# INF-GEO 4310 Imaging

Lecture 16.09.2010

### Fritz Albregtsen Geometrical Optics part II

- Themes today:
  - Imaging by Refraction
  - Geometrical Optics: Diffraction
  - Geometrical Optics: Scattering
- Literature:
  - F. Albregtsen:

"2. Reflection, refraction, diffraction, and scattering"

(pages 37 - 82)

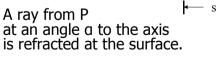
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# Refraction by spherical surface - I

 Convex surface with radius of curvature R facing incident light originating from P on the optical axis.
 A ray from P

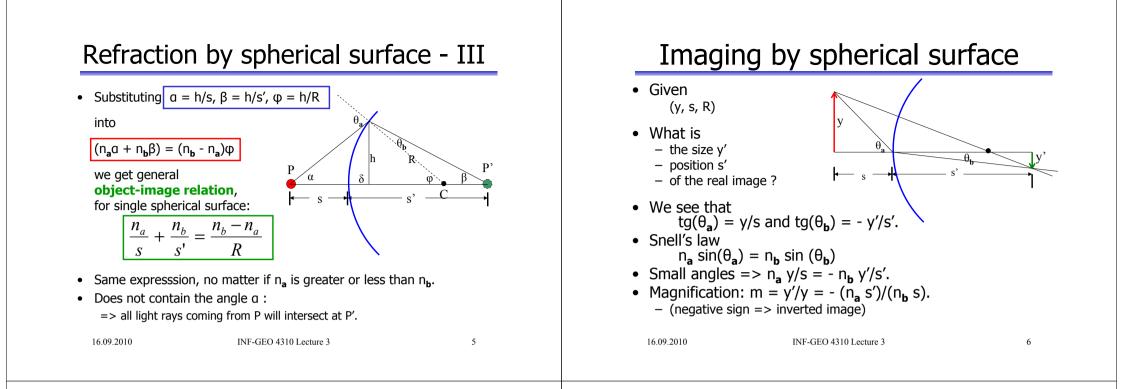


- Angle of refraction is given by Snell's law, refracted ray crosses the optical axis at an angle β.
- All rays from P will intersect axis at the same point P', provided that the angle a is small.

# **Geometrical Optics: Refraction**

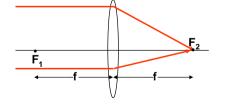
 Imaging by refraction • Refraction at a planar surface (Snell's Law) Refraction at a single spherical surface Thin lenses; "The lensmakers equation" • The camera: erfocal distance opposi "Depth-of-field" are using. If you the he depth of field wi • The eve ce to infinity.⊲ For mera has a hyperfe • The magnifier e focus at 18 feet • The evepiece Microscopes Telescopes Multiple lens systems 16.09.2010 INF-GEO 4310 Lecture 3

#### Refraction by spherical surface - II • Snell's law : $n_a \sin \theta_a = n_b \sin \theta_b$ . Paraxial approximation $=> n_{a}\theta_{a} = n_{b}\theta_{b}$ • Combining this with $\theta_{a} = a + \phi$ gives $\theta_{\rm h} = (a + \phi) n_{\rm a}/n_{\rm h}$ . • Substituting this into $\phi = \beta + \theta_{h}$ we get $(n_a \alpha + n_b \beta) = (n_b - n_a) \phi$ . • Tangents of $\alpha$ , $\beta$ , and $\phi$ are simply $tg(a) = h/(s+\delta), tg(\beta) = h/(s'-\delta), tg(\phi) = h/(R-\delta).$ • If the angle $\alpha$ is small, so are $\beta$ and $\phi$ . • Under the paraxial approximation, $\delta$ may be neglected compared to s, s', and R. • => a = h/s, $\beta = h/s'$ , $\phi = h/R$ . 16.09.2010 INF-GEO 4310 Lecture 3 4



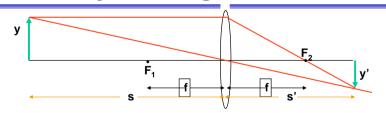
### Thin lenses

- Thin lens: two refracting surfaces close enough to neglect distance between them.
- Centers of curvature of spherical surfaces lie on and define optical axis.

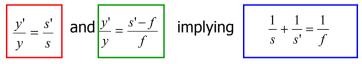


- The first and second focal points are on either side of the lens.
- Focal length: distance from focal point to middle of lens.
  - Focal length of convex lens is positive
  - Focal length of concave lens is negative.

