INF3510 Information Security
University of Oslo
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Lecture 4
Cryptography

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## Terminology



- Cryptography is the science of secret writing with the goal of hiding the meaning of a message.
- Cryptanalysis is the science and sometimes art of breaking cryptosystems.


## Outline

- What is cryptography?
- Brief crypto history
- Security issues
- Symmetric cryptography
- Stream ciphers
- Block ciphers
- Hash functions
- Asymmetric cryptography
- Factoring based mechanisms
- Discrete Logarithms
- Digital signatures
- Quantum Resistant Crypto

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## What is cryptology?



## Model of symmetric cryptosystem



Numerical encoding of the alphabet

| a | b | c | d | e | f | g | h | i | j | k | l | m | n | o |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| p | q | r | s | t | u | v | w | x | y | y | z | x | ø | a |
| 14 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 |  |

Using this encoding many classical crypto systems can be expressed as algebraic functions over $\mathrm{Z}_{26}$ (English alphabet) or $\mathrm{Z}_{29}$ (Norwegian alphabet)

## Caesar cipher

## Example: Caesar cipher

$\ell=\{a b c d e f g h i j k l m n o p q r s t u v w x y z\}$
\& = \{DEFGHIJKLMNOPQRSTUVWXYZABC $\}$
Plaintext: kryptologi er et spennende fag Chiphertext: nUBSWRORJL нu нт vShеQнеGн IDJ
Note: Caesar chipher in this form does not include a variable key, but is an instance of a "shift-cipher" using key $K=3$.

## Shift cipher

Let $ß=\bowtie=Z_{29}$. For $0 \leq K \leq 28$, we define $\mathrm{E}(x, K)=x+K(\bmod 29)$
and
$\mathrm{D}(y, K)=y-K(\bmod 29)$
$\left(x, y \in Z_{29}\right)$
Question: What is the size of the key space?
Puzzle: ct =
LAHYCXPAJYQHRBWNNMNMOXABNLDANLXVVDWRLJCRXWB
Find the plaintext!

## Exhaustive search

For $[i=0, i<26, i++$, Print["Key = ", i, " Plain = ", decrypt[ct, $1, i]]$ Key $=0$ Plain $=$ LAHYCXPAJYQHRBWNNMNMOXABNLDANLXVVDWRLJCRXWB Key = 1 Plain $=$ KZGXBWOZIXPGQAVMMLMLNWZAMKCZMKWUUCVQKIBQWVA Key = 2 Plain = JYFWAVNYHWOFPZULLKLKMVYZLJBYLJVTTBUPJHAPVUZ Key = 3 Plain = IXEVZUMXGVNEOYTKKJKJLUXYKIAXKIUSSATOIGZOUTY Key = 4 Plain = HWDUYTLWFUMDNXSJJIJIKTWXJHZWJHTRRZSNHFYNTSX Key = 5 Plain = GVCTXSKVETLCMWRIIHIHJSVWIGYVIGSQQYRMGEXMSRW Key = 6 Plain = FUBSWRJUDSKBLVQHHGHGIRUVHFXUHFRPPXQLFDWLRQV Key = 7 Plain = ETARVQITCRJAKUPGGFGFHQTUGEWTGEQOOWPKECVKQPU Key = 8 Plain = DSZQUPHSBQIZJTOFFEFEGPSTFDVSFDPNNVOJDBUJPOT Key = 9 Plain = CRYPTOGRAPHYISNEEDEDFORSECURECOMMUNICATIONS Key = 10 Plain = BQXOSNFQZOGXHRMDDCDCENQRDBTQDBNLLTMHBZSHNMR Key = 11 Plain = APWNRMEPYNFWGQLCCBCBDMPQCASPCAMKKSLGAYRGMLQ Key = 12 Plain = ZOVMQLDOXMEVFPKBBABACLOPBZROBZLJJRKFZXQFLKP
-

