

# INF3580 – Semantic Technologies – Spring 2011

## Lecture 11: OWL 2

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OSLO

# Outline

- 1 Reminder: *ALC*
- 2 OWL 2
- 3 Axioms and assertions using individuals
- 4 Restrictions on roles
- 5 Modelling problems
- 6 Roles
- 7 Datatypes

# $\mathcal{ALC}$ Semantics

## Interpretation

An interpretation  $\mathcal{I}$  fixes a set  $\Delta^{\mathcal{I}}$ , the *domain*,  $A^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}}$  for each atomic concept  $A$ ,  $R^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$  for each role  $R$ , and  $a^{\mathcal{I}} \in \Delta^{\mathcal{I}}$  for each individual  $a$ .

## Interpretation of concept descriptions

$$\begin{aligned} \top^{\mathcal{I}} &= \Delta^{\mathcal{I}} \\ \perp^{\mathcal{I}} &= \emptyset \\ (\neg C)^{\mathcal{I}} &= \Delta^{\mathcal{I}} \setminus C^{\mathcal{I}} \\ (C \sqcap D)^{\mathcal{I}} &= C^{\mathcal{I}} \cap D^{\mathcal{I}} \\ (C \sqcup D)^{\mathcal{I}} &= C^{\mathcal{I}} \cup D^{\mathcal{I}} \\ (\forall R.C)^{\mathcal{I}} &= \{a \in \Delta^{\mathcal{I}} \mid \text{for all } b, \text{ if } \langle a, b \rangle \in R^{\mathcal{I}} \text{ then } b \in C^{\mathcal{I}}\} \\ (\exists R.C)^{\mathcal{I}} &= \{a \in \Delta^{\mathcal{I}} \mid \text{there is a } b \text{ where } \langle a, b \rangle \in R^{\mathcal{I}} \text{ and } b \in C^{\mathcal{I}}\} \end{aligned}$$

## Interpretation of Axioms

- $\mathcal{I} \models C \sqsubseteq D$  if  $C^{\mathcal{I}} \subseteq D^{\mathcal{I}}$  and  $\mathcal{I} \models C \equiv D$  if  $C^{\mathcal{I}} = D^{\mathcal{I}}$
- $\mathcal{I} \models C(a)$  if  $a^{\mathcal{I}} \in C^{\mathcal{I}}$  and  $\mathcal{I} \models R(a, b)$  if  $\langle a^{\mathcal{I}}, b^{\mathcal{I}} \rangle \in R^{\mathcal{I}}$ .

# TBox, ABox

- The TBox

- is for *terminological knowledge*,
- is independent of any actual instance data, and
- for  $\mathcal{ALC}$ , it is a set of  $\sqsubseteq$  axioms and  $\equiv$  axioms.
- Example TBox axioms:
  - $TwoCV \sqsubseteq \forall driveAxle.FrontAxle$
  - $FrontDrivenCar \equiv Car \sqcap \forall driveAxle.FrontAxle$ .

- The ABox

- is for *assertional knowledge*,
- contains facts about individuals  $a, b, c$ ,
- a set of concept membership assertions  $C(a)$ ,
- and role assertions  $R(b, c)$ .
- Example ABox axioms:
  - $driveAxle(myCar, axle)$
  - $(FrontAxle \sqcup RearAxle)(axle)$ .

# Modelling patterns

So, what can we say with  $\mathcal{ALC}$ ?

- ✓ Every person has a mother.
- ✓ Penguins eats only fish. Horses eats only chocolate.
- ✗ Every nuclear family has two parents, at least two children and a dog.
- ✓ No smoker is a non-smoker (and vice versa).
- ✗ Everybody loves Mary.
- ✗ Adam is not Eve (and vice versa).
- ✓ Everything is black or white.
- ✓ There is no such thing as a free lunch.
- ✗ Brothers of fathers are uncles.
- ✗ My friend's friends are also my friends.
- ✗ If Homer is married to Marge, then Marge is married to Homer.
- ✗ If Homer is a parent of Bart, then Bart is a child of Homer.

Today we'll learn how to say more.

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# *SHOIN*( $\mathcal{D}$ ) and OWL 2

- OWL 2 is based on the DL *SHOIN*( $\mathcal{D}$ ):
  - *S* for  $ALC^1$  plus role transitivity,
  - *H* for roles hierarchies,
  - *O* for closed classes,
  - *I* for inverse roles,
  - *N* for cardinality restrictions, and
  - *D* for datatypes.
- So, today we'll see:
  - new concept and role builders,
  - new TBox axioms,
  - new ABox axioms,
  - new RBox and axioms, and
  - datatypes!