### **Object-image relation**

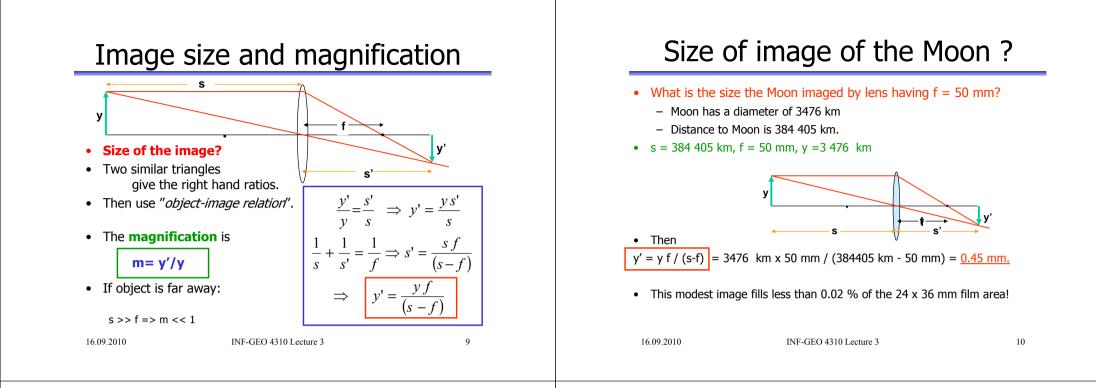


• We have two pairs of similar triangles, giving:



• This is known as the "object-image relation".

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## "The lensmakers equation"

• Lens has two surfaces => object-image relation applied twice:

$$\frac{n_a}{s_1} + \frac{n_b}{s_1'} = \frac{n_b - n_a}{R_1} , \quad \frac{n_b}{s_2} + \frac{n_a}{s_2'} = \frac{n_a - n_b}{R_2}$$

$$s_1 = \text{distance to object, } s_2' = \text{distance to final image. } s_2 = -s_1'.$$
Set  $n_a = 1$ ,  $n_b = n$ . We get
$$\frac{1}{s_1} + \frac{n}{s_1'} = \frac{n - 1}{R_1} , \quad -\frac{n}{s_1'} + \frac{1}{s_2'} = \frac{1 - n}{R_2}$$
• Adding equations:
$$\frac{1}{f} = \frac{1}{s_1} + \frac{1}{s_2'} = (n - 1)(\frac{1}{R_1} - \frac{1}{R_2})$$

• Note that:

- The two focal lengths are always equal, despite different curvatures.

## Chromatic aberration

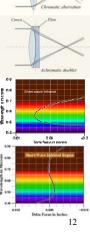
 Index of refraction depends on wavelength
 => images at different λ focus at different distances.

#### • Achromatic lens

- two materials (e.g. crown and flint) bonded
- focus two wavelengths into same focal plane
- Reduces chromatic aberration

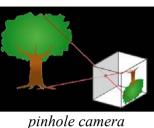
#### Apochromatic lens

- more than two lenses of different materials
- focus three  $\lambda$  (e.g. R,G,B) into same plane
- order of magnitude better than achromat



### The camera (lat.: small room)

- A camera consists of:
  - light-tight box
  - lens (several elements)
  - adjustable aperture
  - controllable shutter
  - film or electronic detectors.



- Fixed focal plane => lens closer to detector for distant object
  - lens farther away from detector for nearby object.
- This is very different from imaging in the eye.

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# f-number and exposure

• Energy per unit area in the focal plane is proportional to - aperture area and length of the exposure time interval. f-number of camera lens N = f/D. Intensity in focal plane is proportional to  $(D/f)^2$ . Changing D by  $\sqrt{2}$  changes intensity by a factor of 2. • f-numbers are often related by  $\sqrt{2}$ • 1/500 s at f/4 all correspond to the same exposure. 1/250 s at f/5.6 • 1/125 s at f/8 Shorter exposure times minimize motion-blurring allows larger effective lens aperture, giving better resolution of details in the image reduced depth of field and depth of focus. 16.09.2010 INF-GEO 4310 Lecture 3 14

# Field of view (FOW)

- Using 24 x 36 mm film, FOW measured along the diagonal will be
  - $-75^{\circ}$  for f = 28 mm (wide angle, landscapes)
  - $-47^{\circ}$  for f = 50 mm ("normal")
  - $-25^{\circ}$  for f = 105 mm (ideal for portraits)
  - $-8^{\circ}$  for f = 300 mm (full moon is  $1/2^{\circ}$ ).
- Replace 24 x 36 mm film with digital detector, => smaller registered field of view.
  - correspond to approximately 1.5 times longer focal lengths in cameras using 24 x 36 mm film.

### Same scene, different focal lengths



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# Zoom lenses

• **Digital zoom:** Cropping and enlarging an image - always lower quality than optical zoom, no resolution gained. Optical zoom: Several lens elements are used - focus and focal length can be varied, maintaining focal plane. • Described by ratio of focal lengths: – a 20 to 200 mm zoom is a 10:1 or "10×" zoom. • Two parts: a fixed-focal-length lens (L3) - an *afocal* zoom lens system (L1 + L2) • does not focus the light alters the size of a beam • alters overall magnification. 16.09.2010 INF-GEO 4310 Lecture 3 17

# The Hitchcock zoom

- Zooming can manipulate perspective in time sequences.
- If the camera is pulled away from the object
  - while lens zooms in to maintain Field Of Wiew, or vice versa,
  - the size of the foreground objects will be constant,
  - but background details will change size relative to foreground.
- Continuous perspective distortion is counter-intuitive:
  - Perspective change without a size change is highly unsettling.
- Special effect used in Hitchcock's Vertigo
  - hence called "Vertigo-" or "Hitchcock-zoom".
  - Also used in "Jaws", "ET", ...

