

IN3060/4060 – Semantic Technologies – Spring 2021

Lecture 7: RDF and RDFS semantics

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Informatics



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Oslo

Outline

- 1 Why we need semantics
- 2 Model-theoretic semantics from a birds-eye perspective
- 3 Repetition: Propositional Logic
- 4 Simplified RDF semantics

Semantics—why do we need it?

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Another look at the Semantic Web cake

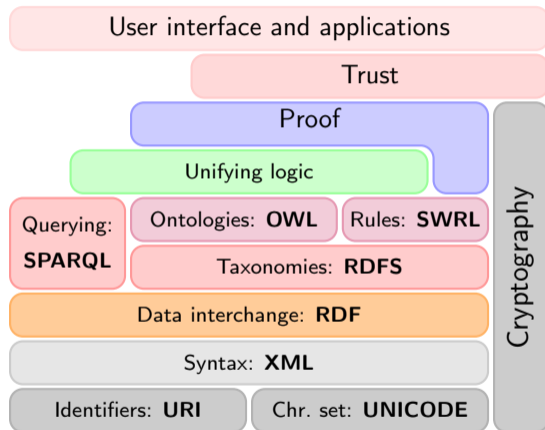


Figure: Semantic Web Stack

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- Specifies how the different components should be interpreted
- And what **entailment** should be taken to mean.

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Formal semantics

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 - the only criterion of correctness is **provability**.

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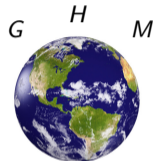
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- How do we know that the inference rules are well-chosen?
- Which manipulations derive conclusions that hold **in the real world**?

Finding out stuff about the World

The “Real World”



G: Aristotle was Greek
H: Aristotle was human
M: Aristotle was mortal

Finding out stuff about the World

Statements

$$G \rightarrow H$$

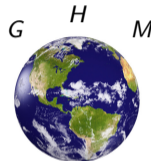
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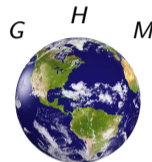


