

**UiO** • **Department of Informatics**  
University of Oslo

**Kyrre Glette – kyrrehg@ifi**

**INF3490 – Swarm Intelligence**

**Particle Swarm Optimization**



# Overview

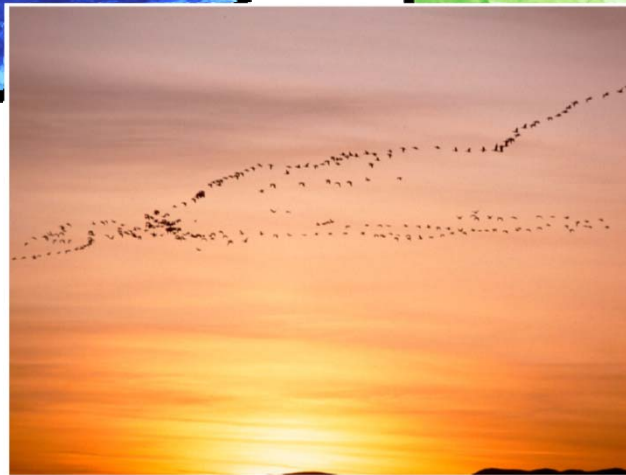
- Introduction to swarm intelligence principles
- Particle Swarm Optimization (PSO)

# Swarms in nature



<http://youtu.be/kdECYXdW9Tc>

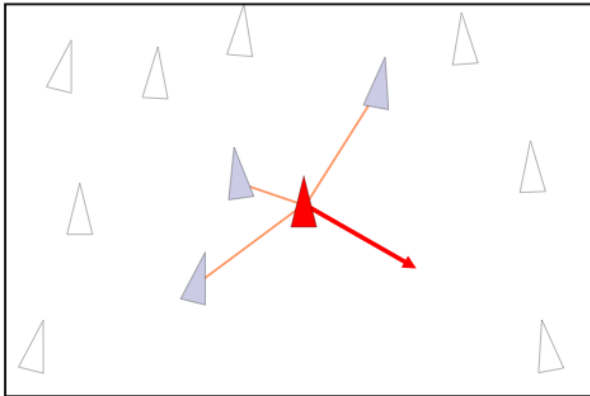
# Fish, birds, ants, termites, ...



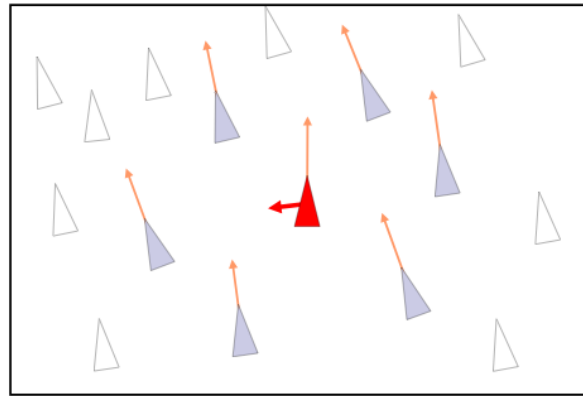
## Key features

- Simple local rules
- Local interaction
- Decentralized control
- Complex global behavior
  - Difficult to predict from observing the local rules
  - *Emergent* behavior

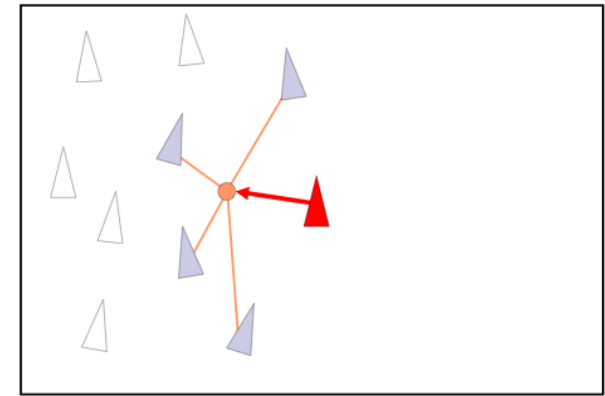
# Flocking model – “boids”