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amara is further away zoome

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(a)

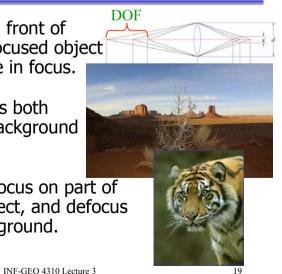
Object

(b)

Large

# Depth of field

- DOF = distance in front of and beyond the focused object that appears to be in focus.
- A large DOF brings both foreground and background into focus.
- A small DOF will focus on part of an interesting object, and defocus a distracting background.



# Lens aperture and Depth Of Field

- Large lens aperture D, low f/D - value:
  - Shorter exposure time
  - Focus more critical
  - Better angular resolution
- Small lens aperture D, high f/D-value:
  - Longer exposure time
  - Focus less critical
  - Poorer angular resolution

#### Near and far limits of DOF What determines DOF? An object at distance *s* from the lens is in focus at image distance *v*. • DOF is determined by three factors: • Objects at $D_{\rm E}$ and $D_{\rm N}$ are in focus at image distances $v_{\rm E}$ and $v_{\rm N}$ . - the focal length of the lens • At the image distance v, they are blurred spots. - the f-number of the lens aperture - the camera-to-object distance. • Increasing the f-number (smaller aperture) increases the DOF. • When blur spot diameter reduces the amount of light transmitted is equal to the acceptable circle of confusion c (COC), the near and far limits of DOF are at $D_{\rm N}$ and $D_{\rm E}$ . increases diffraction • From similar triangles we see that - reduces angular resolution => There is a practical limit to the reduction of aperture. 16.09.2010 INF-GEO 4310 Lecture 3 21 16.09.2010 INF-GEO 4310 Lecture 3 22

# Limits of DOF from N=f/D

"*f*-number" is given by focal length *f* and aperture diameter *d* :

• Substituting for d we get the focus limits on the image side of the lens

$$v_N = \frac{f v}{f - N c} \qquad v_F = \frac{f v}{f + N c}$$

• Thin lens equation:

$$+\frac{1}{v} = \frac{1}{f}$$

Substituting this give limits of DOF in terms of

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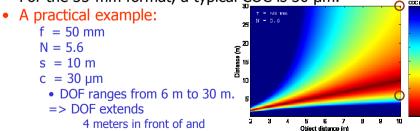
- focal length f
- "f-number" N

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 $D_{N} = \frac{s f^{2}}{f^{2} + N c (s - f)} \qquad D_{F} = \frac{s f^{2}}{f^{2} - N c (s - f)}$ object distance s

### Practical limits of DOF

- DOF beyond the object is always greater than DOF in front of the object.
- For longer focal lengths the ratio tends towards unity.
- For the 35-mm format, a typical COC is 30 μm.



20 meters beyond the focus distance. • A smaller/larger COC gives a larger/smaller DOF.

# DOF of a camera zoom lens

• On an old fashioned zoom lens, far and near limits of DOF indicated for the chosen f-number and focal length.

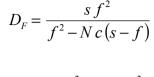


 Hyperfocal distance is the nearest focus distance at which the far limit of the DOF extends to infinity.

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# The hyperfocal distance

- The hyperfocal distance is the nearest focus distance H at which the far limit of the DOF extends to infinity.
- Setting the far limit  $D_F$  to infinity and solving for *s* gives us H:



- $s = H = \frac{f^2}{Nc} + f \approx \frac{f^2}{Nc}$
- Focusing the camera at the hyperfocal distance gives the largest possible DOF for a given *f*-number.
- You will see the hyperfocal distance again later!

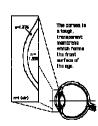
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### The eye

- Eye is nearly spherical and about 2.5 cm in diameter.
  - *cornea* protects the eve, performs much of the focusing
  - iris and pupil controls how much light will be let through
  - lens produces a sharp image
  - retina contains photo detectors
  - optic nerve transmits signals to brain.
- Lens
  - responsible for ca 20 % of the refraction.
  - focal length,  $f \approx 1.5$  cm.
- Focusing
  - Radial ligaments around the lens stretch it to a flattened disc focus on far-away objects.
  - If ring-shaped muscle around the radial fibers is relaxed, lens becomes more spherical and its focal length is shortened
    - Focus on closer objects.
  - Lens retina distance is constant, unlike fixed-focal-length lenses
  - Focusing power in "dioptres", d, where d = 1/f (f in meters)
  - Eye lens  $\approx$  67 d, cornea responsible for 45 d.