Focus!

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<sup>1</sup>Attributive Concept Language with Complements

## OWL 2 and its profiles

- OWL 2 has various *profiles* that correspond to different DLs.
- OWL 2 DL is the “normal” OWL 2 (sublanguage): “maximum” expressivity while keeping reasoning problems decidable—but still very expensive.
- (Other) profiles are tailored for specific ends, e.g.,
  - OWL 2 QL:
    - Specifically designed for efficient database integration.
  - OWL 2 EL:
    - A lightweight language with polynomial time reasoning.
  - OWL 2 RL:
    - Designed for compatibility with rule-based inference tools.
- OWL Full: Anything goes: classes, relations, individuals, ... like in RDFS, are not kept apart. Highly expressive, not decidable. But we want OWL's reasoning capabilities, so stay away if you can—and you almost always can.

OWL 2 Validator: <http://owl.cs.manchester.ac.uk/validator/>



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# Individual identity

- New ABox axioms.
- Express equality and non-equality between individuals.
- Syntax:
  - DL:  $a = b$ ,  $a \neq b$ ;
  - RDF/OWL: `:a owl:sameAs :b`, `:a owl:differentFrom :b`,
  - Manchester: `SameAs`, `DifferentFrom`.
- Semantics:
  - $\mathcal{I} \models a = b$  iff  $a^{\mathcal{I}} = b^{\mathcal{I}}$
  - $\mathcal{I} \models a \neq b$  iff  $a^{\mathcal{I}} \neq b^{\mathcal{I}}$
- Examples:
  - `sim:Bart owl:sameAs dbpedia:Bart_Simpson`,
  - `sim:Bart owl:differentFrom sim:Homer`.
- Remember:
  - Non unique name assumption (NUNA) in Sem. Web,
  - must use `=` and `≠` to get expected results.

# Creating concepts using individuals

- New concept builder.
- Create (anonymous) concepts by explicitly giving all members.
- Called *closed classes* in OWL.
- Syntax:
  - DL:  $\{a, b, \dots\}$
  - RDF/OWL: `oneOf + rdf:List++`
  - Manchester:  $\{a, b, \dots\}$
- Example:
  - $SimpsonFamilyMember \equiv \{Homer, Marge, Bart, Lisa, Maggie\}$
- Note:
  - The individuals does not necessarily represent different objects,
  - we still need  $=$  and  $\neq$  to say that members are the same/different.
  - “Closed classes of data values” are *datatypes*.

## Axioms involving individuals: Closed classes

- Using closed classes we can exclude individuals from classes.
- Example:  $\{NedFlanders\} \sqsubseteq \neg SimpsonFamilyMember$ .
  - Ned Flanders is not a family member of the Simpsons.
  - (or better:  $FlandersFamilyMember \equiv \{NedFlanders, \dots\}$  and  $FlandersFamilyMember \sqsubseteq \neg SimpsonFamilyMember$ .)
- *Closed properties* does not exist in OWL
- (can be done with closed classes),
- but there is *negated role assignment* to exclude relationships from relations/roles (on next slide):

# Axioms involving individuals: Negative Property Assertions

- New ABox axiom.
- Syntax:
  - DL:  $\neg R(a, b)$ ,
  - RDF/OWL: `NegativePropertyAssertion`,
  - Manchester: `a not R b`.
- Semantics:
  - $\mathcal{I} \models \neg R(a, b)$  iff  $\langle a^{\mathcal{I}}, b^{\mathcal{I}} \rangle \notin R^{\mathcal{I}}$ ,
- Notes:
  - Works both for object properties and datatype properties.
- Examples:
  - `:Bart not :hasFather :NedFlanders`
  - `:Bart not :hasAge '2'`

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# Recap of existential and universal restrictions

- Existential restrictions

- have the form  $\exists R.D$ ,
- typically used to connect classes,
- $C \sqsubseteq \exists R.D$ : A  $C$  is  $R$ -related to (at least) *some*  $D$ :
  - Example: A person has a female parent:  $Person \sqsubseteq \exists hasParent.Woman$ .
- Note that  $C$ -objects can be  $R$ -related to other things:
  - A person may have other parents who are not women—but there must be one who's a woman.