Separation – avoid crowding



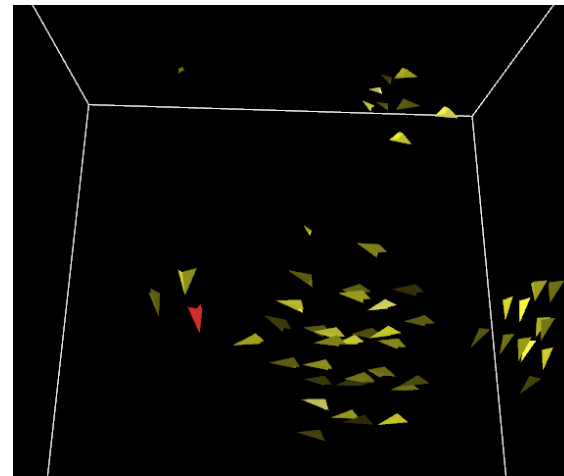
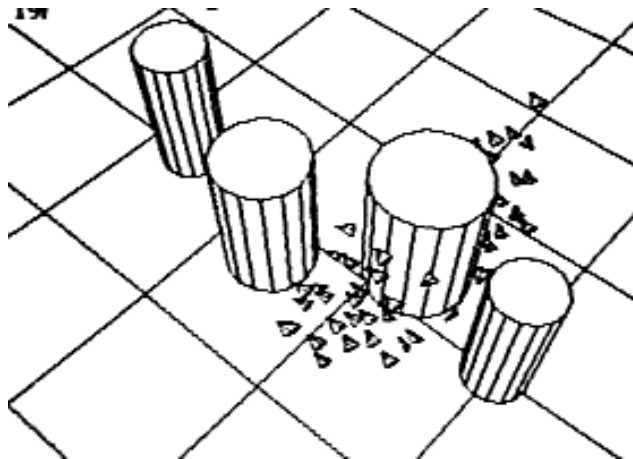
Alignment – steer towards average heading



Cohesion – steer towards average position

Only considering the boid's neighborhood

## Result - boids



Original: <http://youtu.be/86iQiV3-3IA>

Netlogo: “Flocking 3D Alternate” model

# Application: Computer graphics



<http://youtu.be/-jF5sAqBp4w>

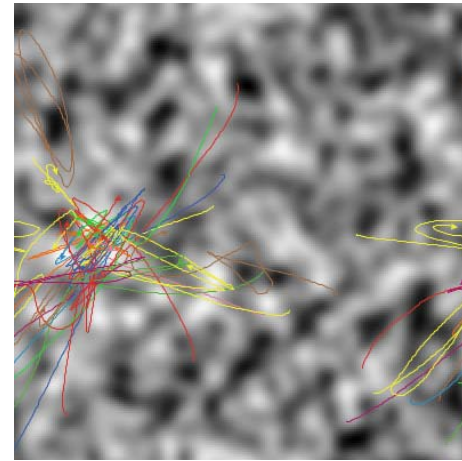
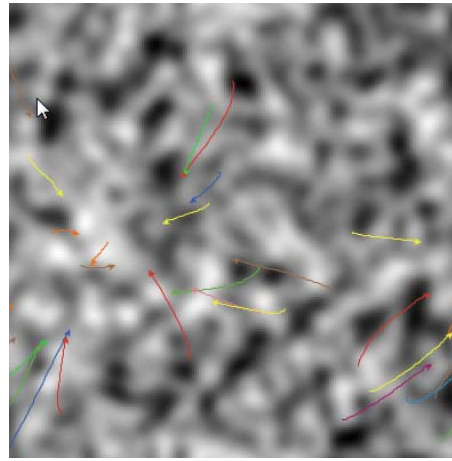
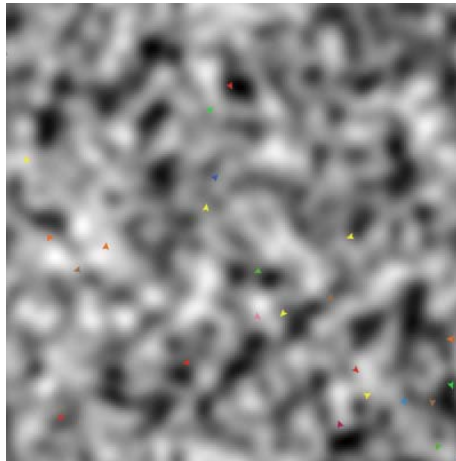


# Applications in bio-inspired computing

- **Particle swarm optimization**
  - Parameter optimization
- **Ant colony optimization**
  - Find shortest paths through graph by using artificial pheromones
- **Artificial immune systems**
  - Classification, anomaly detection
- **Swarm robotics**
  - Achieve complex behavior in robotic swarms through simple local rules

# Particle Swarm Optimization (PSO)

- Optimizes a population of solutions
  - *A swarm of particles*



# Principle

- Evaluate your present position
- Compare it to your previous best and neighborhood best
- Imitate self and others

## Simplified PSO algorithm

- For each particle  $i$  in the swarm
  - Calculate fitness
  - Update local best
  - Find neighborhood best
  - Update velocity
  - Update position

# PSO update formulas

For each dimension  $d$  in particle  $i$ :

## 1. Velocity update

$$v_{id}^{(t+1)} \leftarrow \underbrace{\alpha v_{id}^{(t)}}_{\text{inertia}} + \underbrace{U(0, \beta)}_{\text{random}} \left( \underbrace{p_{id} - x_{id}^{(t)}}_{\text{direction personal best}} \right) + \underbrace{U(0, \beta)}_{\text{random}} \left( \underbrace{p_{gd} - x_{id}^{(t)}}_{\text{direction neighborhood best}} \right)$$

## 2. Position update

$$x_{id}^{(t+1)} \leftarrow x_{id}^{(t)} + v_{id}^{(t+1)}$$

## What happens?

- A particle circles around in a region centered between the bests of itself and its neighbors
- The bests are updated and the particles cluster around better regions in the search space
- The way good solutions are propagated depends on how we define the neighborhood