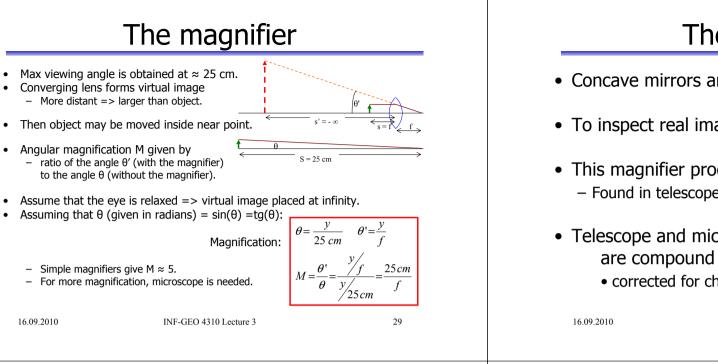
- Accommodation an automatic ability to alter the focal length is affected by ageing.
  - young individuals may alter focal power by up to 4 dioptres.
- Presbyopia near point recedes as one grows older
- *Myopia* (near-sighted) infinity focused in front of retina. - Corrected by diverging lens (f = 1/d < 0).
  - moves virtual image of distant object at or inside far point
- Hyperopia (far-sighted) infinity focused behind retina. - Corrected by converging lens (f = 1/d > 0).
  - forms virtual image of nearby object at or beyond near point.



- Astigmatism different focus in horizontal and vertcal plane. Remedied by lenses that are not rotationally symmetric.







# The eyepiece

- Concave mirrors and lenses form real images.
- To inspect real image, we may use a second lens.
- This magnifier produce an enlarged virtual image.
  - Found in telescopes and microscopes.



 Telescope and microscope oculars are compound lenses

corrected for chromatic and geometric aberrations.

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# **Optical** microscope

- Object just outside first focal point of the objective => real, inverted and enlarged image.
- This image iust inside first focal point of evepiece => a final virtual image.
- Lateral magnification of objective:  $m_1 = -s_1'/s_1$ . - If object close to focal point:  $m_1 = -s_1/f_1$ .
- Angular magnification of eyepiece:  $M_2 = (25 \text{ cm})/f_2$ , (if real image is close to focal plane).
- Total angular magnification M:

(25cm)s $M = m_1 M_2 =$  $f_1 f_2$ 

- Negative sign indicates that image is inverted.
- Use objectives of different f<sub>1</sub> to vary magnification.

## Refracting telescope

### • Objective lens forms real, inverted and reduced image distant object => real image at second focal point.

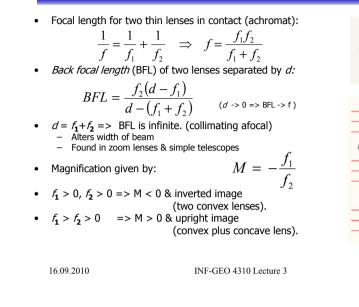
 Real image at the first focal point of evepiece => final virtual image at infinity

=> objective to evepiece distance = sum of focal lengths.

- Angle subtended at the eye by the final virtual image  $\theta' = y'/f_2$  (As with the magnifier)
- Angle of object when viewed by unaided eve  $\theta = -v'/f_{\bullet}$
- Magnification:

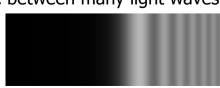
 Negative sign indicates that image is inverted. Use eyepieces of different f, to vary magnification.

### Multiple lenses



## Diffraction by an edge

- Light can bend around corners.
- When a point source casts shadow of a straight edge, the edge of the shadow is not a step edge.
  - some light in the area expected to be in shadow
  - alternating bright and dark fringes in illuminated area.
- Result of interference between many light waves
  - (Huygens' Principle).



# **Geometrical Optics: Diffraction**

- Fraunhofer diffraction pattern
  - Single slit, twin slit, multiple slits
  - Diffraction grating, spectrograph, spectroheliogra spectrograph
- Diffraction profile of circular aperture
  - Airy disc and Rayleigh criterion
  - Effect of central obstruction
- The smallest visible detail
  - In a high quality camera
  - In a compact digital camera
  - In a mobile-phone camera
- Depth of focus
- Convolving PSF and sampling aperture

