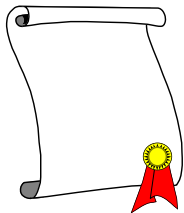


Asymmetric crypto

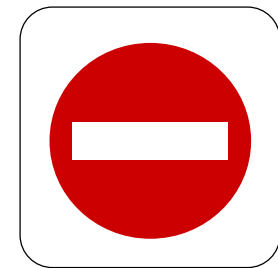
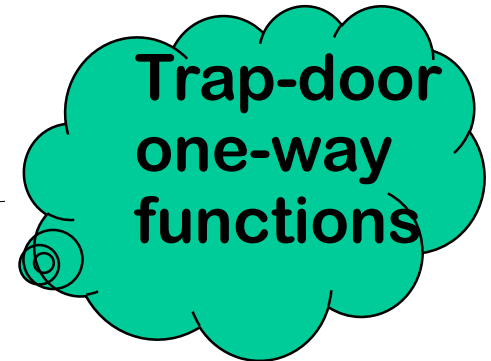
Public key **cryptography** was born in May 1975, the child of two problems and a misunderstanding!



Key Distribution!



Digital signing!



One-way functions

Modular power function

Given $n = pq$, where p and q are prime numbers. No efficient algorithms to find p and q .

Chose a positive integer b and define $f: Z_n \rightarrow Z_n$

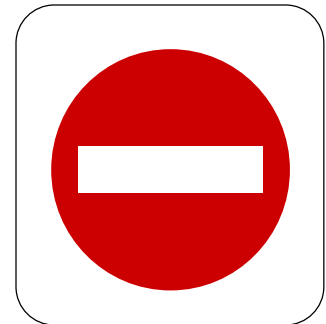
$$f(x) = x^b \text{ mod } n$$

Modular exponentiation

Given prime p , generator g and a modular power $a = g^x \text{ (mod } p)$. No

efficient algorithms to find x . $f: Z_p \rightarrow Z_p$

$$f(x) = g^x \text{ mod } p$$



Diffie-Hellman Key Exchange

- https://www.youtube.com/watch?v=YEBfamv-_do&t=2m6s

Diffie-Hellman key agreement (key exchange)

(provides no authentication)

Alice picks random integer a



$$g^a \bmod p$$



Bob picks random integer b

$$g^b \bmod p$$



Computationally impossible to compute discrete logarithm



Alice computes the shared secret

$$(g^b)^a = g^{ab} \bmod p$$

Bob computes the same secret

$$(g^a)^b = g^{ab} \bmod p.$$

Example

- Z_{11} using $g = 2$:
 - $2^1 = 2 \pmod{11}$ $2^6 = 9 \pmod{11}$
 - $2^2 = 4 \pmod{11}$ $2^7 = 7 \pmod{11}$
 - $2^3 = 8 \pmod{11}$ $2^8 = 3 \pmod{11}$
 - $2^4 = 5 \pmod{11}$ $2^9 = 6 \pmod{11}$
 - $2^5 = 10 \pmod{11}$ $2^{10} = 1 \pmod{11}$
- $\log_2 5 = 4$
- $\log_2 7 = 7$
- $\log_2 1 = 10 \pmod{10}$

Example (2)

$p =$

3019662633453665226674644411185277127204721722044543980521881984280643980698016315342127777985323
7655786915947633907457862442472144616346714598423225826077976000905549946633556169688641786953396
0040623713995997295449774004045416733136225768251717475634638402409117911722715606961870076297223
4159137526583857970362142317237148068590959528891803802119028293828368386437223302582405986762635
8694772029533769528178666567879514981999272674689885986300092124730492599541021908208672727813714
8522572014844749083522090193190746907275606521624184144352256368927493398678089550310568789287558
75522700141844883356351776833964003

$g =$

1721484410294542720413651217788953849637988183467987659847411571496616170507302662812929883501017
4348250308006877834103702727269721499966768323290540216992770986728538508742382941595672248624817
9949179397494476750553747868409726540440305778460006450549504248776668609868201521098873552043631
7965394509849072406890541468179263651065250794610243485216627272170663501147422628994581789339082
7991578201408649196984764863302981052471409215846871176739109049866118609117954454512573209668379
5760420560620966283259002319100903253019113331521813948039086102149370446134117406508009893347295
86051242347771056691010439032429058

Finn a når

$g^a \pmod{p} =$

4411321635506521515968448863968324914909246042765028824594289876687657182492169027666262097915382
0952830455103982849705054980427000258241321067445164291945709875449674237106754516103276658256727
2413603372376920980338976048557155564281928533840136742732489850550648761094630053148353906425838
5317698361559907392252360968934338558269603389519179121915049733353702083721856421988041492207985
6566434665604898681669845852964624047443239120501341277499692338517113201830210812184500672101247
270098803275601662656616757996322304239541426757926222147625965023052419869061244027798941410432
6855174387813098860607831088110617

Solution

a =

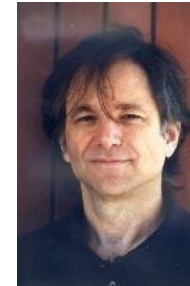
71893136149709653804503478677866573695060790720621260648699193249561437588126371185
81694154929099396752251787268346548051895320171079663652680741564200286881487888963
19895353311170236034836658449187117723820644855184055305945501710227615558093657781
93109639893698220411548578601884177129022057550866690223052160523604836233675971504
25938247630127368253363295292024736143937779912318142315499711747531882501424082252
28164641111954587558230112140813226698098654739025636607106425212812421038155501562
37005192231836155067262308141154795194735834753570104459663325337960304941906119476
18181858300094662765895526963615406

It is easy to compute $g^a \pmod{p}$ {0.016 s}, but it is computationally infeasible to compute the exponent a from the g^a .

