



UiO : **Department of Informatics**
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Swarms and Developmental Systems



Overview

- Biological background
 - Genotype-to-phenotype mapping
- Artificial Developmental Systems
 - Chemistry based approaches (Morphogens)
 - Rewrite systems (L-System)
 - Neural networks (CPPN)
- Swarm Intelligence
 - Particle Swarm Optimization
 - Ant Colony Optimization
 - Reconfigurable Robots



Exercises

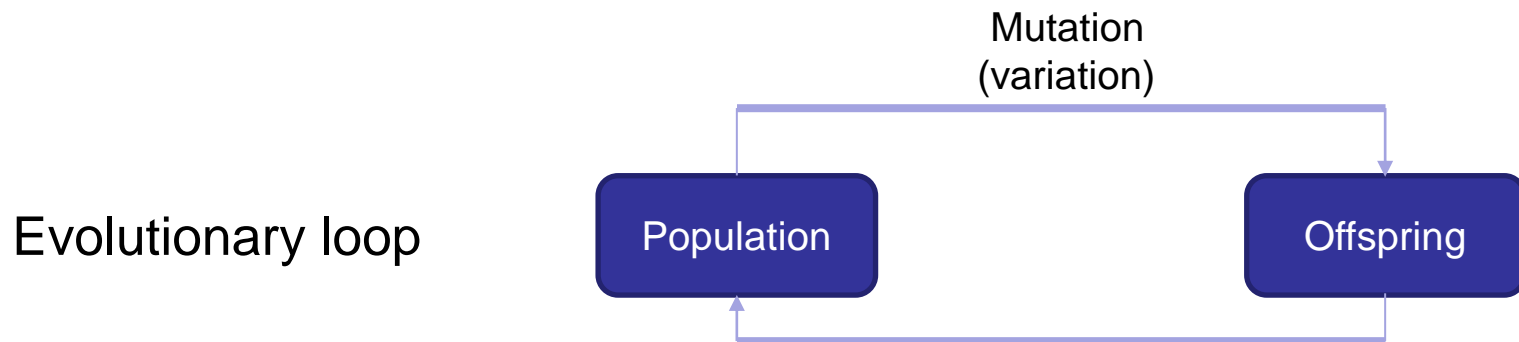
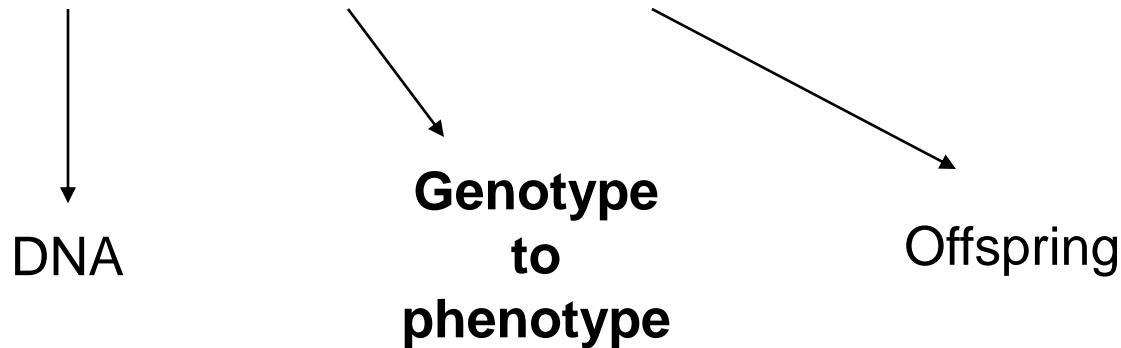
- Particle swarm optimization
- Reaction-diffusion model (Gray-scott algorithm)



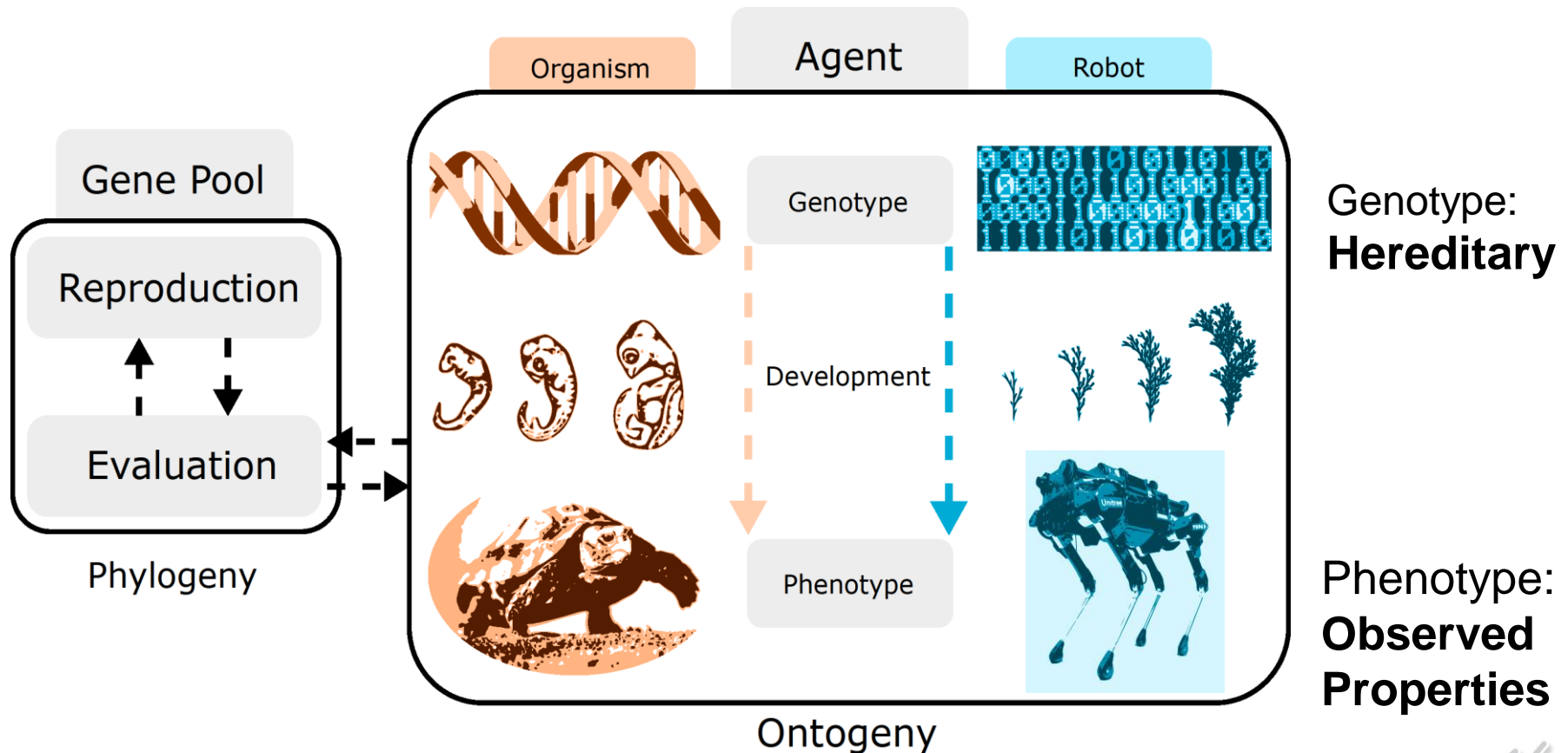
Analogize to optimize or analogize to understand

Evolution emerges through **reproduction**:

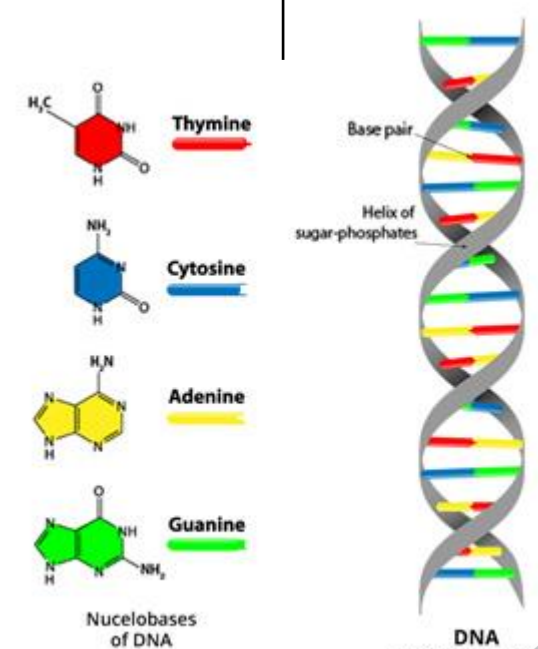
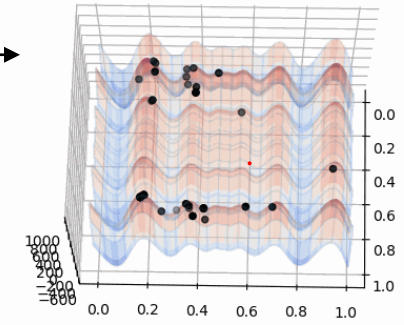
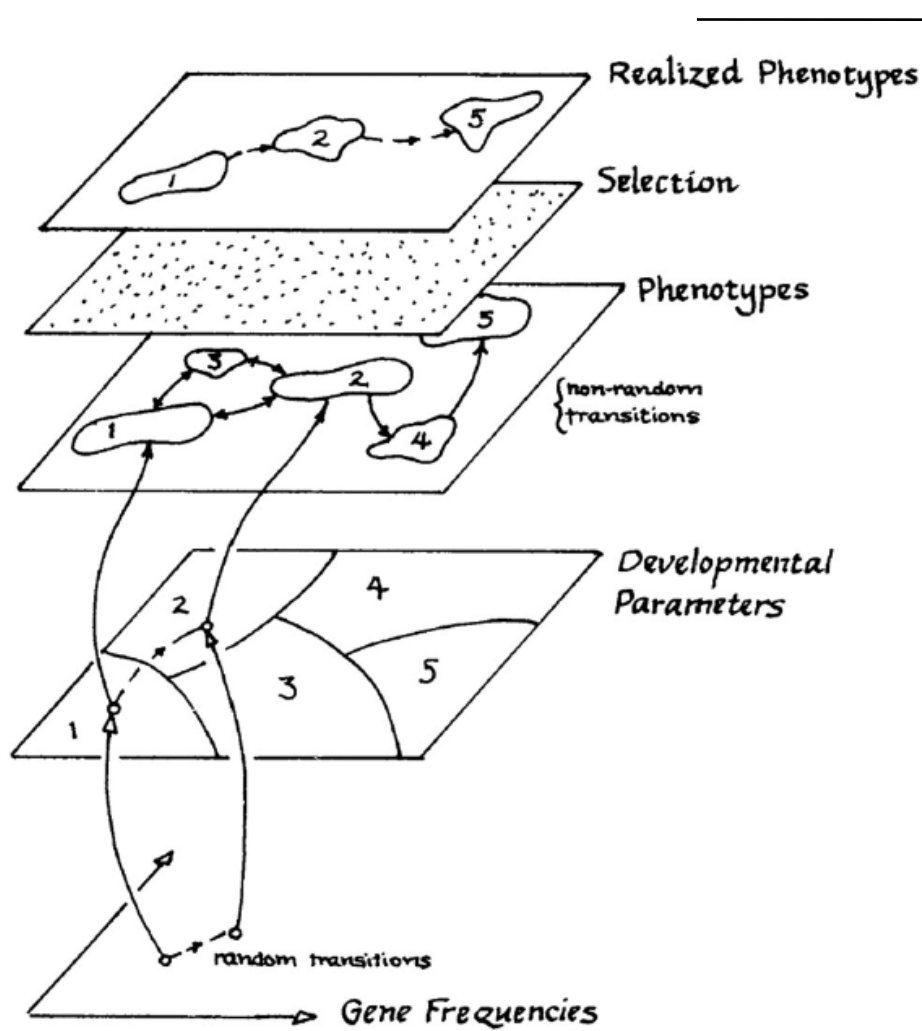
- Storage, processing and transfer of biological information



Genotype-to-phenotype mapping



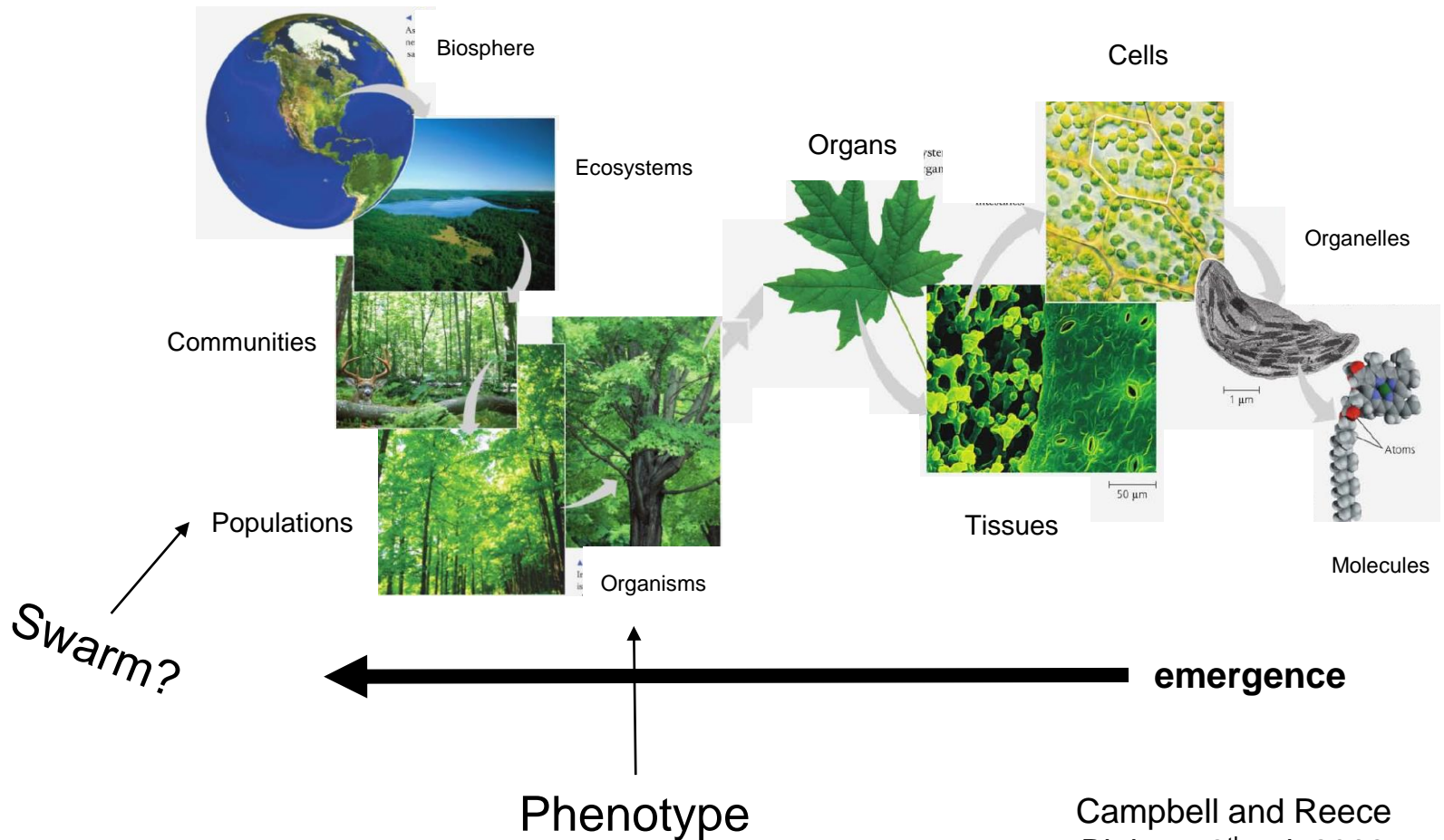
Fitness Landscape



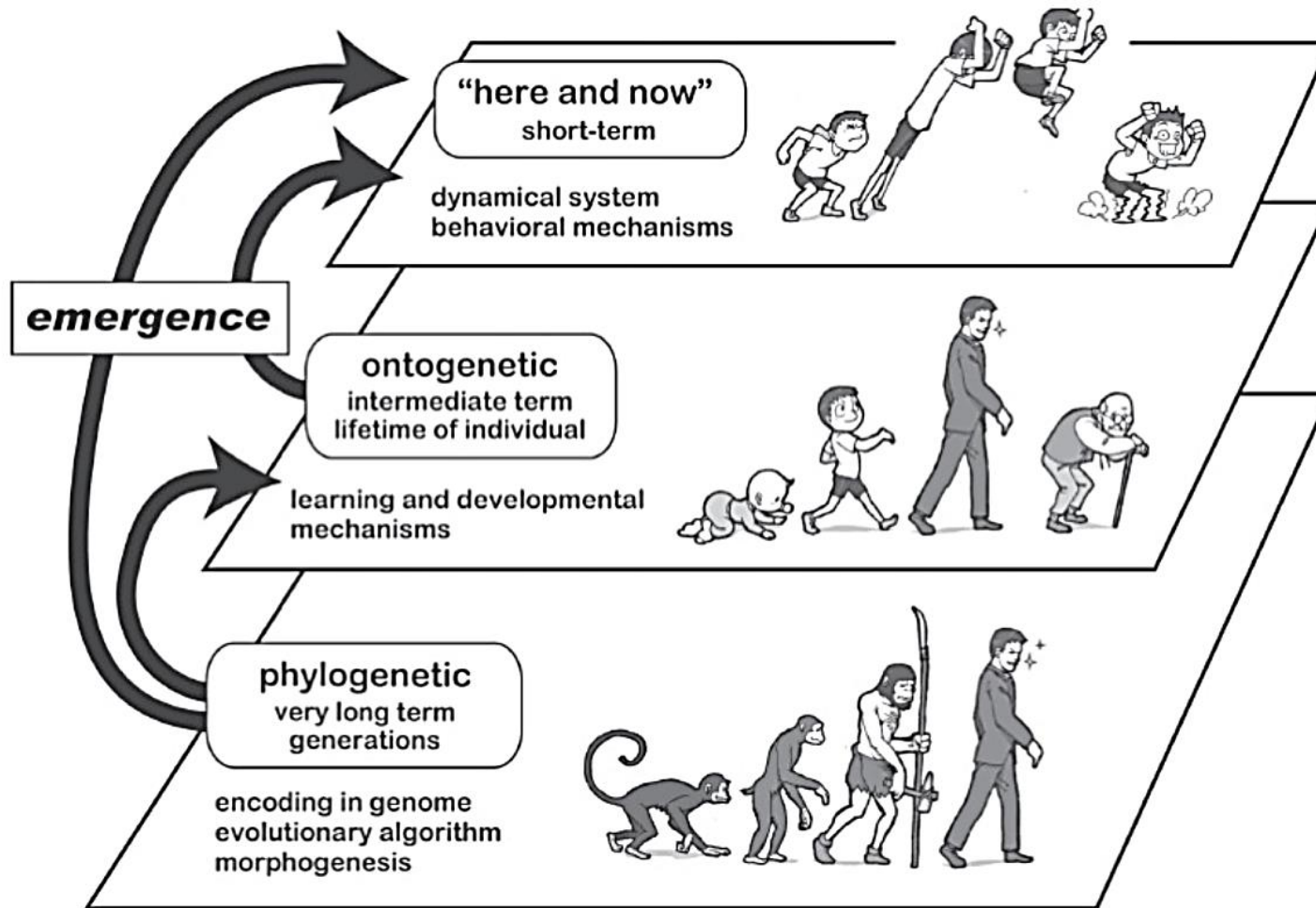
Oster, G. F., & Alberch, P. (1982). Evolution and bifurcation of developmental programs.



