## IN3060/4060 - Semantic Technologies - Spring 2021

Lecture 2: Resource Description Framework (RDF)

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# Mandatory exercises

- First oblig published today (22.01) after lecture.
- Topic RDF.
- Hand in by next Friday (29.01).
- Same schedule for the other small obligs:
  - #2 (29.01 05.02),
  - #3 (05.02 12.02), and
  - #4 (19.02 05.03).
- The larger obligs with two possible attempts:
  - #5 (05.03 19.03) and
  - #6 (26.03 16.04).
- And one short oblig about OTTR
  - #7 (07.05 14.05).
- See *obliger* on the semester page.
- Mr. Oblig.

IN3060/4060 :: Spring 2021 Lecture 2 :: 22nd January 3 / 50

## Today's Plan

- Introduction
- 2 RDF data model
  - Technicalities
  - Features
- 3 RDF serialisations
- 4 RDF vocabularies
- 5 RDF on the web
- 6 Subtleties
- Summary

IN3060/4060 :: Spring 202:

Lecture 2 :: 22nd Januar

2 / 50

# Outline

- Introduction
- 2 RDF data model
  - Technicalities
  - Features
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IN3060/4060 :: Spring 2021 Lecture 2 :: 22nd January 4 / 50

Introduction

### RDF: W3C Overview

- The Resource Description Framework (RDF) is a standard model for data interchange on the Web
- It has features that facilitate data merging even if the underlying schemas differ.
- It extends the linking structure of the Web to use URIs to name the relationship between things as well as the two ends of the link.
- Thus allows data to be mixed, exposed, and shared across different applications.
- This linking structure forms a directed, labelled graph.
- This graph view is the easiest possible mental model for RDF and is often used in easy-to-understand visual explanations.

Adapted from http://w3c.org/RDF.

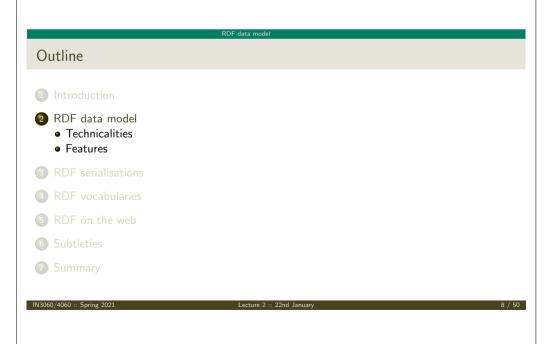
IN3060/4060 :: Spring 2021 Lecture 2 :: 22nd January 5 / 50

Introductio

## RDF, essential 'abouts':

- The Resource Description Framework was initially intended for annotation of web-accessible resources (1999).
- It has since developed into a general purpose language for describing structured information—on the web or elsewhere.
- The goal of RDF is to enable applications to exchange data on the Web in a meaning-preserving way.
- It is considered the basic representation format underlying the Semantic Web.

Semantic Web Stack User interface and applications Central block in the Trust SW stack • First "semantic" block Proof in stack. Unifying logic In the course we will Ontologies: OWL Rules: SWRL explore: SPARQL Vocabularies: RDFS RDF SPARQL Data interchange: RDF RDFS/OWL Logic Syntax: XML Applications Identifiers: URI Chr. set: UNICODE



#### RDF data model Technicaliti

## **RDF** Triples

- All information in RDF is expressed using a *triple* pattern.
- A triple consists of a subject, a predicate, and an object.
   Examples:

subject	predicate	object
Norway	has capital	Oslo
Norway	has king	King Harald
King Harald	born year	1937

- Another word for an RDF triple is a statement or fact.
- The elements of an RDF triple are either
  - URI references,
  - literals, or
  - blank nodes.

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Lecture 2 :: 22nd Januar

0 / 50

#### RDF data model Technicaliti

## URI ⊈ URL

URLs are not the only URIs:

ISBN:

urn:isbn:0-486-27557-4

• Geo:

geo:37.786971,-122.399677

Mail:

mailto:jieyingc@ifi.uio.no

• and many many more . . .