Diffie-Hellman Applications

- **SSL/TLS**
 - (Ephemeral) Diffie-Hellman is nowadays the standard for key exchange in SSL/TLS protocol
- **IPSec (IP Security)**
 - IKE (Internet Key Exchange) is part of the IPSec protocol suite
 - IKE is based on Diffie-Hellman Key Agreement

Ron Rivest, Adi Shamir and Len Adleman



- Read about public-key cryptography in 1976 article by Diffie & Hellman: *“New directions in cryptography”*
- Intrigued, they worked on finding a practical algorithm
- Spent several months in 1976 to re-invent the method for non-secret/public-key encryption discovered by Clifford Cocks 3 years earlier
- Named RSA algorithm

RSA parameters (textbook version)

- Bob generates two large prime numbers p and q and computes $n = p \cdot q$.
- He then computes a public encryption exponent e , such that
- $\gcd(e, (p-1)(q-1)) = 1$ and computes the corresponding decryption exponent d , by solving:

$$d \cdot e \equiv 1 \pmod{(p-1)(q-1)}$$

- Bob's public key is the pair $P_B = (e, n)$ and the corresponding private and secret key is $S_B = (d, n)$.

$$\text{Encryption: } C = M^e \pmod{n}$$

$$\text{Decryption: } M = C^d \pmod{n}$$

RSA toy example

- Set $p = 157$, $q = 223$. Then $n = p \cdot q = 157 \cdot 223 = 35011$ and $(p-1)(q-1) = 156 \cdot 222 = 34632$
- Set encryption exponent: $e = 14213$ $\{\text{gcd}(34632, 14213) = 1\}$
- Public key: $(14213, 35011)$
- Compute: $d = e^{-1} = 14213^{-1} \pmod{34632} = 31613$
- **Private key: $(31613, 35011)$**

- Encryption:
- Plaintext $M = 19726$, then $C = 19726^{14213} \pmod{35011} = 32986$

- Decryption:
- Ciphertext $C = 32986$, then $M = 32986^{31613} \pmod{35011} = 19726$

Factoring record– December 2009

Find the product of

$p = 33478071698956898786044169848212690817704794983713768568$
 $912431388982883793878002287614711652531743087737814467999489$

and

$q = 367460436667995904282446337996279526322791581643430876426$
 $76032283815739666511279233373417143396810270092798736308917?$

Answer:

$n = 123018668453011775513049495838496272077285356959533479219732$
 $245215172640050726365751874520219978646938995647494277406384592$
 $519255732630345373154826850791702612214291346167042921431160222$
 $1240479274737794080665351419597459856902143413$

Computation time ca. 0.0000003 s on a fast laptop!

RSA768 - Largest RSA-modulus that have been factored (12/12-2009)

Up to 2007 there was 50 000\$ prize money for this factorisation!

Computational effort?

- Factoring using NFS-algorithm (Number Field Sieve)
- 6 mnd using 80 cores to find suitable polynomial
- Solding from August 2007 to April 2009 (1500 AMD64-år)
- $192\ 796\ 550 * 192\ 795\ 550$ matrise (105 GB)
- 119 days on 8 different clusters
- Corresponds to 2000 years processing on one single core 2.2GHz AMD Opteron (ca. 2^{67} instructions)

Asymmetric Ciphers: Examples of Cryptosystems

- RSA: best known asymmetric algorithm.
 - RSA = Rivest, Shamir, and Adleman (published 1977)
 - Historical Note: U.K. cryptographer Clifford Cocks invented the same algorithm in 1973, but didn't publish.
- ElGamal Cryptosystem
 - Based on the difficulty of solving the discrete log problem.
- Elliptic Curve Cryptography
 - Based on the difficulty of solving the EC discrete log problem.
 - Provides same level of security with smaller key sizes.