Biological Organization

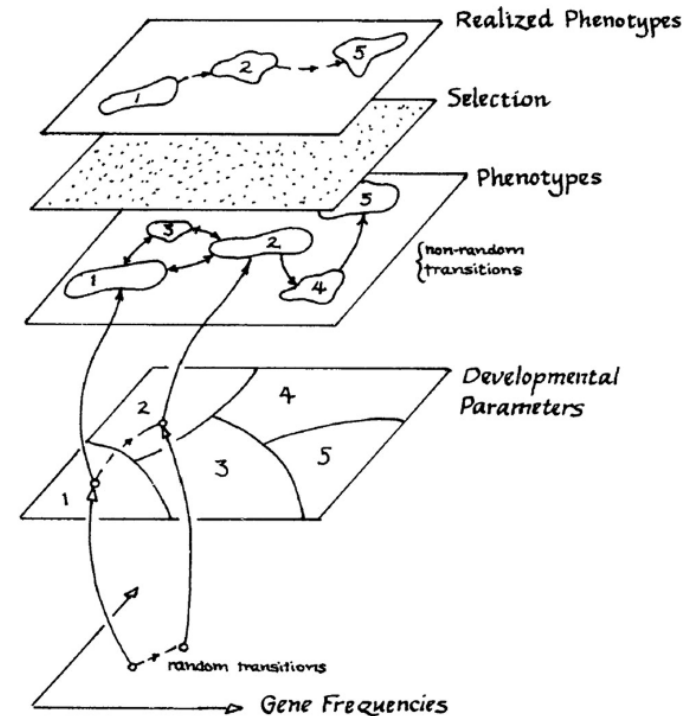


Time scales



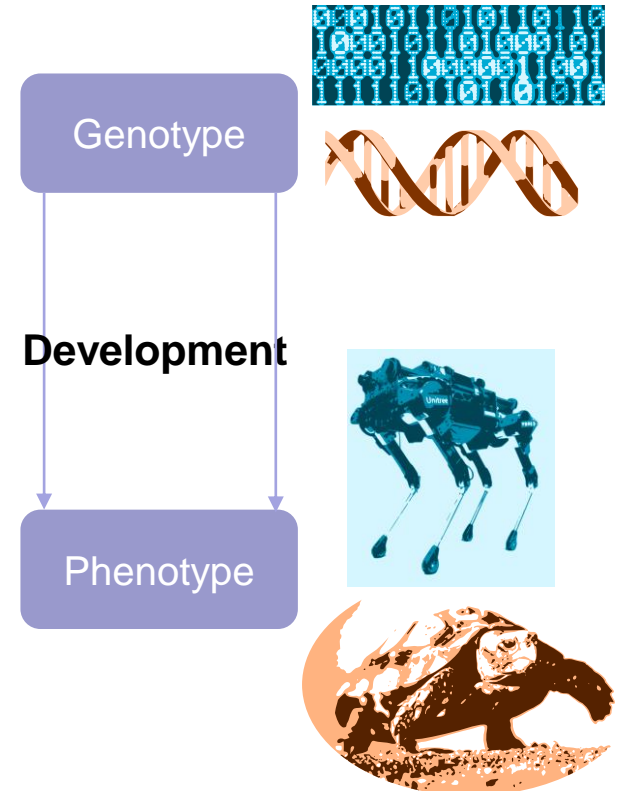
Developmental Systems and Swarms

- Developmental systems act on the genotype to phenotype mapping.
 - Ontogenetic time-scale:
 - In biology from a fertilized egg to a adult organism
- And extended genotype to phenotype map can define collective behaviors seen in swarms



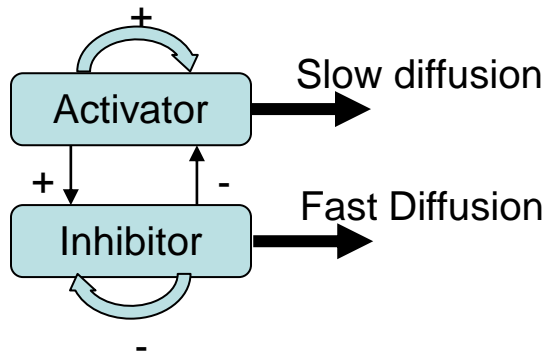
Developmental Systems

- Reuse of information
 - Compact storage
- Modularity
- Self-similarity
- Symmetry
- Scalability



Morphogens

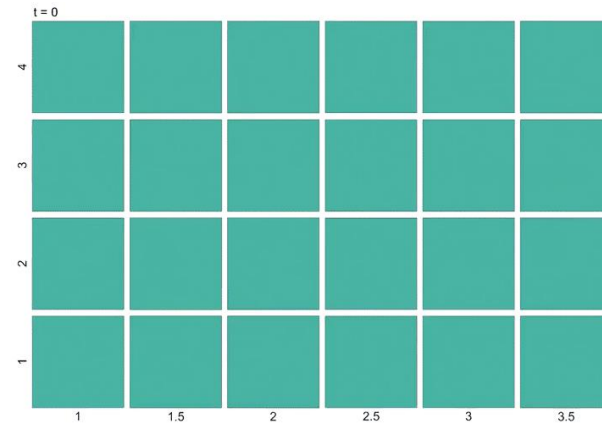
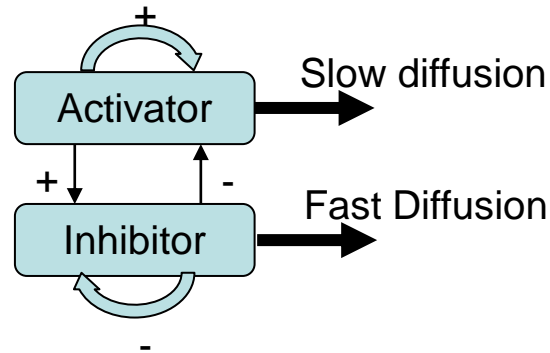
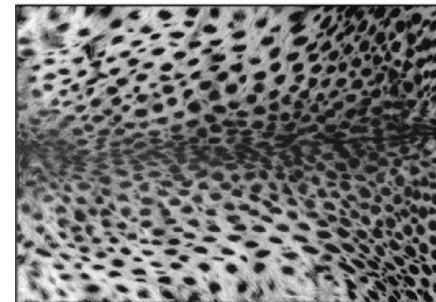
- Morphogenesis:
 - The development of morphological characteristics
- Reaction-diffusion models through self-inhibition



Alan Turing (1952) The Chemical Basis of Morphogenesis

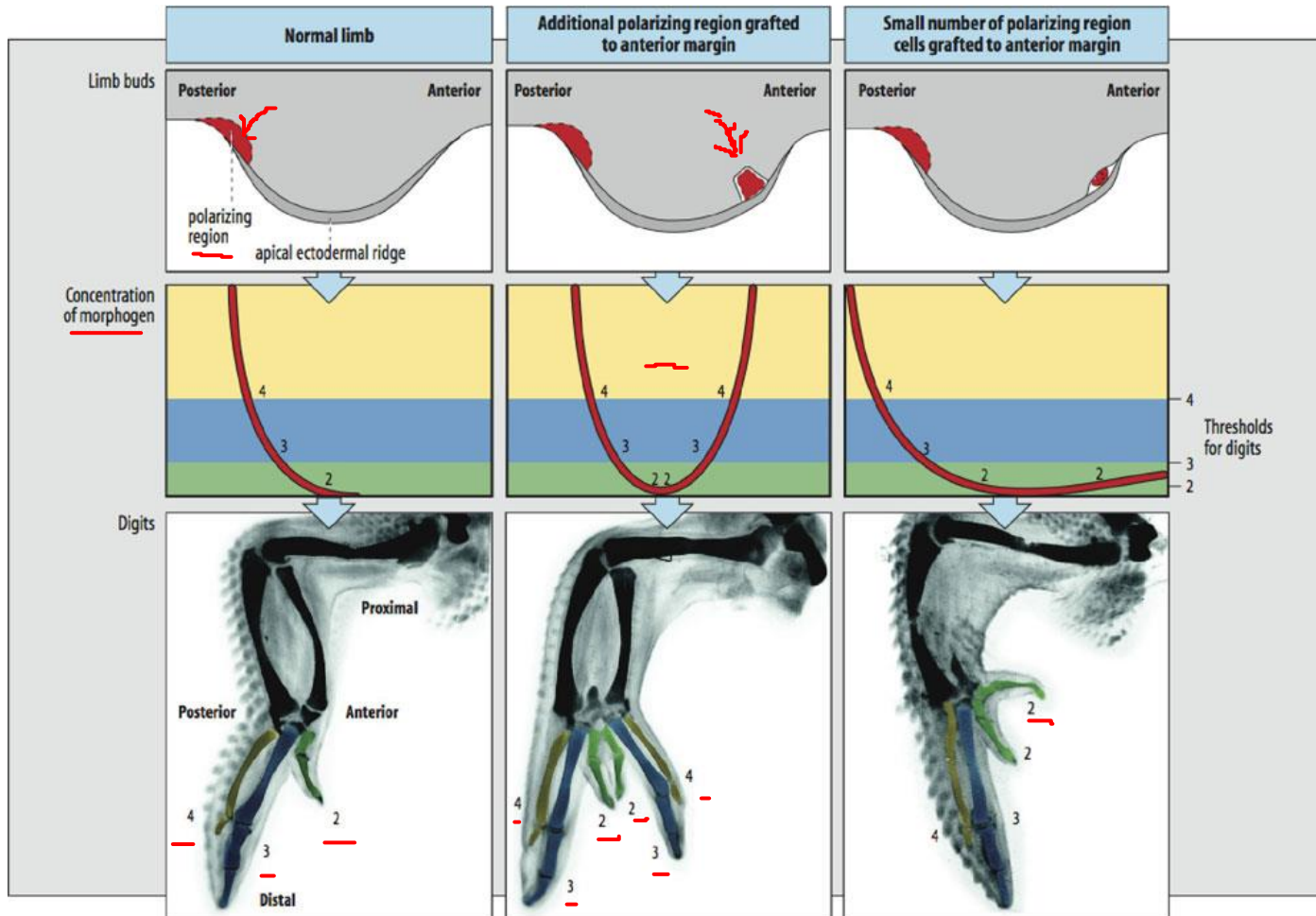
Morphogens

- Reaction-diffusion models through self-inhibition

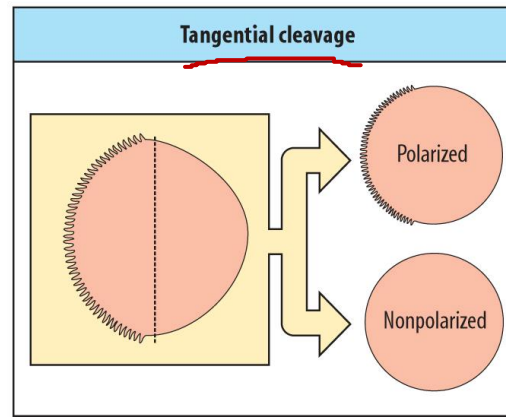
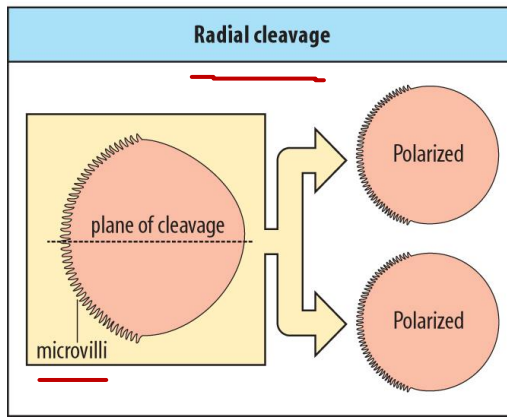
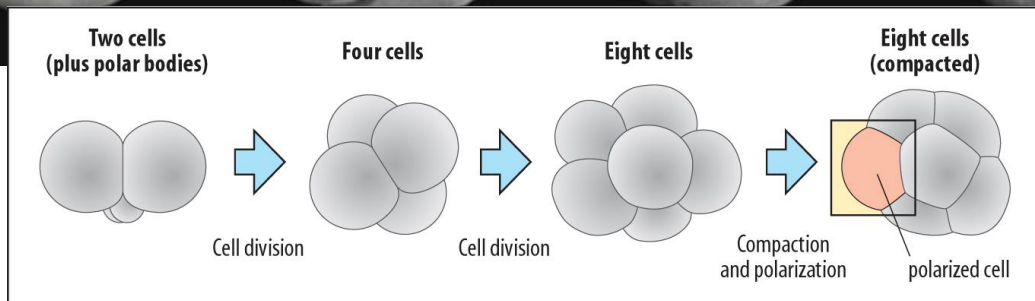
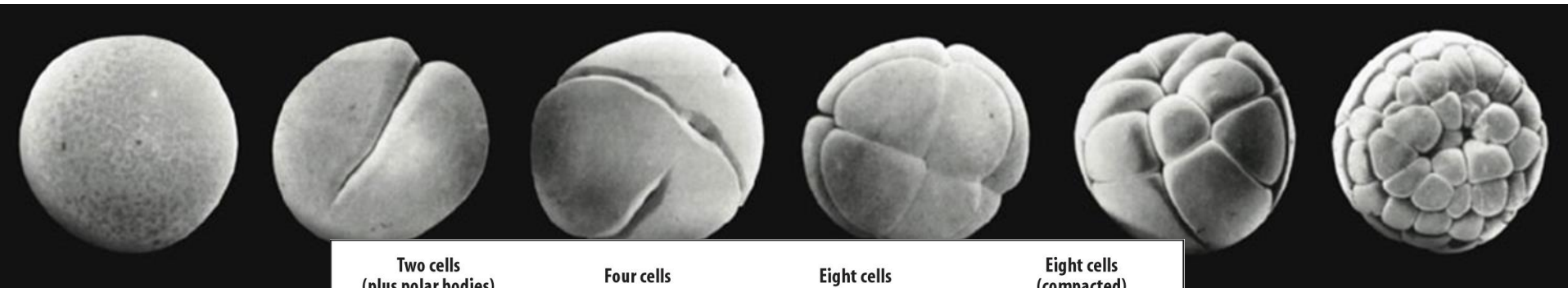