## Lessons learned

- A cipher with a small keyspace can easily be attacked by exhaustive search
- A large keyspace is necessary for a secure cipher, but it is by itself not suffcient
- Monoalphabetical substitution ciphers can easily be broken


## Substitution cipher - example

| a | b | c | d | e | f | g | h | i | j | k | 1 | m | n | o |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| U | D | M | I | P | Y | Æ | K | O | X | S | N | $\AA$ | F | A |


| p | q | r | s | t | u | v | w | x | y | z | $\mathfrak{x}$ | $\varnothing$ | a |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| E | R | T | Z | B | Ø | C | Q | G | W | H | L | V | J |  |

Plaintext: fermatssisteteorem Ciphertext: YPTÅUBZZOZBPBPATPÅ

What is the size of the key space?

$$
8841761993739701954543616000000 \text { (1) } 2^{103}
$$

## Enigma

- German WW II crypto machine
- Many different variants
- Polyalphabetical substitution
- Analysed by Polish and English mathematicians


| Enigma key list |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Geheim! |  | Sonder - Maschinenschlüssel BGT |  |  |
| Datum | Walzenlage | Ringatollung | Steokerverbindungen | Grundetollung |
| 31. 30. 29. | IV $\begin{array}{ccc}\text { IV } & \text { II } \\ \text { III } & \text { I } & \text { II } \\ \text { V } & \text { IV } & \text { I }\end{array}$ |  | Ha at ras bit uy dy or do bo kix oa ki JV O: zk ku by yc du gr <br>  | $\begin{aligned} & \text { vyj } \\ & \text { car } \\ & \text { vis } \end{aligned}$ |
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## Attacking ENIGMA

Posisjon:

Crib:
R O M M E L F


## Practical complexity for attacking Enigma

Cryptoanalytical assumptions during WW II:

- 3 out of 5 rotors with known wiring
- 10 stecker couplings
- Known reflector

```
N=150738274937250 60 17576 676 =
107458687327250619360000 (77 bits)
```



## Cryptanalysis: Attacking Cryptosystems



- Classical Attacks
- Mathematical Analysis
- Brute-Force Attack
- Implementation Attack: Try to extract the key through reverse engineering or power measurement, e.g., for a banking smart card.
- Social Engineering: E.g., trick a user into giving up her password


## Brute-Force Attack (or Exhaustive Key Search)

- Treats the cipher as a black box
- Requires (at least) 1 plaintext-ciphertext pair ( $x_{0}, y_{0}$ )
- Check all possible keys until condition is fulfilled:

$$
d_{\kappa}\left(y_{0}\right)=x_{0}
$$

- How many keys to we need?

| Key length <br> in bit | Key space | Security life time <br> (assuming brute-force as best possible attack) |
| :---: | :---: | :--- |
| 64 | $2^{14}$ | Short term (few days or less) |
| 128 | $2^{128}$ | Long-term (several decades in the absence of <br> quantum computers) |
| 256 | $2^{20 \omega}$ | Long-term (also resistant against quantum <br> computers - note that QC do not exist at the <br> moment and might never exist) |

## Attack models:

## Known ciphertext

Known plaintext
Chosen plaintext (adaptive)
Chosen ciphertext (adaptive)
What are the goals of the attacker?

- Find the secret plaintext or part of the plaintext
- Find the encryption key
- Distinguish the encryption of two different plaintexts

How clever is the attacker?

## Kerckhoff's principles

- The system should be, if not theoretically unbreakable, unbreakable in practice.
- The design of a system should not require secrecy and compromise of the system should not inconvenience the correspondents (Kerckhoffs' principle).
- The key should be rememberable without notes and should be easily changeable
- The cryptograms should be transmittable by telegraph
- The apparatus or documents should be portable and operable by a single person
- The system should be easy, neither requiring knowledge of a long list of rules nor involving mental strain


## Does secure ciphers exist?

-What is a secure cipher?

- Perfect security
- Computational security
- Provable security


A perfect secure crypto system


Offers perfect security assuming the key is perfectly random, of same length as The Message; and only used once. Proved by Claude E. Shannon in 1949.