## Neighborhood topologies

- *gbest*: all particles are connected
  - Every particle gets information about the global best value
  - Can converge (too) fast
- *lbest*: connected to  $K$  nearest neighbors in a wrapped population array
  - Slower convergence, depending on  $K$
  - More areas are searched in parallel
- Several other topologies exist

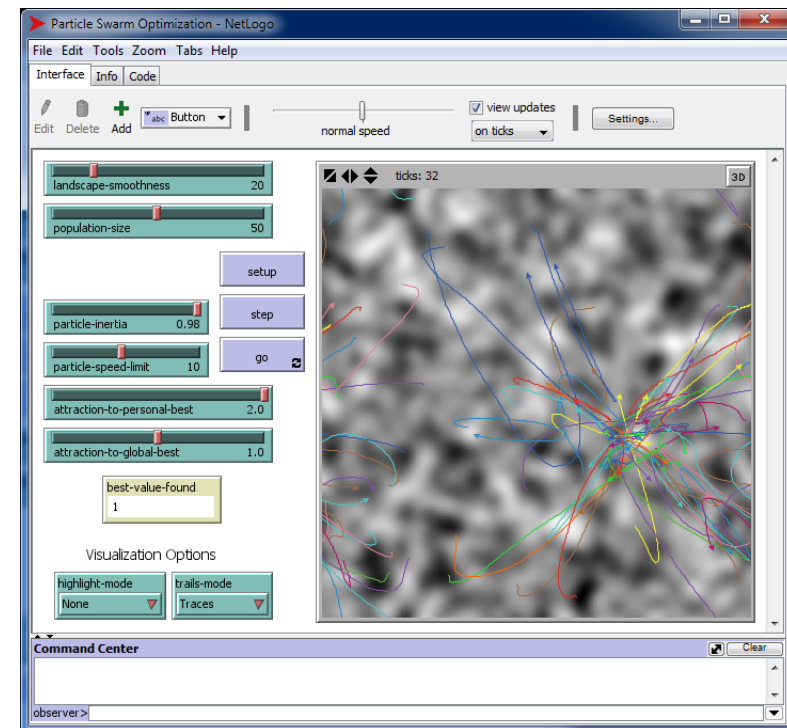
## PSO parameters

- Particle:
  - Usually a D-dimensional vector of real values
  - Binary variant exists
- Swarm size: usually  $10 < N < 100$
- Recommended  $\alpha = 0.7298$
- Recommended  $\beta = 1.4961$



# Parameter experimentation

- NetLogo
  - Particle Swarm Optimization model
- Model uses *gbest* neighborhood
- Download and try
  - Or with java in the browser



## Advantages of PSO

- Few parameters
- Gradient free
- Decentralized control (depends on variant.)
- Simple to understand basic principle
- Simple to implement

## PSO vs. Evolutionary Algorithms

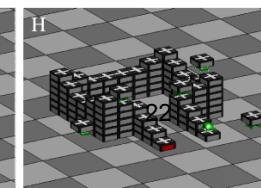
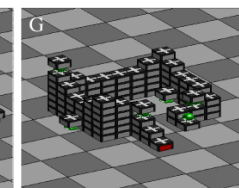
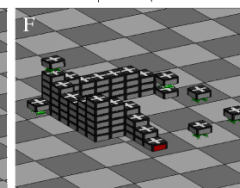
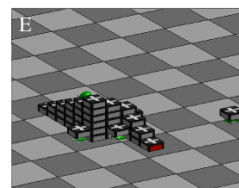
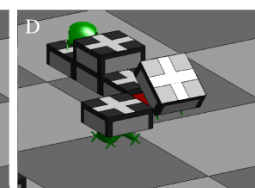
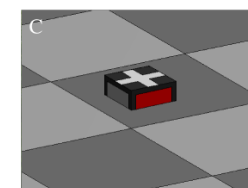
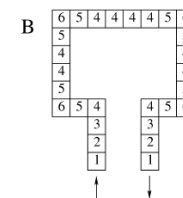
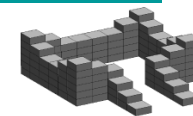
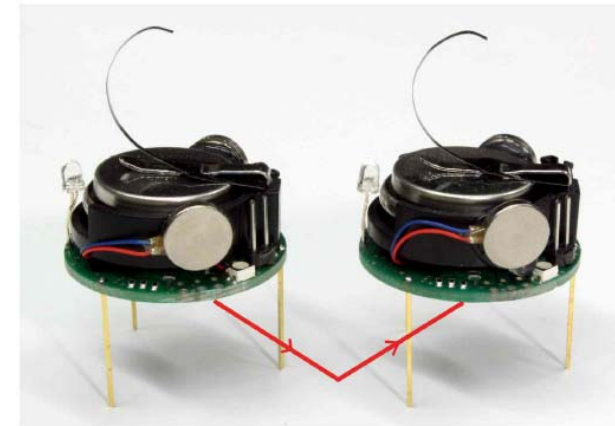
- Both are population based
- PSO: No selection – all particles survive
- Information exchange between solutions:
  - PSO: neighborhood best
  - GA: crossover (and selection)

# PSO applications

- Similar application areas as EAs
  - Most optimization problems
- Image and video analysis
- Electricity network optimization
- Neural networks
- ...