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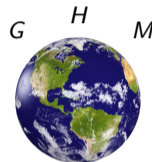
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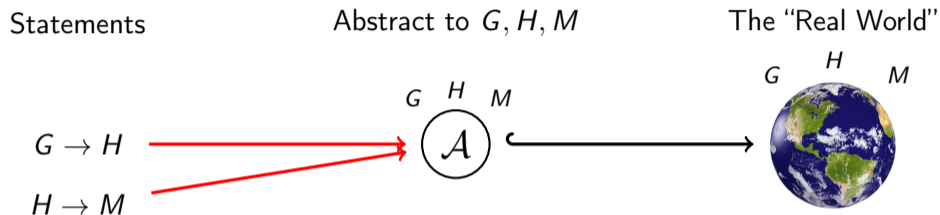
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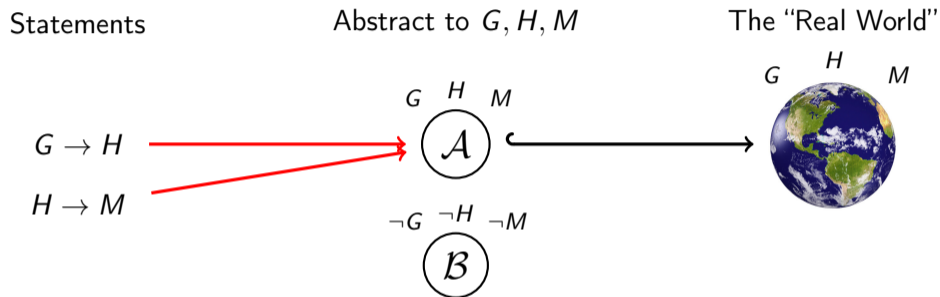
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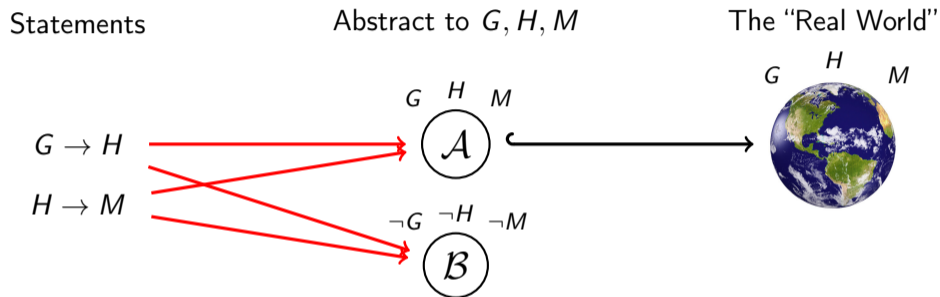
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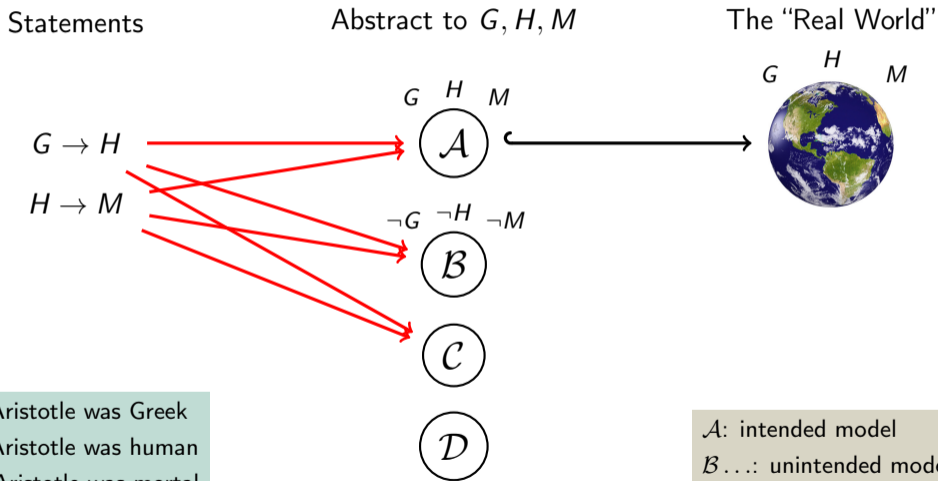
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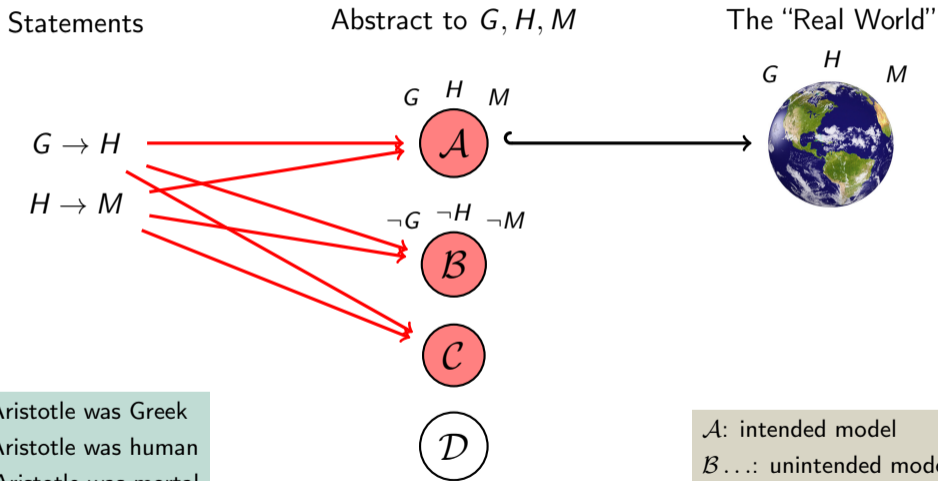
