

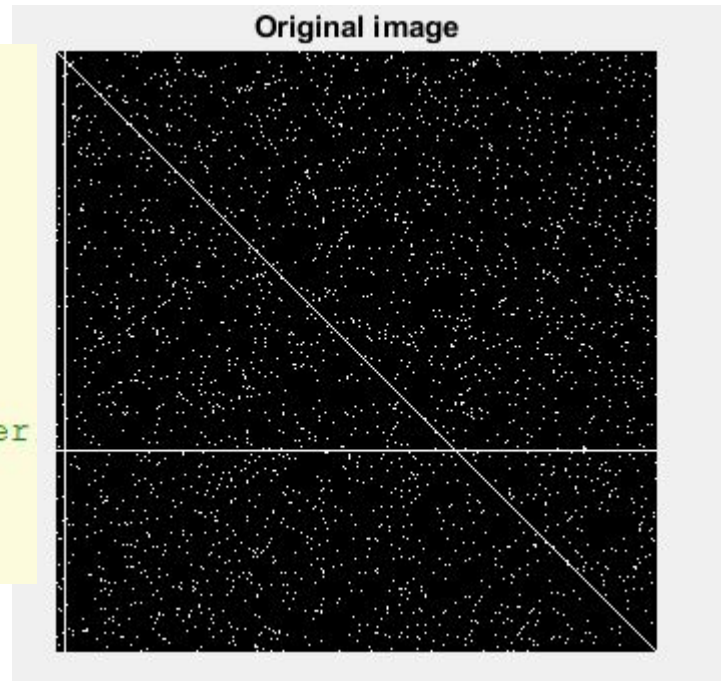


# Week 3

I will go through the weekly exercises at 14:15

# Make a simple image, to see how Hough works

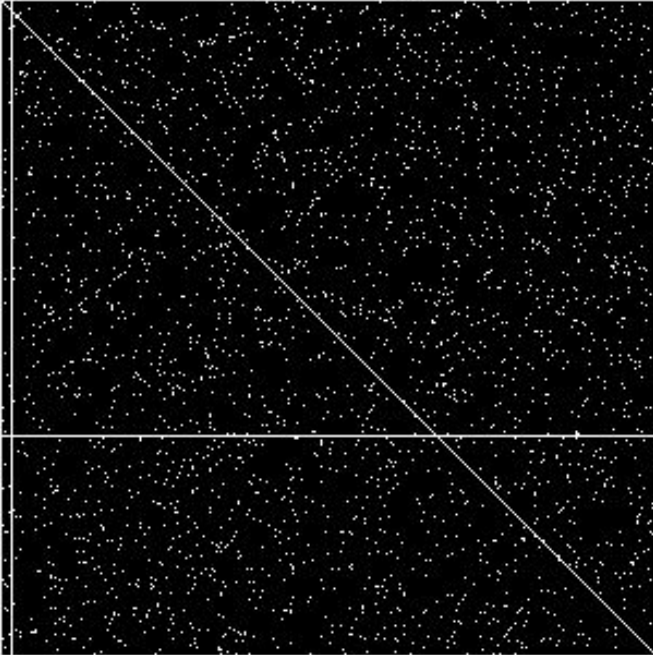
```
% Trying to understand the Hough transform
d=300;
img=eye(d); %make a diagonal matrix
img(1:d,5)= 1; % add a vertical line
img(200,1:d)=1; % add a horizontal line
u = rand(d); %matrix elements ~ uniform(1)
noise = u>0.97;% only use a portion to make noise
img = (img + noise)>0; % add noise and img together
figure(),imshow(img,[])
title('Original image');
```



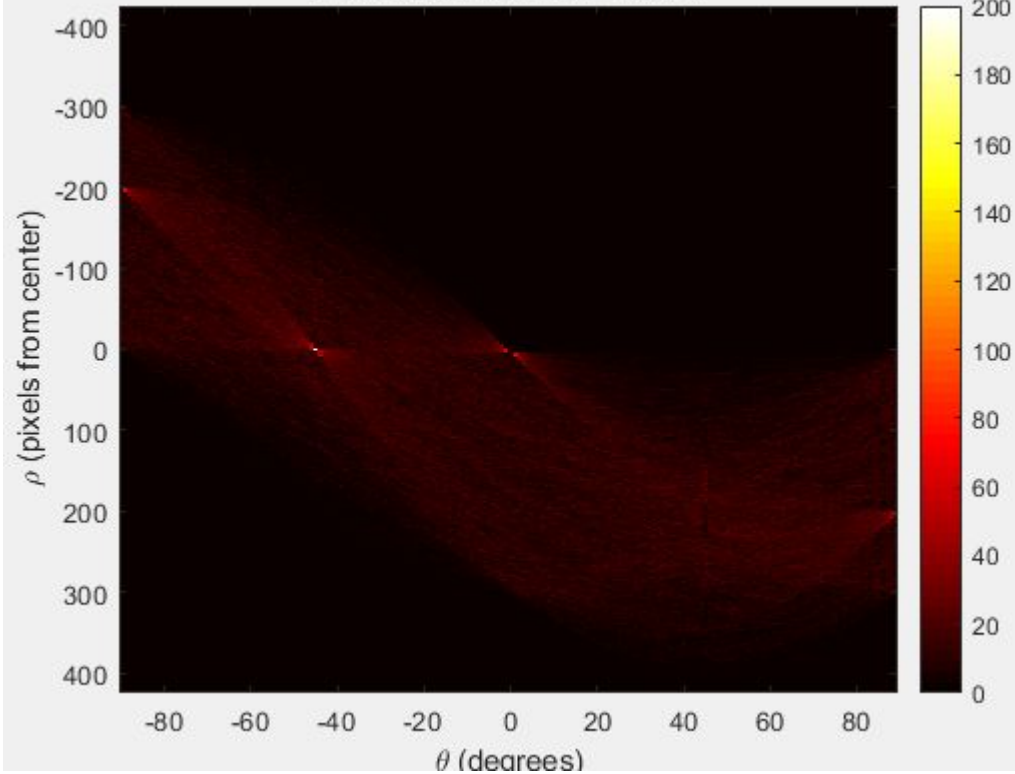
# How does the image look in Hough-space

```
% Compute the Hough transform for the edge image  
[H,theta,rho] = hough(img);
```

Original image



Hough transform of image 1



# First look at the two peaks in the middle

First lets look at (0,4). What line does this correspond to?