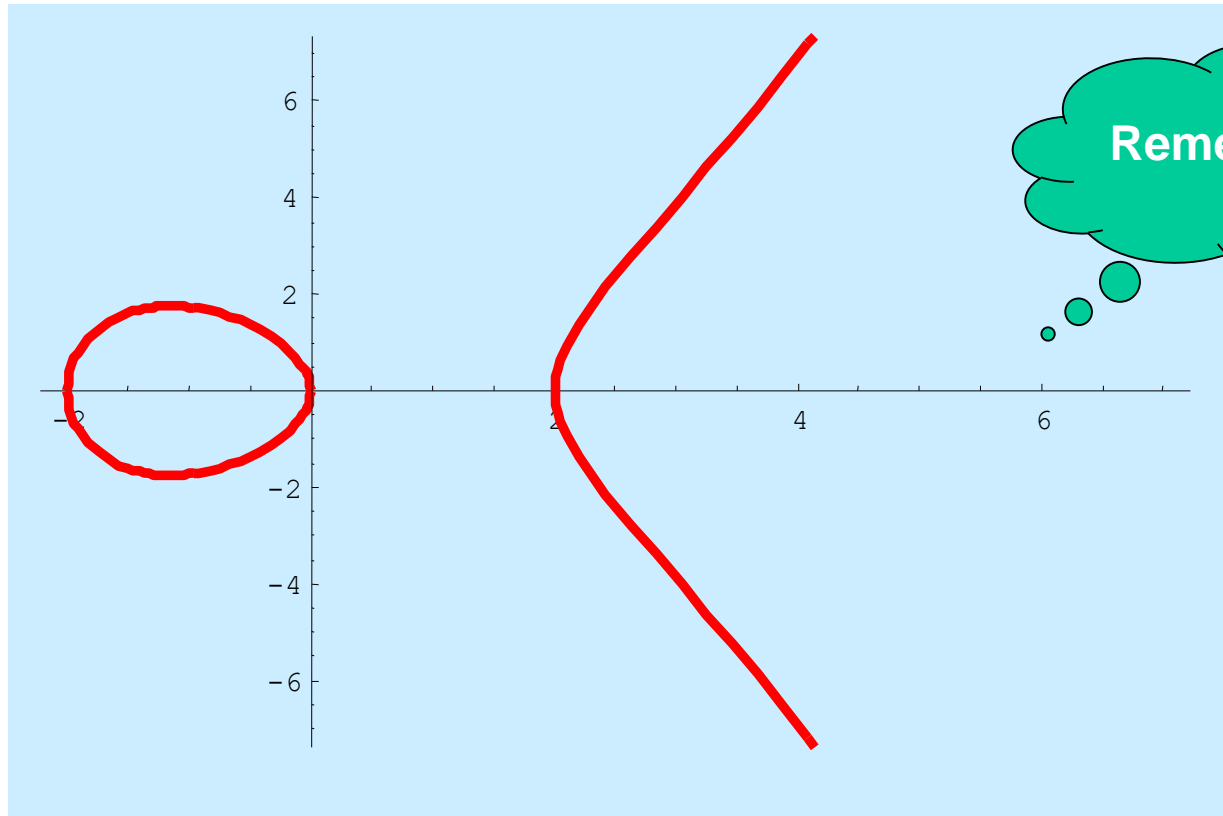
Elliptic curves

- Let $p > 3$ be a prime. An elliptic curve $y^2 = x^3 + ax + b$ over $\text{GF}(p) = \mathbb{Z}_p$ consist of all solutions $(x, y) \in \mathbb{Z}_p \times \mathbb{Z}_p$ to the equation

$$y^2 \equiv x^3 + ax + b \pmod{p}$$

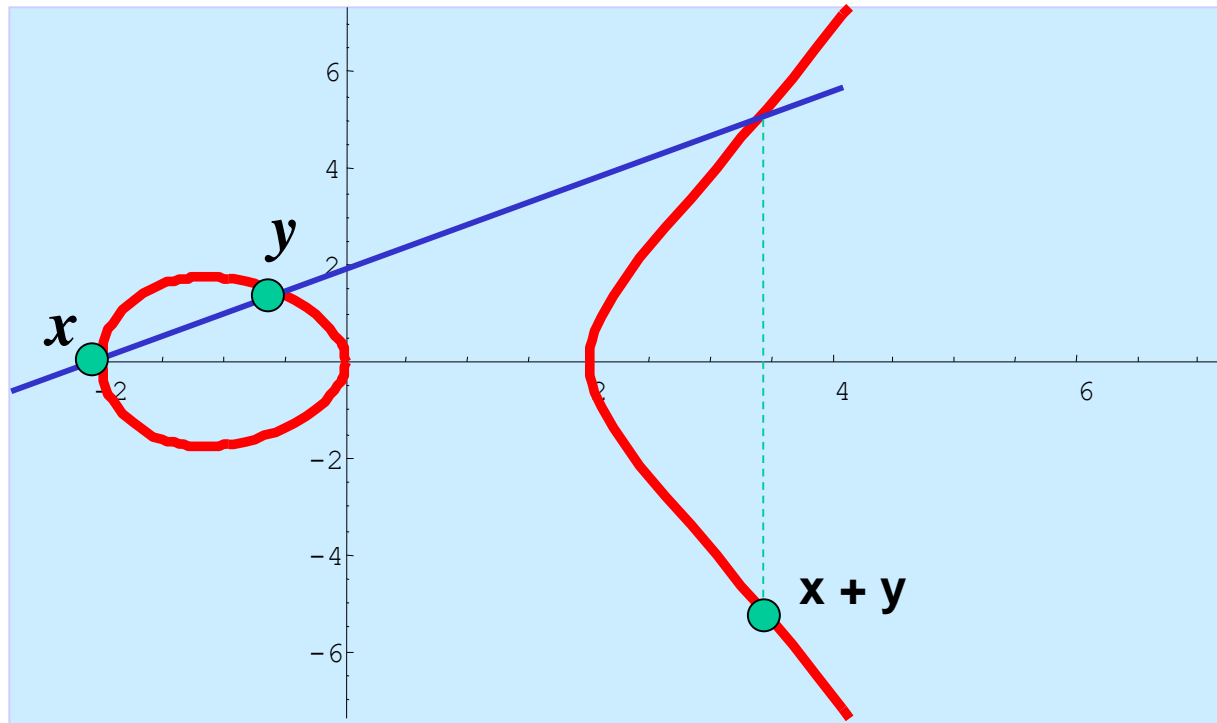
- where $a, b \in \mathbb{Z}_p$ are constants such that $4a^3 + 27b^2 \not\equiv 0 \pmod{p}$, together with a special point \mathcal{O} which is denoted as *the point at infinity*.