RDF data model Technicalities

## Uniform Resource Identifiers (URIs)

- RDF (Resource Description Framework) talks about resources.
  - Almost anything is a resource.
- Resources are identified by URIs (Uniform Resource Identifiers).
- E.g., in dbpedia.org:

Norway: http://dbpedia.org/resource/Norway has capital: http://dbpedia.org/ontology/capital Oslo: http://dbpedia.org/resource/Oslo has king: http://dbpedia.org/ontology/leader

King Harald: http://dbpedia.org/resource/Harald\_V\_of\_Norway

- As identifiers, think of them as just strings (on a special format).
  - Not necessarily dereferenceable.

IN3060/4060 :: Spring 2021

ecture 2 :: 22nd Janua.

10 / 5

RDF data model

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## **URIs and QNames**

- URIs are often long and hard to read and write.
- Most serialisations use an abbreviation mechanism.
  - Define "prefixes", "namespaces".
- E.g., in Turtle serialisation:

```
@prefix dbp: <http://dbpedia.org/resource/> .
@prefix dbp-ont: <http://dbpedia.org/ontology/> .
```

- A *QName* like dbp:Oslo stands for http://dbpedia.org/resource/Oslo
- Remember: It's all just URIs!

11 / 50 IN3000/4000 :: Spring 2021 Lecture 2 :: 22nd January 12 / 50

IN3060/4060 :: Spring 2021 Lecture 2 :: 22nd January 11 / 50

RDF data model Technicalitie

### URIs and data

• We can then state that Norway's capital is Oslo as:

<http://dbpedia.org/resource/Norway> <http://dbpedia.org/ontology/capital> <http://dbpedia.org/resource/Oslo> .

• Or use prefixes:

```
dbp:Norway dbp-ont:capital dbp:Oslo .
```

- But what if we want to state that Oslo's population is 629313?
- We cannot have one URI for every integer, decimal number, string etc.

IN3060/4060 :: Spring 2021

Lecture 2 :: 22nd January

12 / 50

RDF data model Technicalities

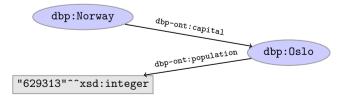
## **RDF** Graphs

• An RDF graph is a set of triples. E.g.,

```
dbp:Norway dbp-ont:capital dbp:Oslo .
dbp:Oslo dbp-ont:population "629313"^^xsd:integer .
```

is an RDF graph containing two triples.

• RDF graphs are often represented as a directed labelled graph:



IN3060/4060 :: Spring 2021 | Lecture 2 :: 22nd January | 15 / 50

RDF data model Technicalities

#### Literals

- Literals are used to represent data values.
- All literals have a datatype.
- Datatypes are also resources, referenced via URIs, and written as: dbp:Oslo dbp-ont:population "629313"^^xsd:integer
- however, if nothing is written, it is assumed to be a string:
   dbp:Oslo dbp-ont:officialName "Oslo" .
  Is short for
   dbp:Oslo dbp-ont:officialName "Oslo"^^xsd:string .
- One can also specify the language of a string using a language tag: dbp:Norway rdfs:label "Norge"@no . dbp:Norway rdfs:label "Norwegen"@de .

IN3060/4060 :: Spring 2021

Lecture 2 :: 22nd January

14 / 50

#### **Problems**

- Can all knowledge be nicely represented with only triples containing URIs and literals?
- What if we didn't know what the capital of Norway was, only that it has a population of 629313 people?

```
dbp:Norway dbp-ont:hasCapitalWithPopulation "629313"^^xsd:integer .
```

- What if we want to model something which is not nicely represented as one URI, e.g. an address?
- UiO has the address "Problemveien 7 0313 Oslo". How should we model this? As a literal?

dbp:UiO dbp-ont:hasAddress "Problemveien 7 0313 Oslo".

As several literals?

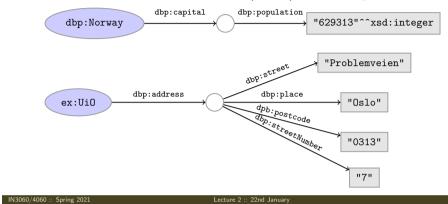
```
dbp:UiO dbp-ont:addsressPlace "Oslo".
dbp:UiO dbp-ont:addsressStreet "Problemveien".
dbp:UiO dbp-ont:addressStreetNumber "7".
dbp:UiO dbp-ont:addressPostcode "0313".
```