# Swarm robotics

- Swarrobot project
  - <http://youtu.be/h-2D-zIU-DQ>
- Kilobot project
  - <http://youtu.be/GnyDAuqorGo>
- TERMES project
  - Termite-inspired swarm assembly robots
  - <http://youtu.be/tCJMGQJnodc>





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**INF3490 – Evolvable Hardware**

**Cartesian Genetic Programming**

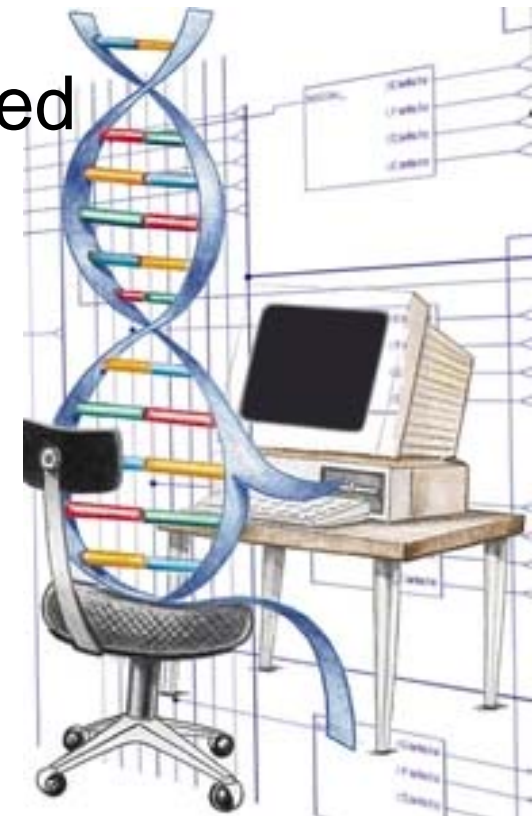


# Overview

- Introduction to Evolvable Hardware (EHW)
- Cartesian Genetic Programming
- Applications of EHW

## Evolvable Hardware (EHW)

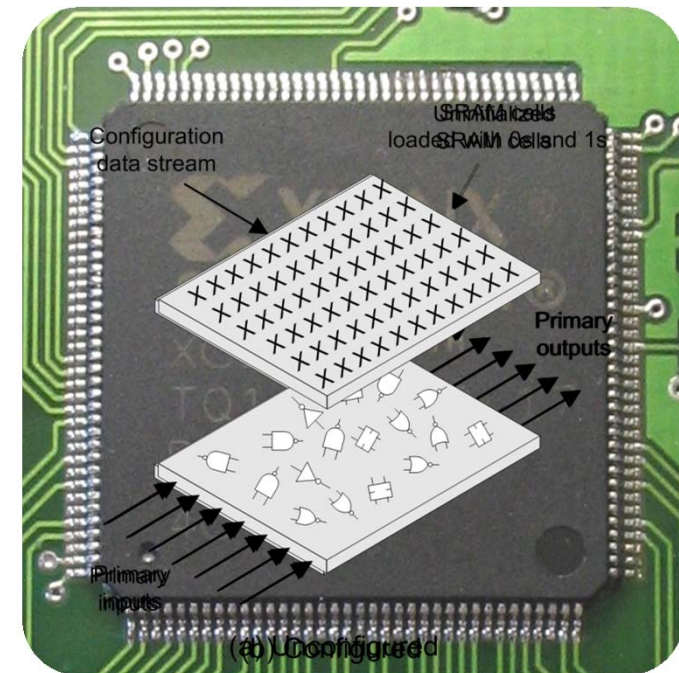
- Hardware systems designed/modified automatically by EAs
- A string of symbols/bits is evolved by an EA and translated into a HW system
- Offline EHW
  - Solutions are simulated in a PC
- Online EHW
  - Solutions are tested on target HW