- Universal restrictions

- have the form  $\forall R.D$ ,
- restrict the things a type of object can be connected to,
- $C \sqsubseteq \forall R.C$  :  $C$  is  $R$ -related to  $D$ 's *only*:
  - Example: A horse eats only chocolate:  $Horse \sqsubseteq \forall eats.Chocolate$ .
- Note that  $C$ -objects may not be  $R$ -related to anything at all:
  - A horse does not have to eat anything—but if it does it must be chocolate.

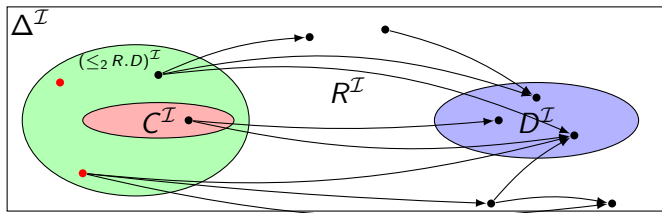
# Cardinality restrictions

- New concept builder.
- Syntax:
  - DL:  $\leq_n R.D$  and  $\geq_n R.D$  (and  $=_n R.D$ ).
  - RDF/OWL: `minCardinality`, `maxCardinality`, `cardinality`.
  - Manchester: `min`, `max`, `exactly`.
- Semantics:
  - $(\leq_n R.D)^{\mathcal{I}} = \{a \in \Delta^{\mathcal{I}} \mid \#\{b : \langle a, b \rangle \in R^{\mathcal{I}} \wedge b \in D^{\mathcal{I}}\} \leq n\}$
  - $(\geq_n R.D)^{\mathcal{I}} = \{a \in \Delta^{\mathcal{I}} \mid \#\{b : \langle a, b \rangle \in R^{\mathcal{I}} \wedge b \in D^{\mathcal{I}}\} \geq n\}$
- Restricts the number of relations a type of object can/must have.
- TBox axioms read:
  - $C \sqsubseteq \square_n R.D$ : "A C is R-related to  $n$  number of D's."
    - $\leq$ : *at least*
    - $\geq$ : *at most*
    - $=$ : *exactly*



# Example cardinality restriction

- $C \sqsubseteq \leq_2 R.D$



- Examples:

- $Car \sqsubseteq \leq_2 driveAxle.T$

- "A car has at least two drive axles."

- $RangeRover \sqsubseteq =_1 driveAxle.FrontAxle \sqcap =_1 driveAxle.RearAxle$

- "A Range Rover has one front axle as drive axle and one rear axle as drive axle".

# One more value restriction

- Existential and Universal restrictions are called *value restrictions*.
- Restrictions of the form  $\forall R.D$ ,  $\exists R.D$ ,  $\leq_n R.D$ ,  $\geq_n R.D$  are called *qualified* when  $D$  is not  $\top$ .
- Qualified: the restriction require  $R$ -relations to “hit”  $D$ 's.
- We can also qualify with a closed class.
- Syntax:
  - RDF/OWL: `hasValue`,
  - DL, Manchester: just use: `{...}`.
- Example:
  - $Bieberette \equiv Girl \sqcap \exists loves.\{J.Bieber\}$

# Self restriction

- New construct builder.
- Local reflexivity restriction. Restricts to objects which are related to themselves.
- Syntax:
  - DL:  $\exists R.Self$
  - RDF/OWL: `owl:hasSelf`,
  - Manchester: `Self`
- Semantics:
  - $(\exists R.Self)^{\mathcal{I}} = \{x \mid \langle x, x \rangle \in R^{\mathcal{I}}\}$
- Examples:
  - $AutoregulatingProcess \sqsubseteq \exists regulate.Self$
  - $\exists hate.Self \sqsubseteq UnhappyPerson$

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# Restrictions, non-unique names and open worlds

Restrictions + the OWA and the NUNA can be tricky, consider:

## TBox:

$Orchestra \sqsubseteq Ensemble$

$ChamberEnsemble \sqsubseteq Ensemble$

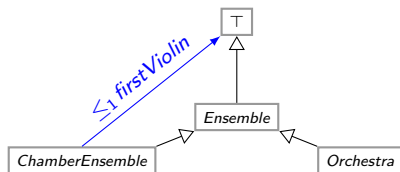
$ChamberEnsemble \sqsubseteq \leq_1 firstViolin.T$

## ABox:

`Ensemble(oslo)`

`firstViolin(oslo, skolem)`

`firstViolin(oslo, lie)`



- Orchestras and Chamber ensembles are Ensembles.
- Chamber ensembles have only one instrument on each voice, in particular, only one first violin.
- oslo has two first violins; is oslo an Orchestra?