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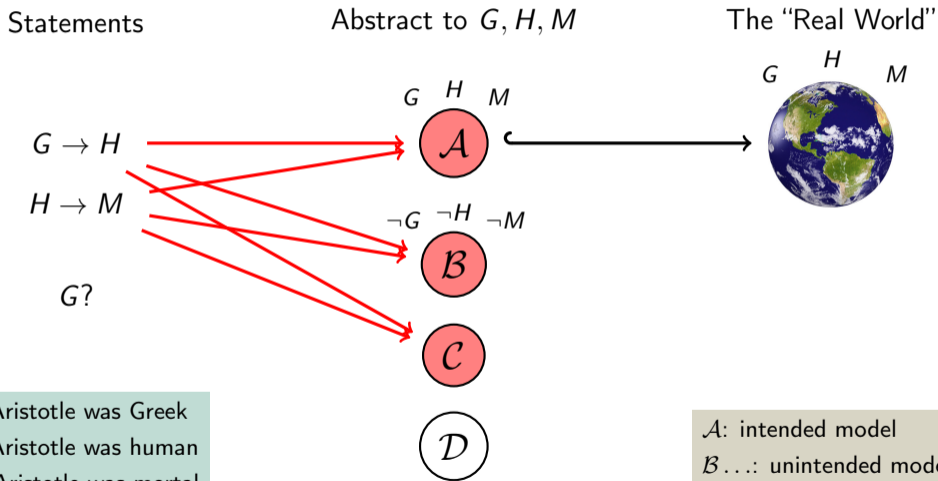
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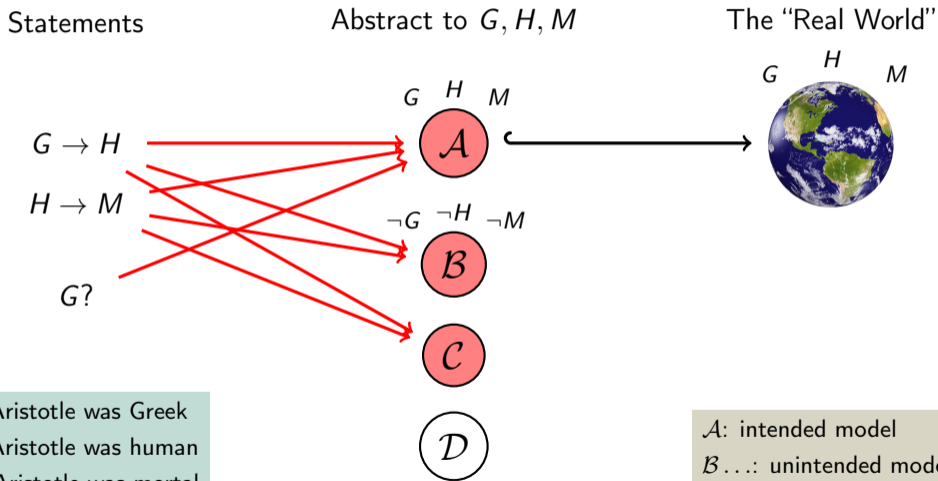
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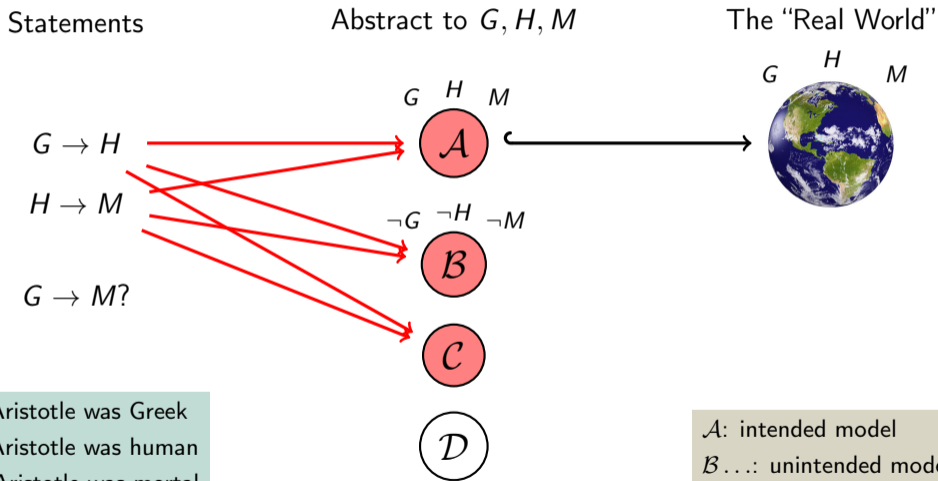
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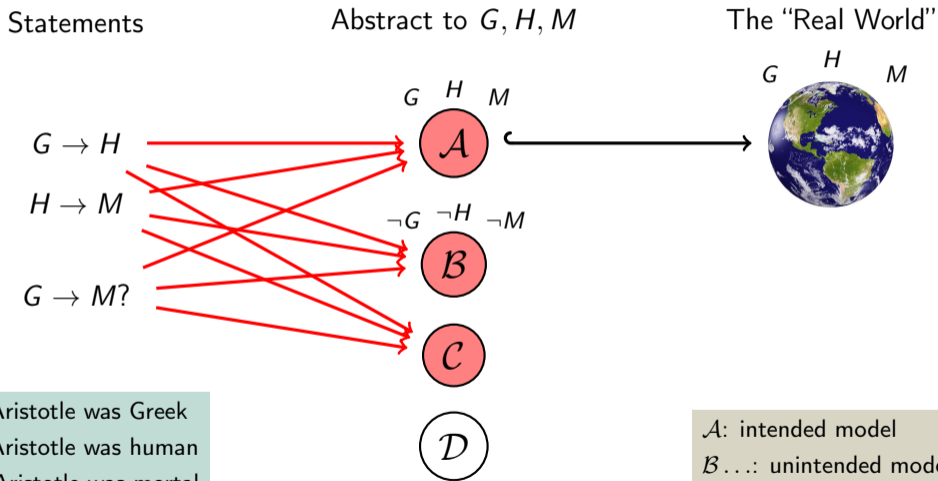
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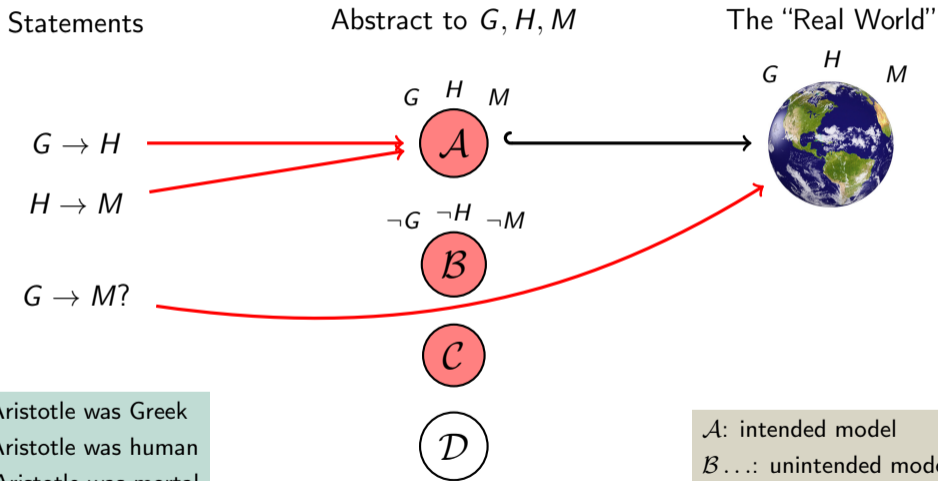
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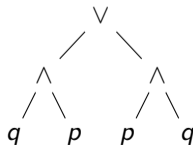
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Propositional Logic: Formulas