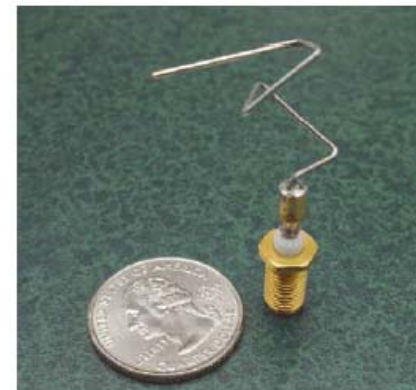
# EHW

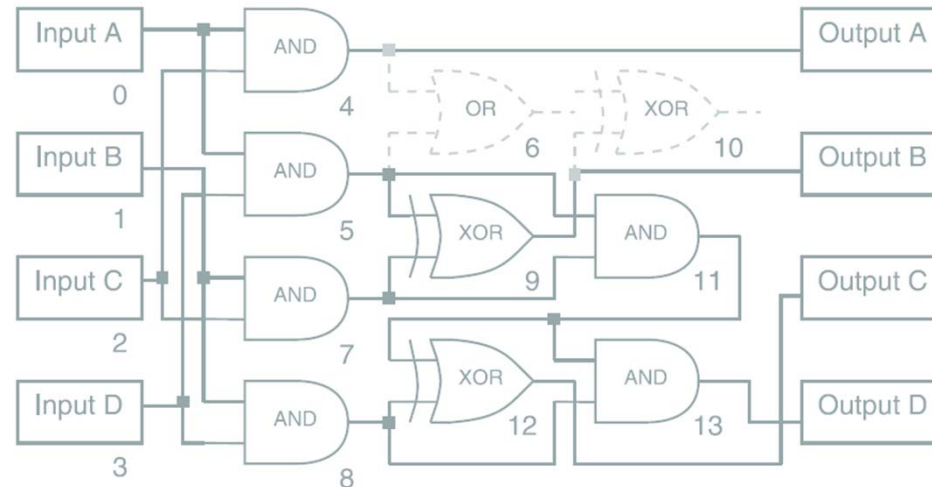
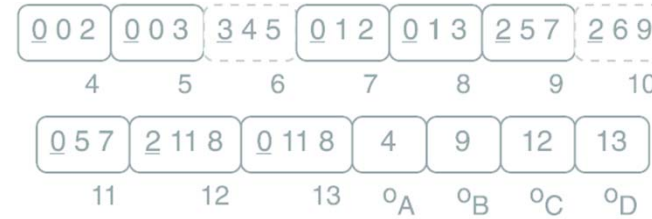
- FPGA
  - Reconfigurable hardware chip
  - Useful for online EHW
- On-chip evolution
  - EA running on the target chip, together with solutions
- Run-time adaptable EHW
  - Evolution can modify the system during operation



## Applications of EHW

- Pattern recognition / classification circuits
- Digital image filters
- Evolution of analog circuits
- Cache mapping functions
- On-the-fly compression for printers
- Spacecraft antenna



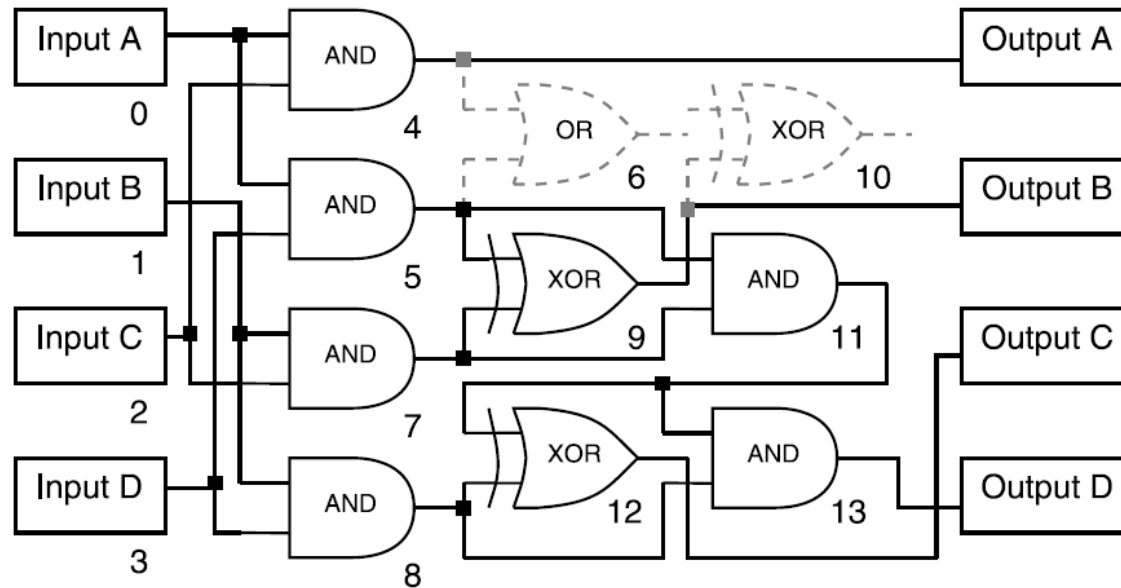
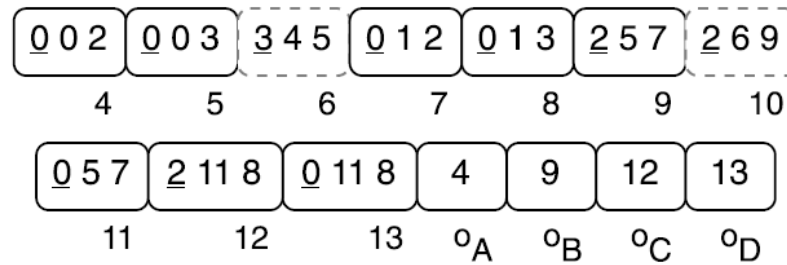