## Unexpected (non-)results

It does not follow from  $TBox + ABox$  that `oslo` is an *Orchestra*:

- An ensemble need neither be an orchestra nor a chamber ensemble, its “just” an ensemble.
- Add “covering axiom”  $Ensemble \sqsubseteq Orchestra \sqcup ChamberEnsemble$ :
  - An ensemble is an orchestra or a chamber ensemble.

It still does not follow that `oslo` is an *Orchestra*:

- This is due to the NUNA.
- We cannot assume that `skolem` and `lie` are distinct.
- The statement `skolem owl:differentFrom lie`, i.e.,  $skolem \neq lie$ , makes `oslo` an orchestra.

If we remove `firstViolin(oslo, lie)`, is `oslo` a *ChamberEnsemble*?

- it does not follow that `oslo` is a *ChamberEnsemble*.
- This is due to the OWA:
- `oslo` may have other first violinists.

## Protégé demo of previous slide

- Make class Ensemble.
- Make subclass Orchestra.
- Make subclass ChamberEnsemble.
- Make object property firstViolin.
- Make `firstViolin max 1` superclass of ChamberEnsemble.
- Make an Ensemble oslo
- Make a Thing skolem
- Make a Thing lie
- Add firstViolin skolem to oslo
- Add firstViolin lie to oslo
- Classify! Nothing happens.
- Add covering axiom: Orchestra or ChamberEnsemble superclass of Ensemble.
- Classify! Nothing happens.
- skolem is different from lie
- Classify! Bingo! oslo is an Orchestra!

# A tempting mistake?

Cardinality restrictions cannot be used to reason with

- intervals or any kind of sequence
- and it cannot be used for arithmetic.
- Example of incorrect modelling:
  - Scotch whisky is casked for (a duration of) more than three years:
  - $Scotch \sqsubseteq Whisky \sqcap \geq_3 casked.Years (*)$



Why incorrect?

- The class *Years* is just a set of objects,
- so the axiom (\*) reads “Scotch is Whisky which is casked in at least three (different) years.”
- These years may be unrelated (other than by type), e.g: 1996, 1999, 2010.
- $\geq_{12} casked.Years$  is not *longer* than  $\geq_3 casked.Years$



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# Roles and RBoxes

- Just as we have TBoxes and ABoxes for axioms concerning concepts and individual respectively,
- there is an RBox for axioms on roles.
- In the RBox we find
  - role relationships axioms and
  - role characteristics axioms.
- Consider these boxes convenient for bookkeeping,
- and they are used in literature.



Boxes!

# Role characteristics and relationships

- A role can be:
  - atomic,
  - the universal role, the empty role,
  - the inverse of a role, or
  - a chain of roles. (The two latter are role builders).
- A role can have the characteristics (axioms):
  - reflexive, irreflexive,
  - symmetric, asymmetric,
  - transitive, or/and<sup>2</sup>
  - functional, inverse functional.
- Role axioms: Let  $R$  and  $S$  be roles, then we can assert
  - subsumption:  $R^{\mathcal{I}} \subseteq S^{\mathcal{I}}$ ,
  - equivalence:  $R^{\mathcal{I}} = S^{\mathcal{I}}$ ,
  - disjointness:  $R^{\mathcal{I}} \cap S^{\mathcal{I}} = \emptyset$ ,
  - key:  $R$  is a *key* for concept  $C$ .



OWL keys!

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<sup>2</sup>Restrictions apply

# New roles

- The universal role, and the empty role—for both object values and data values.
- Syntax:
  - (DL:  $U$  (universal object role),  $mcD$  (universal data value role))
  - RDF/OWL, Manchester: `owl:topObjectProperty`,  
`owl:topDataProperty`, `owl:bottomObjectProperty`,  
`owl:bottomDataProperty`
- Semantics:
  - $U^I = \Delta^I \times \Delta^I$
  - $\mathcal{D}^I = \Delta^I \times \Lambda$
- Reads:
  - all pairs of individuals are connected by `owl:topObjectProperty`,
  - no individuals are connected by `owl:bottomObjectProperty`.
  - all possible individuals are connected with all literals by  
`owl:topDataProperty`,
  - no individual is connected by `owl:bottomDataProperty` to a literal.

