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IN5400 Machine learning for image classification Lecture 5 : Convolutional neural networks Tollef Jahren February 13, 2019





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About today

- Naming convention: Convolutional neural network, ConvNet, CNN
- What is a convolutional neural network?
- The required computation in a convolutional neural network
- Considerations when designing an convolution neural network architecture

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Outline

- Challenges with image classification
- Benchmark: ImageNet
- Fully connected neural network on images
- Convolutional layer
- Convolutional layer hyperparameters
- Convolutional layer example
- Receptive field (Field of View)
- Dilated convolutions
- Pooling
- Depthwise Separable Convolution
- Last layer
- Visualizing and Understanding CNN
- Applications were CNN are used
- Alternative to ConvNet

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Readings

- Text:
- <u>http://cs231n.github.io/convolutional-networks/</u>
- Video:
- <u>https://www.youtube.com/watch?v=bNb2fEVKeEo&index=5&list=PLC1qU-LWwrF64f4QKQT-Vg5Wr4qEE1Zxk</u>

Optional text:

- Receptive field: http://www.cs.toronto.edu/~wenjie/papers/nips16/top.pdf
- Visualizing and Understanding CNN: <u>https://cs.nyu.edu/~fergus/papers/zeilerECCV2014.pdf</u>
- Dilated convolutions: <u>https://arxiv.org/abs/1511.07122</u>
- Optional videos:
- <u>https://www.youtube.com/watch?v=ghEmQSxT6tw</u>
- https://www.youtube.com/watch?v=SQ67NBCLV98

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Challenges with image classification

- Build invariance:
 - Translation
 - Occlusion
 - Illumination
 - View angle variations
 - Deformation
 - Background Clutter
 - Interclass variation

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Building invariance

- Translation
- Occlusion
- Illumination



(all 3 images have same L2 distance to the one on the left)

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• View angle variations



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• Deformation



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• Background Clutter



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• Interclass variation





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The ImageNet challenge

- The images classification challenge
- Dataset
 - 1,431,167 images
 - 1,000 classes



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Fully connected neural network on images

- Most image applications are absolute position invariant.
- A fully connected network will have too many parameters and not able to scale to normal size images and generalize

 $z^1 = W^T x$ $a^1 = g(z^1)$







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Convolutional vs correlation

- **Note**: We will be using **cross correlation**, although we will call it **convolution**. As the network weights are learned there is no real difference.
- 2D cross correlation:

$$z[p,q] = w \star x = \sum_{r=-K}^{K} \sum_{s=-K}^{K} w[r,s] \cdot x[p+r,q+s]$$

• 2D convolution:

$$z[p,q] = w * x = \sum_{r=-K}^{K} \sum_{s=-K}^{K} w[r,s] \cdot x[p-r,q-s]$$

https://www.youtube.com/watch?v=C3EEy8adxvc

Convolution example:

- Input image *x* with shape [4, 4]
- Weight matrix *w* with shape [3, 3]
- Output feature map *z* with shape [2, 2]

$$z[p,q] = w \star x = \sum_{r=-K}^{K} \sum_{s=-K}^{K} w[r,s] \cdot x[p+r,q+s]$$

<i>x</i> =	1	2	3	4		1	2	1			
	2	4	1	2	<i>w</i> =			?	Γ		
	1	3	2	1		2	1	2	$Z \equiv$?	T
	1	2	3	1		1	2	1			



Convolution example:



$$z[0,0] = 1 \cdot 1 + 2 \cdot 2 + 3 \cdot 1$$

+ 2 \cdot 2 + 4 \cdot 1 + 1 \cdot 2
+ 1 \cdot 1 + 3 \cdot 2 + 2 \cdot 1
= 27

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x =								
1 2 3 4								
2	4	1	2					
1	3	2	1					
1	2	3	1					
1	2	3	4					
2	4	1	2					
1	3	2	1					
1	2	3	1					
1 2 3 4								

1	2	3	4
2	4	1	2
1	3	2	1
1	2	3	1

1	2	3	4
2	4	1	2
 1	3	2	1
1	2	3	1





1	2	1
2	1	2
1	2	1

1	2	1
2	1	2
1	2	1

z =

27	

27	33

27	33
29	

27	33
33	29

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Convolutional layer





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Convolutional layer

• We are convolving /sliding the filter spatially across the input image and computing the dot product.