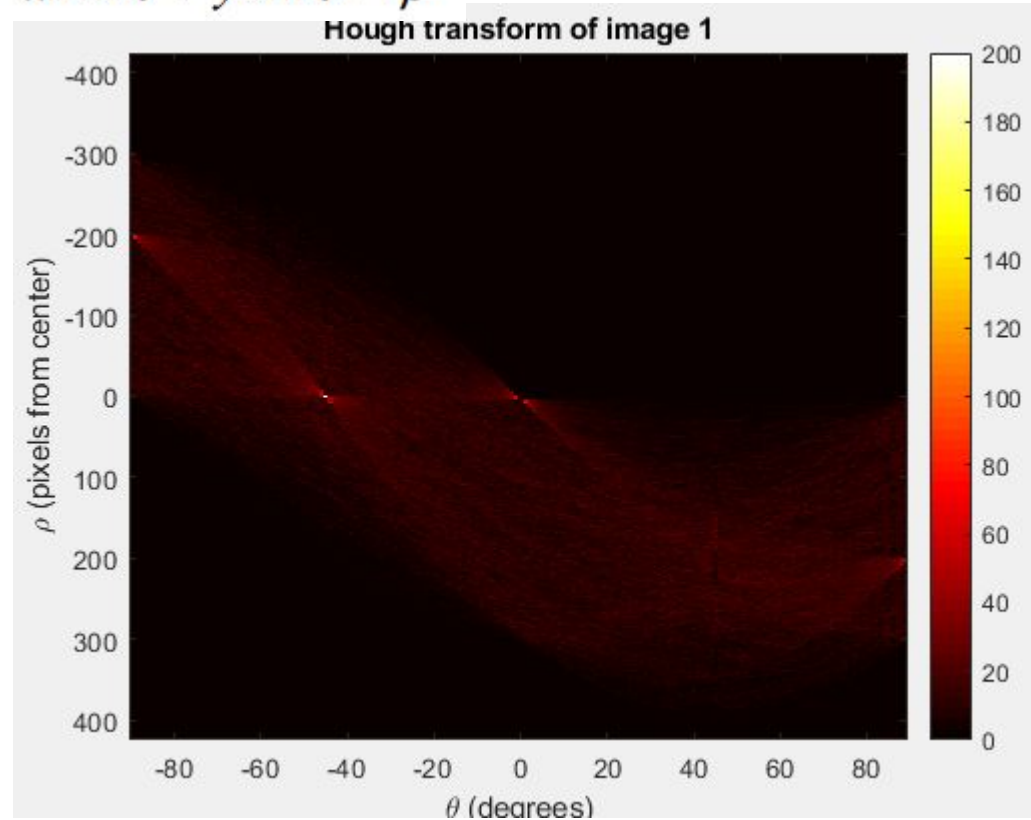
We have the normal representation of a line  $x \cos \theta + y \sin \theta = \rho$



This would be a line perpendicular to the

vector  $x \cos(0) + y \sin(0) = 4$

$$x = 4$$



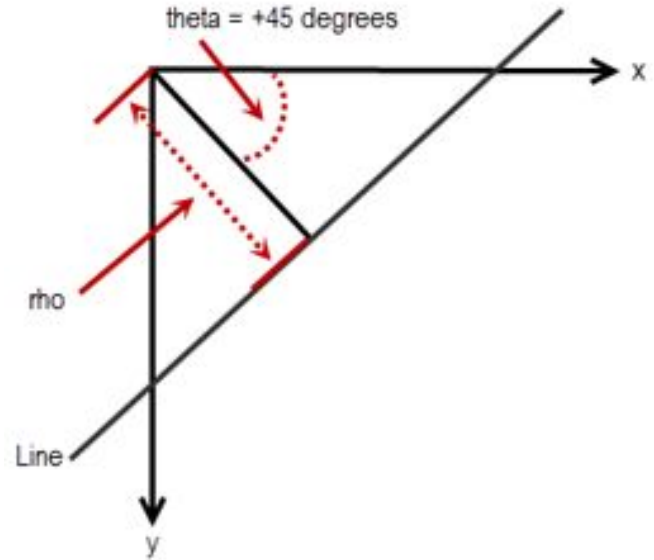
# First look at the two peaks in the middle

First lets look at (0,4). What line does this correspond to?

We have the normal representation of a line  $x \cos \theta + y \sin \theta = \rho$

This would be a line perpendicular to the  
vector  $x \cos(0) + y \sin(0) = 4$   
 $x = 4$

Remember that Matlab uses lefthandsystem  
and origo is in (1,1)

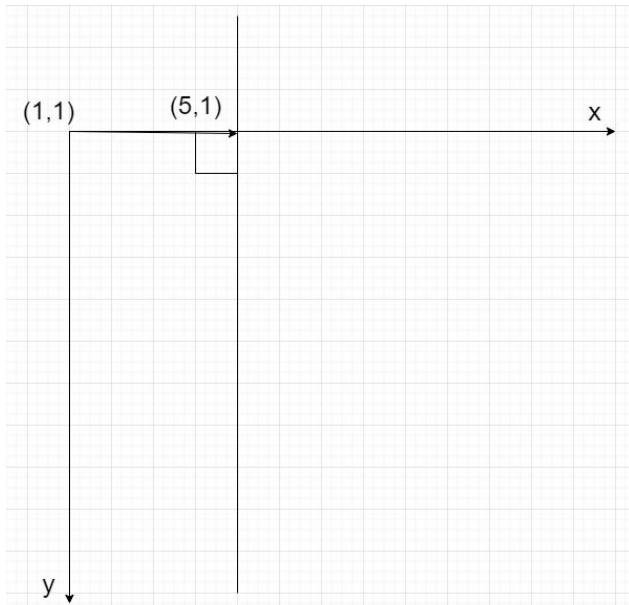


# First look at the two peaks in the middle

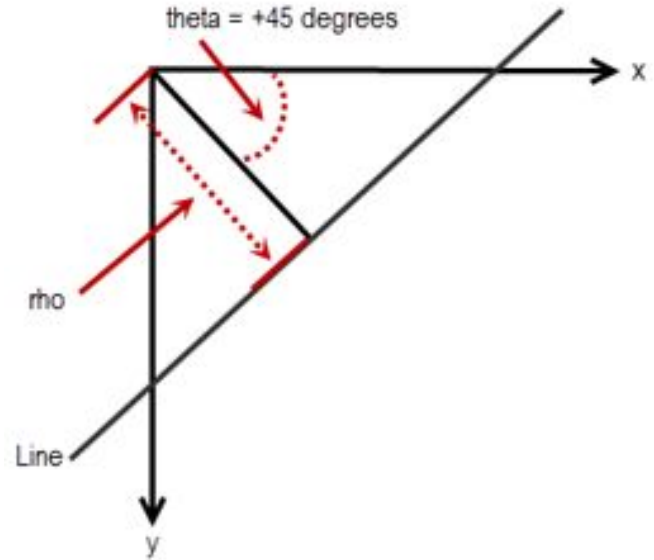
First lets look at (0,4). What line does this correspond to?

We have the normal representation of a line  $x \cos \theta + y \sin \theta = \rho$

This would be a line perpendicular to the vector  $x \cos(0) + y \sin(0) = 4$   
 $x = 4$



Remember that Matlab uses lefthandsystem



# First look at the two peaks in the middle

What line does this correspond to?