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## White House Crypto Room 1960s



## Symmetric encryption

Is it possible to design secure and practical crypto?

## Symmetric stream cipher



## Stream Cipher vs. Block Cipher



## LFSR

Linear feedback shift register


Using $n$ flip-flops we may generate a binary sequence of period $2^{n}-1$

$$
s_{n+i}=c_{0} s_{i}+c_{1} s_{i+1}+\cdots+c_{n-1} s_{i+n-1}
$$

## LFSR - properties

- Easy to implement in HW, offers fast clocking
- The output sequence is completely determined of the initial state and the feedback coefficients
- Using "correct" feedback a register of length $n$ may generate a sequence with period $2^{n-1}$
- The sequence will provide good statistical properties
- Knowing $2 n$ consecutive bits of the key stream, will reveal the initial state and feedback
- The linearity means that a single LFSR is completely useless as a stream cipher, but LFSRs may be a useful building block for the design of a strong stream cipher


## Itrerated block cipher design



## Symmetric block cipher



Ciphertext

- The algorithm represents a family of permutations of the message space
- Normally designed by iterating a less secure round function
- May be applied in different operational modes
- Must be impossible to derive K based on knowledge of P and $C$

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30

## Substitusjon-Permutasjon nettverk (SPN):

## Round function g :



## Data Encryption Standard

- Published in 1977 by the US National Bureau of Standards for use in unclassified government applications with a 15 year life time.
- 16 round Feistel cipher with 64 -bit data blocks, 56-bit keys.
- 56-bit keys were controversial in 1977; today, exhaustive search on 56 -bit keys is very feasible.
- Controversial because of classified design criteria, however no loop hole was ever found.


## EFF DES-cracker

- Dedicated ASIC with 24 DES search engines
- 27 PCBs housing 1800 circuits
- Can test 92 billion keys per second
- Cost 250000 \$
- DES key found July 1998 after 56 hours search
- Combined effort DES Cracker and 100.000 PCs could test 245 billion keys per second and found key after 22 hours

- DES is the "work horse" which over 40 years have inspired cryptographic research and development

- "Outdated by now"!
- Single DES can not be considered as a secure block cipher
- Use 3DES (ANSI
 9.52) or DESX

```
DES(P):
(\mp@subsup{L}{0}{\prime},\mp@subsup{R}{0}{\prime})=IP(P)
FOR i= 1 TO 16
    Li}=\mp@subsup{R}{i-1}{
    R}=\mp@subsup{L}{i-1}{i-f}f(\mp@subsup{R}{i-1}{\prime-
C=IP-1( (R16},\mp@subsup{L}{16}{}
```

64 bit data block
56 bit key
72.057.594.037.927.936

## DES Status

## Advanced Encryption Standard

- Public competition to replace DES: because 56bit keys and 64-bit data blocks were no longer adequate.
- Rijndael nominated as the new Advanced Encryption Standard (AES) in 2001 [FIPS-197].
- Rijndael (pronounce as "Rhine-doll") designed by Vincent Rijmen and Joan Daemen.
- 128-bit block size (Note error in Harris p. 809)
- 128-bit, 196-bit, and 256-bit key sizes.
- Rijndael is not a Feistel cipher.
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## Rijndael encryption

1. Key mix (round key $K_{0}$ )
2. $N_{r}-1$ rounds containing:
a) Byte substitution
b) Row shift
c) Coloumn mix
d) Key mix (round key $K_{i}$ )
3. Last round containing:

| Key | Rounds |
| :---: | :---: |
| 128 | 10 |
| 192 | 12 |
| 256 | 14 |

a) Byte substitution
b) Row shift
c) Key mix (round key $K_{N_{r}}$ )