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### Near- and far-field

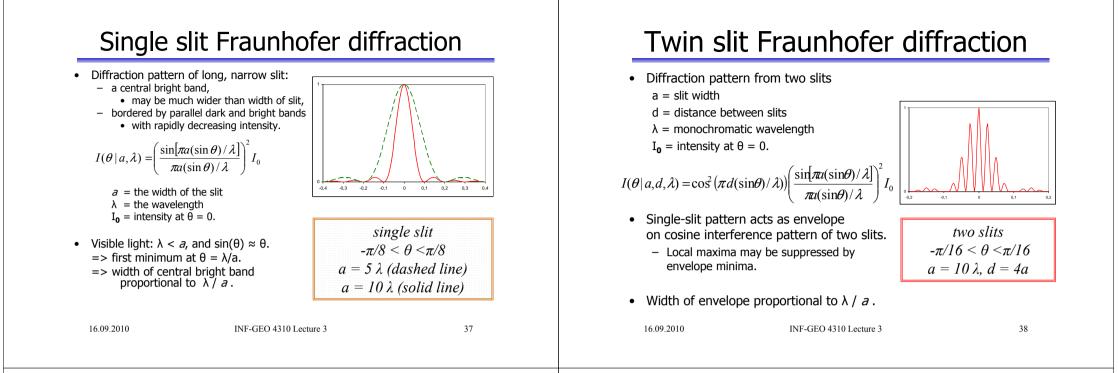
- Fresnel (near-field) diffraction
  - Both light source and observation plane are close to the aperture.
  - Curvature of the wave fronts must be taken into account.
  - Fresnel diffraction effects later in the course.

#### • Fraunhofer (far-field) diffraction

- Wave fronts at aperture and observation plane considered planar.
- usually => light source and observation plane far from slit.
- We may use collimating lenses
  - lens having light source in its primary focal point will collimate the beam before it reaches the aperture;
  - lens behind the aperture may collimate the beam traveling towards the observation plane.
- The near/far-field limit is at the hyperfocal distance !!!

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# Multiple slit diffraction

- Constructive interference for diffracted rays at an angle  $\theta$  that arrive in observation plane with path length difference = integer number of  $\lambda$ : d
- Diffraction pattern from N slits
  - a = width of slit
  - d = distance between slits
  - $\lambda$  = monochromatic wavelength
  - $I_0 = intensity at \theta = 0.$

$$I(\theta \mid a, d, \lambda, N) = \left[\frac{\sin\left(\frac{N\pi d}{\lambda}\sin\theta\right)}{\sin\left(\frac{\pi d}{\lambda}\sin\theta\right)}\right]^2 \cdot \left(\frac{\sin\left[\frac{\pi a}{\lambda}\sin\theta\right]}{\frac{\pi a}{\lambda}\sin\theta}\right]$$

- Principal maxima
  - same positions as in the two-slit case
    width proportional to 1/N.
- N-1 minima between pair of principal maxima
   secondary maxima get smaller as N increases.

 $d \cdot \sin(\theta) = m\lambda, \ m = 0, \pm 1, \pm 2, \dots$   $\int_{0}^{1} \int_{0}^{1} \int_{0}^$ 

### **Diffraction grating**

- An assembly of narrow slits or grooves in planar (or curved) mirror.
- Gratings for  $\lambda$  = 400 to 700 nm usually have about 1000 lines/mm, corresponding to d on the order of 1/1000 mm = 1000 nm.
- When a beam is incident on a grating with an angle θ<sub>i</sub> (measured from the normal of the grating), it is diffracted into several beams.
  - Specular reflection beam is called zero order (m = 0).
  - Other orders given by non-zero integers *m* in **grating equation**.

$$d \cdot [\sin \theta_m(\lambda) + \sin \theta_i] = m \lambda, \ m = 0, \pm 1, \pm 2, \dots$$

d = groove period

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- $\lambda$  = wavelength of incident light
- $\theta_{\mathbf{m}}(\lambda)$  = value of the diffracted angle in order *m*.



 $I_0$ 

# A slit spectrograph

- Light is focused onto entrance slit (e).
- Tilted concave collimating mirror (m1) reflects onto a plane reflecting diffraction grating (g).
- Dispersed light of some order *m* from grating is focused by a second concave mirror (m2) onto detector array (d).
- Special-purpose spectrographs are complex
  - to avoid
    - internal reflections
    - unwanted straylight.

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## Slitless spectrograph

- Gives co-temporal spectra of all parts of extended objects.
- Concave grating produces image at all wavelengths.
  - Spectral resolution given by reflective grating.
  - Angular resolution given by telescope optics.
- X and λ are same direction.
- Images at different  $\lambda$  overlap.
- Spectral and spatial information mixed into complicated image.



image taken by the S082A EUV spectro escope Mount, January 1

# Spectroheliograph

- Produces monochromatic images of the Sun.
- An image of the Sun is focused on a plane.
- A narrow slit lets light into a spectrograph.
- Spectrograph produces a spectrum
  - of the portion of the solar disk imaged on the entrance slit at the same image scale as input image.
- Capture spectrum within an exit slit.
- Image scanned across entrance slit.
- Moving detector behind exit slit at same speed as the image is moving monochromatic image is recorded.