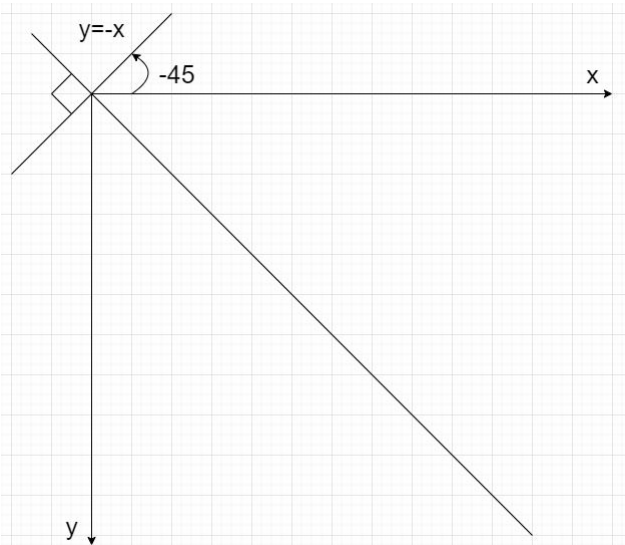
We have the normal representation of a line  $x \cos \theta + y \sin \theta = \rho$



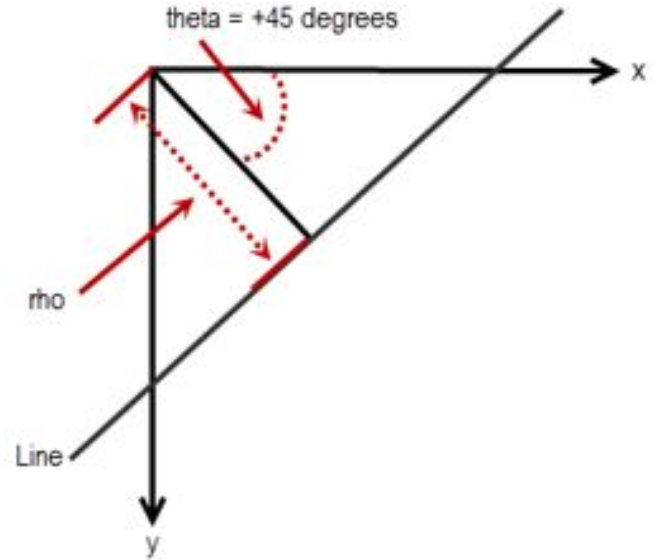
Next lets look at (-45,0)

This would be a line perpendicular to the  
line  $x \cdot \cos(-45) + y \cdot \sin(-45) = 0$