IN3060/4060 :: Spring 2021 Lecture 2 :: 22nd January 16 / 50

#### RDF data model | Tec

#### Blank nodes

- Blank nodes are like resources without a URI.
- Use when resource is unknown, or has no (natural) identifier. E.g.:



RDF data model Feat

Footures

# Why URIs?

- URIs naturally have a "global" scope, unique throughout the web.
  - Contrasts to, e.g., keys in rel. DB which are unique within a table.
  - Helps to avoid name clashes.
  - Example: merging two product catalogues. http://www.abc-company.com/category/item/123 http://www.xyz-company.com/product/123
- URLs are also addresses.
  - Exploit the well-functioning machinery of web browsing.
  - Find data by following data identifiers, i.e., URIs.
- "A web of data."

Lecture 2 :: 22nd January 19 / 50

RDF data model Techn

# RDF Triple Grammar

• Literals and blank nodes may not appear everywhere in triples:

5 p o

• URI references may occur in all positions

V V V

Literals may only occur in object position
Blank nodes may not occur in predicate position

V X V

Why?

- Literals are just values, no relationships from literals allowed.
- Blank nodes in predicate position deemed "too meaningless" and confusing.

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ecture 2 :: 22nd Janua

18 / 50

RDF data r

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# Why triples?

- Any information format can be transformed to triples.
  - Examples:

```
Tabular (spreadsheets, DBs): row column cell Trees (XML): parent path child
```

- Relationships are made explicit and elements in their own right.
  - The predicate, i.e., the relationship, is an element in the triple.
  - Unlike DB columns and binary predicates.
  - Can be described in RDF.
  - "Self-documenting"
- Again, "A web of data".

IN3060/4060 :: Spring 2021 Lecture 2 :: 22nd January 20 / 50

RDE data model Feature

## Why graphs?

- A single, but highly versatile, format.
  - Everything is on the same format: triples!
- Since RDF graphs are just sets of triples, basic set operations are well-defined.
- Merging RDF graphs? Just take their union!
  - With tabular data, table dimensions must match.
  - With trees, a node can only have one parent.
  - Note that graphs need not be connected.
- Extending an RDF graph? Just add more triples!
  - Need not redefine the database table, or
  - to restructure the XML schema.

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Lecture 2 :: 22nd Januar

21 / 5

RDF serialisation

### **RDF** Serialisations

There are many serialisations for the RDF data model:

RDF/XML the W3C standard. Complicated!

<?xml version="1.0"?>
<rdf:RDF xmlns:dbp="http://dbpedia.org/resource/"
xmlns:fodf="http://xmlns.com/foaf/0.1/"
xmlns:rdf="http://xmlns.com/foaf/0.1/"
xmlns:rdf="http://xww.w3.org/1999/02/22-rdf-syntax-ns\#">
<rdf:Description rdf:about="http://dbpedia.org/resource/Harald\_V\_of\_Norway">
<fodf:name>Harald\_V</fodf:name>
</rdf:Description>
</rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rdf:Description></rd>

Turtle convenient, human readable/writable—our choice.

@prefix dbp: <a href="http://dbpedia.org/resource/">
@prefix foaf: <a href="http://xmlns.com/foaf/0.1/">
dbp:Harald\_V\_of\_Norway foaf:name "Harald V"</a>.

N-triples one triple per line. No abbreviations.

<http://dbpedia.org/resource/Harald\_V\_of\_Norway> <http://xmlns.com/foaf/0.1/name> "Harald V" .

Others N3, TriX, TriG, RDF/JSON, ...

IN3060/4060 :: Spring 2021 | Lecture 2 :: 22nd January 23 / 50

RDF serialisatio

### Outline

- Introduction
- 2 RDF data model
  - Technicalities
  - Features
- 3 RDF serialisations
- 4 RDF vocabularies
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Lecture 2 :: 22nd Janua

22 / 50

RDF serialisati

## Turtle: URI references and triples

#### Full URIs are surrounded by < and >:

<http://dbpedia.org/resource/Oslo>

#### Statements are triples terminated by a period:

<http://dbpedia.org/resource/Oslo>
 <http://www.w3.org/1999/02/22-rdf-syntax-ns#type>
 <http://dbpedia.org/ontology/Place> .

#### Use 'a' to abbreviate rdf:type:

<http://dbpedia.org/resource/Oslo>

a <http://dbpedia.org/ontology/Place> .