Elliptic curve over R



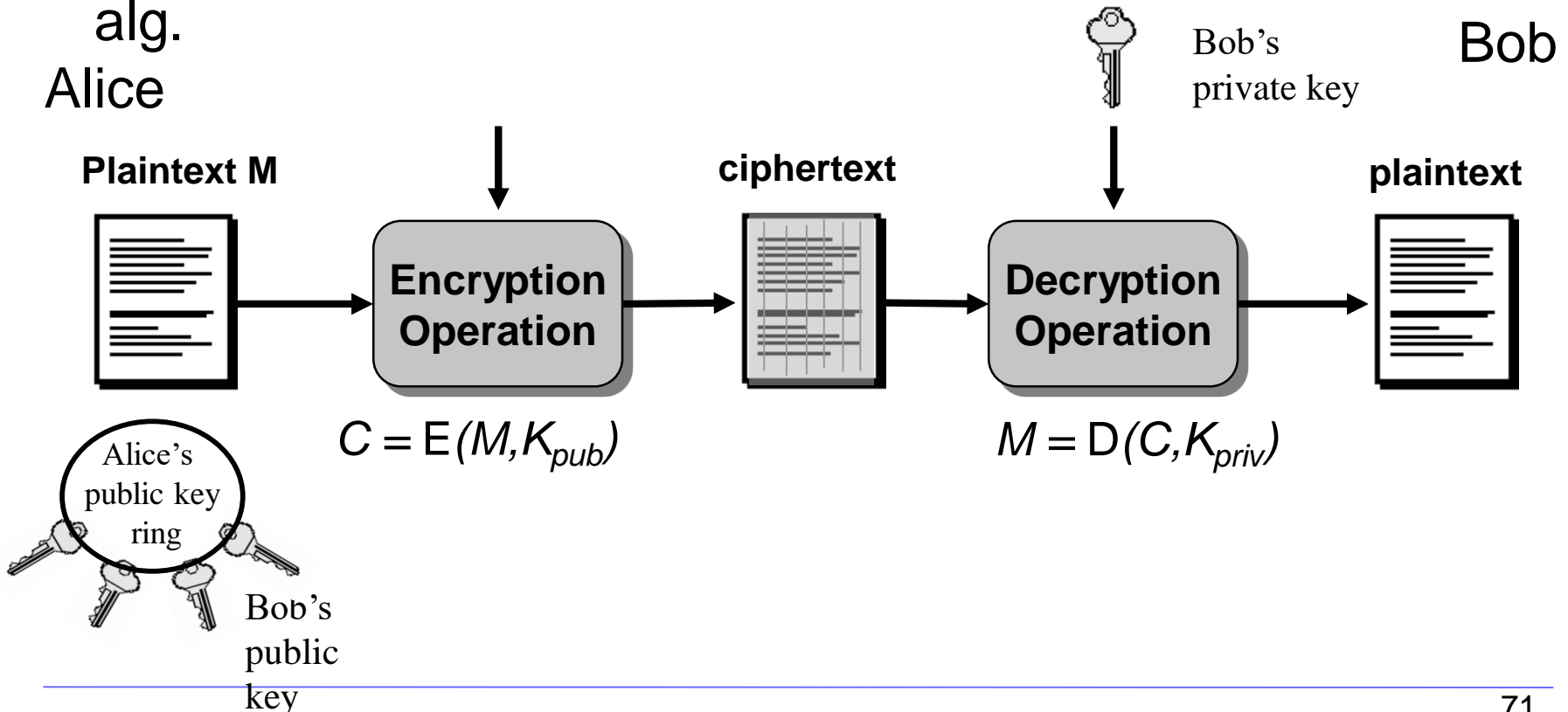
$$y^2 = x^3 - 4x$$

Point addition



Asymmetric Encryption: Basic encryption operation

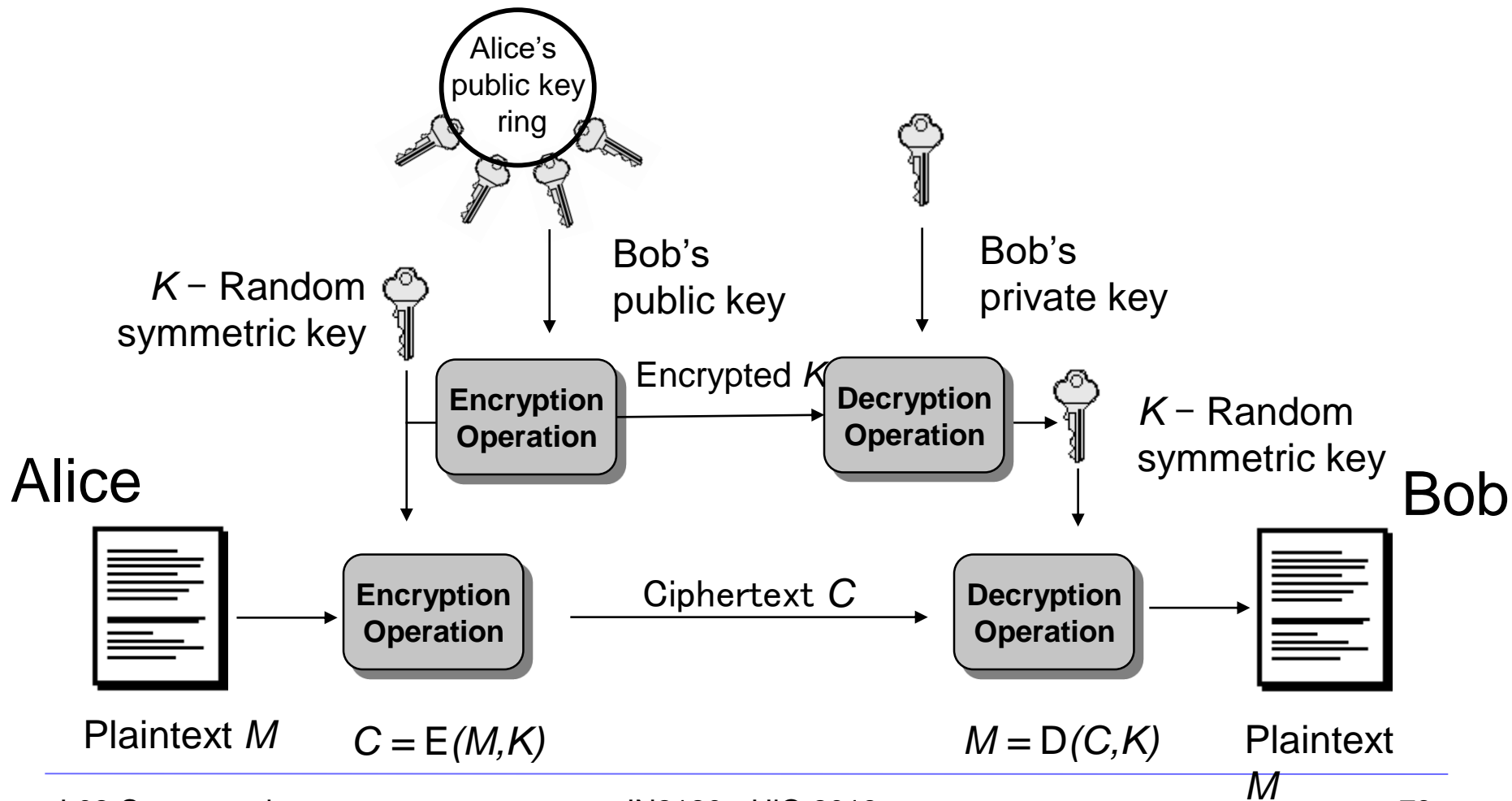
- In practice, large messages are not encrypted directly with asymmetric algorithms. Hybrid systems are used, where only symmetric session key is encrypted with asymmetric alg.



Hybrid Cryptosystems

- Symmetric ciphers are faster than asymmetric ciphers (because they are less computationally expensive), but ...
- Asymmetric ciphers simplify key distribution, therefore ...
- a combination of both symmetric and asymmetric ciphers can be used – a hybrid system:
 - The asymmetric cipher is used to distribute a randomly chosen symmetric key.
 - The symmetric cipher is used for encrypting bulk data.