$$y = -x$$

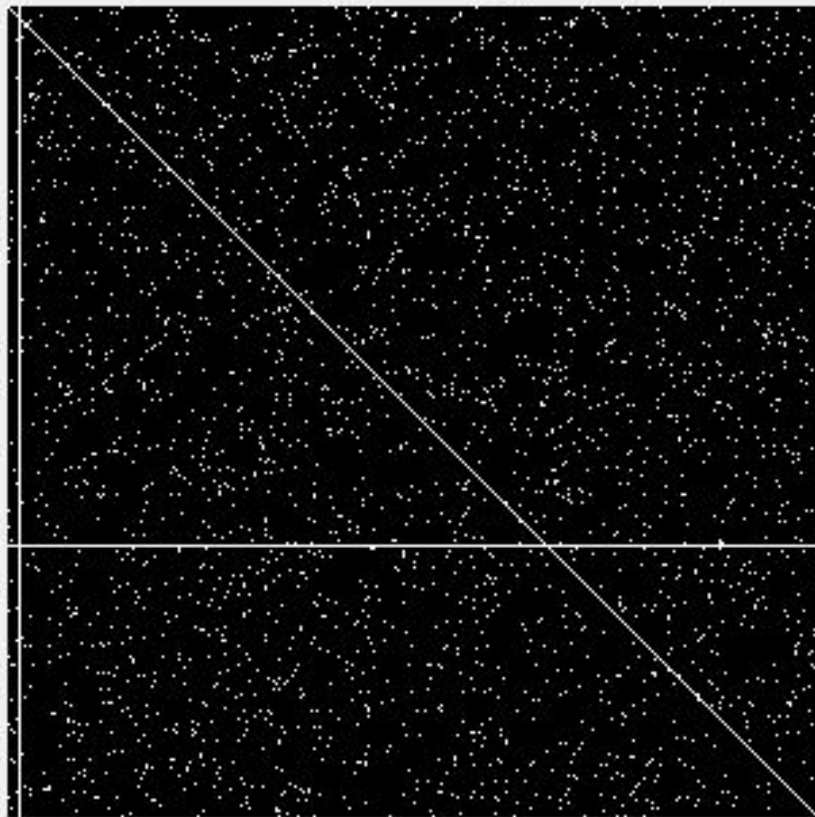


Remember that Matlab uses lefthandsystem

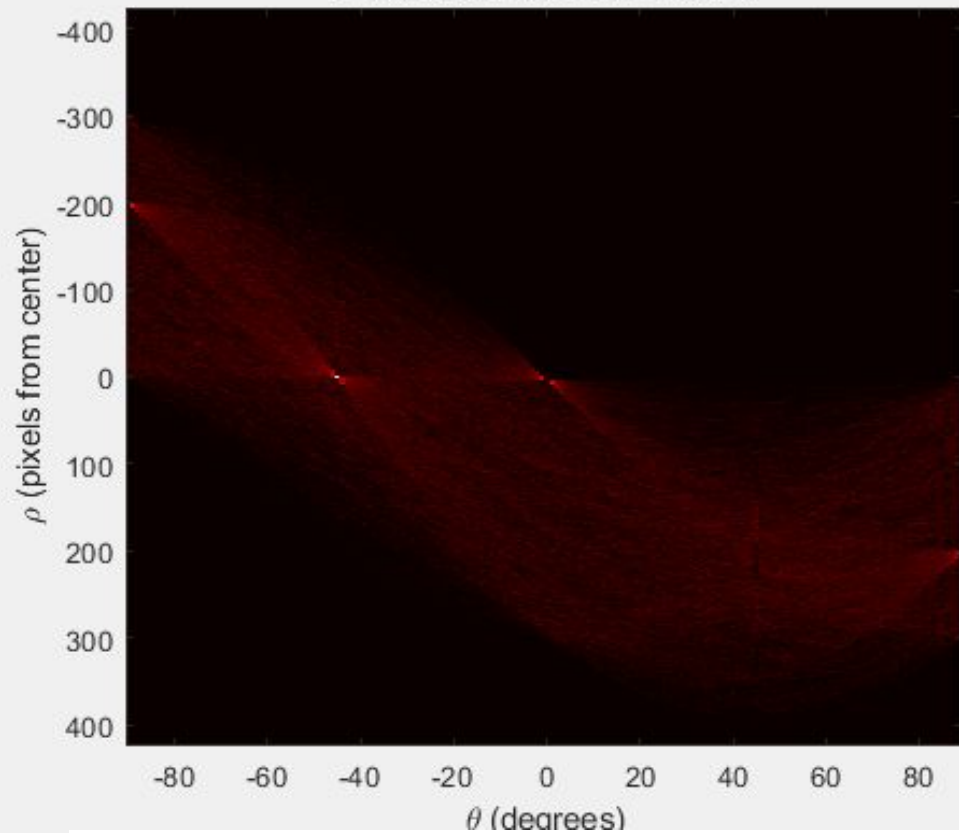


The last line is the horizontal line

Original image



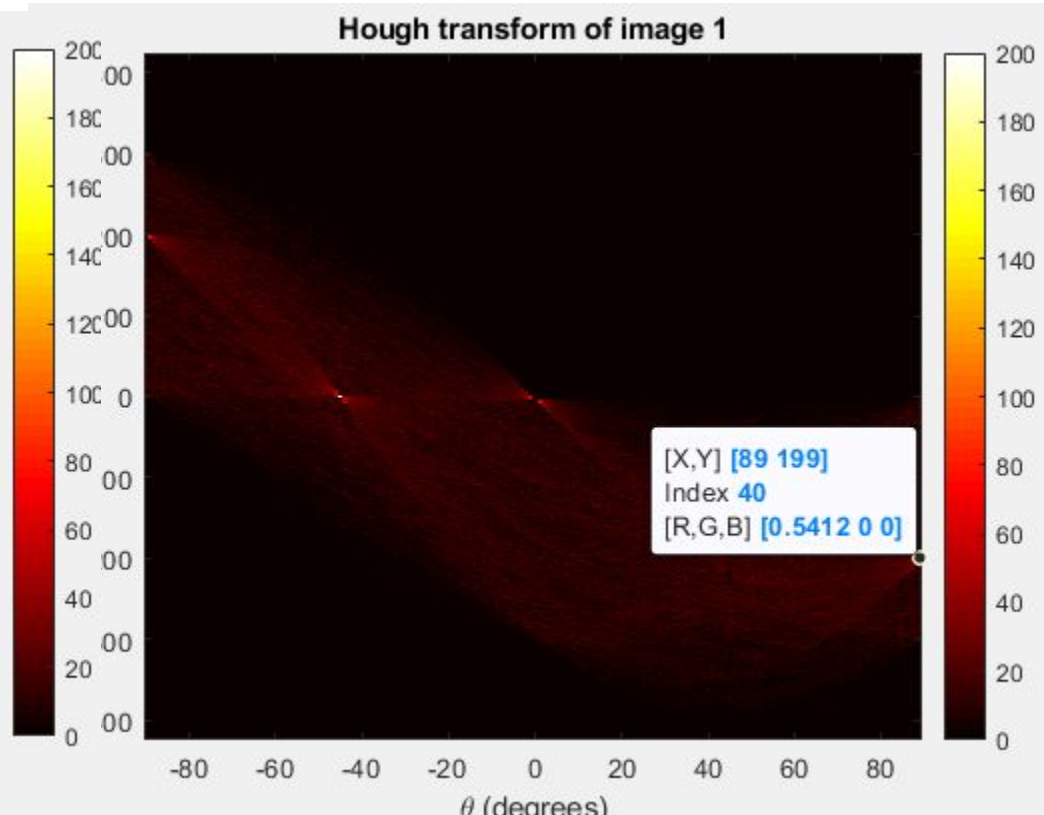
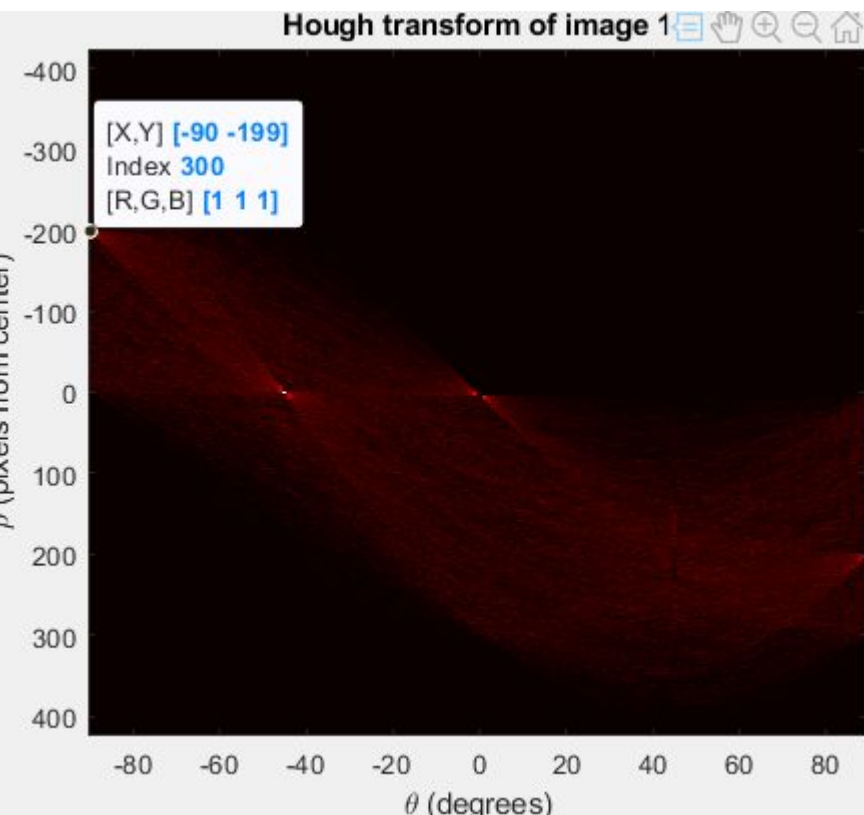
Hough transform of image 1






# The last line

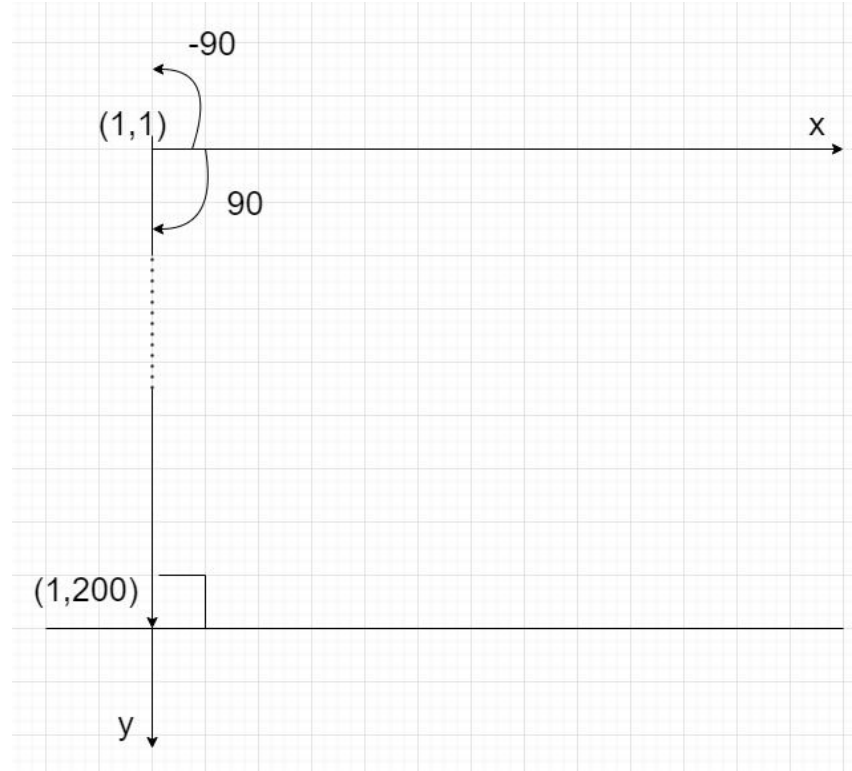
Has two peaks  $(-90, -199)$  and  $(90, 199)$



# The last line

Has two peaks  $(-90, -199)$  and  $(90, 199)$


$$\begin{aligned}x\cos(-90) + y\sin(-90) &= -199 \\x*0 + y*(-1) &= -199 \\y &= 199\end{aligned}$$