Rijndael round function


## Block Ciphers: Modes of Operation

- Block ciphers can be used in different modes in order to provide different security services.
- Common modes include:
- Electronic Code Book (ECB)
- Cipher Block Chaining (CBC)
- Output Feedback (OFB)
- Cipher Feedback (CFB)
- Counter Mode (CTR)
- Galois Counter Mode (GCM) \{Authenticated encryption\}



## Hash functions



## Integrity Check Functions

## Applications of hash functions

- Protection of password
- Comparing files
- Authentication of SW distributions
- Bitcoin
- Generation of Message Authentication Codes (MAC)
- Digital signatures
- Pseudo number generation/Mask generation functions
- Key derivation


## Hash functions (message digest functions)

Requirements for a one-way hash function $h$ :

1. Ease of computation: given $x$, it is easy to compute $h(x)$.
2. Compression: $h$ maps inputs $x$ of arbitrary bitlength to outputs $h(x)$ of a fixed bitlength $n$.
3. One-way: given a value $y$, it is computationally infeasible to find an input $x$ so that $h(x)=y$.
4. Collision resistance: it is computationally infeasible to find $x$ and $x^{\prime}$, where $x \neq x^{\prime}$, with $h(x)=h\left(x^{\prime}\right)$ (note: two variants of this property).

## Frequently used hash functions

- MD5: 128 bit digest. Broken. Often used in Internet protocols but no longer recommended.
- SHA-1 (Secure Hash Algorithm):160 bit digest. Potential attacks exist. Designed to operate with the US Digital Signature Standard (DSA);
- SHA-256, 384, 512 bit digest. Still secure. Replacement for SHA-1 (SHA-2 family)
- RIPEMD-160: 160 bit digest. Still secure. Hash function frequently used by European cryptographic service providers.
- NIST competition for new secure hash algorithm, announcement of winner in 2012: SHA-3 = Keccak


## Properties of hash functions



Ease of Pre-image Collision Weak collision Strong computationresistance resistance collision (2 $2^{\text {nd }}$ pre-image resistance resistance)
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46

## And the winner is?

- NIST announced Keccak as the winner of the SHA-3 Cryptographic Hash Algorithm Competition on October 2, 2012, and ended the fiveyear competition.
- Keccak was designed by a team of cryptographers from Belgium and Italy, they are:
- Guido Bertoni (Italy) of STMicroelectronics,
- Joan Daemen (Belgium) of STMicroelectronics,
- Michaël Peeters (Belgium) of NXP Semiconductors, and
- Gilles Van Assche (Belgium) of STMicroelectronics.



## Keccak and sponge functions



## MAC and MAC algorithms

- MAC means two things:

1. The computed message authentication code $h(M, k)$
2. General name for algorithms used to compute a MAC

- In practice, the MAC algorithm is e.g.
- HMAC (Hash-based MAC algorithm))
- CBC-MAC (CBC based MAC algorithm)
- CMAC (Cipher-based MAC algorithm)
- MAC algorithms, a.k.a. keyed hash functions, support data origin authentication services.


## HMAC




## Public-Key Cryptography

Asymmetric crypto system


## Public key inventors?

Marty Hellman and Whit Diffie, Stanford 1976

R. Rivest, A. Shamir and L. Adleman, MIT 1978


James Ellis, CESG 1970

C. Cocks, M. Williamson, CESG 1973-1974


## One-way functions

## Modular power function

Given $n=p q$, where $p$ and $q$ are prime numbers. No efficient algoritms to find $p$ and $q$.
Chose a positive integer $b$ and define $f: Z_{n} \rightarrow Z_{n}$

$$
f(x)=x^{b} \bmod n
$$

Modular exponentiation
Given prime $p$, generator $g$ and a modular
power $a=g^{x}(\bmod p)$. No


$$
f(x)=g^{x} \bmod p
$$

## Asymmetric crypto

Public key Cryptography was born in May 1975, the child of two problems and a misunderstanding!