# Corresponding mathematical properties and operations

A relation  $R$  over a set  $X$  ( $R \subseteq X \times X$ ) is

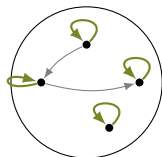
Reflexive:	if $\langle a, a \rangle \in R$ for all $a \in X$
Irreflexive:	if $\langle a, a \rangle \notin R$ for all $a \in X$
Symmetric:	if $\langle a, b \rangle \in R$ implies $\langle b, a \rangle \in R$
Asymmetric:	if $\langle a, b \rangle \in R$ implies $\langle b, a \rangle \notin R$
Transitive:	if $\langle a, b \rangle, \langle b, c \rangle \in R$ implies $\langle a, c \rangle \in R$
Functional:	if $\langle a, b \rangle, \langle a, c \rangle \in R$ implies $b = c$
Inverse functional:	if $\langle a, b \rangle, \langle c, b \rangle \in R$ implies $a = c$

If  $R$  and  $S$  are binary relations on  $X$  then

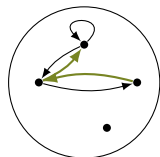
$$\begin{aligned} \langle a, c \rangle \in R \circ S: & \text{ if } \langle a, b \rangle \in R \text{ and } \langle b, c \rangle \in S \text{ for some } b \in X \\ \langle b, a \rangle \in R^{-}: & \text{ if } \langle a, b \rangle \in R. \end{aligned}$$

The syntax for the corresponding axioms is similar, and their semantics should be clear from this slide.

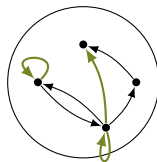
# Role characteristics and operations illustrated



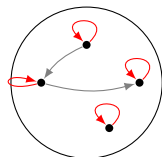
Reflexive



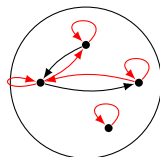
Symmetric



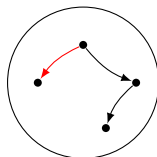
Transitive



Irreflexive

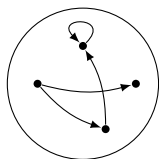
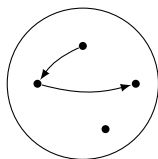
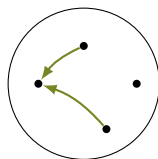
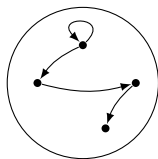
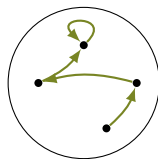


Asymmetric



Functional

# Role chaining and inverses illustrated


 $R$ 

 $S$ 

 $R \circ S$ 

 $T$ 

 $T^-$

# Properties in OWL

Remember: three kinds of *mutually disjoint* properties in OWL:

- ① `owl:DatatypeProperty`
  - link individuals to data values, e.g., `xsd:string`.
  - Examples: `:hasAge`, `:hasSurname`.
- ② `owl:ObjectProperty`
  - link individuals to individuals.
  - Example: `:hasFather`, `:driveAxle`.
- ③ `owl:AnnotationProperty`
  - has no logical implication, ignored by reasoners.
  - Examples: `rdfs:label`, `dc:creator`.



Drive axle!



# Characteristics of OWL properties

- Object properties link individuals to individuals, so all characteristics and operations are defined for them.
- Datatype properties link individuals to data values, so they cannot be
  - reflexive—or they would not be datatype properties,
  - transitive—since no property takes data values in 1. position,
  - symmetric—as above,
  - inverses—as above,
  - inverse functional—for computational reasons,
  - part of chains—as above,
  - so, what remains is: functionality,
  - (and subsumption, equivalence and disjointness).
- (Annotation properties have no logical implication, so nothing can be said about them.)

# Some relations from ordinary language

- Symmetric relations:
  - *hasSibling*
  - *differentFrom*
- Non-symmetric relations:
  - *hasBrother*
- Asymmetric relations:
  - *olderThan*
  - *memberOf*
- Transitive relations:
  - *olderThan*
  - *hasSibling*
- Functional relations:
  - *hasBiologicalMother*
- Inverse functional relations:
  - *gaveBirthTo*



Brother!

