INF3380: Summary

Outline

INF3380: an introduction to parallel programming

- Why?
 - We want to solve *larger* scientific problems *faster*
 - Parallel hardware is now widespread
- How?
 - Given a problem, identify parallelism
 - Design & analysis of parallel algorithms
 - Implementation using OpenMP and/or MPI programming
- Concrete examples

Note: This summary is very general, you should read the book for details!

Decomposition (Chap. 3)

- Decomposition is the first step of developing a parallel algorithm
- A given problem may be decomposed into tasks, in many different ways
- A decomposition can be represented by a task dependency graph:
 - Nodes correspond to tasks
 - Edges indicate that the result of one task is required for processing the next

Granularity and degree of concurrency (Chap. 3)

- Granularity depends on the number of tasks from decomposition
 - fine-grained decomposition
 - coarse-grained decomposition
- Degree of concurrency: the number of tasks can be executed in parallel
 - may change as the execution proceeds
 - finer granularity \rightarrow increased concurrency

Limits on parallel performance (Chap. 3)

- It would appear that the parallel time can be made arbitrarily small by making the decomposition finer in granularity.
- There is, however, an inherent bound on how fine the granularity of a computation can be.
- Concurrent tasks often have to exchange data with other tasks. This results in communication overhead.
- There is a tradeoff between the granularity of a decomposition and associated overheads.

Processes and mapping (Chap. 3)

- In general, the number of tasks from a decomposition exceeds the number of processing elements available
- A parallel algorithm thus must also provide a mapping of tasks to processing elements
- Appropriate mapping is important for parallel performance
 - load balancing
 - interaction minimization
 - assigning tasks on critical path to processing elements as soon as possible

Point-to-point communication cost

A simple cost model:

$$t_{\text{comm}} = t_s + mt_w$$

 t_s — startup time

 t_w — per-word transfer time

m — amount of data transferred

Group communication (Chap. 4)

- Many interactions in practical parallel programs occur in well-defined patterns involving groups of processors.
- Group communication operations are built using point-to-point messaging primitives.
- The actual cost of a group communication depends on
 - the type of communication
 - the number of processors involved
 - the communication network used

Note: Read the book for details!

Analytical modeling (Chap. 5)

- lacktriangledown The parallel runtime T_P of a program depends on the input size the parallel system and p
- $ightharpoonup T_S$: serial time.
- **●** Total overhead: $T_o = T_{all} T_S = pT_P T_S$

Speedup (Chap. 5)

$$S(p) = \frac{T_S}{T_P(p)}$$

- Always consider the best sequential program as the baseline
- ullet Speedup is normally bounded by p, but can have exceptions (superlinear speedup)
- **▶** Parallel efficiency: E = S(p)/p

Cost optimality (Chap. 5)

- **Description** Total cost of a parallel system: $p \times T_P$
- ${\color{red} \blacktriangleright}$ A parallel system is said to be cost-optimal if $p\times T_P$ is asymptotically identical with T_S
- ▶ Parallel efficiency E = O(1) for cost-optimal systems

Scaling (Chap. 5)

Efficiency:

$$E = \frac{S}{p} = \frac{T_S}{pT_P} = \frac{1}{1 + \frac{T_o}{T_S}}$$

- lacktriangle Note: total overhead T_o is typically an increasing function of p
- ullet To maintain a constant level of E, we have to increase the problem size as the same time as p increases
 - if yes → scalable parallel system

Maintaining parallel efficiency (Chap. 5)

- At what rate should the problem size be increased, with respect to p, if we want to maintain a constant parallel efficiency?
- This rate determines the scalability of the system, the slower the better
- ullet Problem size W: the asymptotic number of operations associated with the best serial algorithm to solve the problem

Isoefficiency metric (Chap. 5)

Recall

$$T_P = \frac{W + T_o(W, p)}{p}$$

$$S = \frac{W}{T_P} = \frac{pW}{W + T_o(W, p)}$$

Therefore,

$$E = \frac{S}{p} = \frac{W}{W + T_o(W, p)} = \frac{1}{1 + T_o(W, p)/W}$$

More about isoefficiency metric

• From $E = \frac{1}{1 + T_o(W, p)/W}$ we can get

$$\frac{T_o(W,p)}{W} = \frac{1-E}{E} \quad \Rightarrow \quad W = \frac{E}{1-E}T_o(W,p)$$

For a desired efficiency E, we will have a constant K=E/(1-E), which tells us that W must grow as fast as

$$W = KT_o(W, p)$$

ullet That is, W can usually be obtained as a function of p for maintaining efficiency — isoefficiency function

Serial fraction (Chap. 5)

Suppose

$$W = T_{ser} + T_{par}$$

$$T_{P} = T_{ser} + \frac{T_{par}}{p} = T_{ser} + \frac{W - T_{ser}}{p}$$

Then we can define the serial fraction as

$$f = \frac{T_{ser}}{W}$$

Therefore

$$T_P = f \times W + \frac{W - f \times W}{p} = W \times \left(f + \frac{1 - f}{p}\right)$$