<https://www.youtube.com/watch?v=MR79V9UmM6s>

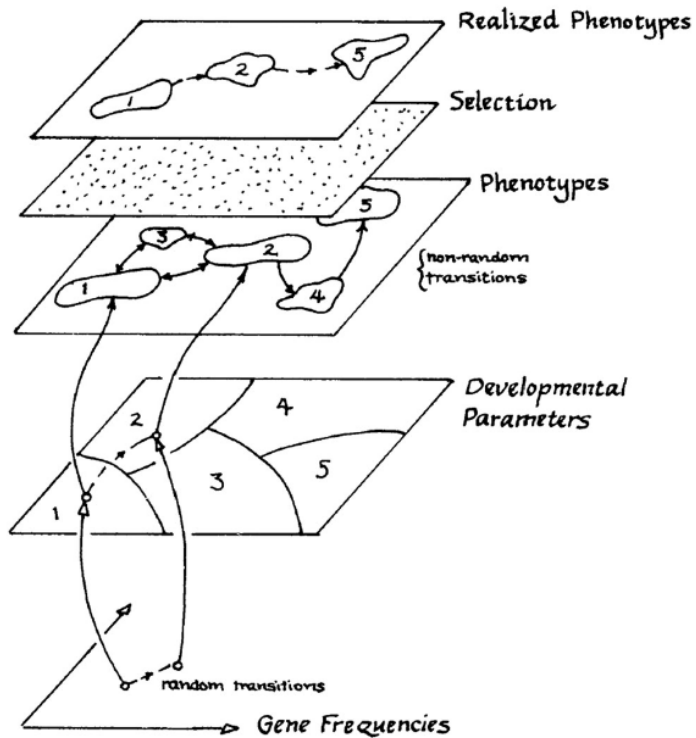
Morphogens



Embryogenesis



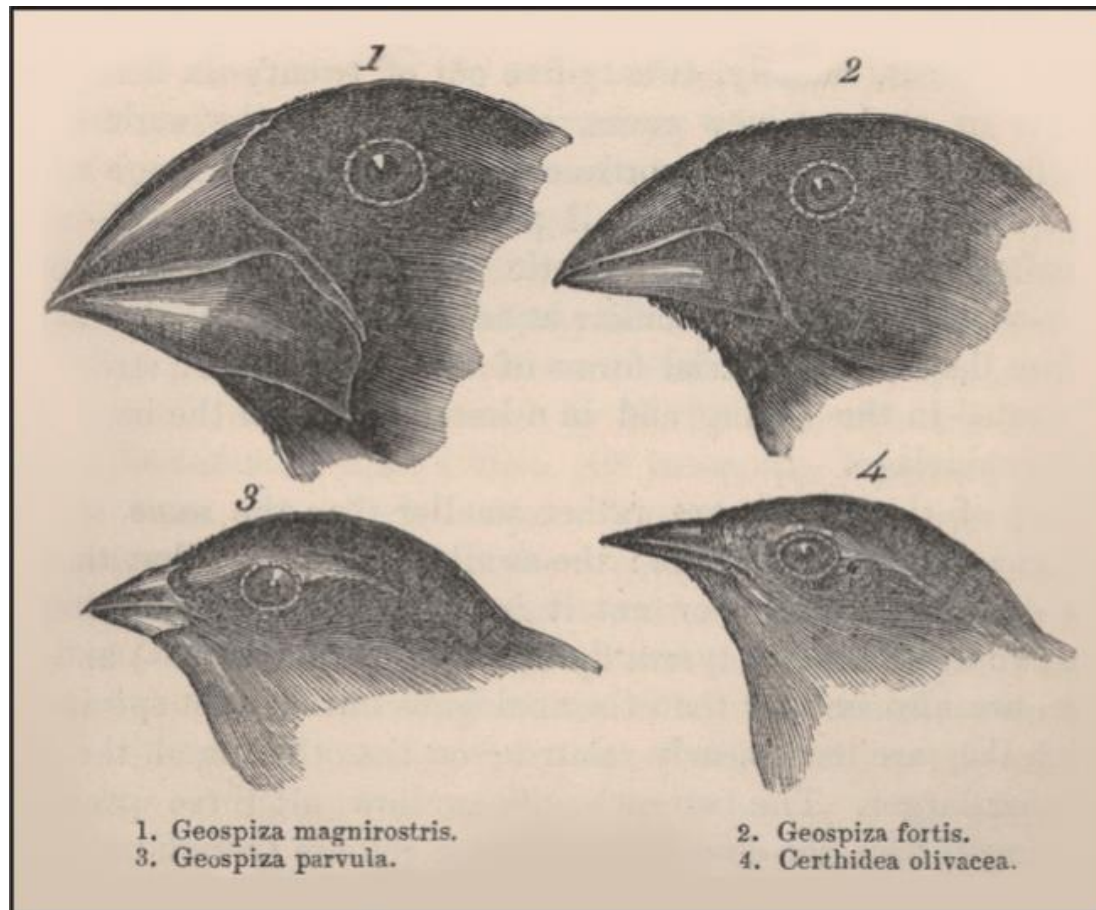
Heterochrony



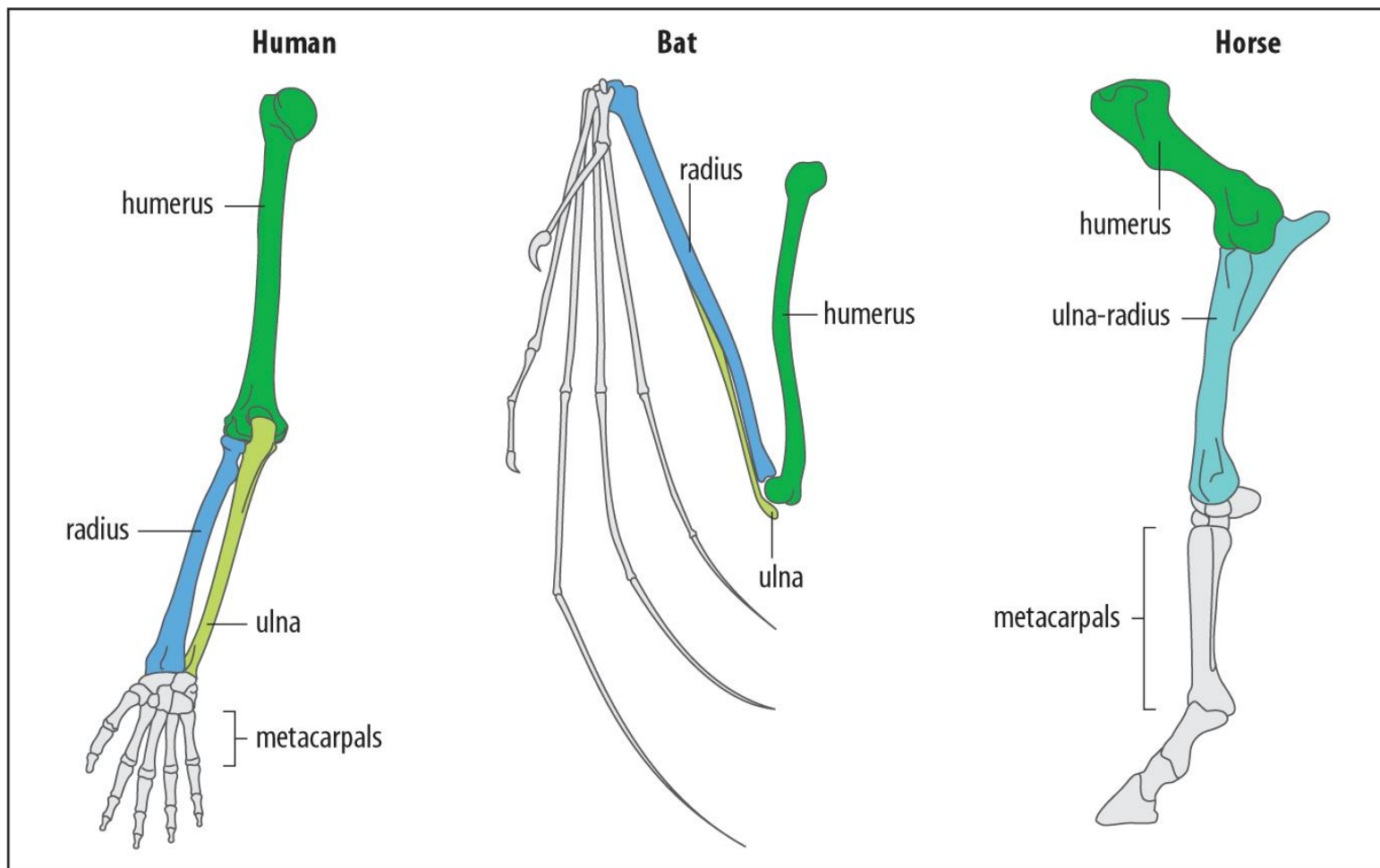
Heterochrony:
Developmental change in
timing or rate of events



Evolution of Heterochrony

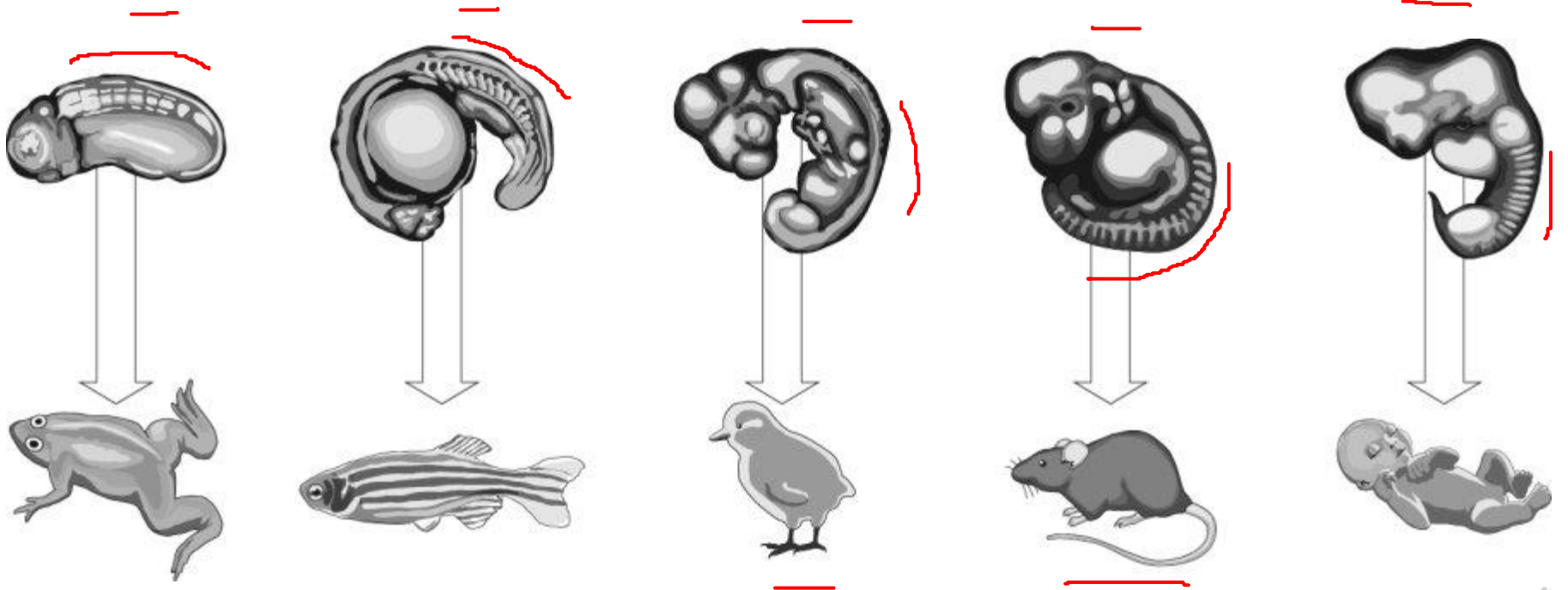


Homologous Evolution



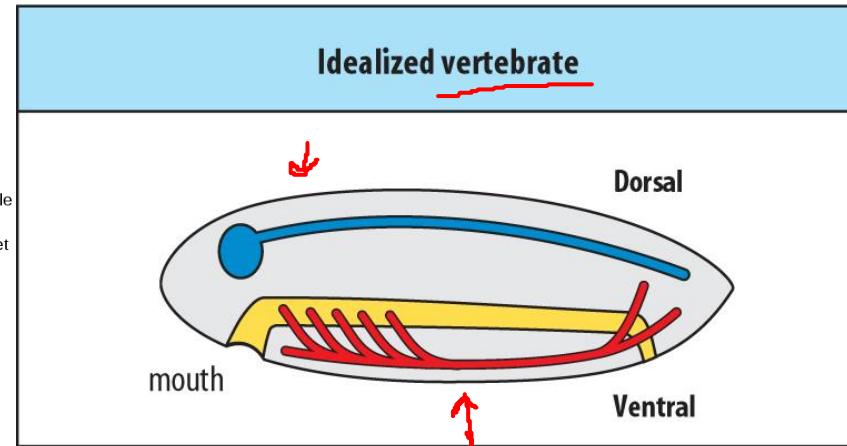
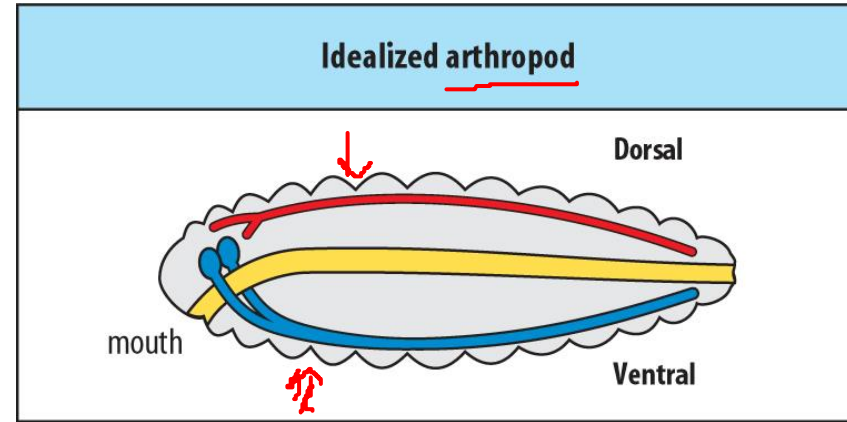
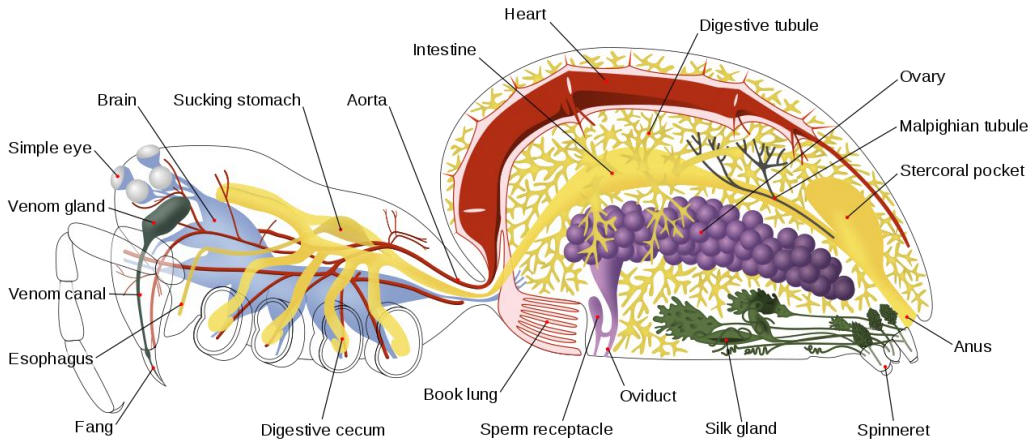
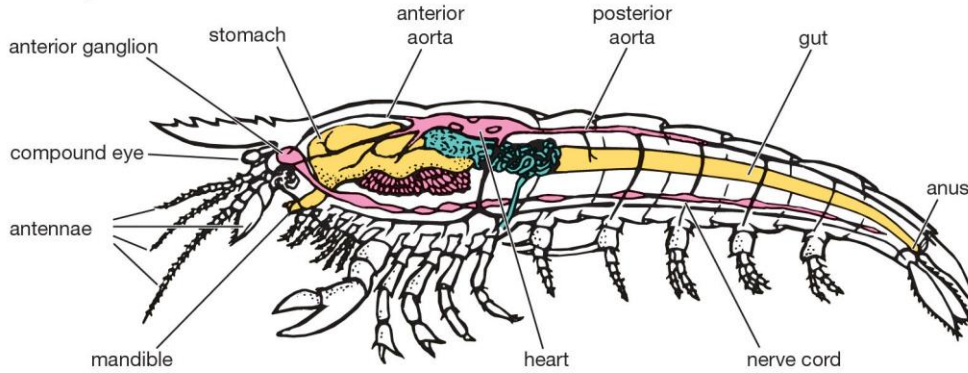
Conserved Developmental plans

- Phylotypic Stage



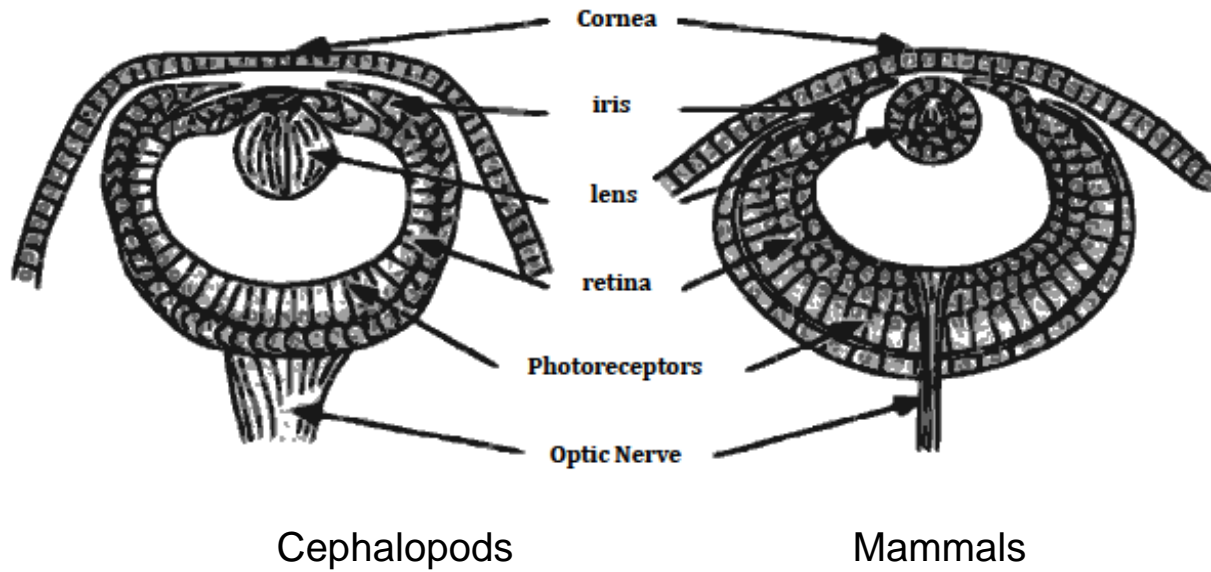
Body organization

Anatomy of a crustacean

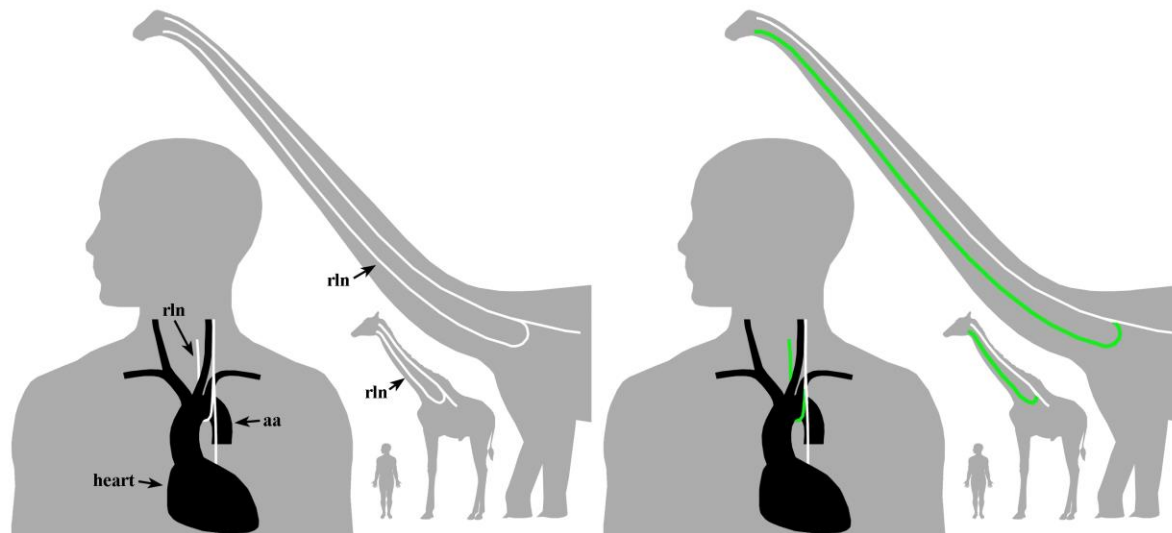


■ nerve cord ■ gut ■ circulatory system

Locked in Imperfection (1)

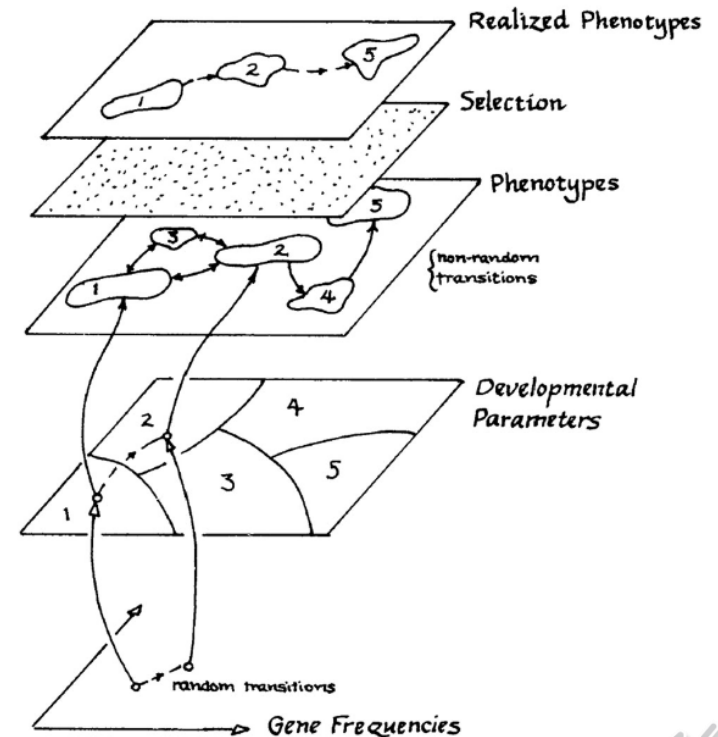


Locked in Imperfection (2)