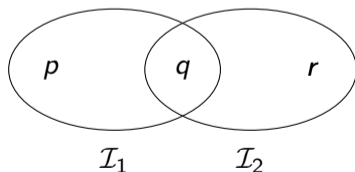
- Formulas are defined “by induction” or “recursively”:
 - 1 Any letter p, q, r, \dots is a formula
 - 2 if A and B are formulas, then
 - $(A \wedge B)$ is also a formula (read: “ A and B ”)
 - $(A \vee B)$ is also a formula (read: “ A or B ”)
 - $\neg A$ is also a formula (read: “not A ”)
- Nothing else is. Only what rules [1] and [2] say is a formula.
- Examples of formulae: p $(p \wedge \neg r)$ $(q \wedge \neg q)$ $((p \vee \neg q) \wedge \neg p)$
- Formulas are just a kind of strings until now:
 - no meaning
 - but every formula can be “parsed” uniquely.

$$((q \wedge p) \vee (p \wedge q))$$



Interpretations

- Logic is about truth and falsity
- Truth of compound formulas depends on truth of letters.
- Idea: put all letters that are “true” into a set!
- Define: An *interpretation* \mathcal{I} is a set of letters.
- Letter p is true in interpretation \mathcal{I} if $p \in \mathcal{I}$.
- E.g., in $\mathcal{I}_1 = \{p, q\}$, p is true, but r is false.