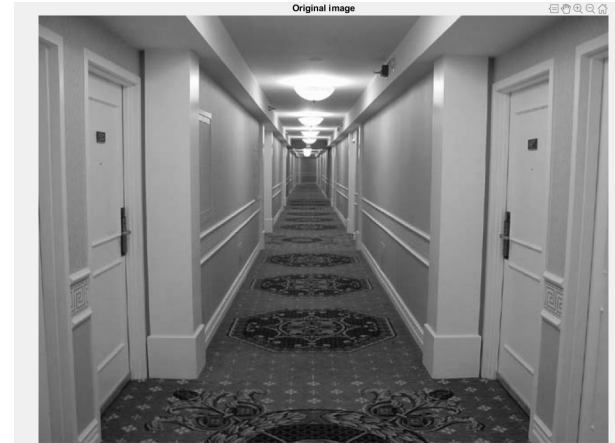


$$\begin{aligned}x\cos(90) + y\sin(90) &= 199 \\x*0 + y &= 199 \\y &= 199\end{aligned}$$

# Load image and find gradient

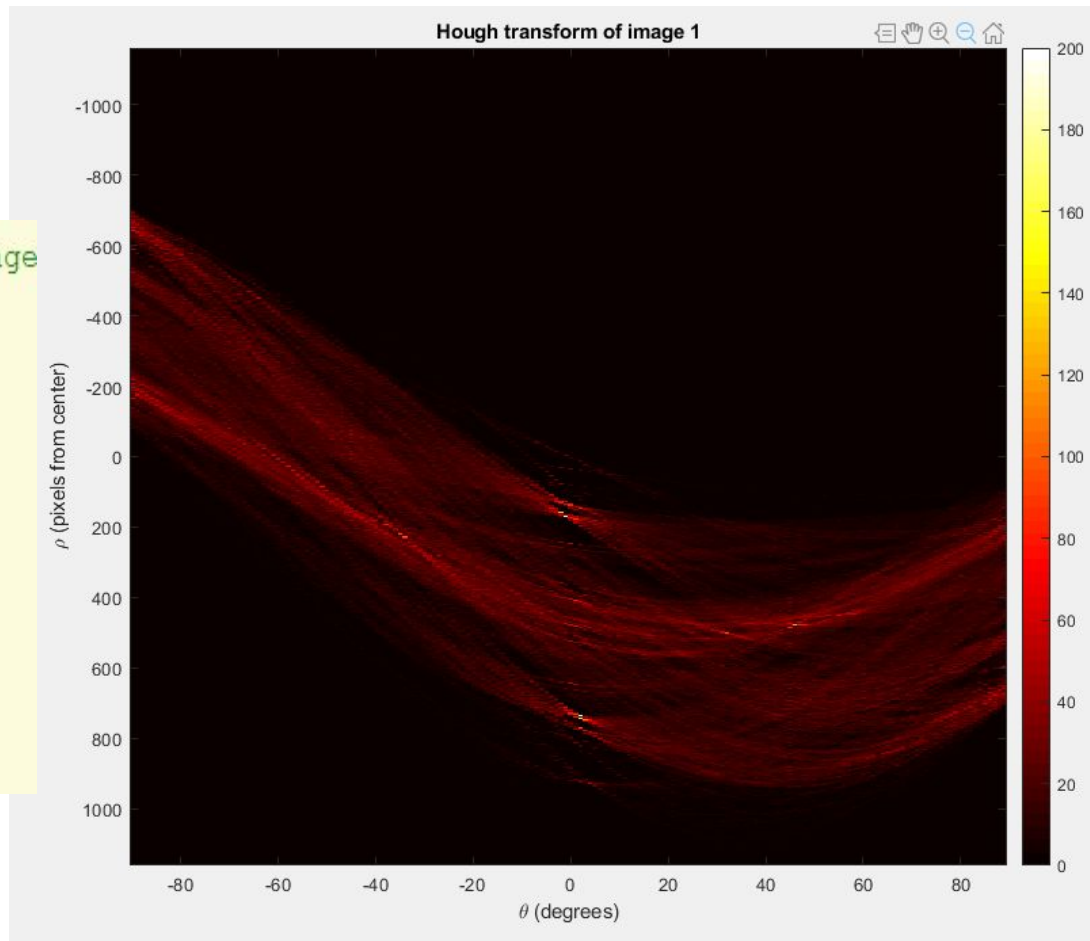
```
% Load and show the corridor image
img=imread('corridor.png');
img=double(rgb2gray(img));
figure(),imshow(img,[])
title('Original image');

% Lets filter the original image with a
% Adjusting the threshold will affect th
% detect.
thresh = 20;
img_edge = edge(img, 'Sobel', thresh);
figure(),imshow(img_edge,[])
title('Sobel magnitude');
```



# Compute Hough

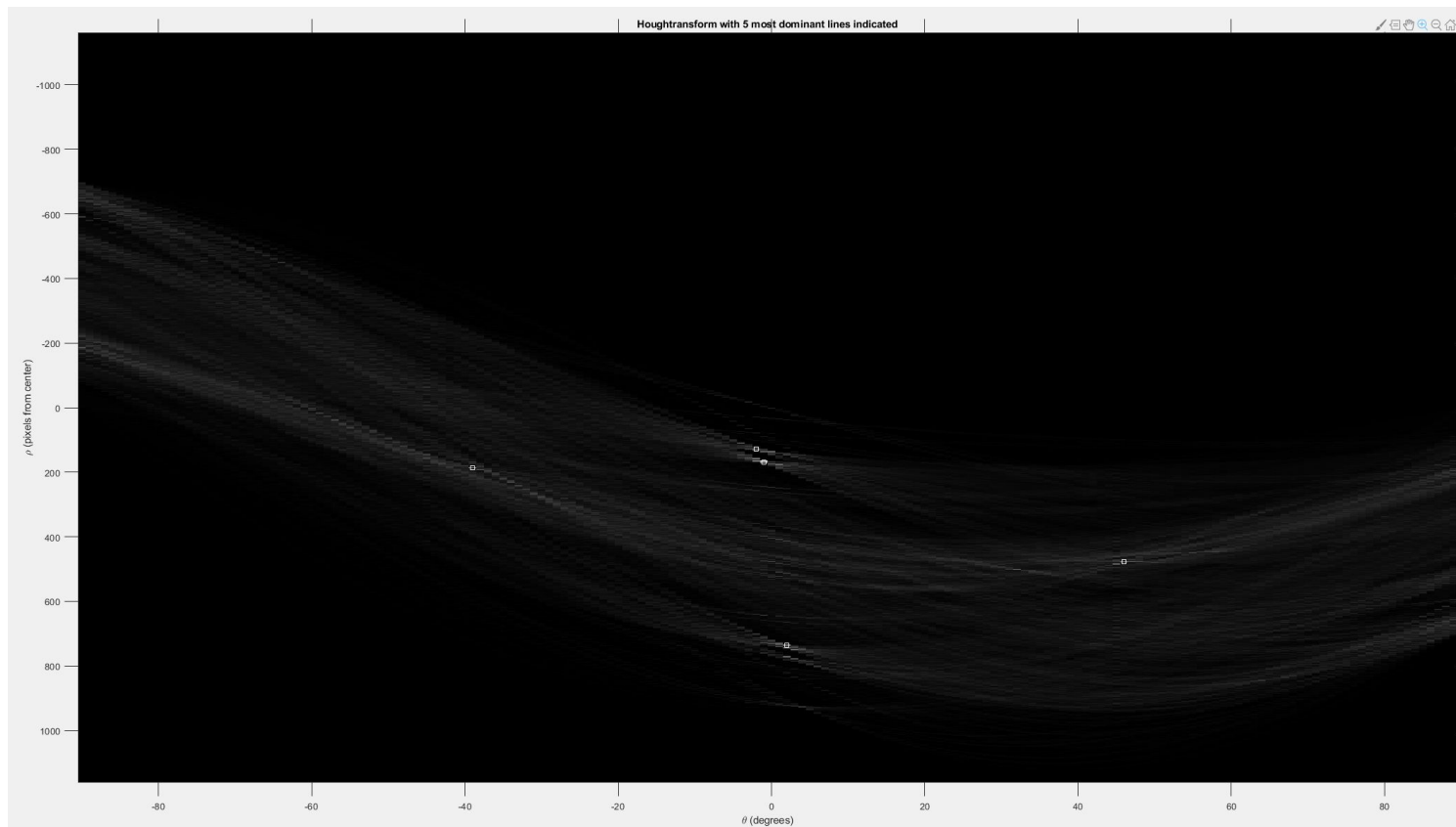
```
% Compute the Hough transform for the edge image
[H,theta,rho] = hough(img_edge);
% Display the accumulator matrix
figure(15);clf
imagesc(theta,rho,H);
colormap hot
colorbar
caxis([0 200 ])
xlabel('\theta (degrees)')
ylabel('\rho (pixels from center)')
title('Hough transform of image 1')
```