Diffie-Hellman key agreement (key exchange) (provides no authentication)

Alice picks random integer a

$g^{a} \bmod p$
$g^{b} \bmod p$
Computationally impossible to compute discrete logarithm

Bob picks random integer b


Alice computes the shared secret

Bob computes the same $\left(g^{b}\right)^{a}=g^{a b} \bmod p$
secret

$$
\left(g^{a}\right)^{b}=g^{a b} \bmod p .
$$

## Example

- $\mathrm{Z}_{11}$ using $g=2$ :
$-2^{1}=2(\bmod 11) 2^{6}=9(\bmod 11)$
$-2^{2}=4(\bmod 11) 2^{7}=7(\bmod 11)$
$-2^{3}=8(\bmod 11) 2^{8}=3(\bmod 11)$
$-2^{4}=5(\bmod 11) \quad 2^{9}=6(\bmod 11)$
$-2^{5}=10(\bmod 11) 2^{10}=1(\bmod 11)$
- $\log _{2} 5=4$
- $\log _{2} 7=7$
- $\log _{2} 1=10(\equiv 0 \bmod 10)$


## Solution

$\mathrm{a}=$
71893136149709653804503478677866573695060790720621260648699193249561437588126371185 81694154929099396752251787268346548051895320171079663652680741564200286881487888963 19895353311170236034836658449187117723820644855184055305945501710227615558093657781 93109639893698220411548578601884177129022057550866690223052160523604836233675971504 25938247630127368253363295292024736143937779912318142315499711747531882501424082252 28164641111954587558230112140813226698098654739025636607106425212812421038155501562 37005192231836155067262308141154795194735834753570104459663325337960304941906119476 18181858300094662765895526963615406

It is easy to compute $g^{a}(\bmod p)\{0.016 \mathrm{~s}\}$, but it is computaionally infeasable to compute the exponent a from the $g^{a}$.

## Example (2)

$\mathrm{p}=$
3019662633453665226674644411185277127204721722044543980521881984280643980698016315342127777985323 7655786915947633907457862442472144616346714598423225826077976000905549946633556169688641786953396 004062371399599729544977400404541673313622576825171747563463840240911791172271560696187007629722 4159137526583857970362142317237148068590959528891803802119028293828368386437223302582405986762635 8694772029533769528178666567879514981999272674689885986300092124730492599541021908208672727813714
8522572014844749083522090193190746907275606521624184144352256368927493398678089550310568789287558 75522700141844883356351776833964003

| $\mathrm{g}=$ |
| :--- |
| 172148 |
|  |
|  |
|  |

1721484410294542720413651217788953849637988183467987659847411571496616170507302662812929883501017 434825030800687783410370272726972149996676832329054021699277098672853850874238294159567224862481 994917939749447675055374786840972654044030577846000645054950424877666860986820152109887355204363 7965394509849072406890541468179263651065250794610243485216627272170663501147422628994581789339082 5760420560620966283259002319100903253019113331521813948039086102149370446134117406508009893347295 86051242347771056691010439032429058
Finn a når
$\mathrm{g}^{\mathrm{a}}(\bmod \mathrm{p})={ }_{4411321635506521515968448863968324914909246042765028824594289876687657182492169027666262097915382}$ 095283045510398284970505498042700025824132106744516429194570987544967423710675451610327665825672 2413603372376920980338976048557155564281928533840136742732489850550648761094630053148353906425838 531769836155990739225236096893433855826960338951917912191504973335370208372185642198804149220798 2700988032756016626566167579963223042395414267579262222147625965023052419869061244027798941410432 6855174387813098860607831088110617

Ron Rivest, Adi Shamir and Len Adleman


- Read about public-key cryptography in 1976 article by Diffie \& Hellman: "New directions in cryptography"
- Intrigued, they worked on finding a practical algorithm
- Spent several months in 1976 to re-invent the method for non-secret/public-key encryption discovered by Clifford Cocks 3 years earlier
- Named RSA algorithm


## RSA parametre (textbook version)

- Bob generates two large prime numbers $p$ and $q$ and computes $n=p q$.
- He then computes a public encryption exponent $e$, such that
- $(e,(p-1)(q-1)))=1$ and computes the corresponding decryption exsponent $d$, by solving:

$$
d e \equiv 1(\bmod (p-1)(q-1))
$$

- Bob's public key is the pair $\mathrm{P}_{\mathrm{B}}=(e, n)$ and the corresponding private and secret key is $S_{B}=(d, n)$.