Confidentiality Services: Hybrid Cryptosystems

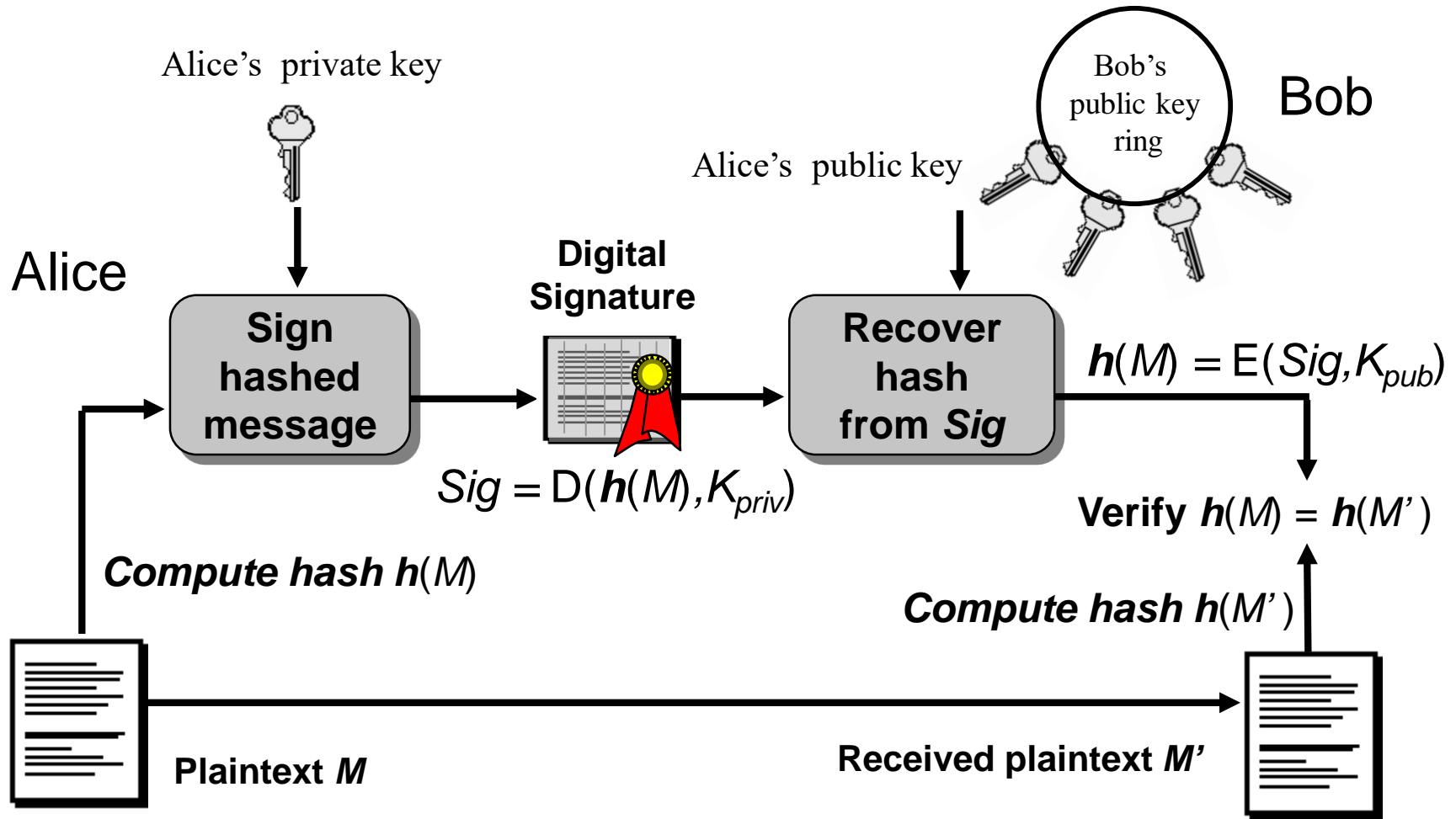


Digital Signatures

Digital Signature Mechanisms

- A MAC cannot be used as evidence that should be verified by a third party.
- Digital signatures used for non-repudiation, data origin authentication and data integrity services, and in some authentication exchange mechanisms.
- Digital signature mechanisms have three components:
 - key generation
 - signing procedure (private)
 - verification procedure (public)
- Algorithms
 - RSA
 - DSA and ECDSA

Practical digital signature based on hash value



Digital Signatures

- To get an authentication service that links a document to A 's name (identity) and not just a verification key, we require a procedure for B to get an authentic copy of A 's public key.
- Only then do we have a service that proves the authenticity of documents 'signed by A '.
- This can be provided by a PKI (Public Key Infrastructure)
- Yet even such a service does not provide **non-repudiation** at the level of persons.

Difference between MACs & Dig. Sig.



- MACs and digital signatures are both authentication mechanisms.
- MAC: the verifier needs the secret that was used to compute the MAC; thus a MAC is unsuitable as evidence with a third party.
 - The third party does not have the secret.
 - The third party cannot distinguish between the parties knowing the secret.



- Digital signatures can be validated by third parties, and can in theory thereby support both non-repudiation and authentication.

Key length comparison:

Symmetric and Asymmetric ciphers offering comparable security

AES Key Size	RSA Key Size	Elliptic curve Key Size
-	1024	163
128	3072	256
192	7680	384
256	15360	512

Another look at key lengths

Table 1. Intuitive security levels.

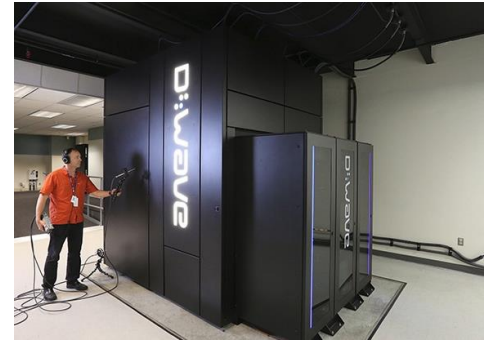
security level	volume of water to bring to a boil	bit-lengths		
		symmetric key	cryptographic hash	RSA modulus
teaspoon security	0.0025 liter	35	70	242
shower security	80 liter	50	100	453
pool security	2 500 000 liter	65	130	745
rain security	0.082 km ³	80	160	1130
lake security	89 km ³	90	180	1440
sea security	3 750 000 km ³	105	210	1990
global security	1 400 000 000 km ³	114	228	2380
solar security	-	140	280	3730



The eavesdropper strikes back!

MIT
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Computing

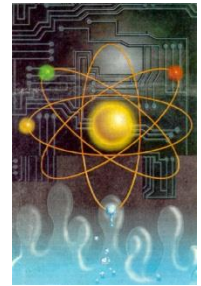
NSA Says It “Must Act Now” Against the Quantum Computing Threat

The National Security Agency is worried that quantum computers will neutralize our best encryption – but doesn't yet know what to do about that problem.