# We want to show the top 5 best candidates for lines

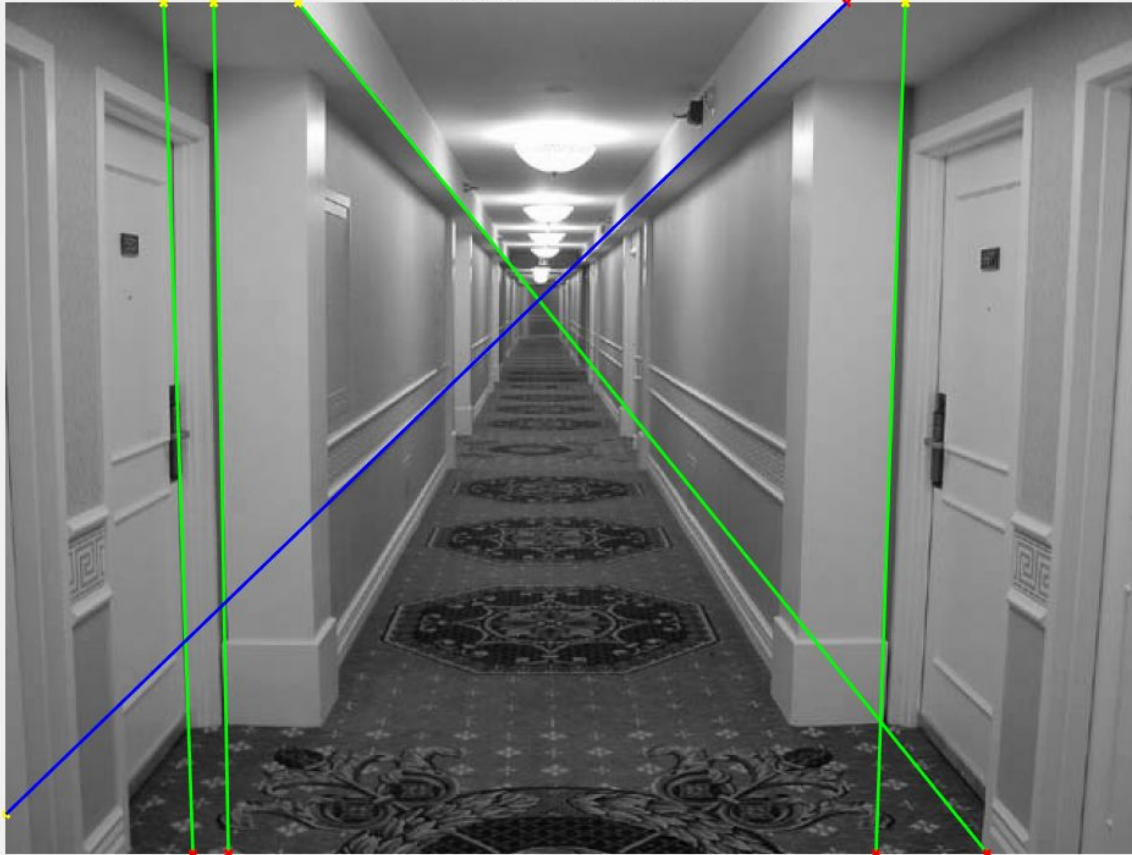


use matlabs inbuilt function  
`houghpeaks(H,numpeaks)`



# Plot the lines we found

Image with lines found indicated



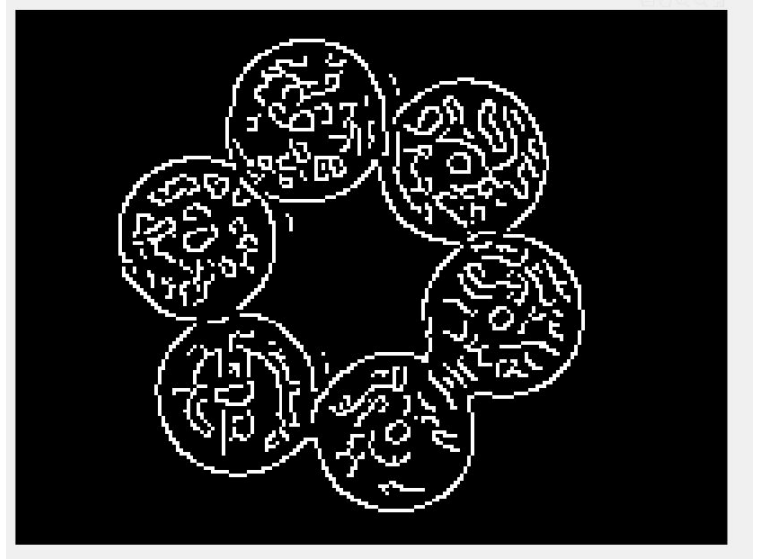
# Exercise - Hough with circles



We have an image consisting of 6 coins, they all have the same radius



Canny edge detector



A circle in the xy-plane is given by

$$(x - x_c)^2 + (y - y_c)^2 = r^2$$



So we have a 3D parameter space. What size, what

### A simple 3D accumulation procedure:

set all  $A[x_c, y_c, r] = 0$ ;