# Examples inverses and chains

Some inverses:

- $hasParent \equiv hasChild^{-}$
- $hasBiologicalMother \equiv gaveBirthTo^{-}$
- $olderThan \equiv youngerThan^{-}$

Some role chains:

- $hasParent \circ hasParent \sqsubseteq hasGrandParent$
- $isLocatedIn \circ isPartOf \sqsubseteq isLocatedIn$



Grandparents!

# Quirks

Role modelling in OWL 2 can get excessively complicated.

- For instance:
  - transitive roles cannot be irreflexive or asymmetric,
  - role inclusions are not allowed to cycle, i.e. not
$$\begin{aligned} \text{hasParent} \circ \text{hasHusband} &\sqsubseteq \text{hasFather} \\ \text{hasFather} &\sqsubseteq \text{hasParent}. \end{aligned}$$
  - transitive roles  $R$  and  $S$  cannot be declared disjoint
- Note:
  - these restrictions can be hard to keep track of
  - the reason they exist are computational, not logical
- Fortunately:
  - There are also *simple* patterns
  - that are quite useful.



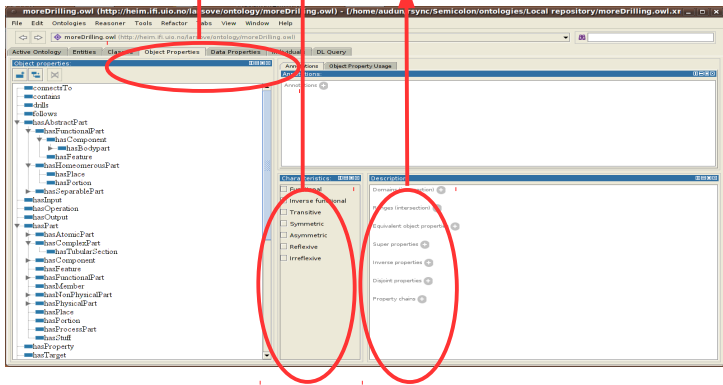
Quirk!

# Managing roles in Protege

Object/datatype property tabs

Role characteristics

Domain/range, role relationships



# OWL keys

- The OWL equivalent of a database primary key, but not completely ...
- Inverse functional properties apply to instances whose existence may only be implied.
- For inverse datatype properties reasoning is impossible in practise.
- OWL Keys apply only to *named instances*, i.e., it's computationally feasible.
- Works for object properties and datatype properties.
- Example: `Course` `hasKey` `{hasCode, hasSemester, hasYear}`:
  - e.g., *this* course is identified by the values ("INF3580", Spring, "2011").
  - if two courses share the same values, they are the same course.

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# Creating datatypes

- Many predefined datatypes are available in OWL:
  - all common XSD datatypes: `xsd:string`, `xsd:int`, ...
  - a few from RDF: `rdf:PlainLiteral`,
  - and a few of their own: `owl:real` and `owl:rational`.
- New datatypes can be defined by boolean operations:  $\neg$ ,  $\sqcap$ ,  $\sqcup$ :
  - `owl:datatypeComplementOf`, `owl:intersectionOf`, `owl:unionOf`.
- Datatypes may be restricted with *constraining facets*, borrowed from XML Schema.
  - For numeric datatypes: `xsd:minInclusive`, `xsd:maxInclusive`
  - For string datatypes: `xsd:minLength`, `xsd:maxLength`, `xsd:pattern`.
- Example:
  - Teenager is equivalent to: (Manchester)  
Person and (age some positiveInteger[>= 13, <= 19])
  - “A teenager is a person of age 13 to 19.”



# Modelling patterns

So, what can we say now?

- ✓ A person has a mother.
- ✓ A penguin eats only fish. A horse eats only chocolate.
- ✓ A nuclear family has two parents, at least two children and a dog.
- ✓ A smoker is not a non-smoker (and vice versa).
- ✓ Everybody loves Mary. ????
- ✓ Adam is not Eve (and vice versa).
- ✓ Everything is black or white.
- ✓ The brother of my father is my uncle.
- ✓ My friend's friends are also my friends.
- ✓ If Homer is married to Marge, then Marge is married to Homer.
- ✓ If Homer is a parent of Bart, then Bart is a child of Homer.

... and more!

# Next week

- Recaps.
- More modelling with OWL/OWL 2.
- What cannot be expressed in OWL/OWL 2?



Cap!