Summary concepts on development

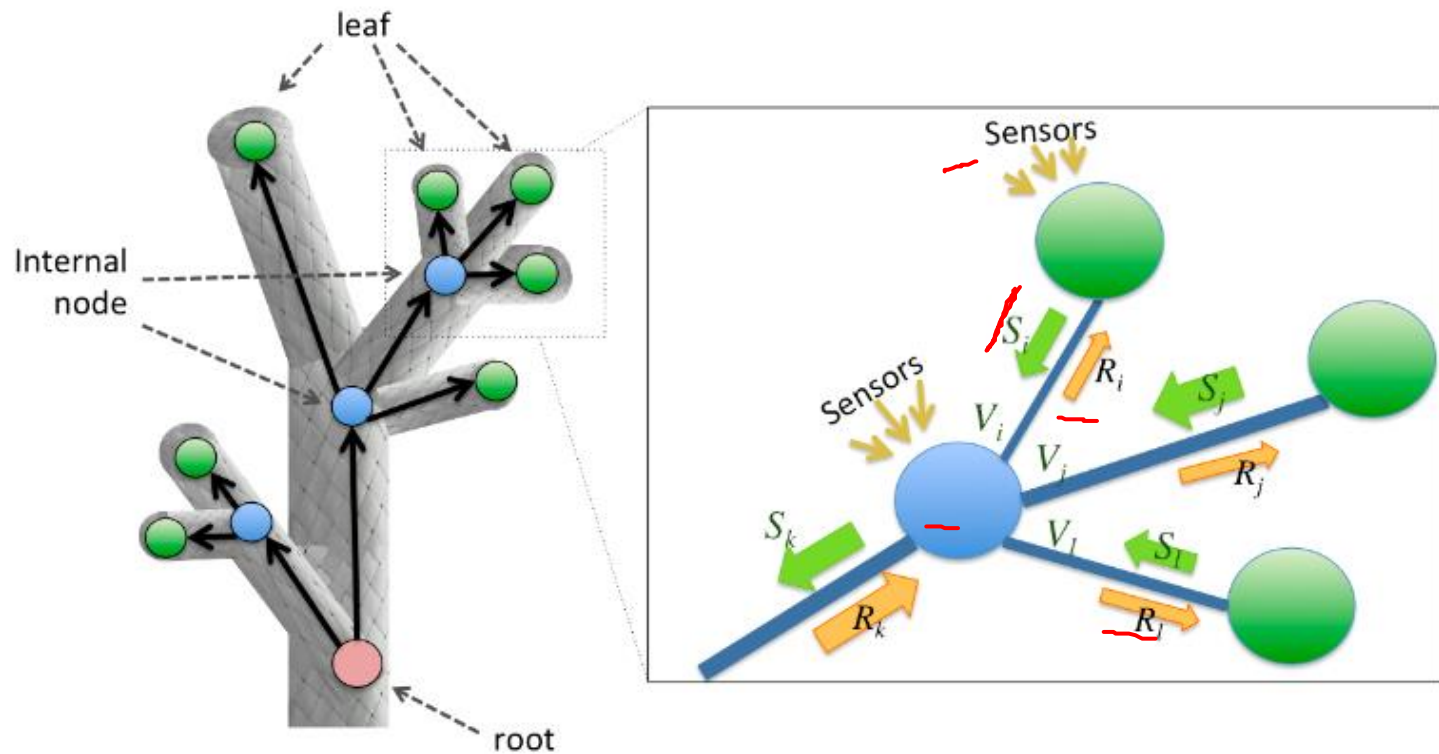
- Morphogens: chemicals that influence development
- Heterochrony: timed expression of morphogens
- Homologous evolution: Shared genetic ancestry



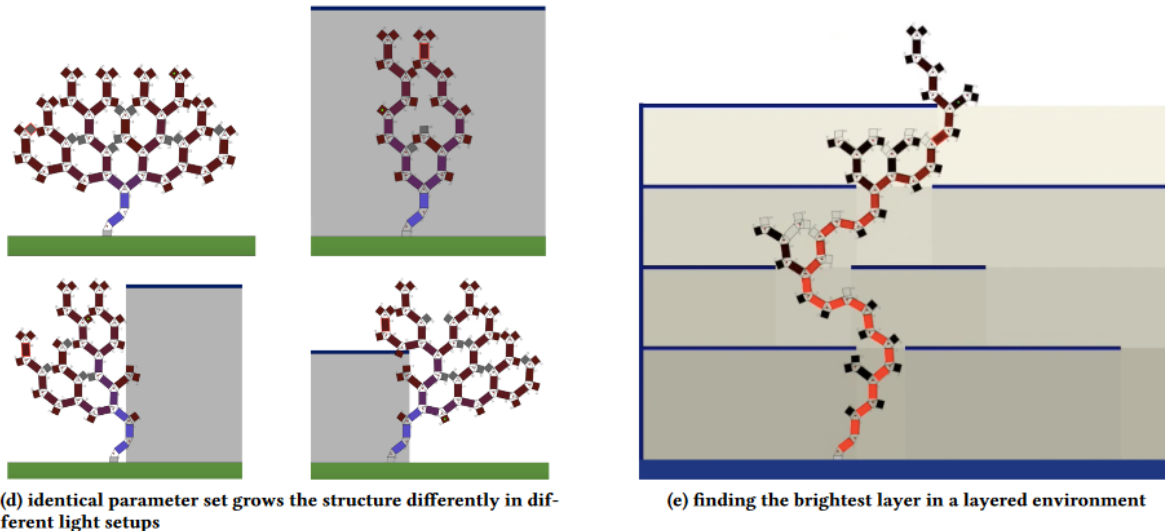
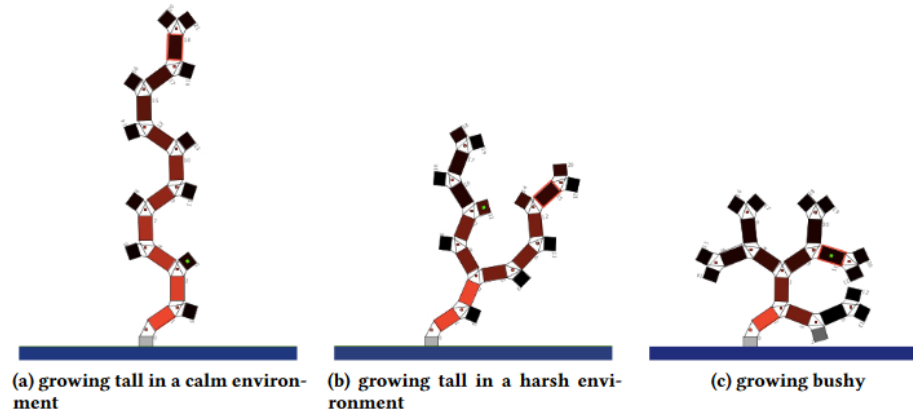
Chemistry inspired developmental systems

- Morphogens
- Reaction-diffusion: Exercise using *Gray-Scott algorithm*

Vascular Morphogenesis

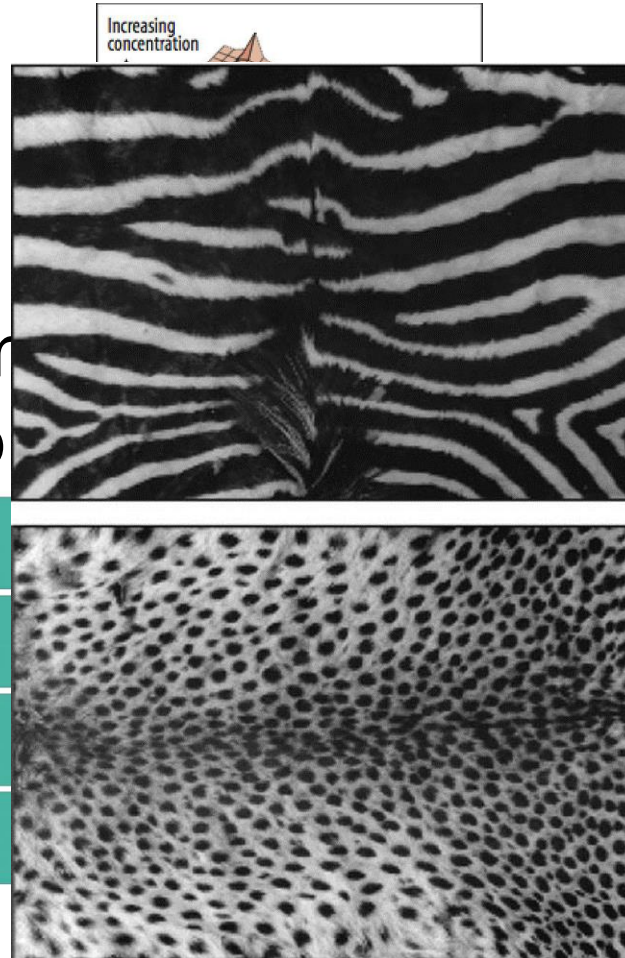
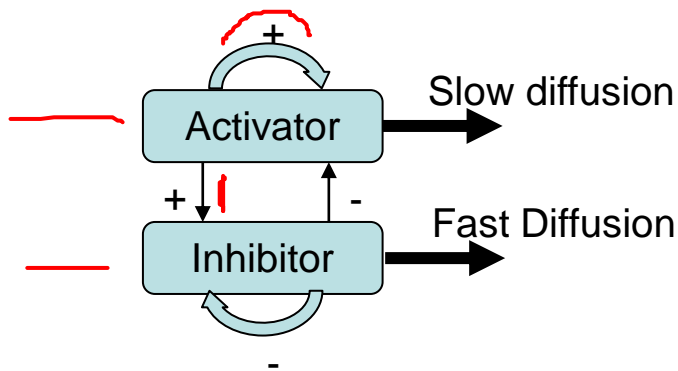


Morphogenesis through light sensing



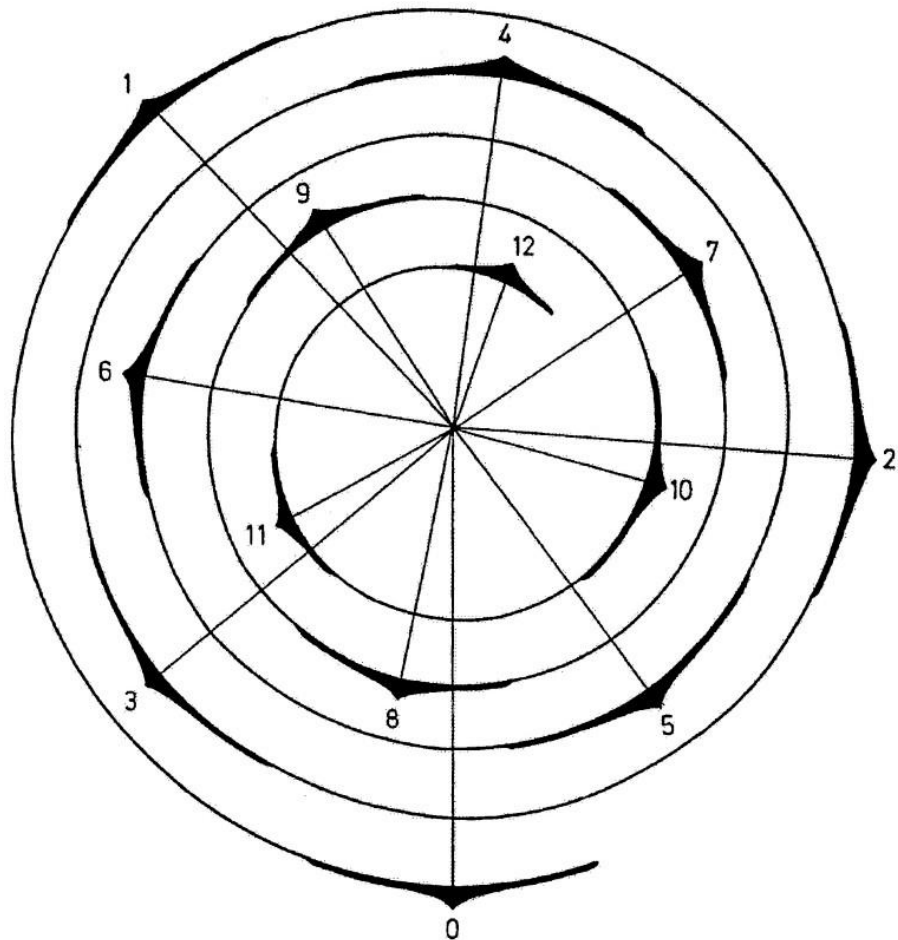
Morphogens

- Reaction-diffusion through self-inhibition

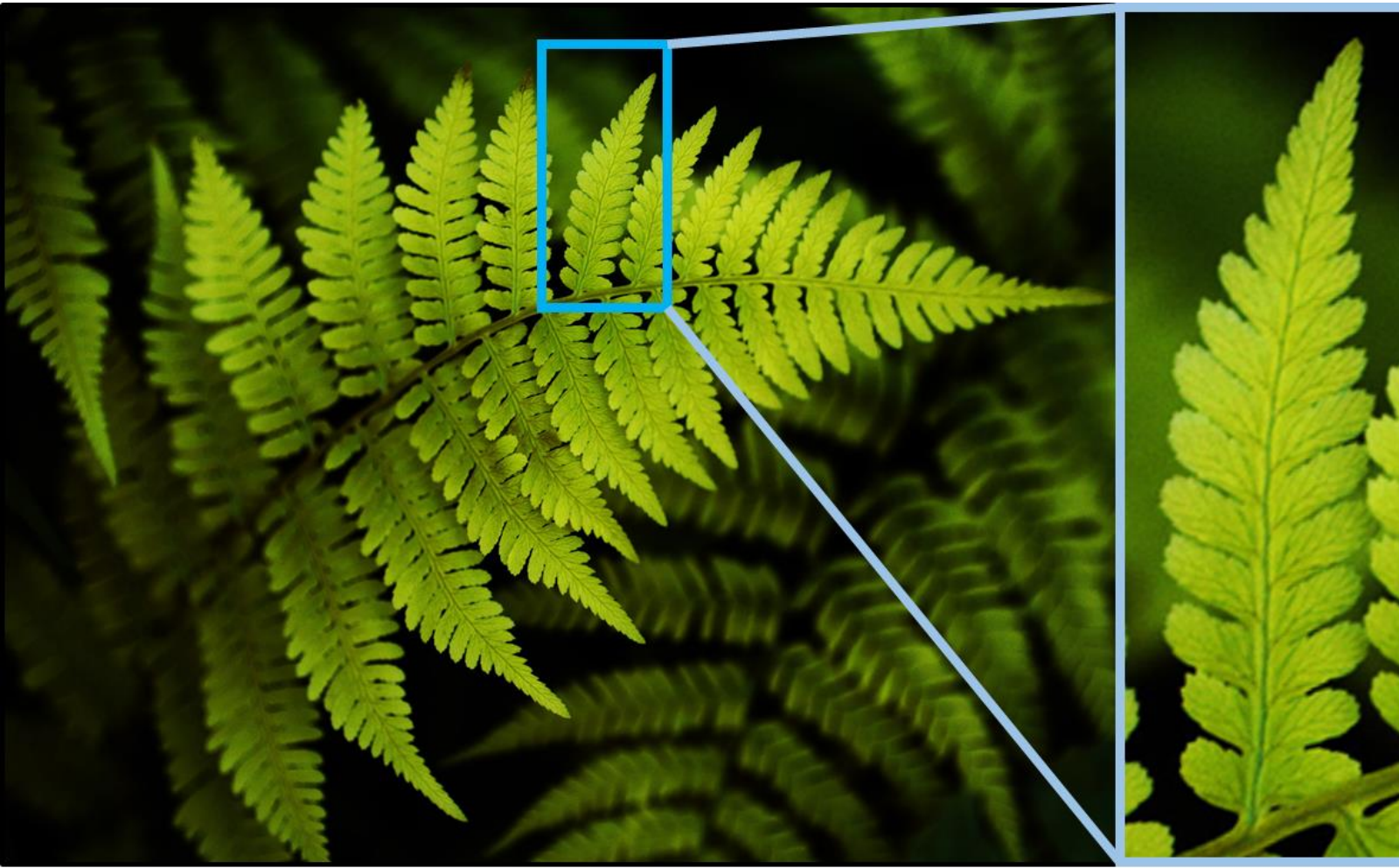


<https://www.youtube.com/watch?v=MR79V9UmM6s>

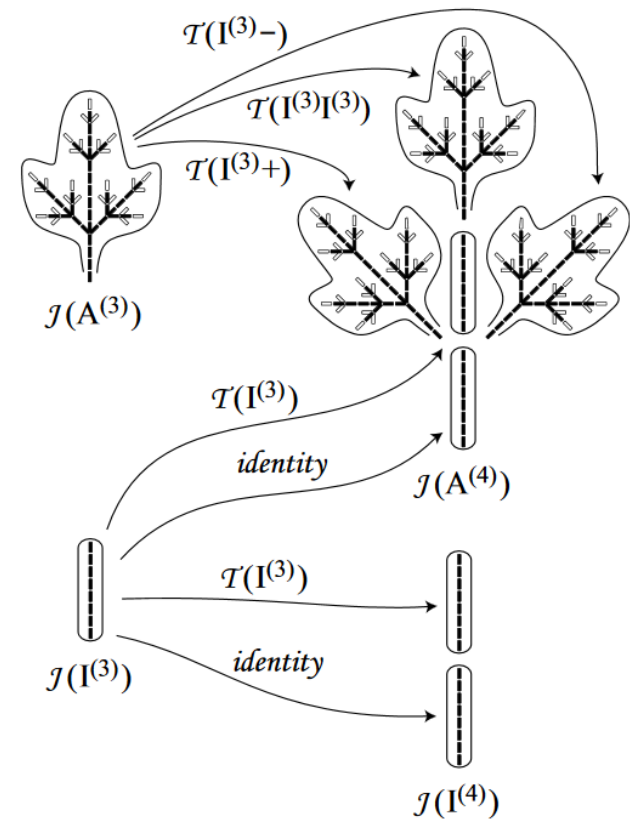
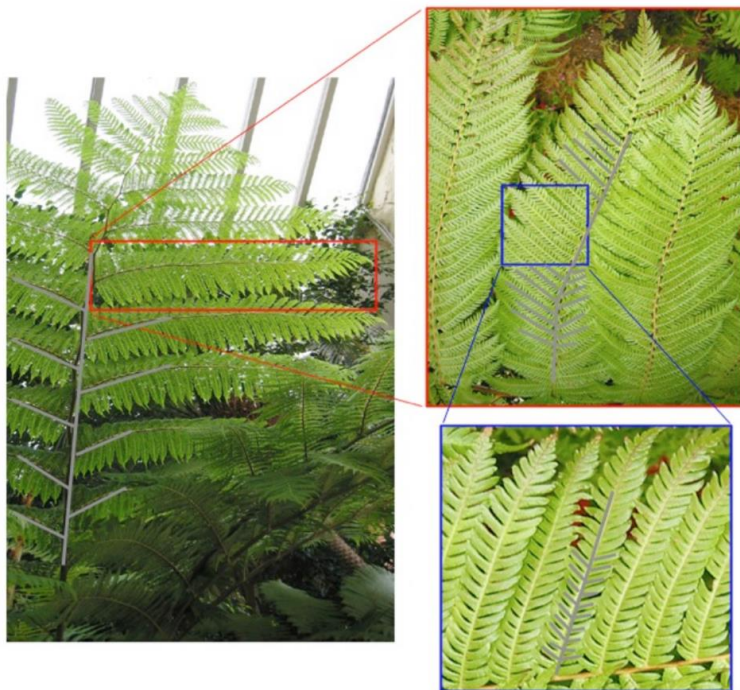
Leaf Phyllotaxis



