IN 5400 Solution hints week2 Exercise 1 Linear regression

a) What is the loss function for linear regression?

The squared error

$$J(w,b) = \frac{1}{2m} \sum_{i=1}^{m} (\hat{y}^{(i)} - y(i))^2$$

b) How does gradient descent update the estimate? Give the general formulae.

$$w = w - \lambda \frac{\partial}{\partial w} J(w, b)$$

Exercise 2

c) Given

$$x = \begin{bmatrix} 1\\2\\3 \end{bmatrix}$$
$$y = \begin{bmatrix} 1.5\\2\\2.5 \end{bmatrix}$$

Plot x,y as points in a plot

d) If we start with w = 0 and b = 0, compute the value of the initial loss function.

$$J = 1/6(1.5*1.5+2*2+2.5*2.5) = 12.5/6 = 2.08$$

e) If we start with w = 0 and b = 0, compute the estimates after one iteration if the learning rate is 1.

$$\frac{\partial}{\partial w}J(w,b) = \frac{\partial}{\partial w}\frac{1}{2m}\sum_{i}(wx^{(i)}+b-y^{(i)})^2 = \frac{2}{2m}\sum_{i}(wx^{(i)}+b-y^{(i)})x^{(i)}$$
$$= 1/3(-1*1.5-2*2-2.5*3) = -13/3 = -4.33$$

$$\frac{\partial}{\partial b}J(w,b) = \frac{\partial}{\partial b}\frac{1}{2m}\sum_{i}(wx^{(i)}+b-y^{(i)})^2 = \frac{2}{2m}\sum_{i}(wx^{(i)}+b-y^{(i)})$$
$$= 1/3(-1.5-2-2.5) = -2$$

The estimates are then:

$$w = 0 - (-4.33) = 4.33, b = 0 - (-2) = 2$$