





Inference rules

Model-theoretic semantics, a quick recap

The previous lecture introduced a model-theoretic semantics for RDF:

- we specified in a mathematically precise way
 - when a triple is true according to a given graph,
 - and when one graph is entailed by another.

Model-theoretic semantics is well-suited for

- studying the behaviour of a logic, since
- it is specified in terms of familiar mathematical objects, such as
 - functions,
 - variables, and
 - relations.

Implementational disadvantages of model semantics

Model-theoretic semantics yields an unambigous notion of entailment,

• But it isn't easy to read off from it what exactly is to be implemented.



- for actually doing the reasoning,
- In order to directly use the model-theoretic semantics,
 - in principle all models would have to be considered.
 - But as there are always infinitely many such interpretations,
 - and an algorithm is a finite object
 - this is impossible.

computing it, that is

Inference rules

Soundness and completeness

Semantics and calculus are typically made to work like chopsticks:

- One proves that,
 - I. every conclusion derivable in the calculus from a set of premises A, is true in all models that satisfy A
 - II. and conversely that every statement entailed by A-models is derivable in the calculus when the elements of A are used as premises.

We say that the calculus is

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- sound wrt the semantics, if (I) holds, and
- complete wrt the semantics, if (II) holds.

Syntactic reasoning

We therefore need means to decide entailment syntactically:

- Syntactic methods operate only on the form of a statement, that is
- on its concrete grammatical structure,
- without recurring to interpretations,
- syntactic reasoning is, in other words, calculation.

Interpretations still figure as the theoretical backdrop, as one typically

• strives to define syntactical methods that are provably equivalent to checking all models

Inference rules

Inference rules

A calculus is usually formulated in terms of

- a set of axioms that represent unquestioned postulates,
- and a set of inference rules for generating new statements.

The general form of an inference rule is:

$$\frac{P_1,\ldots,P_n}{P}$$

- the P_i are premises
- and P is the conclusion.

An inference rule may have,

• any number of premises (typically one or two),

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• but only one conclusion (obviously).

Inference rules

Describing models

Given soundness and completeness of a calculus wrt a semantics:

- the axioms are true in all models (aka valid in the class), and
- P is entailed by all models satisfying P_1, \ldots, P_n

In other words,

- the calculus may be considered a description of the models:
 - P_1, \ldots, P_n -models in which P is false are, for instance, disallowed.
- The calculus thus fixes the basic structure of the world
 - as one chooses to see it

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Inference rules

Inference in the concrete

In a Semantic Web context, inference always means,

• adding triples,

More specifically it means,

- adding new triples to an RDF store (broadly construed),
- on the basis of the triples already in it.

From this point of view a rule

 $\frac{P_1,\ldots,P_n}{P}$

may be read as an instruction;

• "If P_1, \ldots, P_n are all in the store, add P to the store"

RDFS axiomatic triples (excerpt)

RDFS axiomatics

 Only resources have types: rdf:type rdfs:domain rdfs:Resource .
 Domains apply only to properties: rdfs:domain rdfs:domain rdf:Property .
 Ranges apply only to properties: rdfs:range rdfs:domain rdf:Property .
 Only properties are subproperties: rdfs:subPropertyOf rdfs:domain rdf:Property .
 Only classes are subclasses: rdfs:subClassOf rdfs:domain rdfs:Class .

Inference rules

Studying RDFS through inference rules

In this lecture we shall

- study RDFS by example,
- by switching from the semantic point of view,
- to the RDFS inference rules given in the RDFS specification.

All these rules are sound wrt to RDFS semantics, hence

• They will never produce incorrect conclusions

However, as it happens they are not complete, that is

• the calculus will not give you all semantically licensed conclusions.

Inference rules

RDFS incompleteness

The RDFS incompleteness is manifest in certain cases of

• domain and range reasoning.

It is important to be aware of which ones and why, because

- they are quite innocuous looking reasoning patterns,
- that it would otherwise be natural to trust.