Repetition, Self-Similarity and Modularity



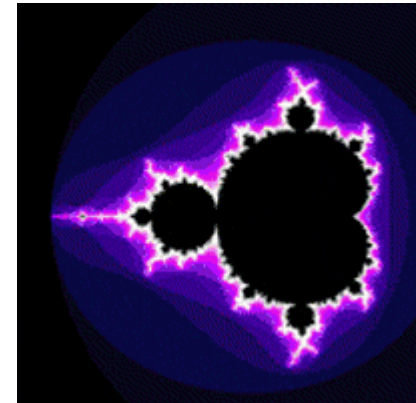
Repetition, Self-similarity and Modularity



Przemyslaw Prusinkiewicz, 2014, Self-Similarity In Plants: Integrating Mathematical And Biological Perspectives

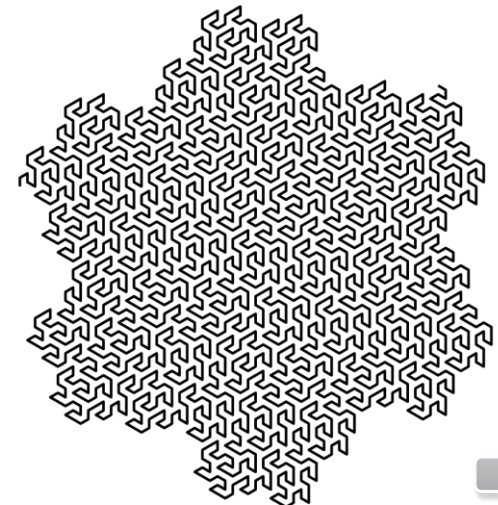
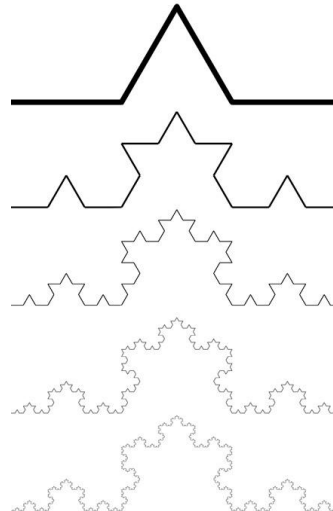
Fractals

- Mandelbrot set
 - $f(c)z = z^2 + c$
 - Behavior of 0 under iteration $f(c)$
 - c is a complex number



Rewriting systems:

- Koch-curve
- Flow-snake
 - (Gosper-curve)



Artificial Development

- Rewriting systems
 - L-System
- Chemistry based approaches
 - Turing patterns

- Rewriting Systems
 - Sequential (Formal Grammar)
 - Parallel (Lindenmayer-System)

$$A \rightarrow AB$$

$$B \rightarrow A$$

Simple rewrite	L-system
AB	AB
AA	ABA
ABAB	ABAAB
AAAA	ABAABABA
ABABABAB	ABAABABAABAAB



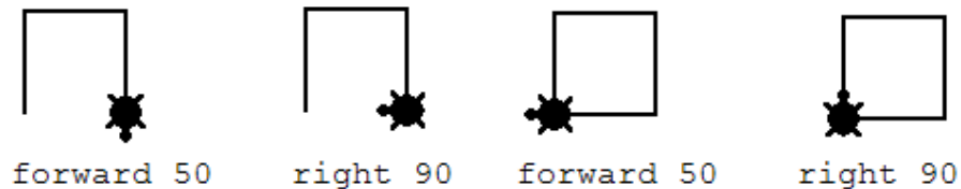
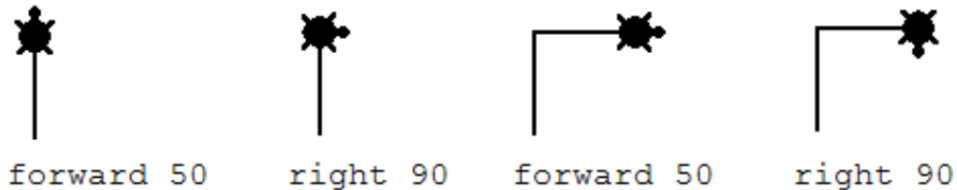
An example L-System

- Alphabet: $\{a,b\}$
- Production rules (grammar)
 - $a \rightarrow ab$
 - $b \rightarrow a$
- Axiom b
- Each symbol is replaced once each iteration



L-Systems for generating graphics: turtle graphics

- Read the string produced by the L-System from left to right changing the state of the turtle



Example L-system for Drawing

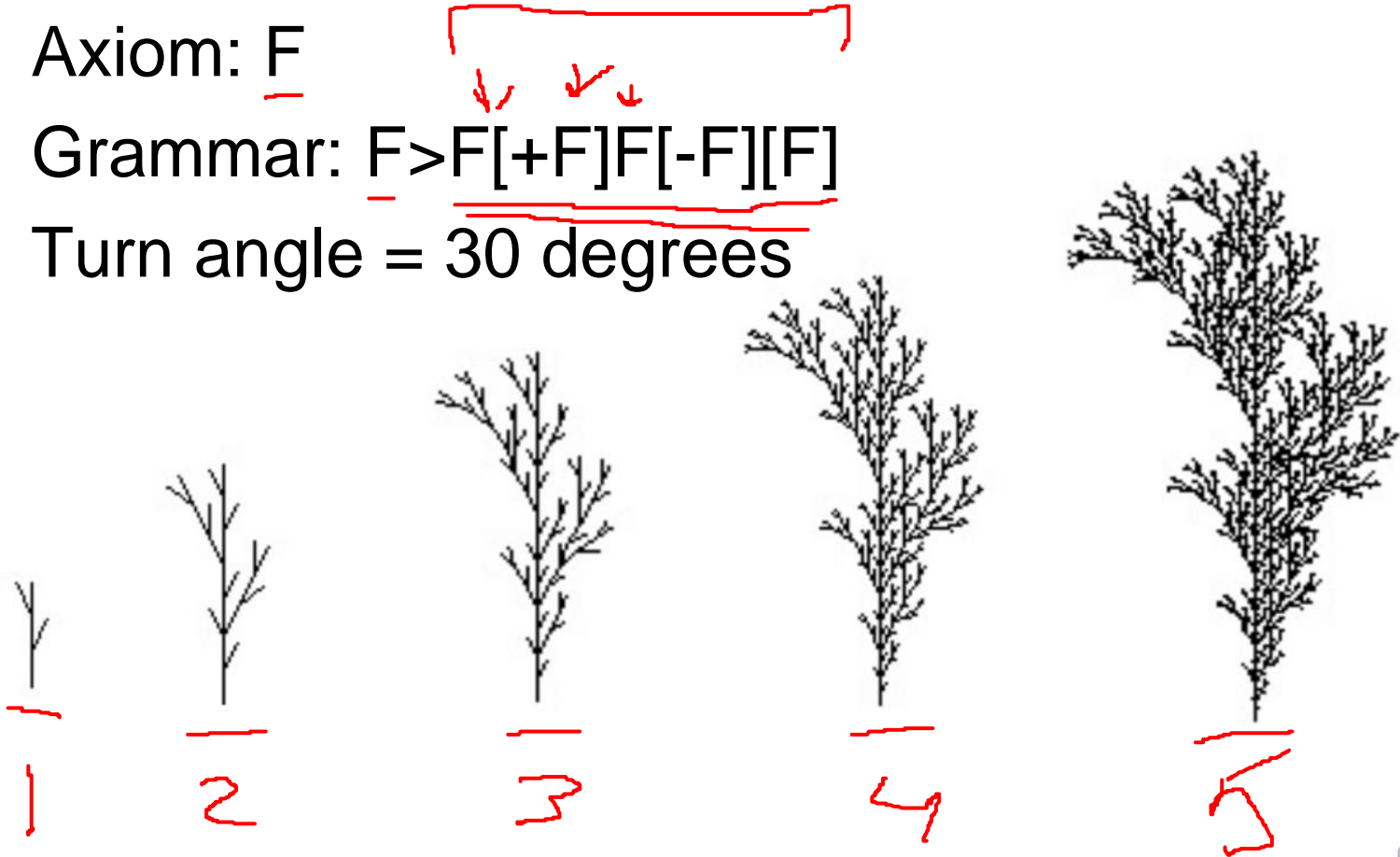
- Alphabet: {F, f, +, -}
 - F: move the turtle forward (drawing a line)
 - f: move the turtle forward (don't draw)
 - +/-: turn right/left (by some angle)
-
- What would FfFfFfFf do?
 - What would F+F+F+F+ do?

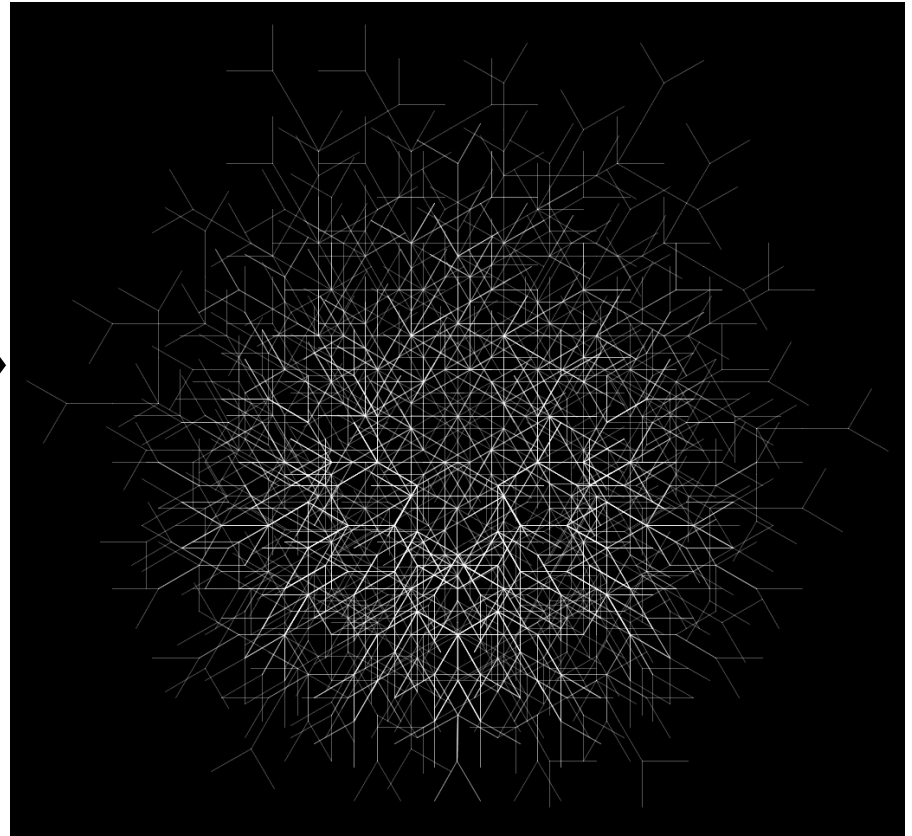
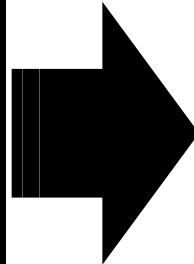
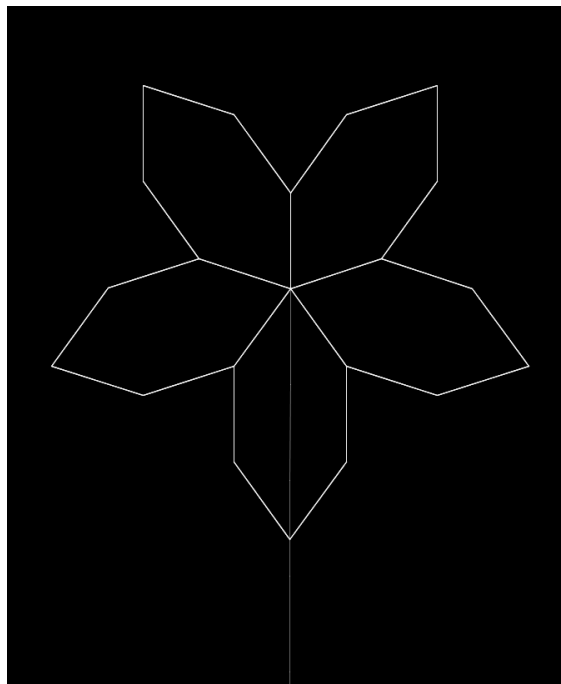
Bracketed L-Systems

- Alphabet: {F, f, +, -, [,]}
- [: push the current state (x, y, heading of the turtle) onto a pushdown stack
-]: pop the current state of the turtle and move the turtle there without drawing
- Enables branching structures!

L-System

- Axiom: F
- Grammar: F \rightarrow F[+F]F[-F][F]
- Turn angle = 30 degrees





Come up with your own rules!

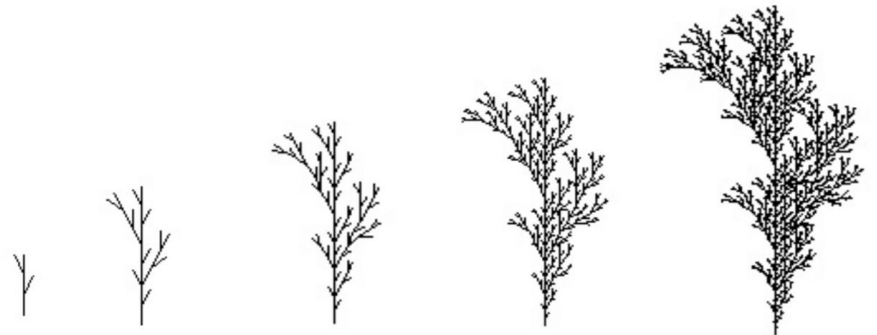
Go to: <https://onlinemathtools.com/l-system-generator>

- Alphabet: {F, f, +, -, [,]}
- [: push the current state (x, y, heading of the turtle) onto a pushdown stack
-]: pop the current state of the turtle and move the turtle there without drawing

Axiom: F

Grammar: $F \rightarrow F[+F]F[-F][F]$

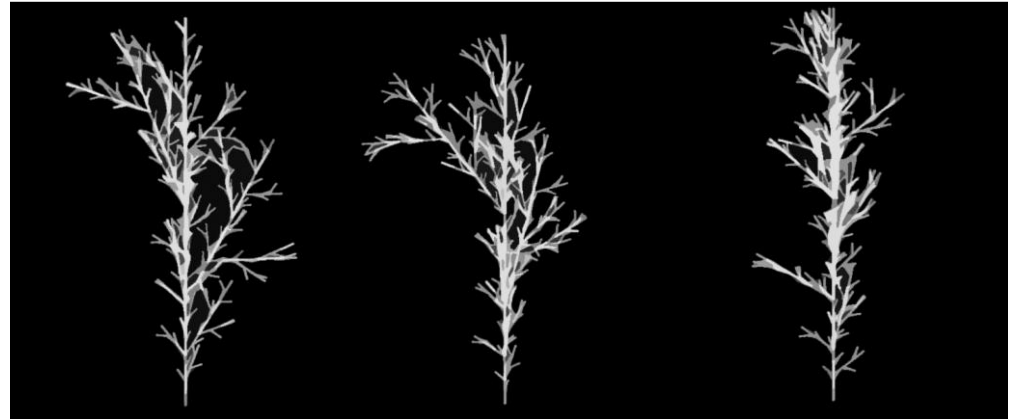
Turn angle = 30 degrees



Types of L-Systems

- Context free: production rules refer only to an individual symbol
- Context-sensitive: production rules can depend on the symbol's neighbors
- Deterministic: one production rules for each symbol
- Non-deterministic: several production rules for a symbol
- Parametric: a symbol references a parameter list

Examples of Stochasticity



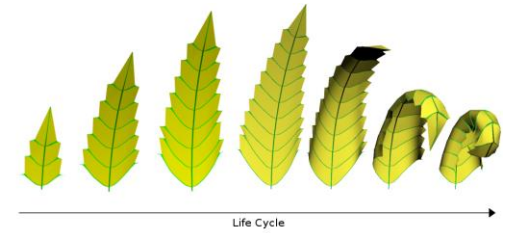
Ecomod by Aleš Zamuda



<https://www.youtube.com/watch?v=O0HUQR1mTbg>
<https://www.youtube.com/watch?v=qiogqd2PIW0>

Unity's Speed Tree





Peyrat et al. 2008

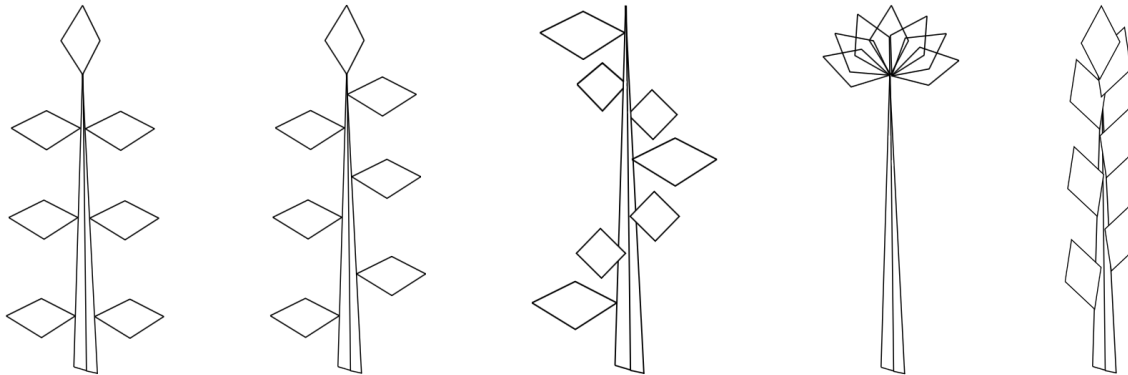


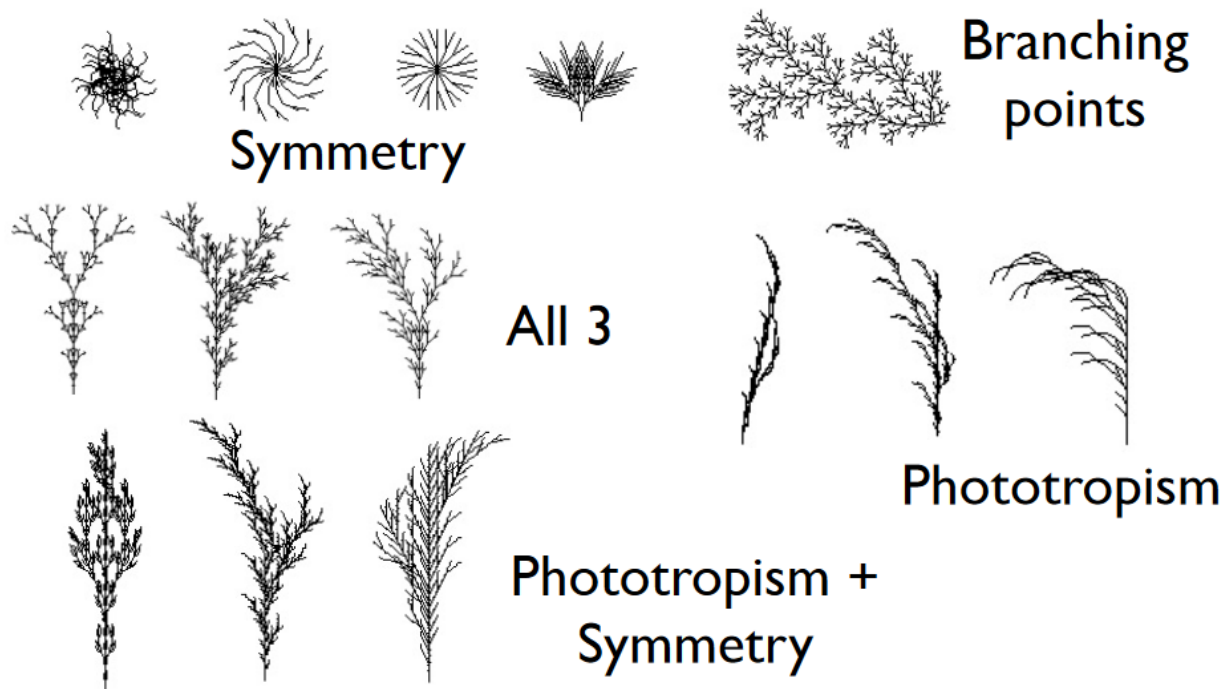
Figure 7: Distributions of leaves, from left to right: stacked (1), staggered (2), spiral (3), bunched (4), and coniferous (5).