# CARTESIAN GENETIC PROGRAMMING

# Cartesian Genetic Programming (CGP)

- A type of Genetic Programming
- Allows restrictions compared to general GP:
  - Integer genome
  - Tree nodes are mapped to a grid
  - Connectivity can be restricted
- Popular in Evolvable Hardware applications
  - But can be used for many other things as well

# Example structure: Digital circuit



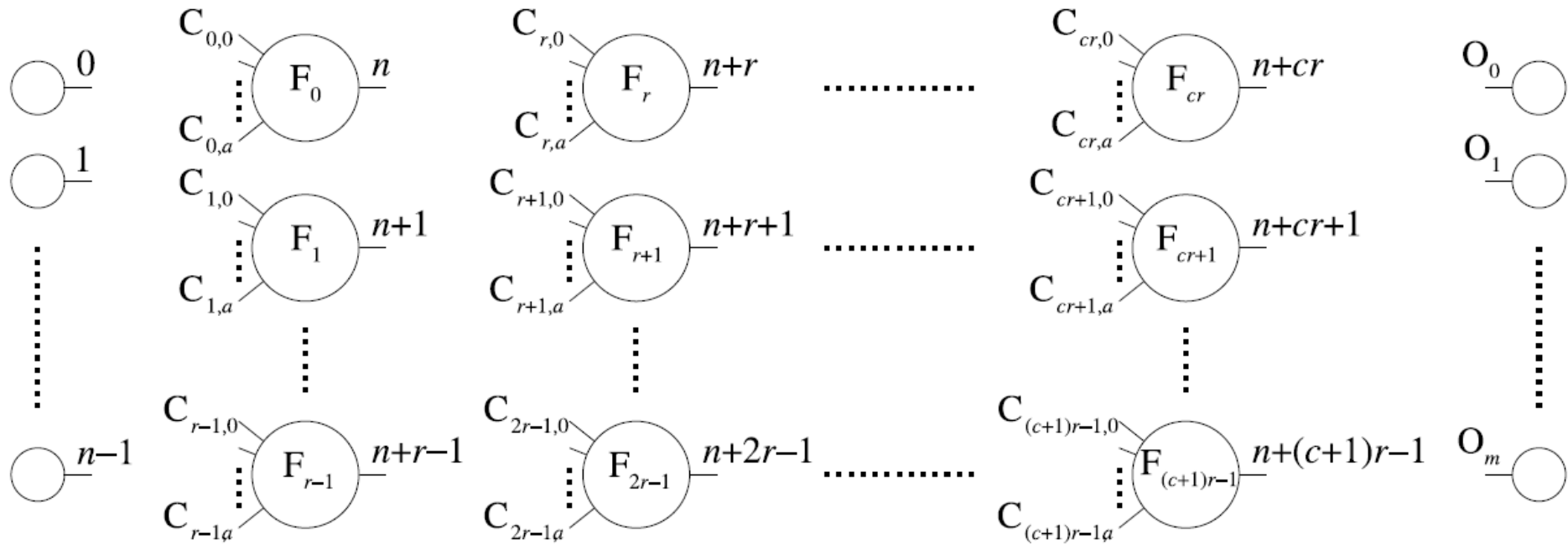
# CGP genome

- Internal node genes:
  - Node type: index to lookup table of functions
  - Inputs: index of other nodes
  - Optional: additional parameters
- Output node gene:
  - Internal node index

## CGP parameters

- Columns:  $n_c$
- Rows:  $n_r$
- Levels-back:  $l$ 
  - How many of the previous columns a node can connect to
- Columns x rows defines the maximum number of nodes in the graph

# General structure



Genome:  $F_0 C_{0,0} \dots C_{0,a} \underline{F_1 C_{1,0} \dots C_{1,a}} \dots F_{(c+1)r-1} C_{(c+1)r-1,0} \dots C_{(c+1)r-1,a} \underline{O_0 O_1 \dots O_m}$

node
function gene
connection gene
outputs



## Advantages of CGP

- Easy implementation
  - Fixed genome size and simple representation
  - Simple mutation and crossover
- Bloat is restricted
  - The number of nodes is restricted
- Regular structure suitable for e.g. hardware implementation
  - A grid structure with limited connectivity ideal for HW routing