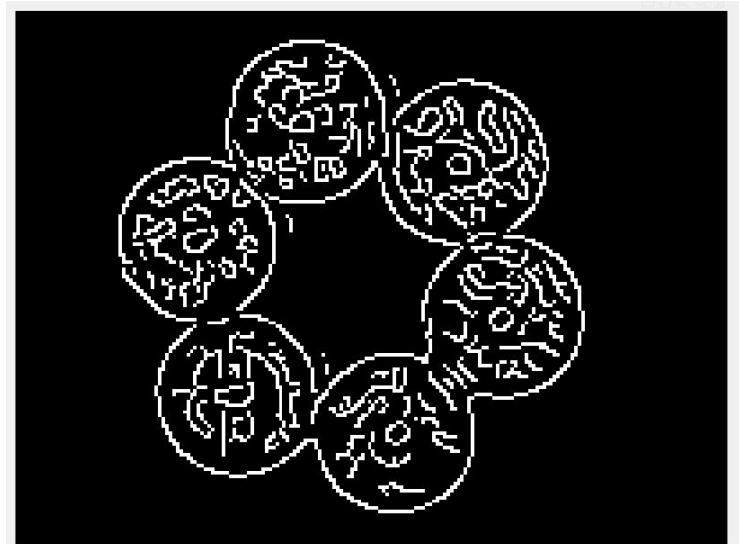
for every  $(x, y)$  where  $g(x, y) > T$

for all  $x_c$

for all  $y_c$

$r = \text{sqrt}((x - x_c)^2 + (y - y_c)^2)$ ;

$A[x_c, y_c, r] = A[x_c, y_c, r] + 1$ ;





A circle in the xy-plane is given by

$$(x - x_c)^2 + (y - y_c)^2 = r^2$$



So we have a 3D parameter space. What size, what

### A simple 3D accumulation procedure:

set all  $A[x_c, y_c, r] = 0$ ;

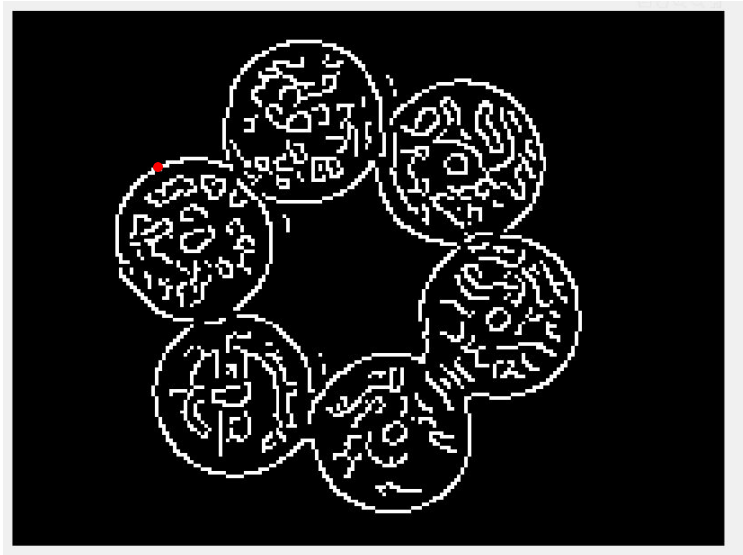
for every  $(x, y)$  where  $g(x, y) > T$

for all  $x_c$

for all  $y_c$

$r = \text{sqrt}((x - x_c)^2 + (y - y_c)^2)$ ;

$A[x_c, y_c, r] = A[x_c, y_c, r] + 1$ ;



A circle in the xy-plane is given by

$$(x - x_c)^2 + (y - y_c)^2 = r^2$$



So we have a 3D parameter space. What size, what

### A simple 3D accumulation procedure:

set all  $A[x_c, y_c, r] = 0$ ;

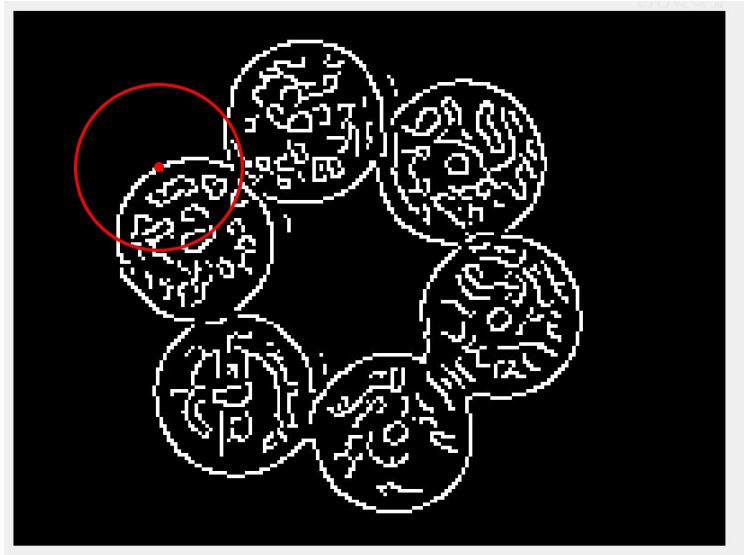
for every  $(x, y)$  where  $g(x, y) > T$

for all  $x_c$

for all  $y_c$

$r = \text{sqrt}((x - x_c)^2 + (y - y_c)^2)$ ;

$A[x_c, y_c, r] = A[x_c, y_c, r] + 1$ ;



A circle in the xy-plane is given by

$$(x - x_c)^2 + (y - y_c)^2 = r^2$$



So we have a 3D parameter space. What size, what

### A simple 3D accumulation procedure:

set all  $A[x_c, y_c, r] = 0$ ;

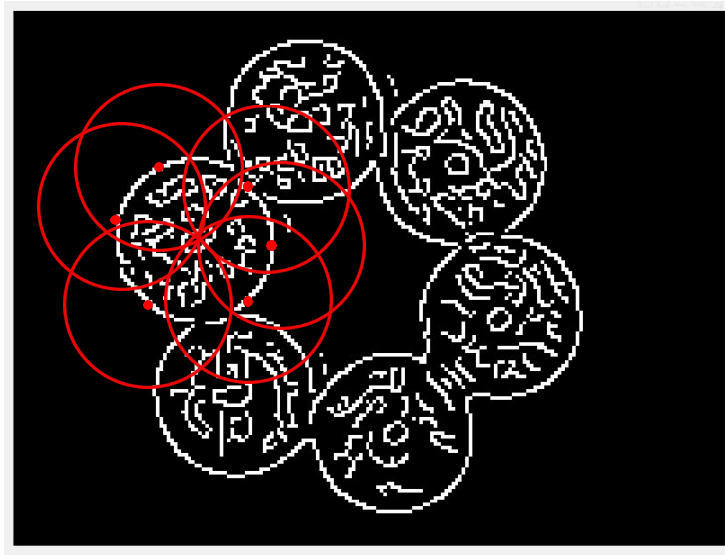
for every  $(x, y)$  where  $g(x, y) > T$