Image taken from: Aleš Zamuda and Janez Brest (2014) Vectorized Procedural Models for Animated Trees Reconstruction using Differential Evolution

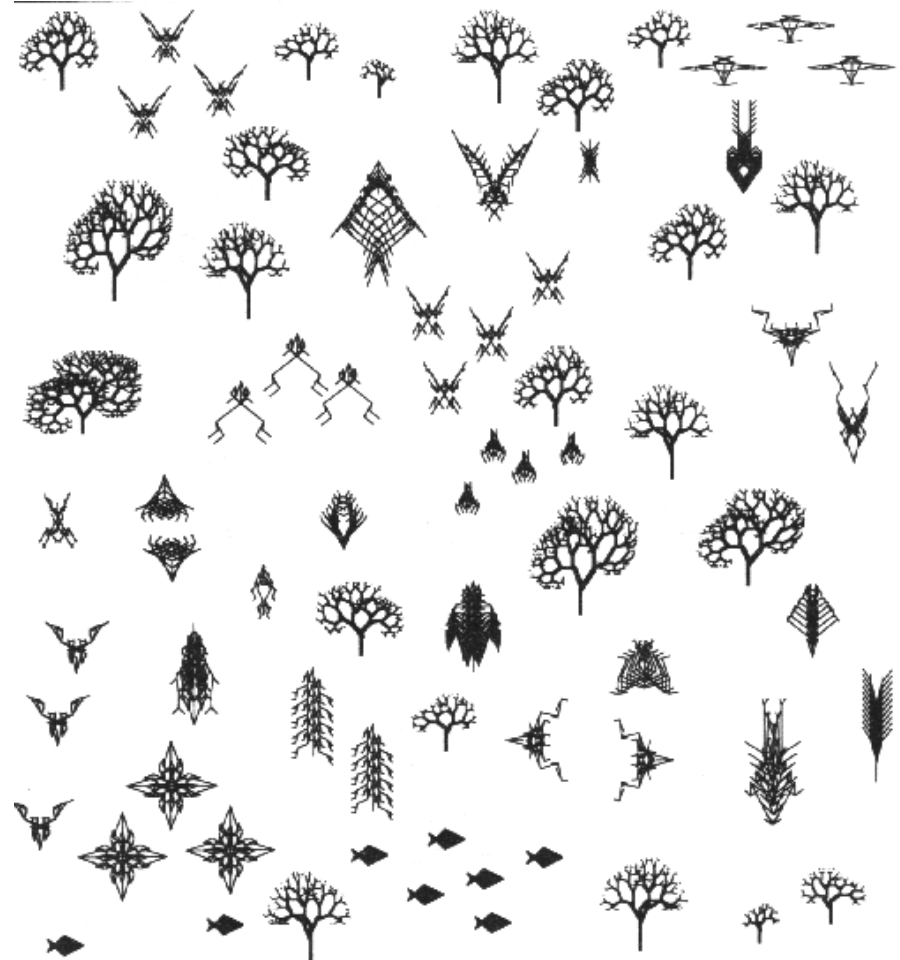
Evolving L-Systems

- Mutation
 - Axiom
 - Production Rules
 - Probabilities
 - Angles
- Fitness
 - Phototropism
 - Bilateral symmetry
 - Proportion of branching points

Evolved L-Systems



Evolved L-Systems



2D L-Systems

- (Matrix rewriting systems)

Axiom:

A

Rules:

A

 \rightarrow

A	B
B	A

B

 \rightarrow

A	A
B	B

Two Expansions:

A

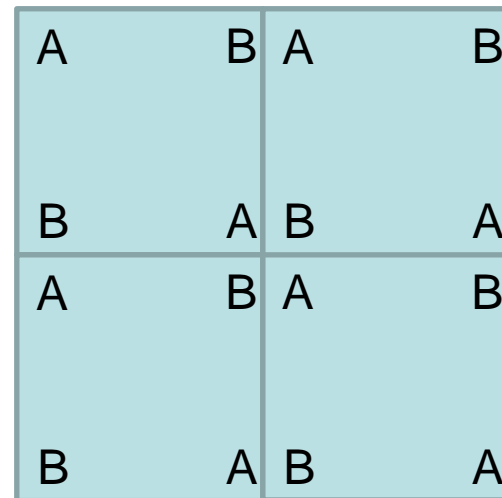
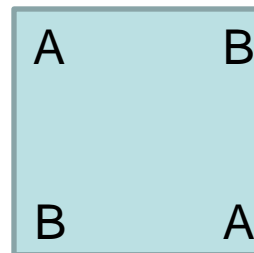
 \rightarrow

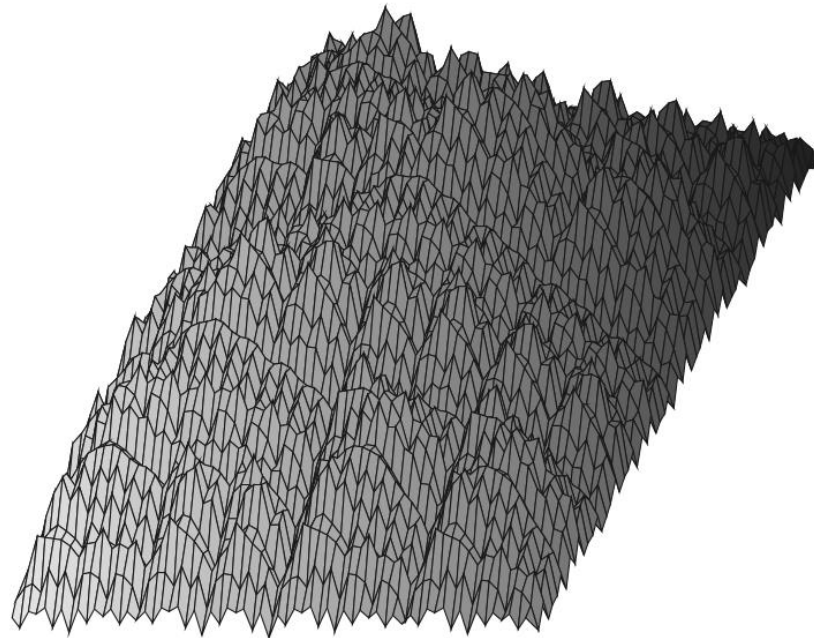
A	B
B	A

A	B	A	A
B	A	B	B
A	A	A	B
B	B	B	A

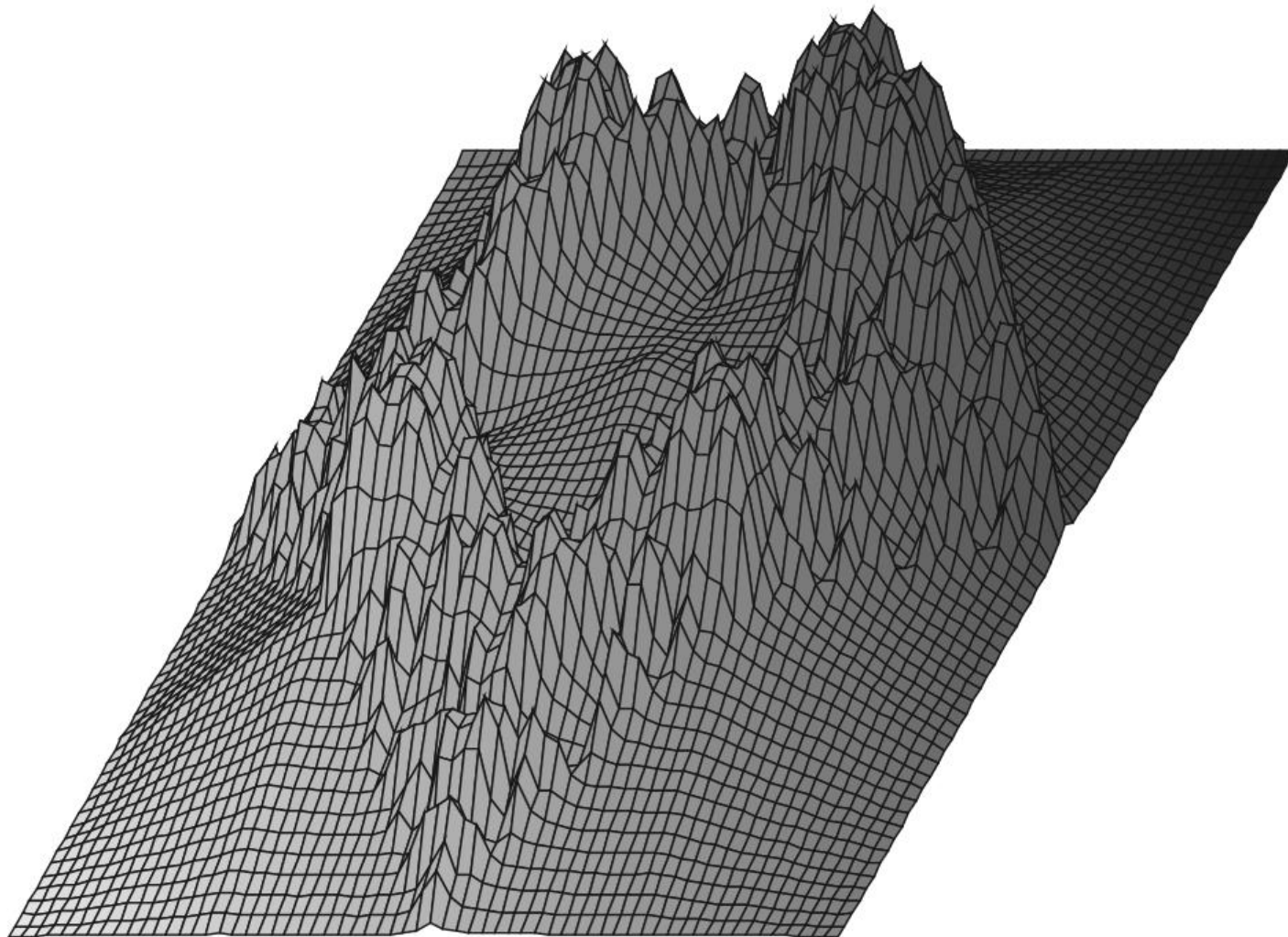
Terrain interpretation of 2D L-Systems

- Letters are interpreted for lowering or raising corners of a square
- E.g. $A=+0.5$, $B=-0.5$

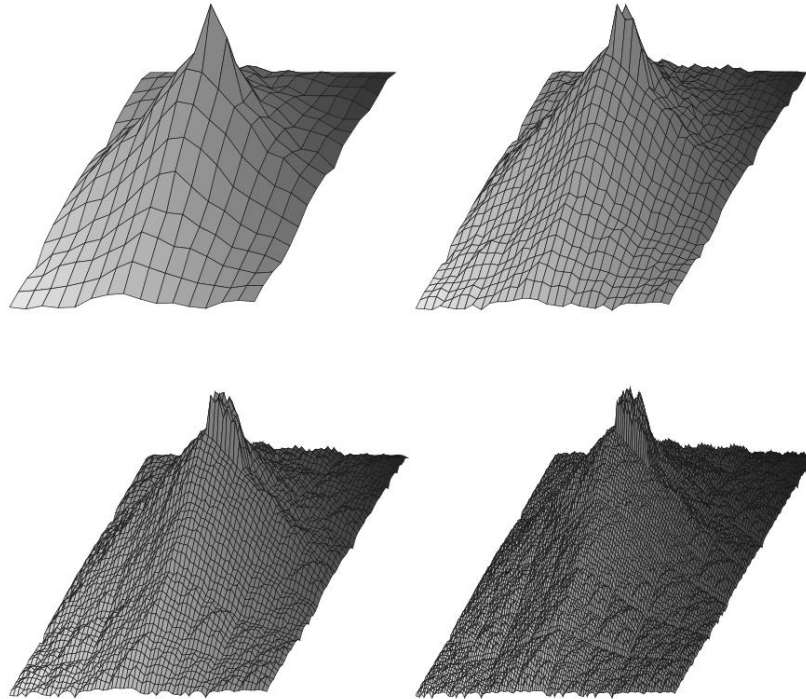




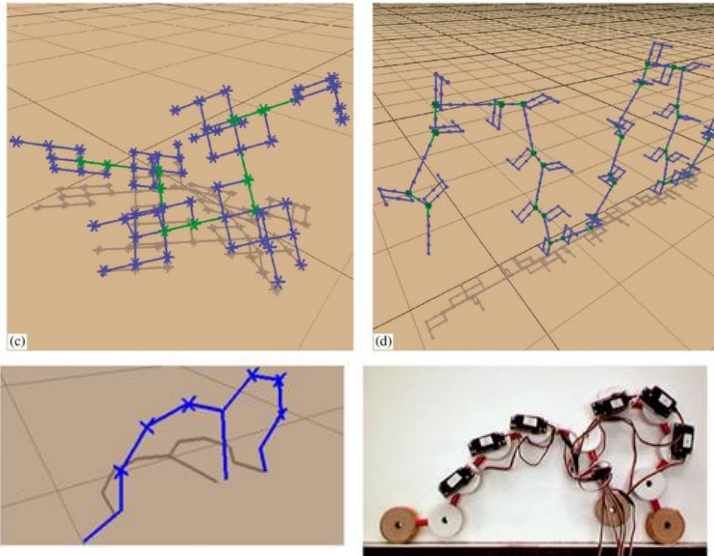
Six rewritings of $A \rightarrow ABBA$, $B \rightarrow AABB$



Infinite resolution!

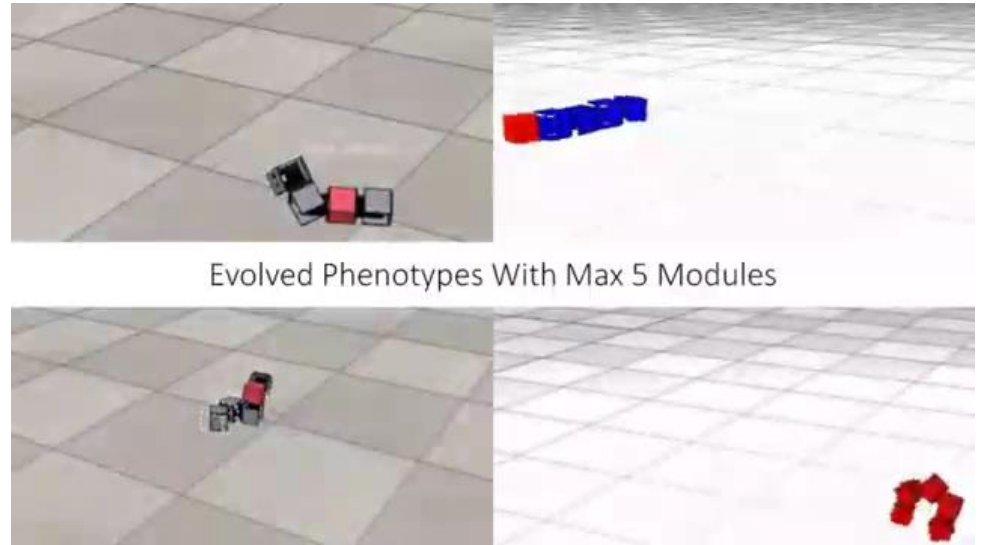


Evolving robots created from L-System



Direct Encoding

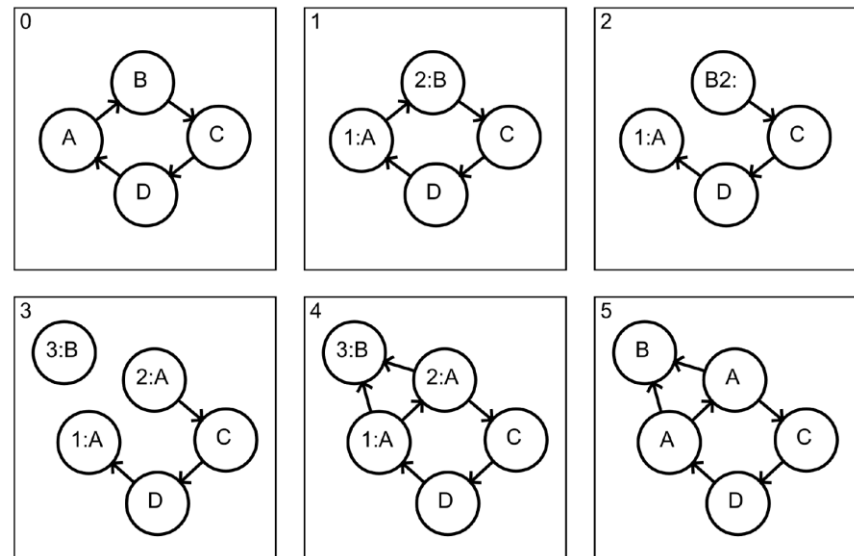
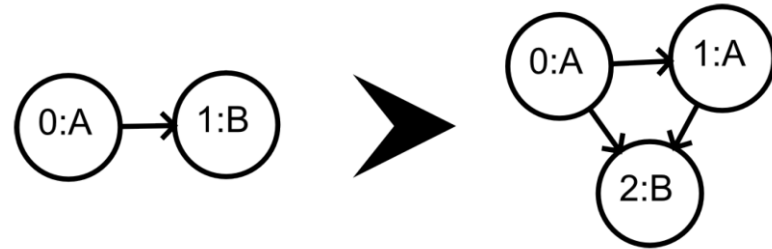
L-System



Hornby and Pollack 2001

Rewriting Graph Grammars

- 1: Identify left-hand subgraph
- 2: Remove edges
- 3: Transform graph
- 4: Copy edges
- 5: Remove marks



Directed graph for evolving virtual creatures

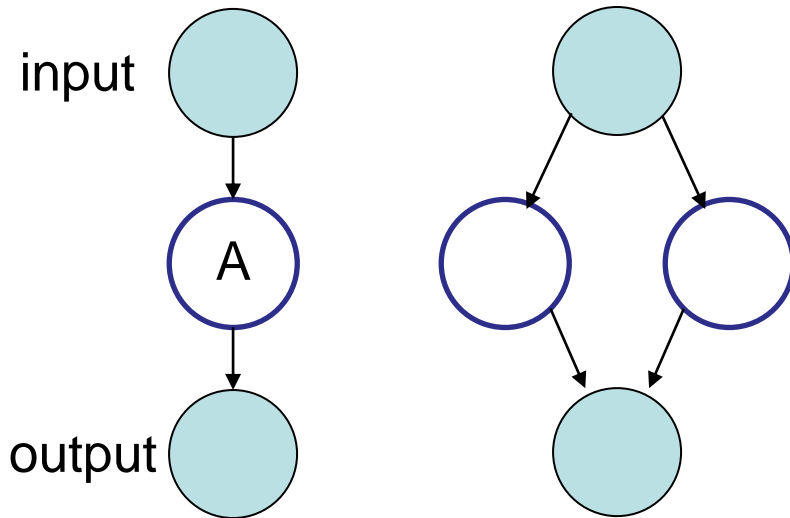
Genotype: directed graph. Phenotype: hierarchy of 3D parts.