Encryption: $\mathrm{C}=\mathrm{M}^{\mathrm{e}}(\bmod n)$ Decryption: $\mathrm{M}=\mathrm{C}^{d}(\bmod n)$

## Factoring record- December 2009

- Find the product of
- $\mathrm{p}=33478071698956898786044169848212690817704794983713768568$
- 912431388982883793878002287614711652531743087737814467999489
- and
- $q=367460436667995904282446337996279526322791581643430876426$
- 76032283815739666511279233373417143396810270092798736308917 ?


## Answer:

$n=123018668453011775513049495838496272077285356959533479219732$ 245215172640050726365751874520219978646938995647494277406384592 519255732630345373154826850791702612214291346167042921431160222 1240479274737794080665351419597459856902143413

Computation time ca. 0.0000003 s on a fast laptop! RSA768 - Largest RSA-modulus that have been factored (12/12-2009) Up to 2007 there was $50000 \$$ prize money for this factorisation!

## RSA toy example

- Set $p=157, q=223$. Then $n=p q=157 \quad 223=35011$ and $(p-1)(q-1)=156 \quad 222=34632$
- Set encryption exponent: $e=14213\{\operatorname{gcd}(34632,14213)=1\}$
- Public key: $(14213,35011)$
- Compute: $d=e^{-1}=14213^{-1}(\bmod 34632)=31613$
- Private key: $(31613,35011)$
- Encryption:
- Plaintext $M=19726$, then $C=19726{ }^{14213}(\bmod 35011)=32986$
- Decryption:
- Cipherertext $C=32986$, then $M=32986^{31613}(\bmod 35011)=19726$

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66

## Computational effort?

- Factoring using NFS-algorithm (Number Field Sieve)
- 6 mnd using 80 cores to find suitable polynomial
- Solding from August 2007 to April 2009 (1500 AMD64-år)
- 192796550 * 192795550 matrise (105 GB)
- 119 days on 8 different clusters
- Corresponds to 2000 years processing on one single core 2.2GHz AMD Opteron (ca. $2^{67}$ instructions)


## Asymmetric Ciphers:

## Examples of Cryptosystems

- RSA: best known asymmetric algorithm.
- RSA = Rivest, Shamir, and Adleman (published 1977)
- Historical Note: U.K. cryptographer Clifford Cocks invented the same algorithm in 1973, but didn't publish.
- ElGamal Cryptosystem
- Based on the difficulty of solving the discrete log problem.
- Elliptic Curve Cryptography
- Based on the difficulty of solving the EC discrete log problem.
- Provides same level of security with smaller key sizes.


## Elliptic curve over R



## Elliptic curves

- Let $p>3$ be a prime. An elliptic curve $y^{2}=x^{3}+a x+b$ over $\operatorname{GF}(p)=Z_{p}$ consist of all solutions $(x, y) \in Z_{p} \times Z_{p}$ to the equation

$$
y^{2} \equiv x^{3}+a x+b(\bmod p)
$$

- where $a, b \in Z_{p}$ are constants such that $4 a^{3}+27 b^{2} \neq 0(\bmod p)$, together with a special point $\quad$ bu which is denoted as the point at infinity.


## Point addition



## Asymmetric Encryption:

Basic encryption operation


- In practice, large messages are not encrypted directly with asymmetric algorithms. Hybrid systems are used, where only symmetric session key is encrypted with asymmetric alg.