for all  $x_c$

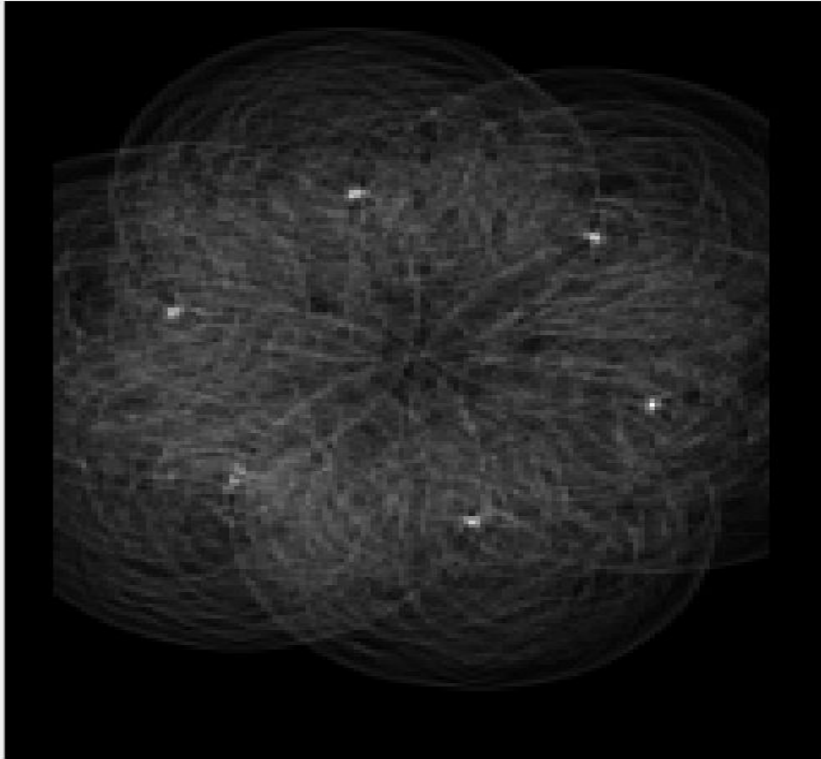
for all  $y_c$

$r = \text{sqrt}((x - x_c)^2 + (y - y_c)^2)$ ;

$A[x_c, y_c, r] = A[x_c, y_c, r] + 1$ ;



# We end up with a Hough image



Here we can clearly see the 6 different centers for the coins. This is the accumulator matrix for radius 22 (which got the highest peak)

```
[maxval, radius] = max(max(max(A)));  
%gives 22 radius  
number_of_circles = 6;  
peaks = houghpeaks(A(:, :, radius), number_of_circles)
```

# Finally we just plot the circles of $r=22$ with the centres we found

```
figure, imshow(ig, [])  
viscircles(peaks, repmat(radius, number_of_circles, 1));
```



# Fast Hough



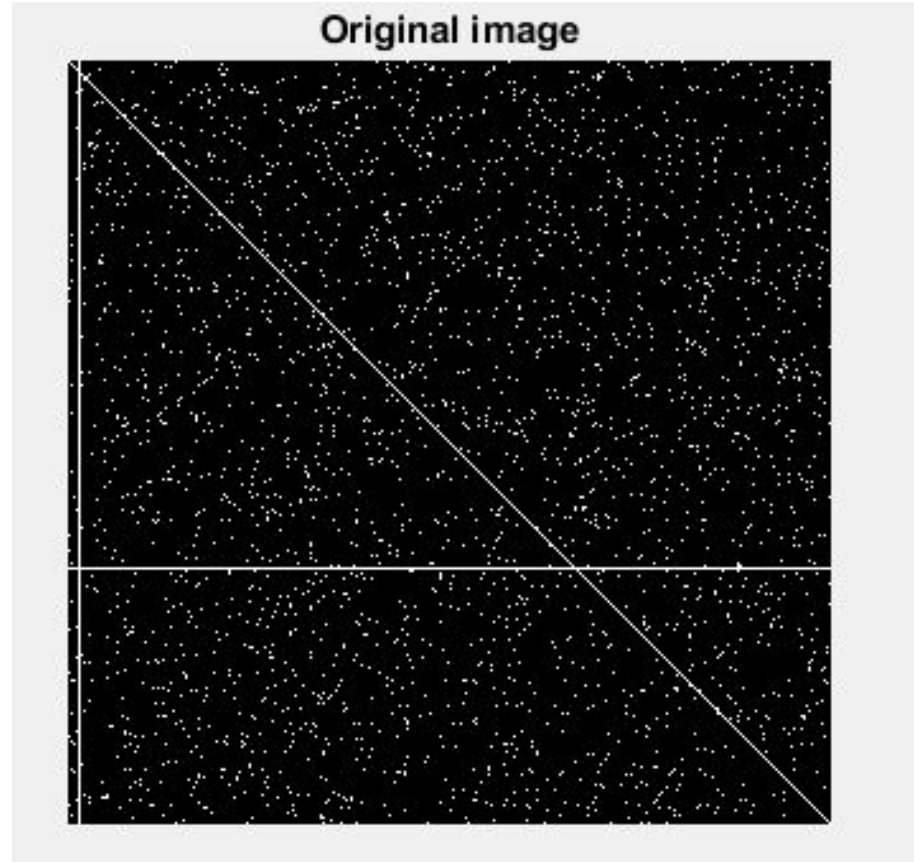
while no line is found

Sample two points in where  $T(x,y) > 0$

Find the line between the two points

Add to the accumulator matrix  $A$

line is found when a point in  $A > \text{threshold}$



# Fast Hough



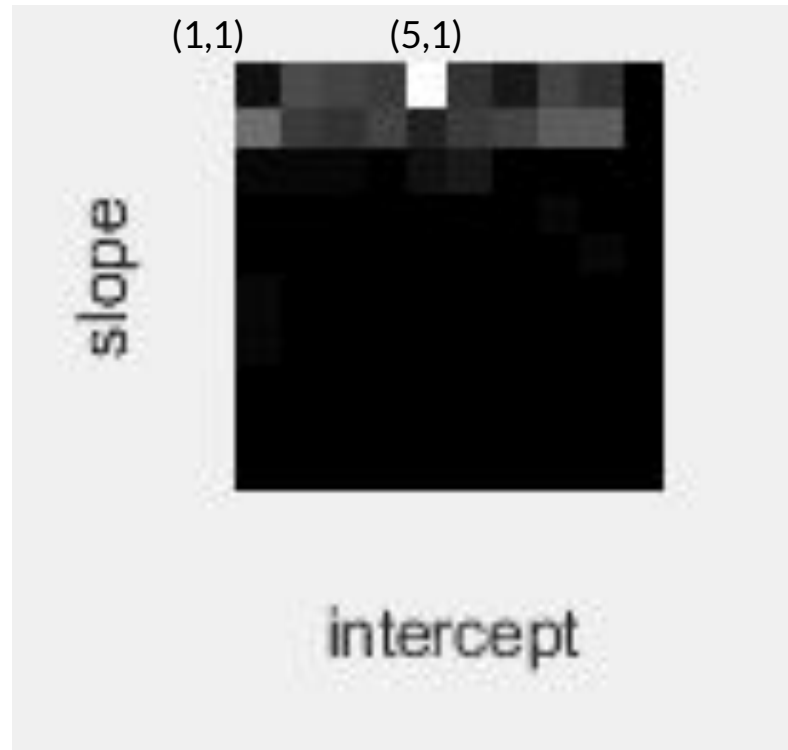
while no line is found

Sample two points in where  $T(x,y) > 0$

Find the line between the two points

Add to the accumulator matrix  $A$

line is found when a point in  $A > \text{threshold}$



# Fast Hough



while no line is found

Sample two points in where  $T(x,y) > 0$   
Find the line between the two points  
Add to the accumulator matrix  $A$

line is found when a point in  $A > \text{threshold}$