Turtle allows any non-zero amount of space between elements in triples.

IN3060/4060 :: Spring 2021 Lecture 2 :: 22nd January 24 / 50

RDF serialisation

Turtle: Namespaces

QNames are written without any special characters.

```
Namespace prefixes are declared with @prefix:
    @prefix dbp: <a href="http://dbpedia.org/resource/">http://dbpedia.org/resource/</a>.
    dbp:Oslo a <a href="http://dbpedia.org/ontology/Place">http://dbpedia.org/ontology/Place</a>.
```

```
A default namespace may be declared:

@prefix dbp: <http://dbpedia.org/resource/> .
    @prefix : <http://dbpedia.org/ontology/> .

dbp:Oslo a :Place .
```

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Lecture 2 :: 22nd January

25 / 50

RDF serialisation

Turtle: Statements sharing elements

```
Instead of:

dbp:Oslo rdf:type dbo:City .

dbp:Oslo :officialName "Oslo" .

dbp:Oslo :population 629313 .
```

```
...statements may share a subject with ';':

dbp:Oslo rdf:type dbo:City ;
:officialName "Oslo" ;
:population 629313 .
```

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RDF serialisation

Turtle: Literals

```
Literal values are enclosed in double quotes:

@prefix dbp: <a href="http://dbpedia.org/resource/">http://dbpedia.org/resource/</a>.

@prefix : <a href="http://dbpedia.org/ontology/">http://dbpedia.org/ontology/</a>.
```

dbp:Norway :officialName "Norge" .

```
Possibly with type or language information:
```

```
dbp:Norway rdfs:label "Norge"@no .
dbp:Oslo :population "629313"^^xsd:integer .
```

#### Numbers and booleans may be written without quotes:

```
dbp:Oslo :population 629313 .
dbp:Oslo :isCapital true .
```

IN3060/4060 :: Spring 2021

Lecture 2 :: 22nd Januar

26 / 50

RDF serialisation

Turtle: Statements sharing elements

```
Instead of:
```

```
dbp:Norway rdfs:label "Norway"@en .
dbp:Norway rdfs:label "Norge"@no .
dbp:Norway rdfs:label "Norge"@no .
```

```
...statements may share subject and predicate with ',':
dbp:Norway rdfs:label "Norway"@en ,
```

```
"Norway rdis:label "Norway"@en ,
"Norwegen"@de ,
"Norge"@no .
```

```
...and in combination:
```

```
dbp:Norway rdfs:label "Norway"@en, "Norwegen"@de, "Norge"@no; :capital dbp:Oslo .
```

IN3060/4060 :: Spring 2021

cture 2 :: 22nd January

28 / 50

RDF serialisation

### Turtle: Blank nodes

Blank nodes are designated with underscores or [...].

```
Norway has a capital with population 629313:

dbp:Norway :capital _:someplace .
_:someplace :population 629313 .
```

```
There is a place with official name Oslo:

[] a :Place ;
:officialName "Oslo" .
```

IN3060/4060 :: Spring 2021

Lecture 2 :: 22nd January

00 / 50

RDF serialisation

Turtle: Other things

```
Use '#' to comment:

# This is a comment.

dbp:Oslo a dbpont:Place . # This is another comment.
```

```
Use '\' to escape special characters:
:someGuy :foaf:name "James \"Mr. Man\" Olson" .
```

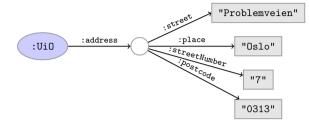
Turtle specification: http://www.w3.org/TR/turtle/.

IN3060/4060 :: Spring 2021 | Lecture 2 :: 22nd January 31 / 50

RDF serialisat

## Question

The blank node here:



has no 'name.'

Why does Turtle use 'blank node identifiers' like \_:someplace?

Answer: makes it easy to use same node in several triples.

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ecture 2 :: 22nd Janua.