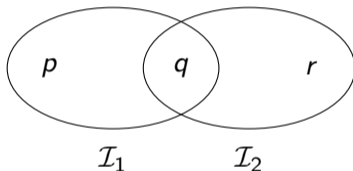
- But in $\mathcal{I}_2 = \{q, r\}$, p is false, but r is true.

Semantic Validity \models

- To say that p is true in \mathcal{I} , write

$$\mathcal{I} \models p$$

- For instance



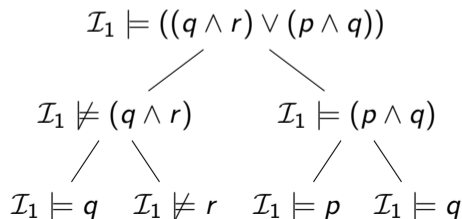
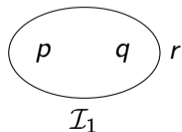
$$\mathcal{I}_1 \models p \quad \mathcal{I}_2 \not\models p$$

- In other words, for all letters p :

$$\mathcal{I} \models p \quad \text{if and only if} \quad p \in \mathcal{I}$$

Validity of Compound Formulas

- Is $((q \wedge r) \vee (p \wedge q))$ true in \mathcal{I} ?
- Idea: apply our rule recursively
- For any formulas A and B, \dots
- \dots and any interpretation \mathcal{I}, \dots
 - $\dots \mathcal{I} \models A \wedge B$ if and only if $\mathcal{I} \models A$ and $\mathcal{I} \models B$
 - $\dots \mathcal{I} \models A \vee B$ if and only if $\mathcal{I} \models A$ or $\mathcal{I} \models B$ (or both)
 - $\dots \mathcal{I} \models \neg A$ if and only if $\mathcal{I} \not\models A$.
- For instance



Truth Table

- Semantics of \neg , \wedge , \vee often given as *truth table*:

A	B	$\neg A$	$A \wedge B$	$A \vee B$
f	f	t	f	f
f	t	t	f	t
t	f	f	f	t
t	t	f	t	t

Tautologies

- A formula A that is true in *all* interpretations is called a *tautology*
- also *logically valid*
- also a *theorem* (of propositional logic)
- written:

$$\models A$$

- $(p \vee \neg p)$ is a tautology
- True whatever p means:
 - The sky is blue or the sky is not blue.
 - P.N. will win the 50km in 2016 or P.N. will not win the 50km in 2016.
 - The slithy toves gyre or the slithy toves do not gyre.
- Possible to derive true statements mechanically. . .
- . . . without understanding their meaning!
- . . . e.g. using truth tables for small cases.

Entailment

- Tautologies are true in all interpretations
- Some formulas are true only under certain assumptions
- A entails B , written $A \models B$ if

$$\mathcal{I} \models B$$

for all interpretations \mathcal{I} with $\mathcal{I} \models A$

- Also: “ B is a logical consequence of A ”
- Whenever A holds, also B holds
- For instance:

$$p \wedge q \models p$$

- Independent of meaning of p and q :
 - If it rains and the sky is blue, then it rains
 - If P.N. wins the race and the world ends, then P.N. wins the race
 - If 'tis brillig and the slythy toves do gyre, then 'tis brillig
- Also entailment can be checked mechanically, without knowing the meaning of words.

Question

Given the letters

P – Ola answers none of the questions correctly

Q – Ola fails the exam

Which of the following are tautologies of propositional logic?

- 1 Q
- 2 $\neg Q$
- 3 $P \rightarrow Q$
- 4 $Q \rightarrow (P \rightarrow Q)$

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Triples are true or false **on the basis of what each part refers to.**

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Literals: A literal value is a concrete data item, such as an integer or a string.

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The semantics of typed and language tagged literals is considerably more complex.

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- Forget blank nodes and literals for a while!