Confidentiality Services:
Hybrid Cryptosystems


## Hybrid Cryptosystems

- Symmetric ciphers are faster than asymmetric ciphers (because they are less computationally expensive ), but ...
- Asymmetric ciphers simplify key distribution, therefore ...
- a combination of both symmetric and asymmetric ciphers can be used - a hybrid system:
- The asymmetric cipher is used to distribute a randomly chosen symmetric key.
- The symmetric cipher is used for encrypting bulk data.


## Digital Signatures

## Digital Signature Mechanisms

- A MAC cannot be used as evidence that should be verified by a third party.
- Digital signatures used for non-repudiation, data origin authentication and data integrity services, and in some authentication exchange mechanisms.
- Digital signature mechanisms have three components:
- key generation
- signing procedure (private)
- verification procedure (public)
- Algorithms
- RSA
- DSA and ECDSA

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## Digital Signatures

- To get an authentication service that links a document to $A$ 's name (identity) and not just a verification key, we require a procedure for $B$ to get an authentic copy of $A$ 's public key.
- Only then do we have a service that proves the authenticity of documents 'signed by $A$ '.
- This can be provided by a PKI (Public Key Infrastructure)
- Yet even such a service does not provide nonrepudiation at the level of persons.

Practical digital signature based on hash value


## Difference between MACs \& Dig. Sig.

- MACs and digital signatures are both authentication mechanisms.

- MAC: the verifier needs the secret that was used to compute the MAC; thus a MAC is unsuitable as evidence with a third party.
- The third party does not have the secret.
- The third party cannot distinguish between the parties knowing the secret.

- Digital signatures can be validated by third parties, and can in theory thereby support both non-repudiation and authentication.


## Key length comparison:

Symmetric and Asymmetric ciphers offering comparable security

| AES Key Size | RSA Key Size | Elliptic curve Key <br> Size |
| :---: | :---: | :---: |
| - | 1024 | 163 |
| 128 | 3072 | 256 |
| 192 | 7680 | 384 |
| 256 | 15360 | 512 |

## The eavesdropper strikes back!



## Computing

## NSA Says It "Must Act Now" Against the Quantum Computing <br> Threat

The National Security Agency is worried that quantum
computers will neutralize our best encryption-but doesn't yet
know what to do about that problem

by TomSimonite Febnuary3.2016

## Another look at key lengths



## Quantum Computers

- Proposed by Richard Feynman 1982
- Boosted by P. Schor's algorithm for integer factorization and discrete logarithm in quantum polynomial time
- Operates on qubit - superposition of 0 and 1
- IBM built a 7-bit quantum computer and could find the factors of the integer 15 using NMR techniques in 2001
- NMR does not scale
- Progress continues, but nobody knows if or when a large scale quantum computer ever can be constructed
- QC will kill current public key techniques, but does not mean an end to symmetric crypto
- Post Quantum Crypto (PQC) represents current research initiatives to develop crypto mechanisms that can resist quantum computer attacks!


## Current world record of QF!

| Number | \# of factors | Table 5: Quantum factorization records <br> \# of qubits <br> needed | Algorithm | Year <br> implemented |
| :---: | :---: | :---: | :---: | :---: |
| 15 | 2 | 8 | Implemented <br> without prior <br> knowledge of <br> solution |  |
|  | 2 | 8 | Shor | $2001[2]$ |

Brave new crypto world


Scientific America Technology, Jan 2017
Quantum Computers Ready to Leap Out of the Lab in 2017

Google, Microsoft and a host of labs and start-ups are racing to turn scientific curiosities into working machines
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Quantrum conviputing has long seemed like one of thase technologies that are 20 yeurs axaty, aud dulwars will be: Hul 2017 could be the year that lhe field sheds ste research-orly image
 lights, and have set challenging gaals for this yoar: Tincir amhition retlects a broudes Lrasisition talinty place al start ups and waadernie essearch habs dilke to move forn pure scieace towards engineering

Tcopleam manly hindring things," says Christophee Monron, a physiciest
 TonQ in 2015 . Tre neser seen anything like that. It's no longer just ressarch."

End of lecture