30 / 50

RDF vocabula

### Outline

- Introduction
- 2 RDF data model
  - Technicalities
  - Features
- 3 RDF serialisations
- 4 RDF vocabularies
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3060/4060 :: Spring 2021 | Lecture 2 :: 22nd January

### Vocabularies

- Families of related notions are grouped into vocabularies.
- Usually the same namespace/prefix is shared.
- Some important, well-known namespaces—and prefixes:

```
rdf: <a href="mailto:rdf">rdf: //www.w3.org/1999/02/22-rdf-syntax-ns#> - RDF</a>
rdfs: <http://www.w3.org/2000/01/rdf-schema#> - RDF Schema
foaf: <http://xmlns.com/foaf/0.1/> - Friend of a friend
dcterms: <http://purl.org/dc/terms/> - Dublin Core
```

- Usually, a description is published at the namespace base URI.
- Note that the prefix is not standardised.
  - However, in practice many are.
  - Oprefix rdf: <a href="http://xmlns.com/foaf/0.1/">http://xmlns.com/foaf/0.1/</a>> would be highly irregular.

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## Example vocabularies: FOAF, Dublin Core

Some example resources:

FOAF: person data and relations.

- foaf:Person
- foaf:knows
- foaf:firstName. foaf:lastName, foaf:gender

Dublin Core: library metadata.

- dcterms:creator, dcterms:contributor
- dcterms:format, dcterms:language, dcterms:licence

#### Examples:

```
ifi:jieyingc rdf:type foaf:Person .
ifi:jieyingc foaf:knows ifi:martingi .
ifi:jieyingc dcterms:creator ifi:rdf-lecture .
```

## Example vocabularies: RDF, RDFS

Some example resources:

RDF: describing RDF graphs.

- rdf:Statement
- rdf:subject, rdf:predicate, rdf:object
- rdf:type

RDFS: describing RDF vocabularies.

- rdfs:Class
- rdfs:subClassOf, rdfs:subPropertyOf
- rdfs:domain. rdfs:range
- rdfs:label

#### Examples:

```
dbp:Oslo rdf:type dbp-ont:Place .
dbp:Norway rdfs:label "Norge"@no .
dbp:Capital rdfs:subClassOf dbp:City .
```

IN3060/4060 :: Spring 2021 Lecture 2 :: 22nd January

### Outline

- Introduction
- 2 RDF data model
  - Technicalities
  - Features
- B RDF serialisations
- 4 RDF vocabularies
- **6** RDF on the web
- 6 Subtleties
- Summary

## Where is it?

- In files:
  - In some serialisation: XML/RDF, Turtle, ...
  - Typically small RDF graphs, i.e., max. a few 100 triples, e.g.,
    - Vocabularies: http://xmlns.com/foaf/spec/index.rdf.
    - Tiny datasets: http://folk.uio.no/martingi/foaf.rdf.
- From SPARQL endpoints:
  - Data kept in a triple store, i.e., a database.
  - RDF is served from endpoint as results of SPARQL queries.
  - Exposes data (in different formats)
    - with endpoint frontends, e.g., http://dbpedia.org/resource/Norway, or
    - by direct SPARQL query: http://dbpedia.org/sparql.
- There are many RDFizers which convert data to RDF.
  - Tabular files (CSV, Excel): XLWrap.
  - Relational DB: D2RQ (http://sws.ifi.uio.no/d2rg/) or R2RML (https://www.w3.org/TR/r2rml/).
  - W3C keeps a list: http://www.w3.org/wiki/ConverterToRdf.

IN3060/4060 :: Spring 2021 Lecture 2 :: 22nd January

## Linked Open Data

Tim Berners-Lee's recipe for 5 star web data:

- Make data available on the Web (any format) under an open license.
- 2 Make it available as structured data (e.g., Excel, not image scans).
- 3 Use non-proprietary formats (e.g., CSV instead of Excel).
- Use URIs to identify data items; make them referable on the Web.
- Sink your data to other's data to provide context.

Adapted from http://www.w3.org/DesignIssues/LinkedData.html

## Creating RDF data and vocabularies

- Designing an easy-to-use and robust namespace is non-trivial.
- Naming is difficult.
- Reuse existing vocabularies if possible. Don't reinvent.
- URIs are also addresses, consider publishing issues when naming.
- Adhere to the policies described in *best practice* documents:
  - Best Practice Recipes for Publishing RDF Vocabularies
    - http://www.w3.org/TR/2008/NOTE-swbp-vocab-pub-20080828/
  - Cool URIs for the Semantic Web
    - http://www.w3.org/TR/cooluris/
- Use http://www.example.[com/net/org] for prototyping and documentation.