## Other features of CGP

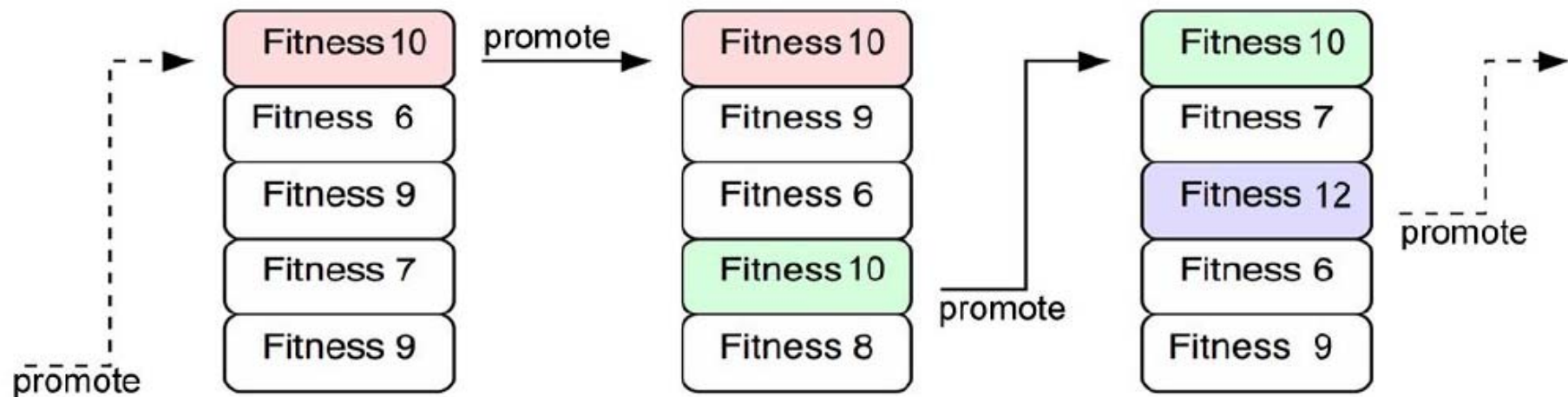
- Reuse of parts of the tree is possible
- Allows multiple outputs
- Parts of the genome may be non-coding
  - This has an analogy in biology, where only a fraction of the DNA is composed of *exons* (“coding” genes).
  - The other part is called *introns* (non-coding genes, sometimes called “junk” DNA). It is however believed that these are useful for something.
  - Likewise, the genetic redundancy (neutrality) in CGP is thought to be positive for the evolutionary search.

## Genetic operations in CGP

- Mutation
  - Select randomly a number of genes to mutate
  - Change to new (valid) random values
- Crossover
  - One-point crossover or other variants directly on the genome
- Usually only mutations are used
  - Many applications find crossover to have a destructive effect - it disrupts the tree structure too much

## Evolution in CGP

- The most popular is a variant of ES called (1+4) ES
- Choose children which have  $\geq$  fitness than parent



## CGP can code:

- Circuits
- Mathematical functions / equations
- Neural networks
- Programs
- Machine learning structures
- ...

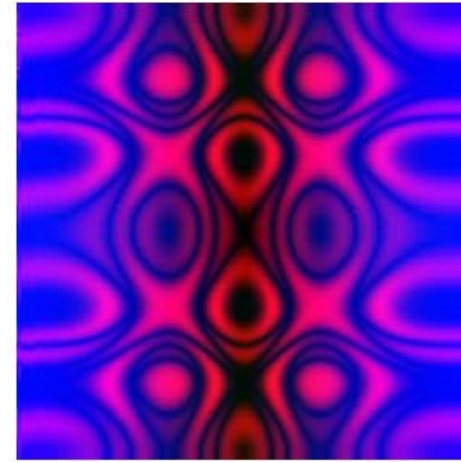
## Example: Art

- Inputs: image pixel position  $x, y$
- Outputs:  $r, g, b$  intensities per pixel
  - Or single monochrome intensity