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```
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- DL syntax, without namespaces:

loves(romeo, juliet)

Lady(juliet)

Lady \sqsubseteq *Person*

loves \sqsubseteq *knows*

dom(*loves*, *Lover*)

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- Given these, it will be possible to say whether a triple holds or not.

An example “intended” interpretation

- $\Delta^{\mathcal{I}_1} = \left\{ \text{[Image 1]}, \text{[Image 2]}, \text{[Image 3]} \right\}$



An example “intended” interpretation

- $\Delta^{\mathcal{I}_1} = \left\{ \text{romeo}, \text{juliet}, \text{mercutio} \right\}$
- $\text{romeo}^{\mathcal{I}_1} = \text{romeo}$ $\text{juliet}^{\mathcal{I}_1} = \text{juliet}$

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- $\Delta^{\mathcal{I}_1} = \left\{ \text{romeo}, \text{juliet}, \text{person} \right\}$
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- In fact, there is *no way* of ensuring they denote only what we think!

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$$\text{romeo}^{\mathcal{I}_1} = \text{img7} \in \text{Person}^{\mathcal{I}_1} = \Delta^{\mathcal{I}_1}$$

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- Given an interpretation \mathcal{I} , define \models as follows:

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$$\text{Lover}^{\mathcal{I}_1} = \left\{ \text{[Image 1]}, \text{[Image 2]} \right\} \subseteq \text{Person}^{\mathcal{I}_1} = \left\{ \text{[Image 1]}, \text{[Image 2]}, \text{[Image 3]} \right\}$$

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$$\text{Lover}^{\mathcal{I}_1} = \left\{ \text{[img alt="Jennifer Aniston"]}, \text{[img alt="Angelina Jolie"]} \right\} \subseteq \text{Person}^{\mathcal{I}_1} = \left\{ \text{[img alt="Jennifer Aniston"]}, \text{[img alt="Angelina Jolie"]}, \text{[img alt="Will Smith"]} \right\}$$

- $\mathcal{I}_2 \not\models \text{Lover} \sqsubseteq \text{Person}$ because
 $\text{Lover}^{\mathcal{I}_2} = \mathbb{N}$ and $\text{Person}^{\mathcal{I}_2} = \{2, 4, 6, 8, 10, \dots\}$

Finding out stuff about Romeo and Juliet

Statements

$loves(romeo, juliet)$
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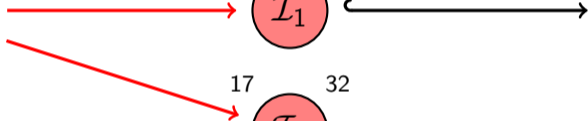
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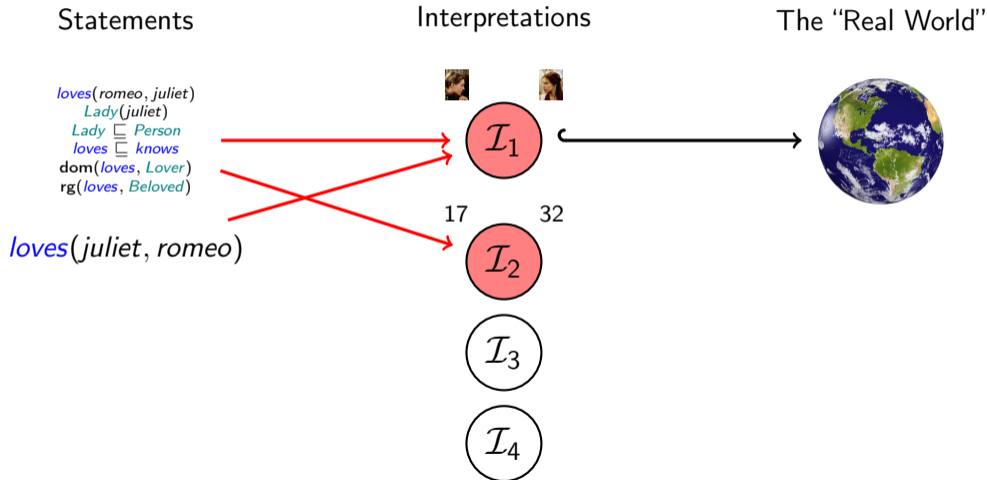
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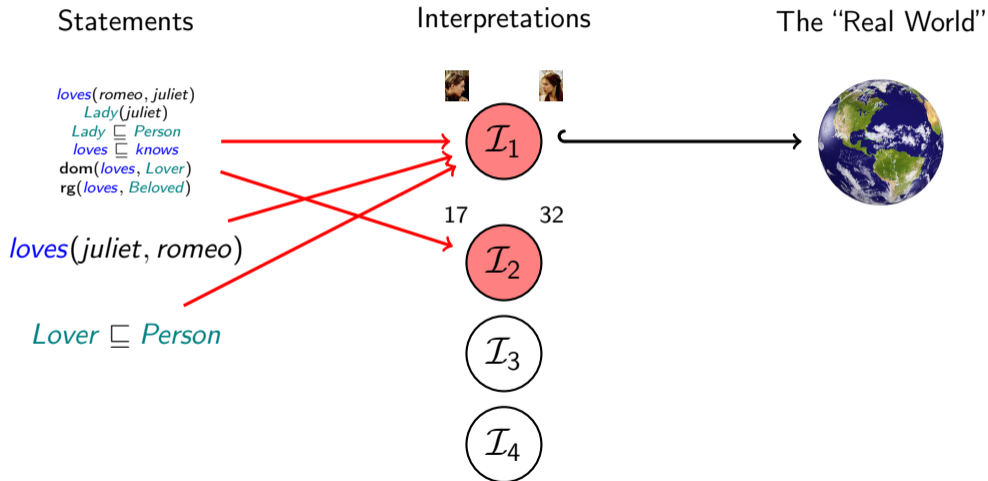
The "Real World"