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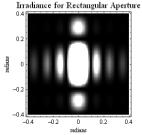
### Diffraction by rectangular aperture

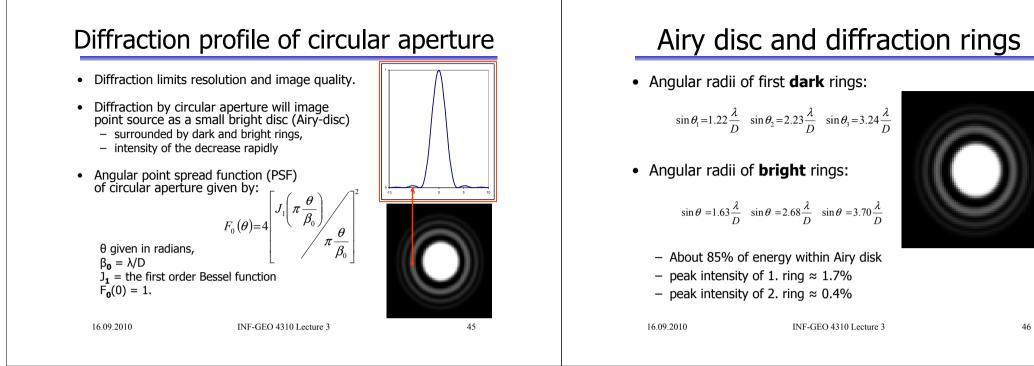
• An a x b aperture gives two orthogonal 1-D diffraction patterns:

$$I(\theta, \varphi \mid a, b, \lambda) = \left(\frac{\sin[\pi a(\sin\theta)/\lambda]}{\pi a(\sin\theta)/\lambda}\right)^2 \left(\frac{\sin[\pi b(\sin\varphi)/\lambda]}{\pi b(\sin\varphi)/\lambda}\right)^2$$

The widths of the central bright band are inversely proportional to the ratio of the size of the aperture (a,b) to the wavelength  $\lambda$ .

Diffraction pattern of rectangular aperture: Horizontal aperture  $a = 10 \lambda$ Vertical aperture  $b = 5 \lambda$ For a  $\pm$  0.4 radians range of  $\theta$  and  $\phi$ .



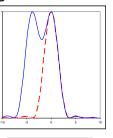


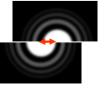
# Rayleigh criterion

- Cross-section through diffraction-limited image
  - two equally bright point sources at infinity
  - angular separation between point sources:

$$\sin\theta = 1.22\frac{7}{1}$$

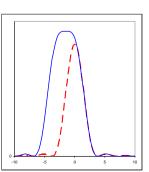
- Corresponds to overlaying two patterns
- maximum of first on first minimum of second.
- 27 % "dip" between the peaks.
- This is the "Rayleigh criterion".
  - For small angles,  $\sin \theta = \theta$ .

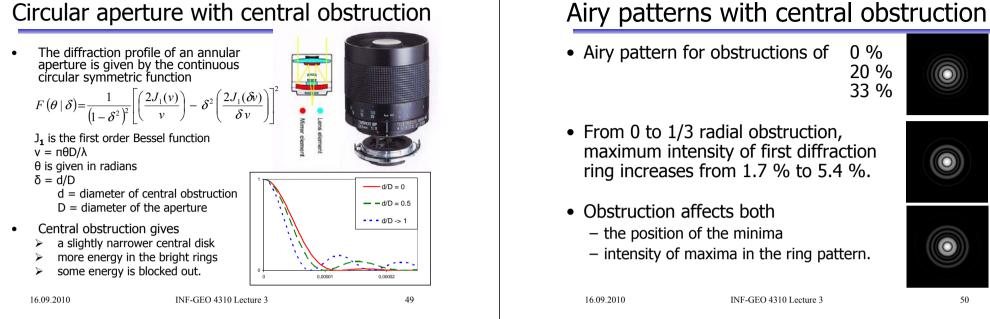




### Sparrow criterion

- If the point sources are moved closer than the Rayleigh criterion, the "dip" will become shallower, until it becomes a flat plateau.
- This angular separation is the Sparrow criterion.
- The limit when two point sources "melt together".
- Sparrow:  $\theta = 0.952 \lambda/D$ .





## Smallest detail visible ... to the eye

- Pupil diameter ≈ 2 mm in bright light.
- Angular resolution of human eye  $\approx$  60 lines per degree.
  - 120 alternating black and white lines of equal thickness.
- A4 "landscape" paper at 30 cm distance covers 50° x 40°.
  - 3 000 black and 3 000 white vertical stripes should be resolved
  - 2 400 black and 2400 white horizontal stripes should be resolved.
- Rayleigh criterion for D=2.5 mm at  $\lambda$ =550 nm:

$$\sin \theta = \frac{1.22 \,\lambda}{D} = \frac{1.22 \,x 550 \,x 10^{-9}}{2.5 \,x 10^{-3}} = 2.7 \,x 10^{-4}$$

Converting from radians to degrees:

 $\theta$ 

$$=2.7 \times 10^{-4} \frac{180}{\pi} \approx \frac{1}{60}$$

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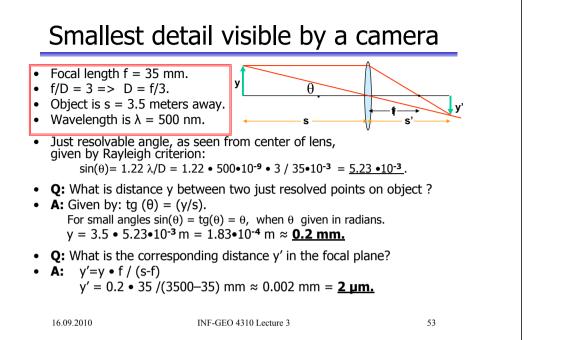
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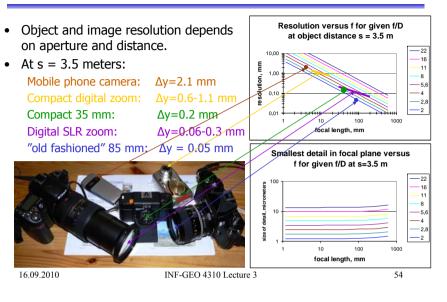
### Accomodation distance ... Near point

- = The closest distance we may focus sharply with the unaided eye.
  - 7 cm for a 10 year old,
  - 10 cm for a 20 year old,
  - 14 cm for a 30 year old,
  - 22 cm for a 40 year old,
  - 40 cm for a 50 year old.
- 100 cm for a 60 year old.
- 6 000 dots / 11 inches, ≈ 550 dpi.
- 47 yrs => s  $\approx$  30 cm.
  - printer better than 600 dpi is a waste.
- 20 yrs => s = 10 cm.
  - can inspect the printout at 10 cm distance
    - Will need 1 200 dpi (common for printing high guality images).



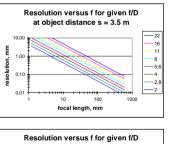


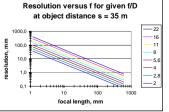
### Resolution and detail – medium distance



### Object resolution versus distance

- For a given lens and f/D, size of smallest resolvable object detail increases linearly with distance.
- Keeping f/D constant, size of smallest resolvable object detail decreases linearly with focal length.
- Keeping focal length constant, size of smallest resolvable object detail increases linearly with f/D.

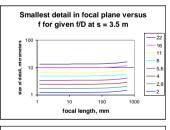


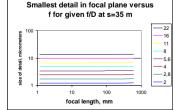


### Image resolution versus distance

- For given lens and f/D, size of smallest resolvable detail in image is independent of object distance, except when f is comparable to s.
- Keeping f/D constant, size of smallest resolvable object is independent of focal length, except when f is comparable to s.
- Keeping focal length constant, size of smallest resolvable object detail increases linearly with f/D.

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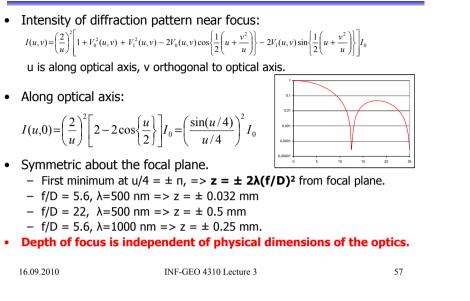




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### Diffraction limited depth of focus



### Intensity along optical axis

- A contour plot of the intensity I(u,v) in a meridional plane near the focus of a converging spherical wave diffracted by a spherical aperture.
- Vertical u-axis is the optical axis, and the horizontal v-axis is in the focal plane.
- The maxima and minima along the v-axis correspond to bright and dark rings of focal plane diffraction pattern.
- Maxima and minima along the u-axis illustrate "depth-of-focus".
- Contour plot from M. Born and E. Wolf: "Principles of Optics", Pergamon Press, 4th. Ed., 1970.

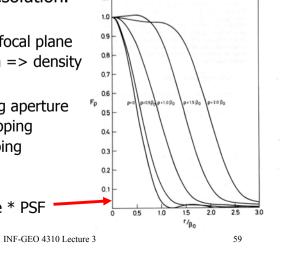
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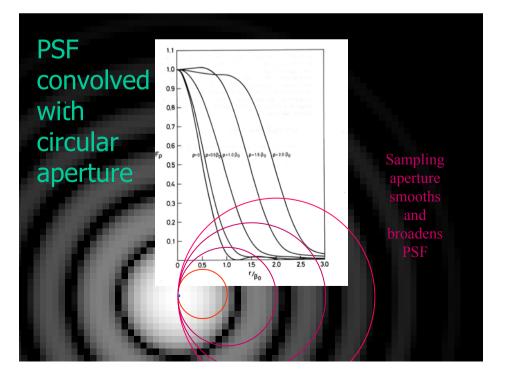
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### Convolving PSF and sampling aperture