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• The input volume and the filer has always the same depth (blue value).



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- The activation from a local region is computed:
- $z = w^T x + b$



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 If we filter the input volume 6 times using 5x5x3 filters, we get an output volume with 6 channels (depth)



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Activations

• We use an activation function separately on all elements of the output volume



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Convolution neural network hyperparameters

- Stride
- Padding
- Kernel (filter/weights) size

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Stride

- Stride is the **spatial step length** in the convolution operation.
- Example: Input volume 7x7x1, kernel (filter) size 3x3x1
- The stride is an important parameter for determining the spatial size of the output volume





Stride

• What about stride equal to 3?



Padding

- The output volume can get a lower spatial dimension compared to the input volume. We can solve this by padding the input volume. Common to use zero padding.
- Abbreviations: Stride (*S*), spatial filter size (*F*), input spatial size (N^i), output spatial size (N^{i+1}) and padding (*P*)
- For S = 1, we can achieve $N^0 = N^1$ by selecting P equal to:

$$P = \frac{(F-1)}{2}$$

• Calculation of the spatial output size:

$$N^{i+1} = \frac{N^i - F + 2P}{S} + 1$$

0	0	0	0	0	0		
0							
0							
0							
0							

Padding examples

• Remember:
$$N^{i+1} = \frac{N^i - F + 2P}{S} + 1$$

• Parameters:

$$- N^0 = 7$$

$$- P = 0$$

$$- F = 3$$

• Stride 1
$$\rightarrow \frac{7-3+2\cdot 0}{1} + 1 = 5$$

• Stride 2
$$\rightarrow \frac{7-3+2\cdot 0}{2} + 1 = 3$$

• Stride 3
$$\rightarrow \frac{7-3+2\cdot 0}{3} + 1 = 2.33$$

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Padding examples

• Remember, to keep $N^i = N^{i+1}$ with S = 1 use:

$$P = \frac{(F-1)}{2}$$

- $F = 3 \rightarrow \text{zero pad with } 1$
- $F = 5 \rightarrow$ zero pad with 2
- $F = 7 \rightarrow \text{zero pad with } 3$

Kernel size (filter bank)

- Each filter has a size of $[F_c, F_h, F_w]$ e.g. [3, 5, 5]
- Multiple filters (F_N) can be applied at each layer and the filter bank are represented by a 4-D tensor
 - $[F_N, F_c, F_h, F_w]$
- F_N corresponds to the depth of the next layer
- This is a practical representation and used by many deep learning frameworks.


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0 0 0 0 0 0 0

A one-layer, two-filter network



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0 0 0 0 0 0 0

A one-layer, two-filter network



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A one-layer, two-filter network



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A one-layer, two-filter network



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Receptive field (Field of View)

• How much of the input image is available for a particular neuron?



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How large area influence the end result?

- With a convolutional network the receptive field increase with each layer
- 3 inputs influence each node in the first hidden layer



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How large area influence the end result?

- With a convolutional network the receptive field increase with each layer
- 3 inputs influence each node in the first hidden layer
- 5 influence the next



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How large area influence the end result?

- With a convolutional network the receptive field increase with each layer
- 3 inputs influence each node in the first hidden layer

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- 5 influence the next
- 7 influence the next



The receptive field grow with k-1 for each layer

- Two 3x3 filters give equal receptive field as one 5x5 filer
- Should we use 3x3 or 5x5?