Nevertheless, RDFS reasoners usually do not implement them, so

- one may easily end up spending hours trying to fix,
- something that isn't really broken (just badly specified).

We shall see in lecture 7 that these flaws do not carry over to OWL.

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RDFS basics

RDFS in a nutshell

RDFS has often been thought of as a *schema language* for RDF.

- For reasons I shall come back to, this is a habit to suspend,
 - at least if a RDF schema is thought of in analogy to, say, a DTD,
 - as something that limits the set of valid documents.
- RDFS is best thought of as simple system for reasoning about types,
- that is, as a simple ontology language.

RDFS supports three principal kinds of reasoning pattern:

- I. Type propagation:
 - "The beetle is a car, and a car is a motorised vehicle, so ..."
- II. Property inheritance:
 - "Martin lectures at Ifi, and anyone who does so is employed by Ifi, so ..."
- III. Domain and range reasoning:
 - "Only people have birth certificates. Martin has one, therefore ..."

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RDFS basics

Concepts in the RDFS datamodel

Corresponding vocabulary items

- RDFS classes:
 - rdfs:Resource: The class of resources, everything.
 - rdfs:Class: The class of classes.
 - rdf:Property: The class of properties (from rdf)
- RDFS properties
 - rdfs:domain: The domain of a relation.
 - rdfs:range: The range of a relation.
 - rdfs:subClassOf: Concept inclusion.
 - rdfs:subPropertyOf: Property inclusion.

RDFS basics

Talking about sets and relations

Thus RDFS is about sets and relations:

- Nodes are grouped into rdfs:Classes.
- One class may be an rdfs:subClassOf another.
- Edges are grouped into rdf:Properties.
- Properties may be given rdfs:domains and rdfs:ranges





RDFS basics

contd.

Finally,

• a property may be a rdfs:subPropertyOf another.

Stated plainly RDFS is thus

- a simple language for defining class and property taxonomies,
- that is, for defining simple hierarchies of concepts and relations,
- with the ability to interconnect the two by domains and ranges.

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Things to note

This is not an entirely accurate depiction, since

- there is no clear distinction between data and ontology in RDFS.
- This is due to the non-extensional semantics of RDFS:

RDFS basics

Remember;

- Properties may act both as objects and relations, and
- classes may act both as objects and sets,
- in effect blurring the line.

Nevertheless, this tends to be a convenient way to think about it.

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RDFS design patterns
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RDFS design patterns Example **RDFS** ontology: ex:KillerWhale rdf:type rdfs:Class . ex:Mammal rdf:type rdfs:Class . ex:Vertebrate rdf:type rdfs:Class . ex:KillerWhale rdfs:subClassOf ex:Mammal . ex:Mammal rdfs:subClassOf ex:Vertebrate . **RDF** facts: ex:Keiko rdf:type ex:KillerWhale . Inferred triples: ex:Keiko rdf:type ex:Mammal . ex:Keiko rdf:type ex:Vertebrate . and, ex:Keiko rdf:type rdfs:Resource . (from the axiomatic triples). INF3580 :: Spring 2010 Lecture 6 :: 2nd March





RDFS design pattern

- rdf:type, and
- rdf:Property

Rules for property reasoning:

• Transitivity:

u rdfs:subPropertyOf v .v rdfs:subPropertyOf x .u rdfs:subPropertyOf x .rdfs5

• Reflexivity:

u rdf:type rdf:Property .
u rdfs:subPropertyOf u .

• Property transfer:

p rdfs:subPropertyOf p' . u p v . u p' v . rdfs7

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RDFS design patterns

Solution

RDFS Ontology:

writer rdf:type rdf:Property .

author rdf:type rdf:Property .

author rdfs:subPropertyOf dcterms:creator .

writer rdfs:subPropertyOf dcterms:creator .