- PSF determines resolution.
- Ideal:
  - Point sampling in focal plane
  - Sampling theorem => density
- Reality:
  - Extended sampling aperture
  - Fixed, non-overlapping
  - Movable, overlapping
    - Rectangles
    - Circles
  - Sampling aperture \* PSF





### **Geometrical Optics: Scattering**

- What is scattering?
- Some effects of scattering
  - Atmospheric blurring and straylight in images
  - Turbidity in liquids
  - Subsurface scattering in non-metallic materials and in tissues
- Doppler-shifted straylight

# What is scattering?

- Scattering causes radiation to deviate from a straight trajectory.
  - microscopic irregularities in surfaces
  - non-uniformities in transparent media
- Elastic scattering : no (or a very small) loss or gain of energy
- Inelastic scattering : some change in energy
- Absorption : substantial or complete loss of energy
- Single scattering : one localized scattering center.
   treated as a random phenomenon, described by probability distribution.
- Multiple scattering : radiation is scattered several times.
   randomness of interaction averaged out by large number of events
   => deterministic angular distribution of intensity PSF.
- Observed blurred image:
  - convolution of true image with PSF (diffraction + scattering).

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### Inverse scattering problem

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- A difficult challenge!
- Observe blurred object + scattering around it.
- Determine

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- scattering parameters (PSF)
- distribution of radiation before scattering (true object).
- In general, the inverse is not unique.
- PSF can be determined by observing image of some wellknown object through the same scattering medium.
- PSF then used to deconvolve image of unknown object.

### Wavelength dependence of scattering

#### Rayleigh scattering

- in transparent solids, liquids and gases.
- wavelength dependence ~  $\lambda^{-4}$

- Blue sky: Blue light is scattered much more than red light.
  - We observe blue light coming from all directions of the sky.
  - At higher altitudes, less scattering particles => sky is much darker.
- **Red sunset**: Sunlight must pass through greater air mass.
  - More scattering of blue light, little scattering of red light => red-hued sky.
- Mie scattering
  - scattering by spheres larger than Rayleigh range.
  - wavelength dependence  $\sim$  1/\lambda.
  - shape of scattering center significant

spheres, spheroids and ellipsoids.

• theory only applies well to



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# Atmospheric scattering

- Object is illuminated by sunligh
- Incident radiation detector:



- Specular reflectionDiffuse reflection
- radiation scattered in the air:
  - scattered before reaching object
  - specular and diffuse reflection, scattered onto detector.
- Important to shield detector to minimize straylight.
- Even with shielding, scattering will be present.
- Corrections important
  - In high precision measurements (e.g., astrophysics, ...)
  - Remote sensing (radiation passing twice through atmosphere)

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# High density of scatterers

- Vapors:
  - an object that is seen through mist or fog will look blurred.
  - at some distance the object will disappear into the background fog.
- Water:
  - Particles / organisms act as scatterers
  - cause haziness that indicate water quality
  - turbidity can be measured using Secchi disk
    - lowered into water until it can no longer be seen.
- Translucent solids:
  - light penetrates non-metallic surface and scatters inside material
  - either absorbed or leaving the material at a different location.
     This phenomenon is called *subsurface scattering (SSS)*.
  - This phenomenon is called *subsurface scattering* (555).
     The effect is a "softer" image than a metallic surface would give.
- Tissues:
  - human skin, salmon fillets, etc show *subsurface scattering* may depend on wavelength, condition of tissue, etc.
  - Thus, measuring SSS may be useful for
    - quality inspection of e.g., fish and meat
    - medical diagnostic work.

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# Straylight integral

- Straylight causes a blurring of the image (here the Sun).
- Given
  - circular symmetric PSF, Ψ(r),
  - true intensity  $\Phi_{c}(p')$
- Observed intensity I(p) given by integral equation:

$$I(p) = \int_{\oplus} \Phi_{C}(p') \Psi(r) d\omega$$

- p and p' are directions in the sky
- r is the angle between them.
- Integration is performed over the solid angle of the Sun.

# Doppler shifted straylight

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- Different parts of the Sun have different line-of-sight velocities.
- => Observed intensity contain straylight with different Doppler velocities.

 $I(d,\lambda) = 2 \int_{\rho_0}^{\rho_1} \int_{0}^{\alpha_0} \Phi_C(a) (1 - I_C(a)) \exp\left[-(\lambda - \Delta \lambda)^2 / w^2(d)\right] \Psi(\rho) d\rho d\alpha$ 

- $\Phi_{c}$  = true continuum intensity distribution across the solar disc
- w = Doppler width of Gaussian absorption line profile
- $I_c$  = central intensity of absorption line
- d = distance from the centre of the solar disc
- $\lambda$  = wavlength within a spectral line
- Ψ(r) = circular symmetric PSF, :
- Straylight introduce errors = 0.1 1.0 m/s,
- Amplitudes of global solar oscillations ≈ 0.1 m/s.
   => Error ≈ velocity oscillation signal.