Finding out stuff about Romeo and Juliet



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Example: Range/Domain semantics

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$$\langle x, y \rangle \in \textit{knows}^{\mathcal{I}_2}, \quad \text{i.e.} \quad x \leq y,$$

we also have

$$x \in \mathbb{N} \quad \text{i.e.} \quad x \in \textit{Beloved}^{\mathcal{I}_2}$$

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- Then $\mathcal{I}_1 \models \mathcal{A}$ and $\mathcal{I}_2 \models \mathcal{A}$

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- in *any* interpretation \mathcal{I} with $\mathcal{I} \models \mathcal{A}$...
- $\text{juliet}^{\mathcal{I}} \in \text{Lady}^{\mathcal{I}}$ and $\text{Lady}^{\mathcal{I}} \subseteq \text{Person}^{\mathcal{I}}, \dots$

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- and therefore $\mathcal{I} \models \text{Person}(\text{juliet})$

Finding out stuff about Romeo and Juliet

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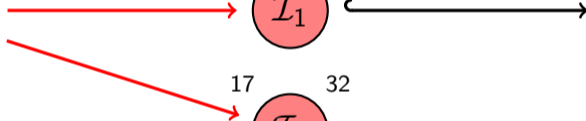
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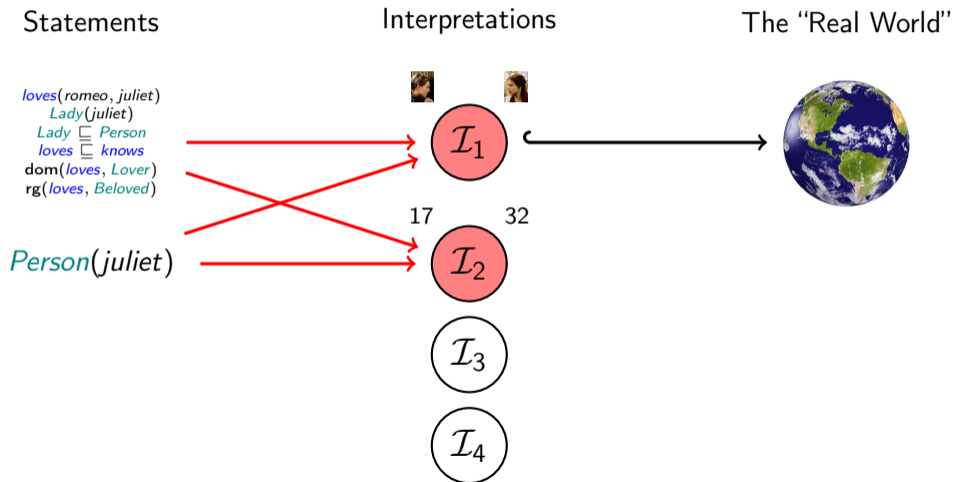
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The "Real World"



