

Abstraction Guided Synthesis of Synchronization

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Algorithm overview

- Find a trace that breaks the specification (verification)
- Refine abstraction or modify program?
 - Add an atomicity constraint
 - Refine abstraction
- If no problem traces, implement program!

Simple example program

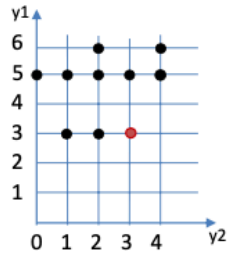
```
T1 {  
1: x += z  
2: x += z  
}
```

```
T2 {  
1: z++  
2: z++  
}
```

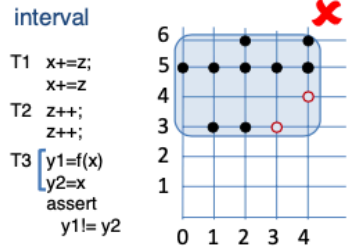
```
T3 {  
1: y1 = f(x)  
2: y2 = x  
3: assert  
   (y1 ≠ y2)  
}
```

```
f(x) {  
  if (x==1)  
    return 3;  
  else if (x==2)  
    return 6;  
  else return 5;  
}
```

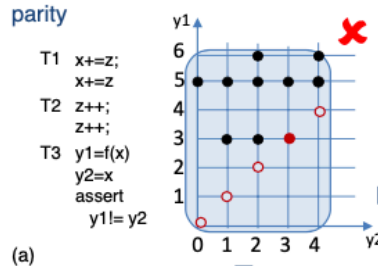
Possible steps in the algorithm



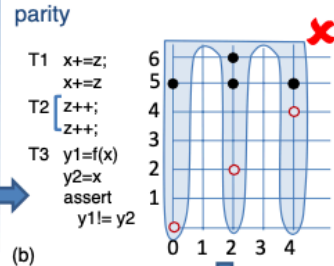
(I)



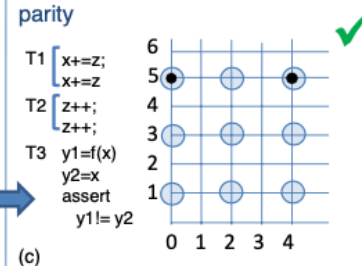
(II)



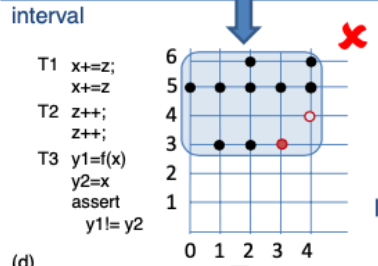
(a)



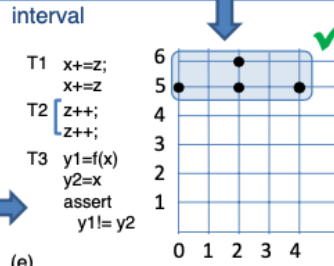
(b)



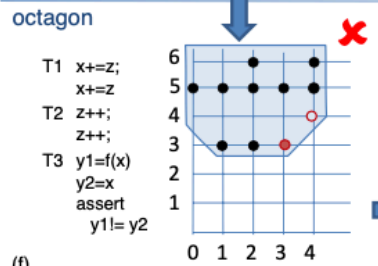
(c)



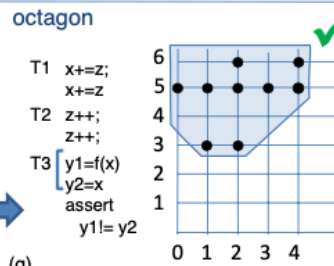
(d)



(e)



(f)



(g)

Example program with full information

- Only one invalid trace
 - `z++; x+=z; y1=f(x); z++; x+=z; y2=x; assert`
- Atomicity constraint:
 - $[y1=f(x), y2=x] \vee [x+=z, x+=z] \vee [z++, z++]$

<pre>T1 { 1: x += z 2: x += z }</pre>	<pre>T2 { 1: z++ 2: z++ }</pre>	<pre>T3 { 1: y1 = f(x) 2: y2 = x 3: assert (y1 ≠ y2) }</pre>	<pre>f(x) { if (x==1) return 3; else if (x==2) return 6; else return 5; }</pre>
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Algorithm 1: Abstraction-Guided Synthesis.

Input: Program P , Specification S , Abstraction α **Output:** Program satisfying S under α

```
1  $\varphi = true$ 
2 while  $true$  do
3    $\Pi = \{\pi \mid \pi \in \llbracket P \rrbracket_{\alpha} \cap \llbracket \varphi \rrbracket, \pi \not\models S\}$ 
4   if  $\Pi$  is empty then return  $implement(P, \varphi)$ 
5    $\pi = \text{select trace from } \Pi$ 
6   if  $shouldAvoid(\pi, \alpha)$  then
7      $\psi = \text{avoid}(\pi)$ 
8     if  $\psi \neq false$  then  $\varphi = \varphi \wedge \psi$ 
9     else abort
10  else
11     $\alpha' = \text{refine}(\alpha, \pi)$ 
12    if  $\alpha' \neq \alpha$  then  $\alpha = \alpha'$ 
13    else abort
14  end
15 end
```

Reference

- Martin Vechev, Eran Yahav, and Greta Yorsh. Abstraction-guided synthesis of synchronization. In POPL, volume 10, pages 327–338, 2010