Parameter efficiency

- Two 3x3 filters give equal receptive field as one 5x5 filter
- Should we use 3x3 or 5x5 filters?
- Assumption:
 - The filter count in all layers are $(F_c = F_c^i = F_c^{i+1})$ and we don't account for biases.
- Number of parameters:
 - 3x3 filter $\rightarrow (3 \cdot 3 \cdot F_c) \cdot F_c + (3 \cdot 3 \cdot F_c) \cdot F_c = 18F_c^2$
 - 5x5 filter $\rightarrow (5 \cdot 5 \cdot F_c) \cdot F_c = 25F_c^2$
- Note: Many 3x3 filters will lead to a larger memory footprint during training as the system must store the values for backpropagation.

Smaller spatial filter size is more parameter efficient

- A network with many parameters generally need more training data and computation time
- A larger receptive field per parameter is good
- More layers can give more reuse



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Strided convolutions

- By skipping positions we can cover a larger area with less computation
- The effect of the receptive field for the next layer is important



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The effect of strided convolutions

- We still cover the whole input
- With stride of two we have increased the receptive field from 5→7 in layer 2



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The effect of strided convolutions

- Receptive field : *R*
- Spatial filter size: F
- Stride: S
- Layer index: $\mathbf{k} \in \{1, 2, 3, \dots, n\}$ $R^{k} = R^{k-1} + \left[\left(F^{k} - 1 \right) \cdot \prod_{i=1}^{k-1} S^{i} \right]$
- Essentially all the following layers will have a receptive field multiplied by S^k



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Theoretical vs effective receptive field

 "Effective receptive field only takes up a fraction of the full theoretical receptive field"



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With strides, spatial dimensions will become smaller

• Usually some of the of the network capacity is preserved through an increasing number of channels



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Can the network still remember positions?

- Yes, the network can still encode positional information in the **depth** dimension
- A network can pass positional information (right, left etc.) to different channels





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Dilated convolutions

• Larger receptive field, without reducing spatial dimension or increasing the parameters



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Dilated convolutions

- Skipping values in the kernel
- Same as filling the kernel with every other value as zero
- Still cover all inputs
- Larger kernel with no extra parameters



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A growing dilation factor can give similar effect as stride

- With a constant dilation factor you get the similar effect as using a larger kernel ٠
- With growing dilation factor you can get an even larger receptive field, while still ٠ covering all inputs



Fisher Yu, Vladlen Koltun (2016) Multi-scale Context Aggregation by Dilated Convolutions

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Growing dilation factor

- 1-D example:
 - Filter size: F = 3
 - Layer: $k \in \{1, 2, 3, ..., n\}$
 - Receptive field : $R^k = 2^{k+1} 1$
 - Dilation factor: $l = 2^{k-1}$



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Pooling

- Spatial reduction and forcing invariance
- Operates over each activation map (channel) independently
- No learnable weights
- Two methods:
 - Max pooling
 - Average pooling



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Max pooling

- A strided maximum filtering •
- Choosing the maximum value ٠ inside the kernel

	Sing	gle d	epth	slice
x	1	1	2	4
	5	6	7	8
	3	2	1	0
	1	2	3	4
				У

max pool with 2x2 filters

and stride 2

6	8
3	4

Max-pooling: invariance built-in

- With max-pooling you explicitly ٠ remove some spatial information
- This can help both position and ٠ rotation invariance



Single depth slice

1

1

Х



У

max pool with 2x2 filters and stride 2

6	8
3	4

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Max-pooling have some important problems

- Even if we want our final results to be positional invariant, we may need positional information in the earlier representations
- Only a small part of the network is updated with gradients each step (learning slower)
- We calculate a lot of values that is not "used"





Х



max pool with 2x2 filters and stride 2

6	8
3	4

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Depthwise Separable Convolution

- Depthwise separable convolution is an efficient convolutional layer. It is composed of two steps:
 - Depthwise convolution
 - Pointwise convolution
- Depthwise convolution :
 - Input volume of shape $[N_c, N_h^i, N_w^i]$
 - We use N_c different kernels of shape $[F_c = 1, F_h, F_w]$ on the input channels individually
 - Output volume [N_c , N_h^{i+1} , N_w^{i+1} ,]