by Tom Simonite February 3, 2016



Quantum Computers

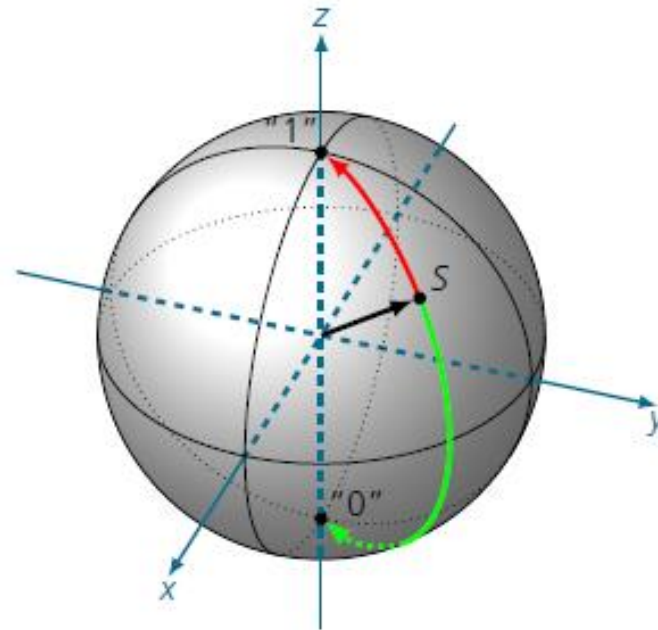


- Proposed by Richard Feynman 1982
- Boosted by P. Schor's algorithm for integer factorization and discrete logarithm in quantum polynomial time
- Operates on qubit – superposition of 0 and 1
- IBM built a 7-bit quantum computer and could find the factors of the integer 15 using NMR techniques in 2001
- NMR does not scale
- Progress continues, but nobody knows if or when a large scale quantum computer ever can be constructed
- QC will kill current public key techniques, but does not mean an end to symmetric crypto

Classical bit vs. qubits

• 1

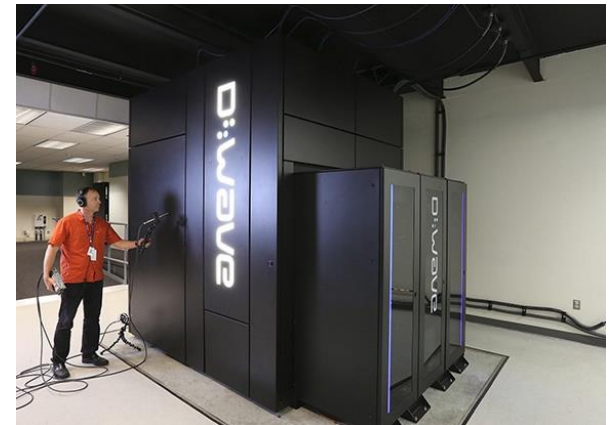
• 0



$$\Psi = \alpha |0\rangle + \beta |1\rangle, \text{ where } |\alpha|^2 + |\beta|^2 = 1$$

QC impact to cryptography

- When will a quantum computer be built?
 - 15 years, \$1 billion USD, nuclear power plant (PQCrypto 2014, Matteo Mariani)
- Impact:
 - Public key crypto:
 - ~~RSA~~
 - ~~Elliptic Curve Cryptography (ECDSA)~~
 - ~~Finite Field Cryptography (DSA)~~
 - ~~Diffie-Hellman key exchange~~
 - Symmetric key crypto:
 - AES Need larger keys
 - Triple DES Need larger keys
 - Hash functions:
 - SHA-1, SHA-2 and SHA-3 Use longer output



Current world record of QF!

Table 5: Quantum factorization records

Number	# of factors	# of qubits needed	Algorithm	Year implemented	Implemented without prior knowledge of solution
15	2	8	Shor	2001 [2]	×
	2	8	Shor	2007 [3]	×
	2	8	Shor	2007 [3]	×
	2	8	Shor	2009 [5]	×
	2	8	Shor	2012 [6]	×
21	2	10	Shor	2012 [7]	×
143	2	4	minimization	2012 [1]	✓
56153	2	4	minimization	2012 [1]	✓
291311	2	6	minimization	not yet	✓
175	3	3	minimization	not yet	✓

2017



Two variants of quantum safe crypto

Quantum cryptography:

- The use of **quantum mechanics** to guarantee secure communication.
- It enables two parties to **produce a shared random secret key** known only to them, which can then be used to encrypt and decrypt messages.

Quantum resistant cryptography:

- The use of cryptographic mechanisms based on computationally difficult **problems for which no efficient quantum computing algorithm is known**

QKD via satellite

nature International weekly journal of science

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NATURE | NEWS 🔗 📄


China's quantum satellite clears major hurdle on way to ultrasecure communications

Probe sends entangled photons — which could underpin quantum-based data encryption — over unprecedented distance.

Daive Castelvocchi

15 June 2017

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Jin Liwang/China via ZUMA Wire

A composite photo from December 2016 shows a link established between China's quantum satellite Micius and a ground station in the Tibet Autonomous Region.