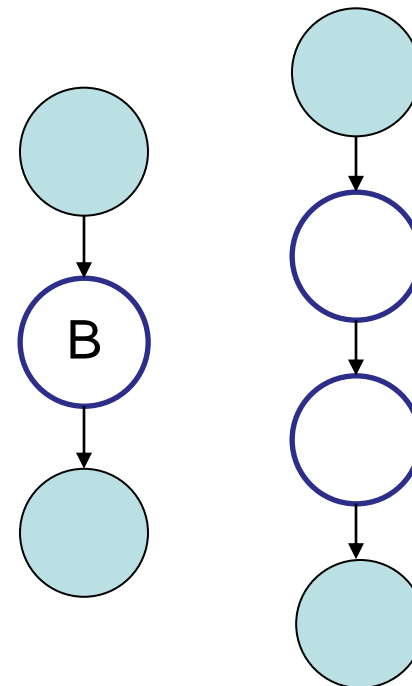
Cellular Encoding

- Simulate cell division to create networks

Parallel division

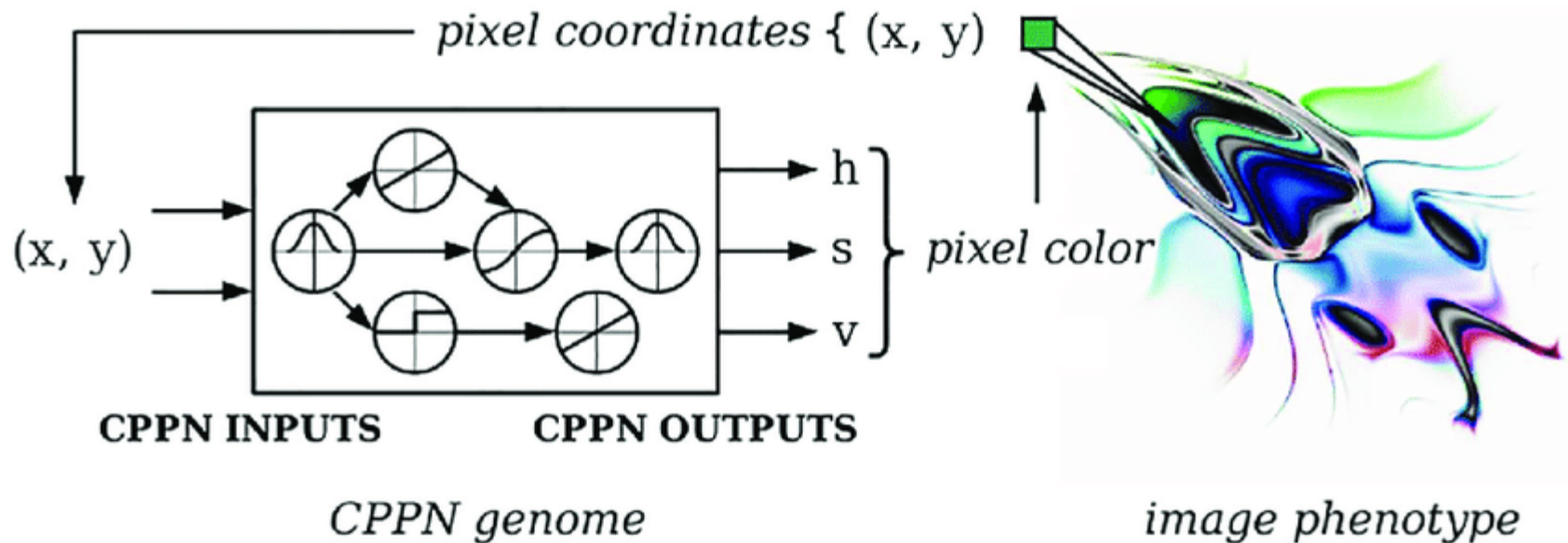


Sequential division

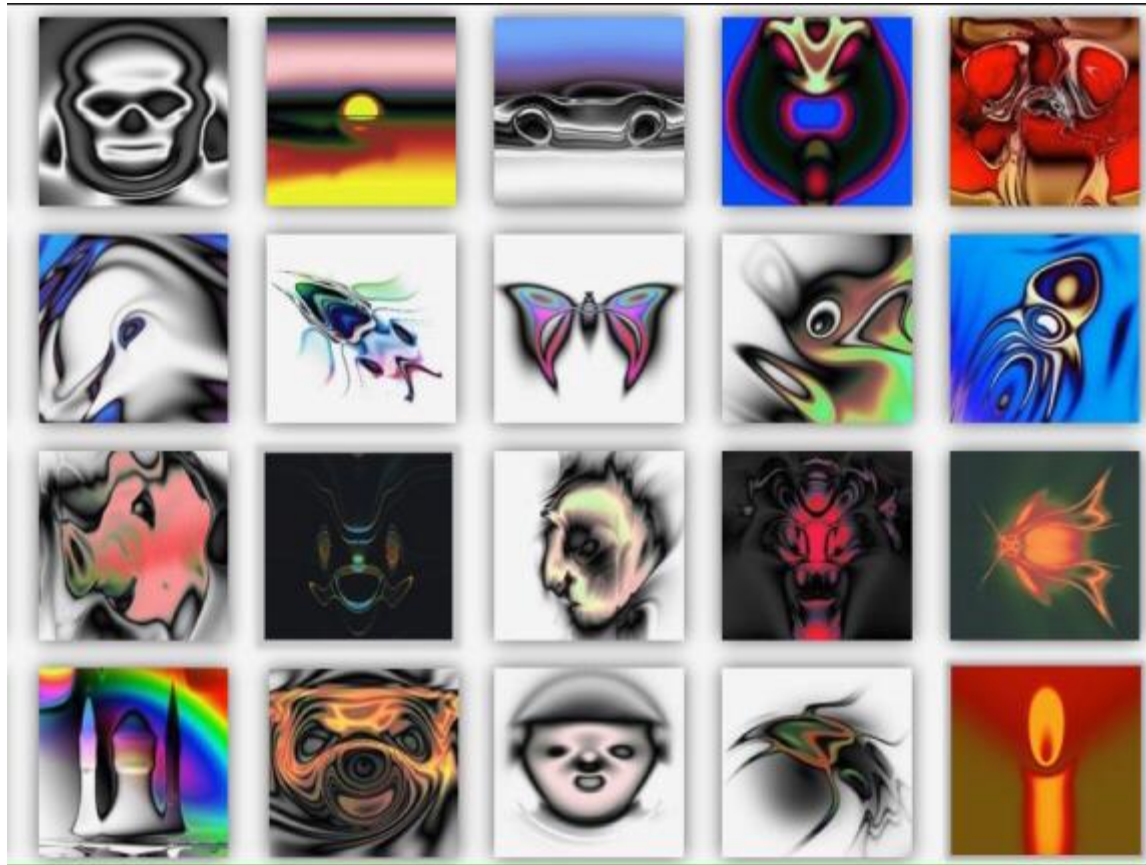


A Neural Network as a Developmental Abstraction?

- Compositional Pattern Producing Network (CPPN)

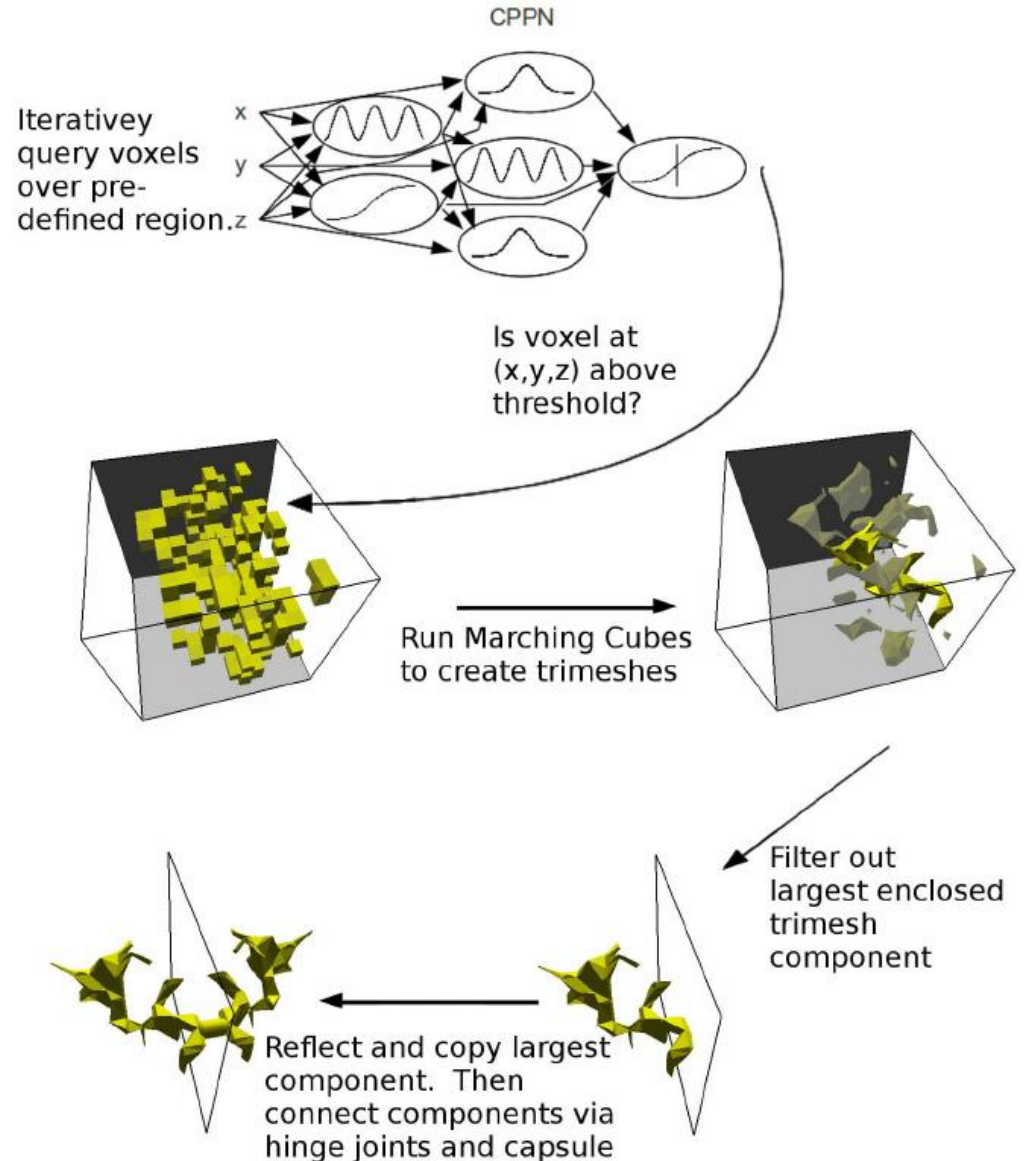


A Neural Network as a Developmental Abstraction?



<http://picbreeder.org/>

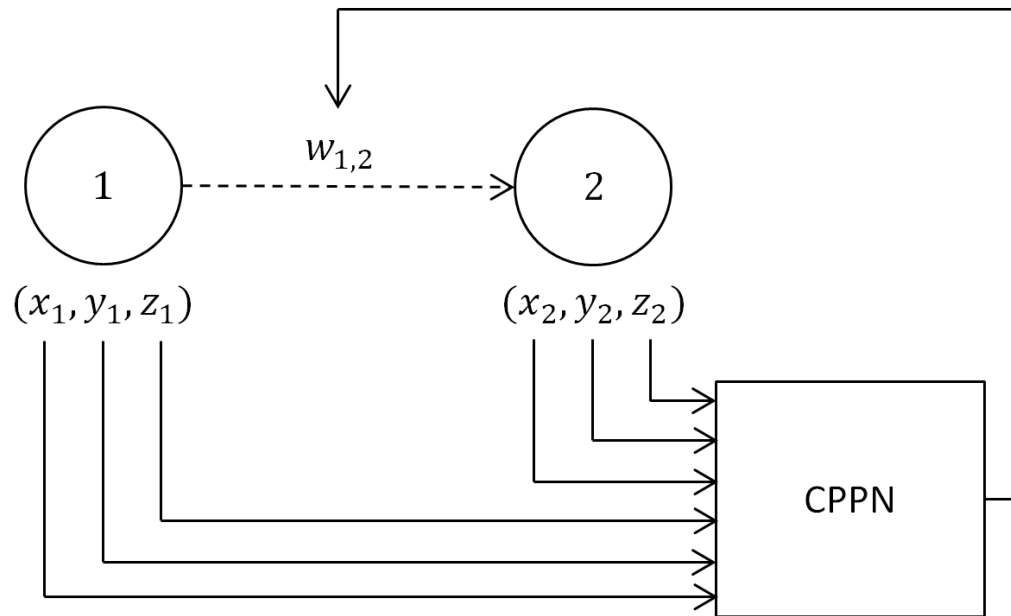
Using CPPNs to create robots



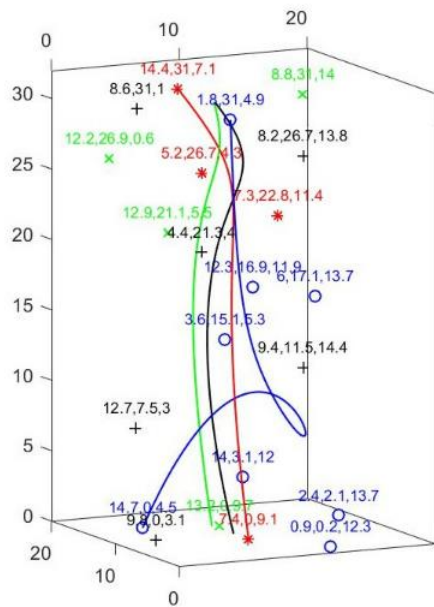
See this link for how CPPNs can be used to create soft-robots:
https://www.youtube.com/watch?v=EXuR_soDnFo

HyperNEAT

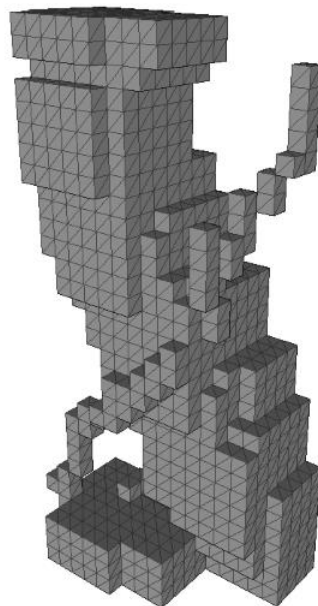
- Asks a CPPN about how assign weights to a neural network



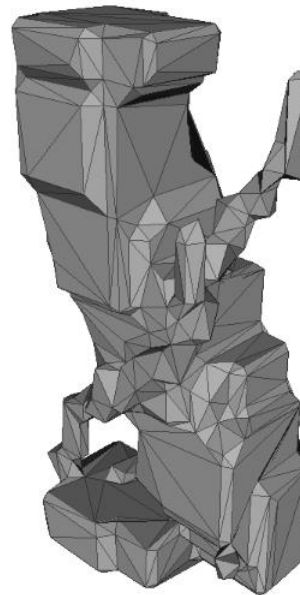
Bezier Curve for Creating Robot Components



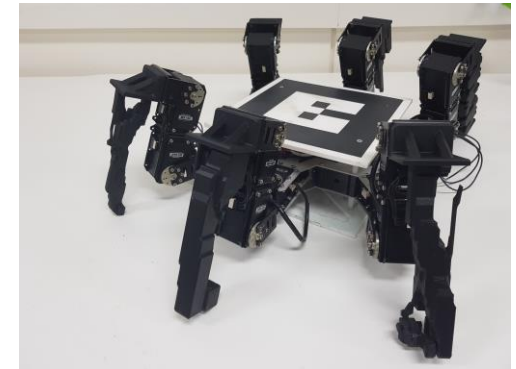
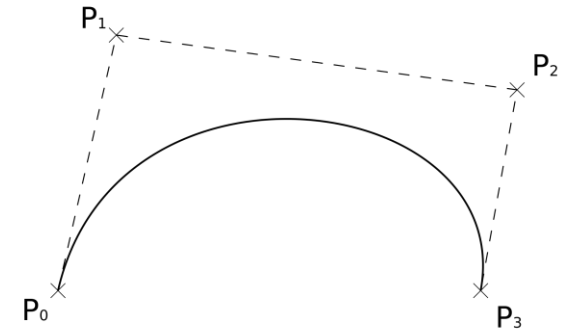
(a)



(b)