Effects:

- Any individual for which author or writer is defined,
- will have the same value for the dcterms:creator property.
- The work of integrating the data is thus done by the RDFS engine,
- instead of by a manual editing process.
- Legacy applications that use e.g. author can operate unmodified.

Example I: Harmonizing terminology

Integrating data from multiple sources in general requires:

• Harmonisation of the data under a common vocabulary.

The aim is to

- make similar data answer to the same standardised queries,
- thus making queries independent of the terminology of the sources

For instance:

- Suppose that a legacy bibliography system S uses author, where
- another system T uses writer

And suppose we wish to integrate S and T under a common scheme,

• For instance Dublin Core

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RDFS design patterns

Example II: Keeping track of employees

Large organizations (e.g. universities) offer different kinds of contracts;

- for tenured positions (professors, assisting professors, lecturers),
- for research associates (Post Docs),
- for PhD students,
- for subcontracting.

Employer/employee information can be read off from properties such as:

- profAt (professorship at),
- tenAt (*tenure at*),
- conTo (contracts to),
- funBy (is funded by),
- recSchol (receives scholarship from).

RDFS design patterns

Organising the properties



RDFS design patterns

cont.

We may now query on different levels of abstraction :

Aggregating employment relations

SELECT ?temp ?perm ?all WH	ERE {
?temp :tempEmp _:x .	
<pre>?perm :permEmp _:y .</pre>	
?all <mark>:empBy</mark> _:z .	
}	

And get different aggregates in return:

all	perm	temp
Arild	Arild	
Jenny	Jenny	
Martin		Martin
Audun		Audun
Trond		Trond

Querying the inferred model

RDFS design patterns

Formalising the tree:

:profAt rdf:type rdfs:Property .

:tenAt rdf:type rdfs:Property .

:profAt rdfs:subPropertyOf :tenAt

..... and so forth.

Given a data set such as:

:Arild :profAt :UiO . :Audun :fundBy :UiO .

:Martin :conTo :OLF .

:Trond :recSchol :BI .

:Jenny :tenAt :SSB .

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RDFS design patterns



Triggered by combinations of

- rdfs:range
- rdfs:domain
- rdf:type

Rules for damain and range reasoning :

• Typing first coordinates:



• Typing second coordinates:

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RDFS design pattern

Domain and range contd.

- rdfs:domain and rdfs:range tell us how a property is used.
- rdfs:domain types the possible possible subjects of these triples,
- whereas rdfs:range types the possible objects,
- When we assert that property p has domain C, we are saying
 - that whatever is linked to anything by p,
 - must be an object of type C,
 - wherefore an application of p suffices to type that resource.

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RDFS design pattern

Example I: Combining domain, range and subClassOf

Suppose we have a class tree that includes:

:SymphonyOrchestra rdfs:subClassOf :Ensemble .

and a property :conductor whose domain and range are:

:conductor rdfs:domain :SymphonyOrchestra .

:conductor rdfs:range :Person .

Now, if we assert

:OsloPhilharmonic :conductor :Saraste .

we may infer;

:OsloPhilharmonic rdf:type :SymphonyOrchestra .

:OsloPhilharmonic rdf:type :Ensemble .

:Saraste rdf:type :Person .

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RDFS design patterns

Example II: Filtering information based on use

Consider once more the dataset:

- :Arild :profAt :UiO .
- :Audun :fundBy :UiO .
- :Martin :conTo :OLF .
- :Trond :recSchol :BI .
- :Jenny :tenAt :SSB .

and suppose we wish to filter out everyone but the freelancers:

- State that only freelancers :contractsTo an organisation,
- i.e. introduce a class :Freelancer,
- and declare it to be the domain of :contractsTo: :freelancer rdf:type rdfs:Class . :contractsTo rdfs:domain :Freelancer .