Quantum Resistant Cryptography

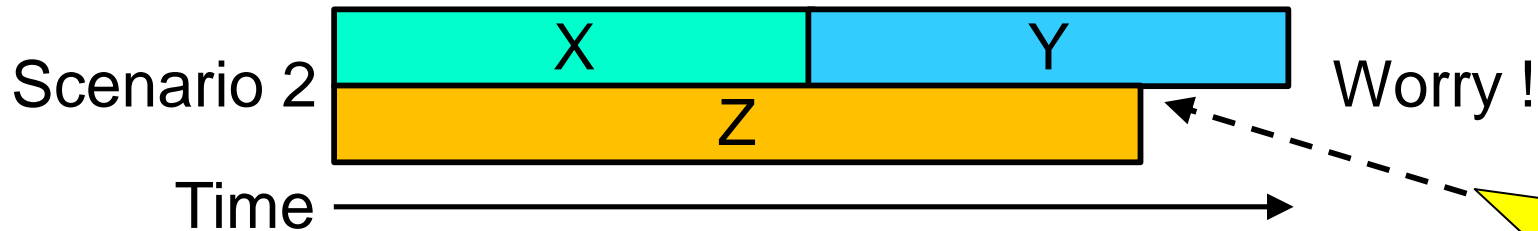
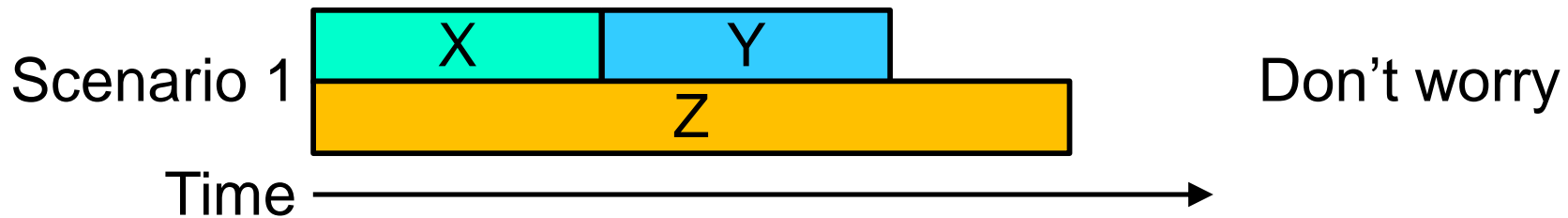
- **Code Based Asymmetric Algorithms**
- **Lattice Based Asymmetric Algorithms**
- Asymmetric Crypto based on Multivariate Polynomials
- Asymmetric Crypto based on Cryptographic Hash Functions
- Asymmetric Crypto based on Isogenies of (supersingular) elliptic curves

Should we worry about quantum computing?

X: Time it takes to develop post-quantum crypto

Y: Time period traditional crypto must remain secure

Z: Time it takes to develop practical quantum computers



If $X + Y > Z$ then worry



Recent news

[News room](#) > [News releases](#) >

IBM Announces Advances to IBM Quantum Systems & Ecosystem

-- Client systems with 20 qubits ready for use; next-generation IBM Q system in development with first working 50 qubit processor
-- IBM expands its open-source quantum software package QISKit; offers the world's most advanced ecosystem for quantum computing

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Yorktown Heights, N.Y. - 10 Nov 2017: IBM (NYSE: [IBM](#)) announced today two significant quantum processor upgrades for its [IBM Q](#) early-access commercial systems. These upgrades represent rapid advances in quantum hardware as IBM continues to drive progress across the entire quantum computing technology stack, with focus on systems, software, applications and enablement.

Recent news

KVANTEDATAMASKIN

Svenske forskere får nær en milliard kroner til å utvikle kvantedatamaskin



AV: HARALD BROMBACH | MASKINVARE | PUBLISERT: 15. NOV. 2017 - 12:00



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Med et budsjett på nærmere en milliard svenske kroner (omtrent 970 millioner NOK) skal professor Per Delsing ved Chalmers tekniska högskola i Göteborg lede et initiativ som har som mål å utvikle en virkelig kraftig kvantedatamaskin.



– Målet vårt er å ha en fungerende kvantedatamaskin med minst hundre qubit. En slik datamaskin har mye større regnekraft enn de beste superdatamaskinene i dag og kan bli brukt til for eksempel å løse optimaliseringsproblemer, avansert maskinlæring og tunge beregninger av egenskapene til molekyler, sier Delsing i en pressemelding.

Andre områder hvor kvanteteknologien er aktuell, er innen kryptering og design av medisiner.

Les også: [Intels nye brikke skal være et gjennombrudd innenfor kvantedatamaskiner](#)

ARTIKKELER FORTSETTER UNDER ANNONSER



Minst 100 qubit

En qubit er i denne sammenheng en elektrisk mikrobrikke som tar vare på kvantetilstanden til ett enkelt foton. Mens 100 vanlig bit vanligvis er en ganske ubetydelig datamengde i dagens tradisjonelle datamaskiner, kan man i kvantedatamaskiner prosessere enorme datamengder selv med relativt få qubit.

IBM kunngjorde [i forrige uke](#) at selskapet har fått en prosessor med 50 qubit til å fungere, så 100 qubit er ikke til å kimse av, selv om det svenske prosjektet skal pågå i et tiår.

I likhet med blant annet IBM, skal den svenske forskningsgruppen benytte superledende kretser. Superledende qubit-er er noe forskere ved Chalmers har jobbet med i nærmere 20 år.

ANNONSE

Ledige IT-stillinger JOBB

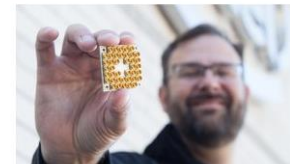
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IKT servicedesk
Drammen

NMBU - Norges miljø- og
Seksjonsjef Seksjon for
Brukerstøtte
As, Akershus

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Rådgiver IKT servicedesk
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LES OGSÅ



Intels nye brikke skal være et gjennombrudd innenfor kvantedatamaskiner



Brave new crypto world.....



End of lecture