Finding out stuff about Romeo and Juliet



Countermodels

- If $\mathcal{A} \not\models T, \dots$
- then there is an \mathcal{I} with
 - $\mathcal{I} \models \mathcal{A}$
 - $\mathcal{I} \not\models T$
- Vice-versa: if $\mathcal{I} \models \mathcal{A}$ and $\mathcal{I} \not\models T$, then $\mathcal{A} \not\models T$
- Such an \mathcal{I} is called a *counter-model* (for the assumption that \mathcal{A} entails T)
- To show that $\mathcal{A} \models T$ does *not* hold:
 - Describe an interpretation \mathcal{I} (using your fantasy)
 - Prove that $\mathcal{I} \models \mathcal{A}$ (using the semantics)
 - Prove that $\mathcal{I} \not\models T$ (using the semantics)

Countermodel Example

- \mathcal{A} as before:

$$\mathcal{A} = \{ \textit{loves}(\textit{romeo}, \textit{juliet}), \textit{Lady}(\textit{juliet}), \textit{Lady} \sqsubseteq \textit{Person}, \\ \textit{loves} \sqsubseteq \textit{knows}, \text{dom}(\textit{loves}, \textit{Lover}), \text{rg}(\textit{loves}, \textit{Beloved}) \}$$

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- Does $\mathcal{A} \models \textit{Lover} \sqsubseteq \textit{Beloved}$?

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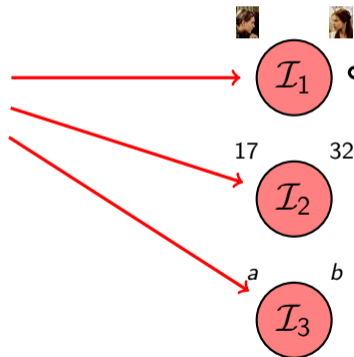
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- $\mathcal{I} \not\models \text{Lover} \sqsubseteq \text{Beloved}$!

Countermodels about Romeo and Juliet

Statements

$loves(romeo, juliet)$
 $Lady(juliet)$
 $Lady \sqsubseteq Person$
 $loves \sqsubseteq knows$
 $dom(loves, Lover)$
 $rg(loves, Beloved)$

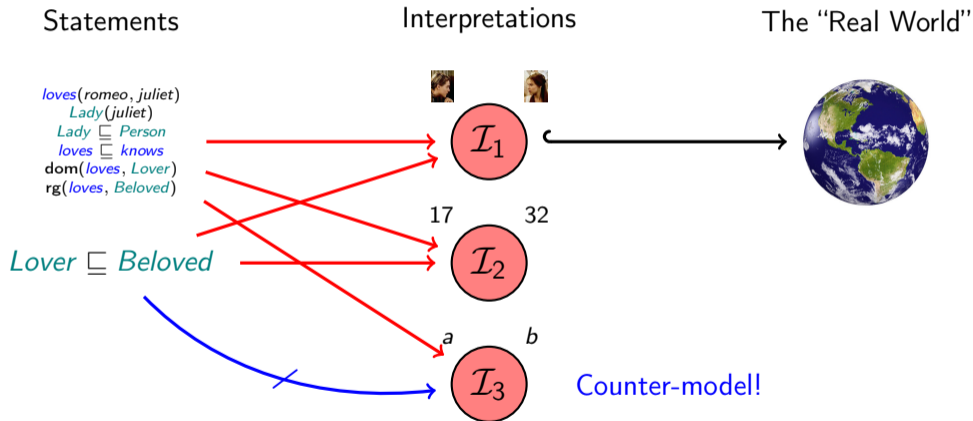
Interpretations



The “Real World”



Countermodels about Romeo and Juliet



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Supplementary reading on RDF and RDFS semantics:

- <http://www.w3.org/TR/rdf-mt/>
- Section 3.2 in Foundations of SW Technologies