RDFS design patterns The incompleteness of RDFS That is: • We make :conductor a subproperty of _:x, • _: x is a generic relation between people and orchestras, • to be used whenever we want the associated restrictions. We would then want to be able to reason as follows (names abbreviated): :Oslo :vis :Abadi . :vis rdfs:subProp _:x . rdfs2 <u>:Oslo _:x :Aba</u>di . ____rdfs7 _:x rdfs:domain :Person :Abadi rdfs:type :Person 39 / 47INF3580 :: Spring 2010 Lecture 6 :: 2nd March

A conspicuous non-pattern

Suppose we elaborate on our music example in the following way:



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Contd.
However, we cannot use rdfs2 and rdfs7 in this way,
since it requires putting a blank in predicate position,
which is not legitimate RDF.
Hence, the conclusion is not derivable.
Nevertheless,
this really *is* a semantically valid inference,
... you are hereby encouraged to check this for yourself,
whence the RDFS rules are incomplete wrt. RDFS semantics.

RDFS design patterns

Assessing the situation

 RDFS reasoners usually implement only the standardised incomplete rules, so

• they do not guarantee complete reasoning.

Better therefore;

- if all you need is the three RDFS reasoning patterns,
- to use OWL and OWL reasoners instead.

Unless, of course

- you need to talk about properties and classes as objects,
- that is, you need the meta-modelling facilities of RDFS,
- but people rarely do.

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Domains, ranges and open worlds

Gentle RDFS

Recall that RDF Schema was conceived of as a schema language for RDF.

- However, the statements in an RDFS ontology never trigger inconsistencies.
- This is due to the open world semantics of RDFS.
- Example: Say we have the following triples;

:isRecordedBy rdfs:range :Orchestra .
:Turangalila :isRecordedBy :Boston .

- Suppose now that Boston is not defined to be an Orchestra:
 - i.e., there is no triple :Boston rdf:type :Orchestra . in the data.
- Then if the closed world assumption were adopted,
- it would follow that :Boston is not an :Orchestra,
- which contradicts the rule rdfs7:

:isRecordedBy rdfs:range :Orchestra . :Turangalila :isRecordedBy :Boston . :Boston rdf:type :Orchestra . rdf

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Domains, ranges and open worlds

Contd.

Instead;

- RDFS infers a new triple.
- More specifically it adds :Boston rdf:type :Orchestra .
- which is precisely what rdfs7 is designed to do.

This is open world reasoning in action:

- Instead of saying "I know that :Boston is not an :Orchestra",
- RDFS says ":Boston is an :Orchestra, I just didn't know it."

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- RDFS will not signal an inconsistency, therefore
- but rather just add the missing information

Domains, ranges and open world

Ramifications

This fact has two important consequences:

- RDFS is useless for validation,
 - ... understood as sorting conformant from non-conformant documents,
 - since it never signals an inconsistency in the data,
 - it just goes along with anything,
 - and adds triples whenever they are inferred,
 - It is *in this respect* more like a database schema,
 - which declares what joins are possible,
 - but makes no statement about the validity of the joined data.
 - Note though, that validation functionality beyond RDFS is often implemented in RDFS reasoners.
- PRDFS has no notion of negation at all
 - For instance, the two triples
 - ex:Martin rdf:type ex:Smoker .,
 - ex:Martin rdf:type ex:NonSmoker .

are not inconsistent.

• (It is not possible to in RDFS to say that ex:Smoker and ex:nonSmoker are disjoint).

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Domains, ranges and open worlds Supplementary reading • For RDFS design patterns: Semantic Web for the Working Ontologist. Allemang, Hendler. Morgan Kaufmann 2008 Read chapter 6. Foundations of • For RDFS semantics: Semantic Web Read chapter 3. Technologies



Expressive limitations of RDFS

Hence,

- RDFS cannot express inconsistencies,
- so any RDFS graph is consistent.

Therefore,

- RDFS supports no reasoning services that require consistency-checking.
- If consistency-checks are needed, one must turn to OWL.
- More about that in the next lecture.

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