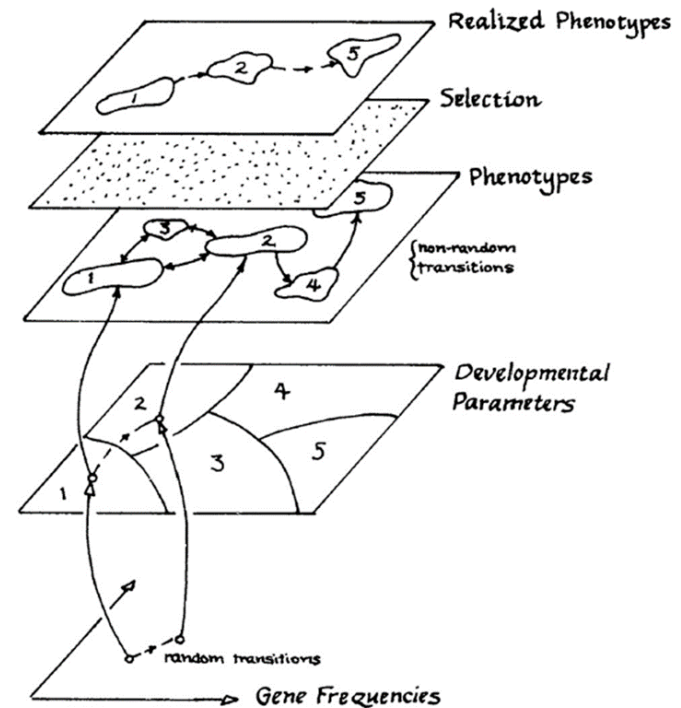


(c)



Developmental Systems

- Rewriting Systems
- Morphogens
- Neural Networks
- Bezier Curves



Swarm Intelligence

- Boids
- Particle Swarm Optimization
- Ant Colony Optimization
- Reconfigurable Robots

Swarm intelligence

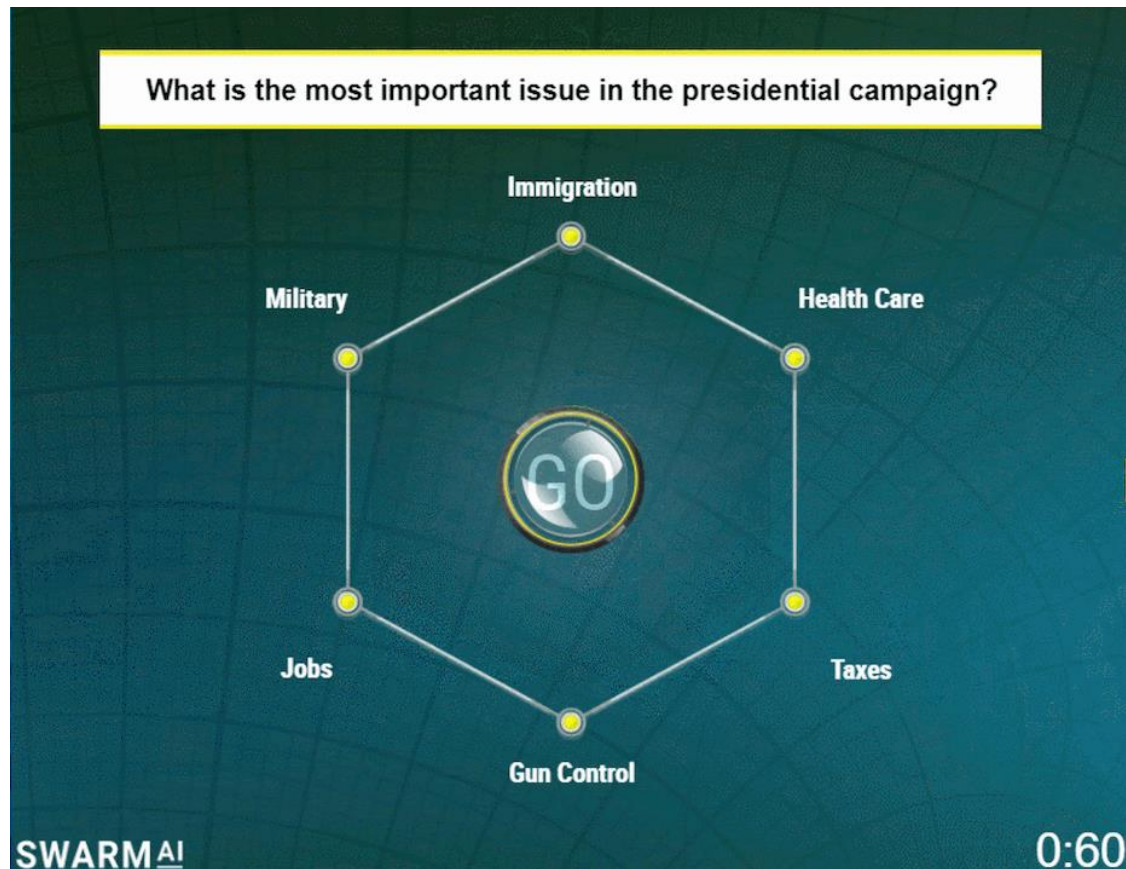
- “The study of large collections of relatively simple agents that can collectively solve problems that are too complex for a single agent or that can display the robustness and adaptability to environmental variation displayed by biological agents”.
- Brain of brains (hive mind)
- Emergent intelligence forms
- Hive mind
- Bees dance
- How swarms can enhance the intelligence in groups

Swarm intelligence

- “The study of large collections of relatively simple agents that can **collectively solve problems** that are too complex for a single agent or that can display the robustness and adaptability to environmental variation displayed by biological agents”.
- Brain of brains (hive mind)



Human swarm intelligence similar to 'wisdom of the crowd'



Swarm Intelligence

- Emergent collective behavior:
 - Aggregation
 - Clustering
 - Foraging
 - Nest construction
- Extended phenotype:
 - How an animal's genes can affect the world
 - E.g. is a beehive is an extended part of a bee?

Boids

- Boid: ‘bird-oid object’
- Three rules:
 - **Separation**: boids steer away from close neighbors
 - **Alignment**: boids steer towards the average heading of their neighbors
 - **Cohesion**: boids steer towards the average position of its neighbors
- Exhibit aggregation
- Sebastian Lague: <https://www.youtube.com/watch?v=bqtqItqcQhw>

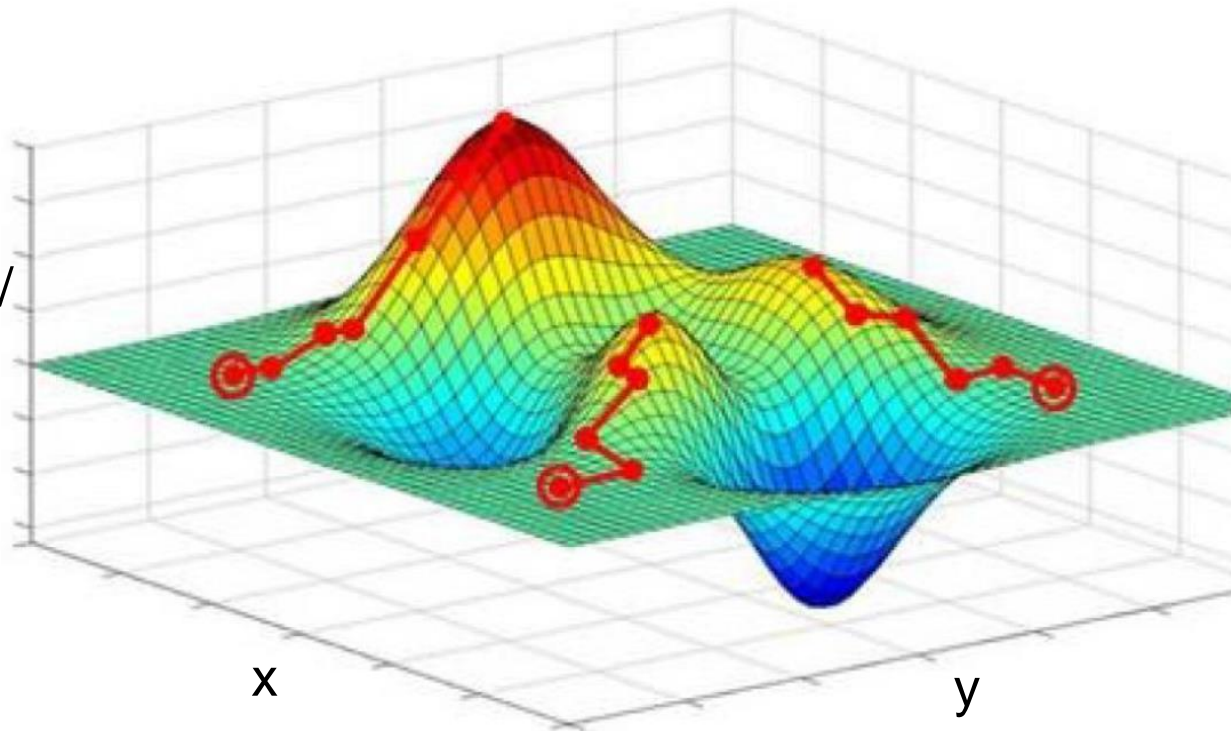


Particle Swarm Optimization (PSO)

- Population based metaheuristic like evolutionary algorithms
- Candidate solutions are *particles*
- A particle contains *positional* and *velocity* parameters
 - Position defines the adjustable/mutable parameters of an individual
 - Velocity represents how these parameters are updated
- The positional parameters can be viewed as the *genotype* of individuals.

Gradient ascent/descent of particles

Performance/
fitness



Particle Swarm Optimization (PSO)

- (eq 1) updates positional parameters x
- (eq 2) updates velocity parameters v

- C_1 and C_2 are *acceleration constants*
- pb and gb are the *particle's best* and *global best* positions found

$$\underline{x_{i,d}(it+1)} = \underline{x_{i,d}(it)} + \underline{v_{i,d}(it+1)} \quad (1)$$

$$\begin{aligned} v_{i,d}(it+1) &= v_{i,d}(it) \\ &+ C_1 * Rnd(0,1) * [\underline{pb_{i,d}(it)} - x_{i,d}(it)] \\ &+ C_2 * Rnd(0,1) * [\underline{gb_d(it)} - x_{i,d}(it)] \end{aligned} \quad (2)$$

Caption:

i particle's index, used as a particle identifier;

d dimension being considered, each particle has a position and a velocity for each dimension;

it iteration number, the algorithm is iterative;

$x_{i,d}$ position of particle i in dimension d ;

$v_{i,d}$ velocity of particle i in dimension d ;

C_1 acceleration constant for the cognitive component;

Rnd stochastic component of the algorithm, a random value between 0 and 1;

$pb_{i,d}$ the location in dimension d with the best fitness of all the visited locations in that dimension of particle i ;

C_2 acceleration constant for the social component;

Creating a PSO strategy

- See the PSO exercise online

$$x_{i,d}(it + 1) = x_{i,d}(it) + v_{i,d}(it + 1) \quad (1)$$

$$\begin{aligned} v_{i,d}(it + 1) &= v_{i,d}(it) \\ &+ C_1 * Rnd(0, 1) * [pb_{i,d}(it) - x_{i,d}(it)] \\ &+ C_2 * Rnd(0, 1) * [gb_d(it) - x_{i,d}(it)] \end{aligned} \quad (2)$$

Ant Colony Optimization (ACO)

- **Stigmergy**: social communication through modification of the environment



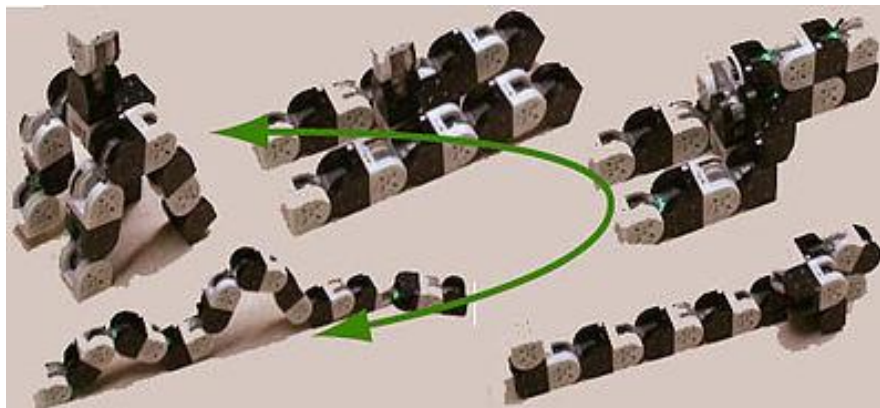


Why swarm systems?

- **Continuous adaptation:** dynamic network routing and urban transportation
- **Decentralized, Asynchronous**
- **Collective decision making**

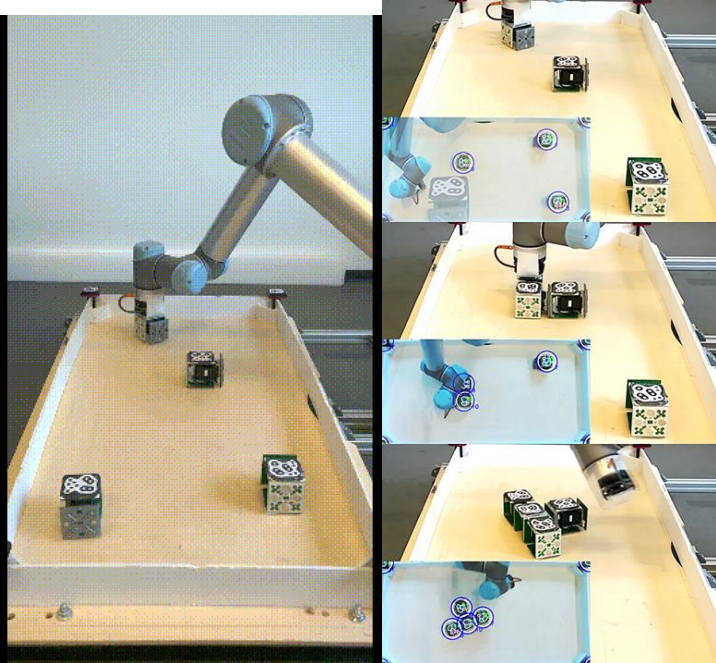
Reconfigurable robots

- Robots composed of modules that can change the shape of the robot to adjust its functionality
 - Possibly autonomously

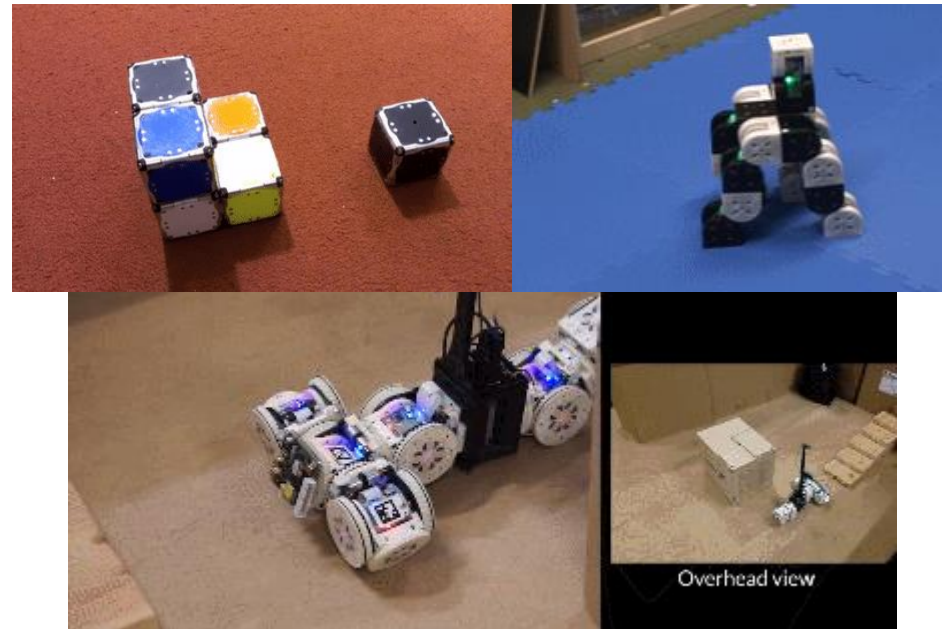


Reconfigurable modular robots

Passive Approaches

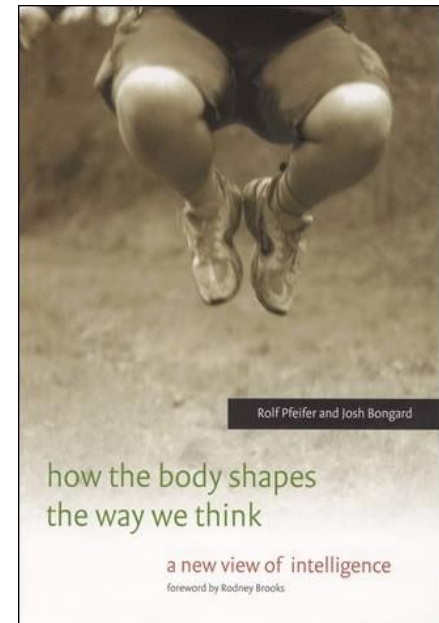
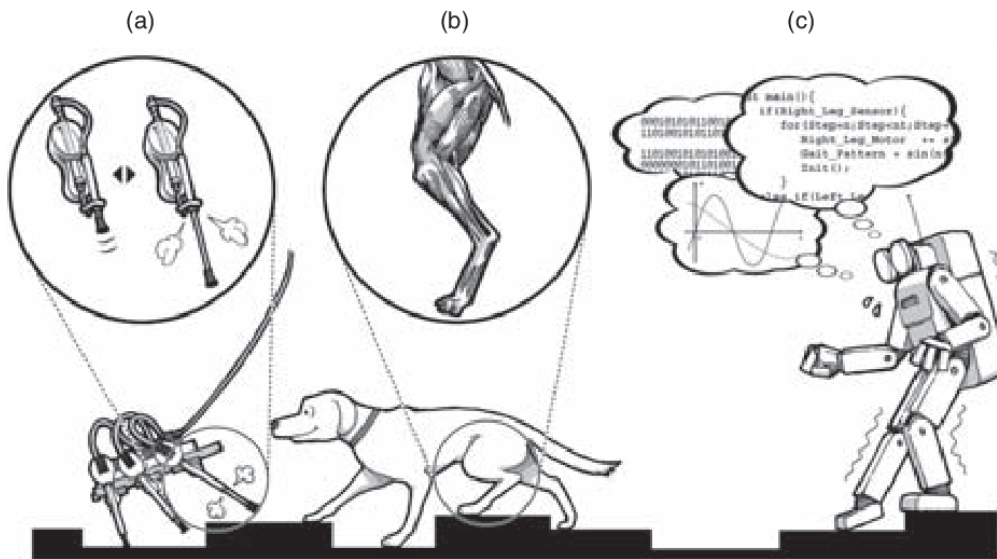


Active swarm approaches



Useful evolutionary robotics

- Shape-changing: evaluation different body shapes



Summary

- Boids
- Particle Swarm Optimization
- Ant Colony Optimization
- Reconfigurable Robots

Take home message

- Design artificial systems considering the genotype to phenotype mapping
 - Compact storage
 - Reuse of information
 - Modularity
 - Decentralized controllers