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Pointwise convolution

- Pointwise convolutions are ordinary convolutions with :
 - kernels of shape: [F_c , $F_h = 1$, $F_w = 1$]
 - Filter bank: $[F_N, F_c, 1, 1]$



Depthwise Separable Convolution – Summary

- Depthwise separable convolution = Depthwise convolution + Pointwise convolutions
- Lets compare the number of parameters in a depthwise separable convolution and a convolutional layer:

 $[F_N = 512, F_c = 256, F_h = 3, F_w = 3]$

• Parameters in a depthwise separable convolution:

 $- F_{c} \cdot 1 \cdot F_{h} \cdot F_{w} + F_{N} \cdot F_{c} \cdot 1 \cdot 1 = 133,376$

• Parameters in a **convolutional layer**:

 $-F_N \cdot F_c \cdot F_h \cdot F_w = 1,179,648$

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Structure of the last layer(s) – dense layer

- At the end we normally have a feature map of some spatial size and channels (N_c, N_w, N_h) .
- Assume we have a 3 class classification problem and want our output to be a vector of length 3.
- We can flatten the input feature map and stack dense layers



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Structure of the last layer(s) – fully convolutional

- We can make sure the last layer has the same number of channels as we have classes.
- A 3 class problem yields $N_c = 3$
- Average over the spatial dimensions N_w and N_h

$$N_h$$

$$N_w$$

$$N_c = 3$$

$$N_h = 1$$

$$N_c = 3$$

$$N_w = 1$$
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Visualizing and Understanding ConvNets

- AlexNet, the winner of the ImageNet classification challenge 2012.
- Filter bank of size (11x11x3)x96 for the first convolutional layer:
- Visualizing the learnt weights



Figures copyright Alex Krizhevsky, Ilya Sutskever, and Geoffrey Hinton, 2012.



Visualizing and Understanding deeper layers

- Looking at the filer coefficient directly at deeper layer is not meaningful.
- Visualization with Deconvnet



Zeiler M.D., Fergus R. (2014) Visualizing and Understanding Convolutional Networks



Hierarchical learning

- A convolution neural network is built up as a hierarchy were the complexity (abstraction) is increased by depth.
- A hierarchical structure is parameter efficient



Reuse of features

- Each filter kernel is applied at all spatial positions
- Features are reused:
 - edges, fur, eye, grass
- Reuse instead of retraining many times
 over



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Data driven

- A convolutional neural network still "remembers" shapes, rotation, size.
- No fundamental understanding of the concept "cat"

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Application of convolutional neural network

- Classification
- Detection
- Segmentation
- Reinforcement learning (game playing)
- Image captioning

Classification

Images for ImageNet ٠







ultimate (sport) hurling flag football association football rugby sevens



harness racing

skijoring

carting

arena football indoor american football arena football canadian football american football women's lacrosse





ninc-ball blackball (pool) trick shot eight-ball straight pool



container ship	motor scooter	leopard
container ship	motor scooter	leopard
lifeboat	go-kart	jaguar
amphibian	moped	cheetah
fireboat	bumper car	snow leopard
drilling platform	golfcart	Egyptian cat



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Detection







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Segmentation





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Reinforcement learning (game playing)





Image captioning

Describes without errors



A person riding a motorcycle on a dirt road.



Two dogs play in the grass.



Somewhat related to the image

on a ramp.



A group of young people playing a game of frisbee.



Two hockey players are fighting over the puck.



A little girl in a pink hat is blowing bubbles.

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Alternative to ConvNet

Note: Not part of curriculum

- Rotation equivariant vector field networks
 - https://arxiv.org/abs/1612.09346
- Capsule Network
 - https://arxiv.org/abs/1710.09829



CNN vs dense net on cifar10



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