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Optimization and Search Methods (selection)

- 1. Exhaustive search
- 2. Greedy search and hill climbing
- 3. Gradient ascent
- 4. Simulated annealing

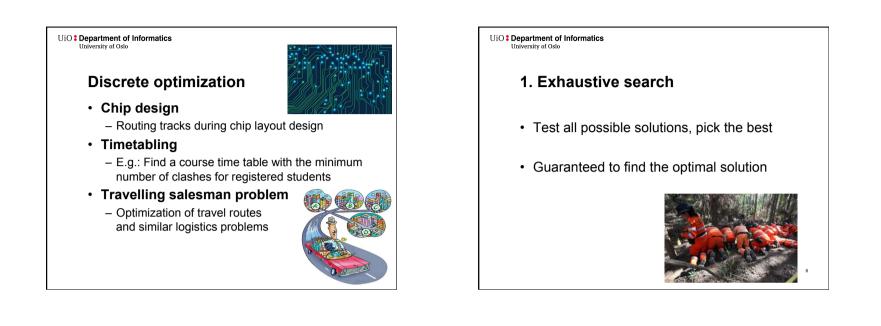
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Optimization

We need

- A numerical representation *x* for all possible solutions to the problem
- A function *f*(*x*) that tells us how good solution *x* is
- A way of finding
 - $\max_{x} f(x)$ if bigger f(x) is better (benefit)
 - $\min_{x} f(x)$ if smaller f(x) is better (cost)

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Exhaustive search

Only works for simple discrete problems, but can be approximated in continuous problems

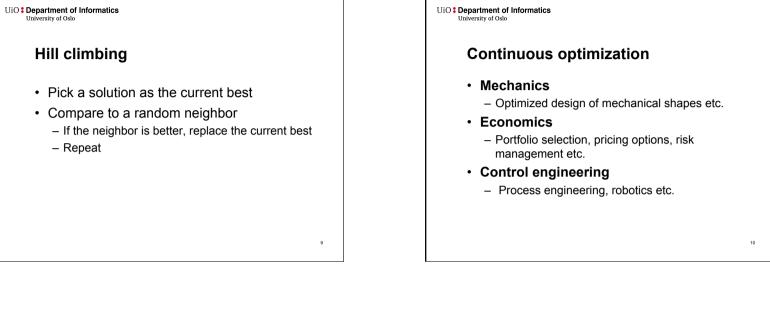
- Sample the space at regular intervals (grid search)
- Sample the space randomly *N* times

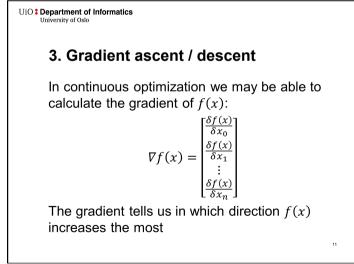
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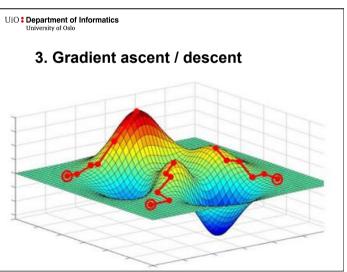
2. Greedy search

- · Pick a solution as the current best
- · Compare to all neighboring solutions
 - If no neighbor is better, then terminate
 - Otherwise, replace the current best with the best of the neighbors
 - Repeat

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Gradient ascent / descent

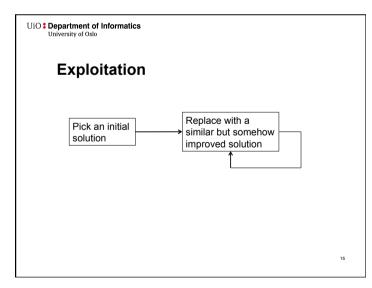
Starting from $x^{(0)}$, we can iteratively find higher $f(x^{(k+1)})$ by adding a value proportional to the gradient to $x^{(k)}$:

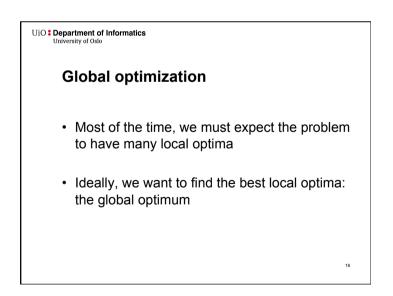
$$x^{(k+1)} = x^{(k)} + \gamma \nabla f(x^{(k)})$$

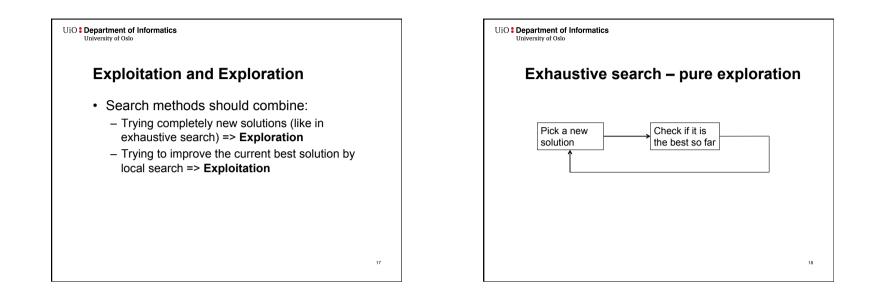
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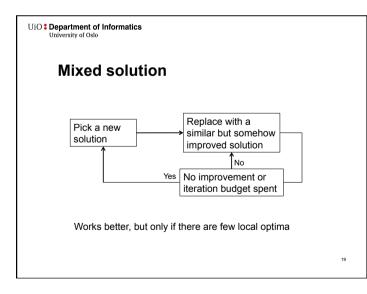
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Local optima
Algorithms like greedy search, hill climbing and gradient ascent/descent can only find local optima:
They will only move through a strictly improving chain of neighbors

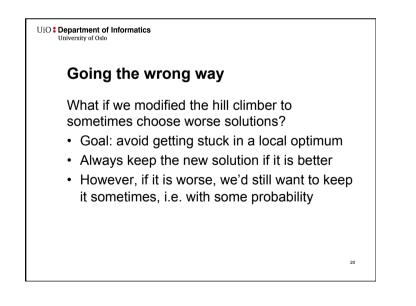
• Once they find a solution with no better neighbors they stop

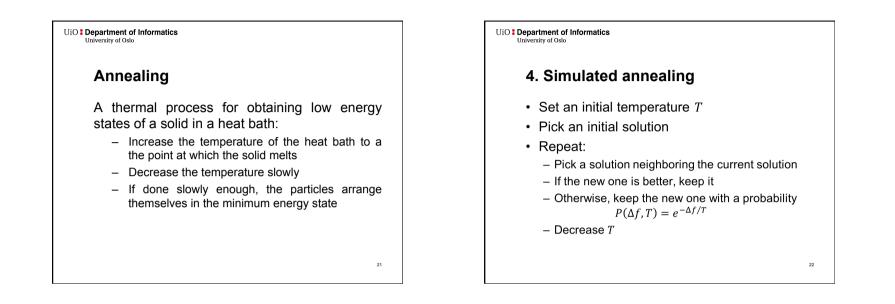


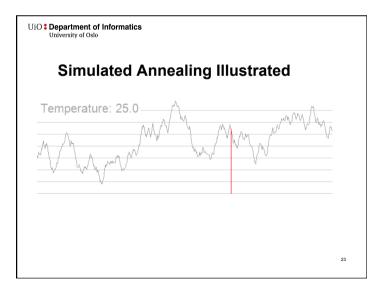












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Repetition Questions

- Which two classes of problems do we work with in optimization?
- What must you accept to obtain optimal solution?
- What controls the search in simulated annealing?

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