#### Web of Data

- The point of publishing data as described in this lecture is to have self-describing and self-documenting data.
- Decouples data from applications.
- Lightens the programming burden.
- Semantic Web applications should be/are generic and general purpose, exploiting rich and knowledge intensive data sets.

Subtleties

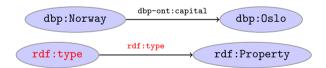
#### Outline

- Introduction
- 2 RDF data model
  - Technicalities
  - Features
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- 4 RDF vocabularies
- 5 RDF on the web
- 6 Subtleties
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IN3060/4060 :: Spring 2021 Lecture 2 :: 22nd January 41

Subtletie

## RDF graphs are not graphs



- Drawing dbp:Norway dbp-ont:capital dbp:Oslo is straight-forward.
- But what about rdf:type rdf:Property?
- RDF graphs are sets of triples, not graphs.
- The set of nodes, i.e., subjects and object, and edges, i.e., predicates, of an RDF graph need not be disjoint.

IN3060/4060 :: Spring 2021 | Lecture 2 :: 22nd January | 43 / 50

Subtleti

## URIs are not necessarily unique

- URIs are just strings, not a "global identification service".
- There is nothing stopping you from using rdf:type as the URI for your favourite data item.
- However, don't do that!
- The simple rule of only creating URIs in a namespace domain you control should keep you out of trouble.
  - Again, put data on the URI address.
- Trust is an important (and work-in-progress) layer in the SW stack.

\$3060/4060 :: Spring 2021 Lecture 2 :: 22nd January 42 / 50

Subtlet

# Be careful when merging RDF files

Merging the two RDF files containing named blank nodes

```
File 1

ifi:martige :owns _:myCar .
_:myCar a lotus:Esprit .

File 2

ifi:martingi :owns _:myCar .
_:myCar a iicv:Sahara .
```

gives the RDF graph:

```
File 1 U File 2

ifi:martige :owns _:myCar .

ifi:martingi :owns _:myCar .

_:myCar a lotus:Esprit, iicv:Sahara .

ifi:martige :owns rdf:type lotus:Esprit

ifi:martingi :owns rdf:type iicv:Sahara
```

Subtletie

## Rename blank nodes

Renaming \_:myCar to \_:myCar2 in File 2.

```
File 1

ifi:martige :owns _:myCar .

_:myCar a lotus:Esprit .

File 2

ifi:martingi :owns _:myCar2 .

_:myCar2 a iicv:Sahara .
```

gives the RDF graph:

Subtleties

## More complex statements (cont.)

What if I want to state that "Jieying thinks iOS is better than Linux, but Martin does not."

```
Reification, statements describing statements

_:s rdf:subject ex:ios;
   rdf:predicate ex:betterThan;
   rdf:object ex:linux.

:jieyingc :thinks _:s .
:martingi :thinksNot _:s .
```

Reification allows us to describe agents' (e.g. people, sensors) beliefs, knowledge, etc. or meta information about a statement, e.g. "added by", "imestamp", etc.

IN3060/4060 :: Spring 2021 | Lecture 2 :: 22nd January 47 / 50

Subtleti

## More complex statements

We can use triples to form complex statements, e.g.:

Turtle shorthand for lists

:in3060 :hasLecturers (:martingi :jieyingc :olemholt ) .

IN3060/4060 :: Spring 2021

Lecture 2 :: 22nd January

46 / 50

Summ

### Outline

- Introduction
- 2 RDF data model
  - Technicalities
  - Features
- 3 RDF serialisations
- A RDF vocabularies
- 5 RDF on the web
- 6 Subtleties
- Summary

IN3060/4060 :: Spring 2021 Lecture 2 :: 22nd January 48 / 50

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## Summary

- RDF is a general format for describing resources.
- Data is represented as triples, consisting of
  - URIs for describing resources,
  - literals for data,
  - blank nodes for unknown data or more complex relationships.
- Sets of triples form RDF graphs.
- Naturally extends the linking structure of the web.
- Allows meta-data as a part of the data.
- Allows data to be easily linked to other datasets.
- Is completely independent of any application.

IN3060/4060 :: Spring 2021 Lecture 2 :: 22nd January 49 / 50

Summa

That's it for today!

Remember the mandatory assignment.

3060/4060 :: Spring 2021 Lecture 2 :: 22nd January 50 / 50