MPI programming (Chap. 6)

- MPI is the de-facto standard of message passing programming
- Assumption: each process's own memory is not directly accessible by other processes
- Collaboration between the processes is through sending and receiving messages between the processes
 - a message is an array of predefined data types
 - point-to-point communication
 - collective communication
- The global data structure is normally divided among the processes (as little duplication as possible)

MPI basics (Chap. 6)

- The working units are called MPI processes
- An MPI communicator is group of processes
- Each process within a communicator has a unique rank, between 0 and #procs-1
- Carelessly programmed MPI communications may deadlock
- Non-deterministic features of an MPI program
 - Between communications, the different processes may proceed at different paces
 - If a process is expecting two messages from two senders, the order of arrival is normally not known beforehand
- Synchronization
 - explicit MPI_Barrier
 - implicit collective commands or matching MPI_Send and MPI_Recv

Overlap communication with computation (Chap. 6)

- Performance may be improved on many systems by overlapping communication with computation
- Use of non-blocking communication and completion routines
- For example, initiate the communication with MPI_Isend and MPI_Irecv, continue with computation, finish with MPI_Wait

OpenMP programming (Chap. 7)

- OpenMP is the most user-friendly thread programming standard
- Thread programming is a natural model for shared-memory architecture
 - Execution unit: thread
 - Many threads have access to shared variables
 - Information exchange is (implicitly) through the shared variables

The programming model of OpenMP (Chap. 7)

- Multiple cooperating threads are allowed to run simultaneously
- The threads are created and destroyed dynamically in a fork-join pattern
 - An OpenMP program consists of a number of parallel regions
 - Between two parallel regions there is only one master thread
 - In the beginning of a parallel region, a team of new threads is spawned
 - The new threads work simultaneously with the master thread
 - At the end of a parallel region, the new threads are destroyed

The memory model of OpenMP (Chap. 7)

- Most variables are shared between the threads
- Each thread has the possibility of having some private variables
 - Avoid race conditions
 - Passing values between the sequential part and the parallel region
- Very important to decide: which variables should be shared? which should be private?

Practicalities

- First step: identify parallelism in a sequential algorithm
 - find out the operations that can be done simultaneously
- Good work division is important
 - even distribution of the work load among computational units
 - keep the overhead of resulting communication low
- On distributed memory, data should be divided as well
- Be aware of needed synchronizations (both MPI and OpenMP)
- Be aware of possible deadlocks (both MPI and OpenMP)
- Be aware of possible racing conditions (OpenMP)

Matrix-vector multiplication (Chap. 8)

- Multiply a dense $n \times n$ matrix A with an $n \times 1$ input vector x to yield an $n \times 1$ result vector y.
- Rowwise 1D partitioning
- 2D block partitioning

Matrix-matrix multiplication (Chap. 8)

- $m{P}$ $C = A \times B$, where A, B and C are all square $n \times n$ matrices
- **2** D block data partitioning, each block is an $(n/q) \times (n/q)$ submatrix.
 - Simple parallel algorithm
 - Cannon's algorithm
 - The DNS algorithm

Solving a system of linear equations (Chap. 8)

- Parallelization of a simple Gaussian elimination algorithm

```
1.
          procedure GAUSSIAN ELIMINATION (A, b, y)
2.
          begin
3.
             for k := 0 to n-1 do
                                             /* Outer loop */
4.
             begin
5.
                 for i := k + 1 to n - 1 do
6.
                    A[k,j] := A[k,j]/A[k,k]; /* Division step */
7.
                y[k] := b[k]/A[k,k];
8.
                A[k, k] := 1;
9.
                 for i := k + 1 to n - 1 do
10.
                 begin
11.
                    for i := k + 1 to n - 1 do
                       A[i,j] := A[i,j] - A[i,k] \times A[k,j]; /* Elimination step */
12.
13.
                    b[i] := b[i] - A[i,k] \times y[k];
                    A[i,k] := 0;
14.
15.
                 endfor; /* Line 9 */
                       /* Line 3 */
16.
             endfor;
17.
          end GAUSSIAN ELIMINATION
```

Parallel sorting (Chap. 9)

- Odd-even transposition
- Shellsort
- Quicksort

Note: Read the book for details!

Parallel graph algorithms (Chap. 10)

- Minimum spanning tree: Prim's algorithm
- Single-source shortest paths: Dijkstra's algorithm
- All-pairs shortest paths: Dijkstra's algorithm & Floyd's algorithm

Note: Read the book for details!

About the exam

- 4-hour digital exam (using keyboard and mouse)
- One A4-sheet (two-sided) with handwritten notes and a calculator are allowed at the exam