$$r = f_1(x, y)$$

$$g = f_2(x, y)$$

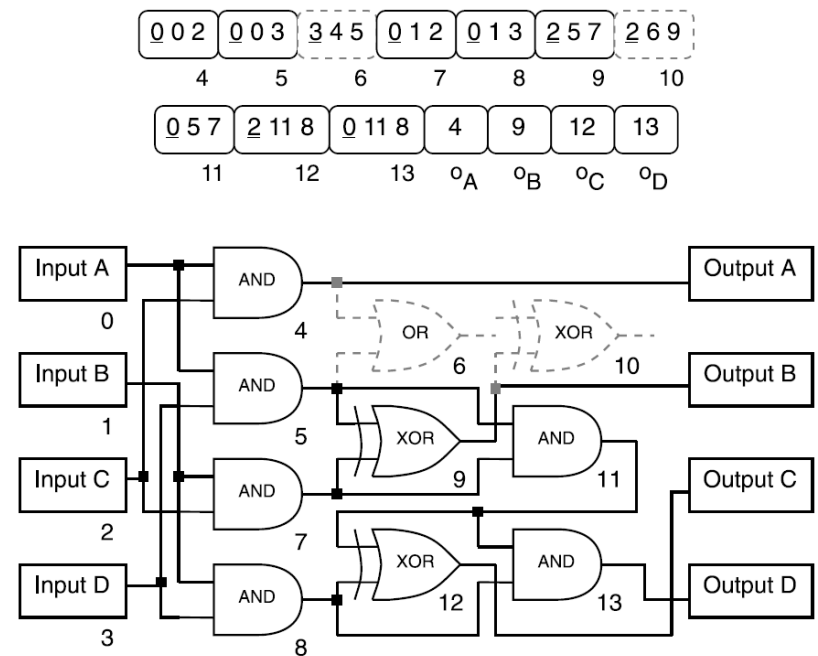
$$b = f_3(x, y)$$



Function gene	Function definition
0	$x$
1	$y$
2	$\sqrt{x + y}$
3	$\sqrt{ x - y }$
4	$255( \sin(\frac{2\pi}{255}x) + \cos(\frac{2\pi}{255}y) )/2$
5	$255( \cos(\frac{2\pi}{255}x) + \sin(\frac{2\pi}{255}y) )/2$
6	$255( \cos(\frac{3\pi}{255}x) + \sin(\frac{2\pi}{255}y) )/2$
7	$\exp(x + y) \pmod{256}$
8	$ \sinh(x + y)  \pmod{256}$

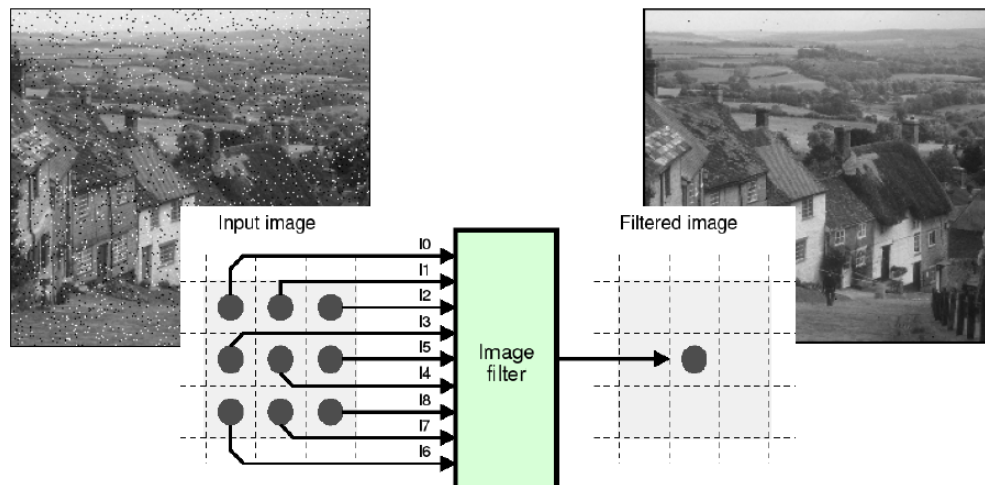
# Example: Evolvable Hardware 1

- Evolution of combinational circuit, e.g. multiplier
- 2-bit multiplier:  
2x2=4 inputs  
4 outputs
- Fitness:  
# correct output combinations (of 16)



## Example: Evolvable Hardware 2

- Evolution of digital image filters
- Input: distorted image
- Output: filtered image
- Fitness: distance between filtered and original image



Number	Function	Description
0	$x \vee y$	binary or
1	$x \wedge y$	binary and
2	$x \oplus y$	binary xor
3	$x + y$	addition
4	$x + y^s$	addition with saturation
5	$(x + y) \gg 1$	average
6	$Max(x, y)$	maximum
7	$Min(x, y)$	minimum



# Example result (slide from Sekanina)

a) Image corrupted by 5% salt-and-pepper noise

PSNR: 18.43 dB (peak signal to noise ratio)

b) Original image

c) Median filter (kernel 3x3)

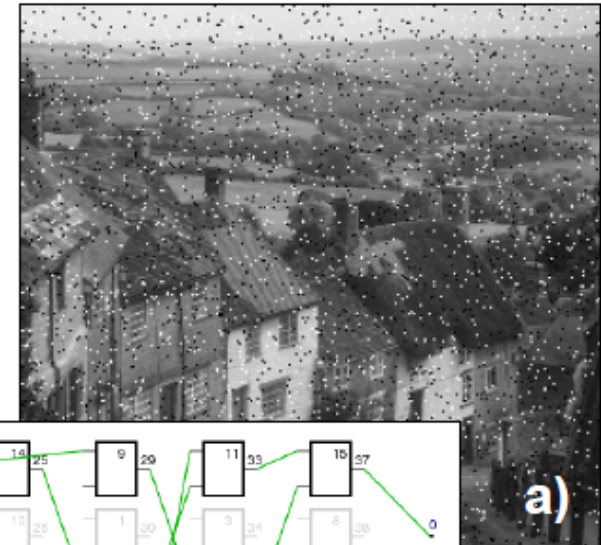
PSNR: 27.92 dB

268 FPGA slices; 305 MHz

d) Evolved filter (kernel 3x3)

PSNR: 37.50 dB

200 FPGA slices; 308 MHz



## Challenges of EHW

- Scalability – It's hard to evolve large systems!
  - General challenge in EC
  - Evolution of larger combinational circuits is difficult
    - Large *and* difficult search space
    - Time-consuming fitness function
    - 4x4 multiplier is hard
- On-chip evolution
  - Less flexibility offered by HW
  - Reconfiguration can be challenging