# INF3580/4580 – Semantic Technologies – Spring 2017 Lecture 8: RDF and RDFS semantics

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# Oblig 5

- Published today
- First delivery due 21 March
- Final delivery due 11 April
- Extra question for INF4580 students
- "Real" semantics of RDF and RDFS
- Foundations book: Section 3.2
- Still OK to ignore some complications, see oblig text
- We provide an excerpt of Sect. 3.2 with unimportant parts removed.
- Go to group sessions!

#### Why we need semantics

2 Model-theoretic semantics from a birds-eye perspective

- 3 Repetition: Propositional Logic
- 4 Simplified RDF semantics

### Outline

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A formal semantics for RDFS became necessary because

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### Another look at the Semantic Web cake

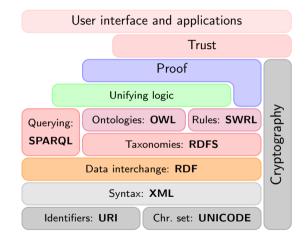


Figure: Semantic Web Stack

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  - and in particular what entailment should be taken to mean.

Why we need semantics

### Example: What is the meaning of blank nodes?

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$$\frac{P \rightarrow Q, P \lor R \vdash Q}{P \rightarrow Q \vdash (P \lor R) \rightarrow Q}$$

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- How do we know that the inference rules are well-chosen?
- Which manipulations derive conclusions that hold in the real world?

Model-theoretic semantics from a birds-eye perspective

# Finding out stuff about the World

The "Real World"



- G: Aristotle was Greek
- H: Aristotle was human
- M: Aristotle was mortal

Statements

 $G \to H$  $H \to M$ 

G: Aristotle was Greek

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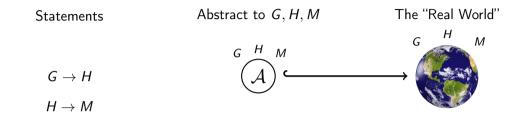
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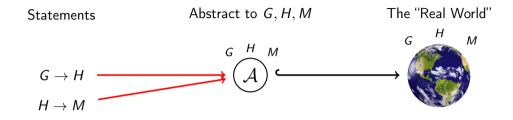


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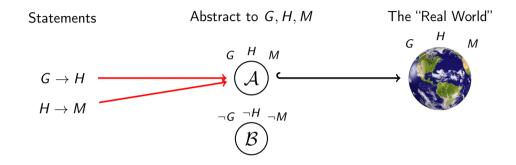
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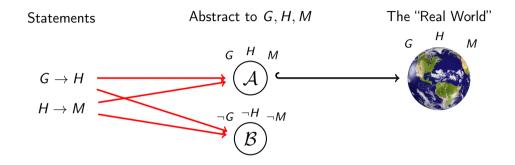
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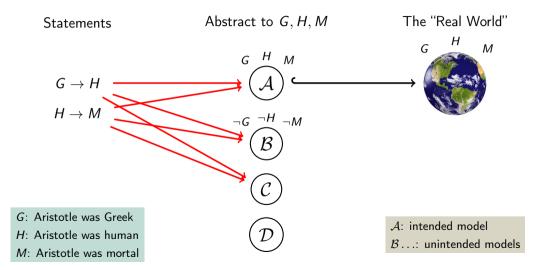


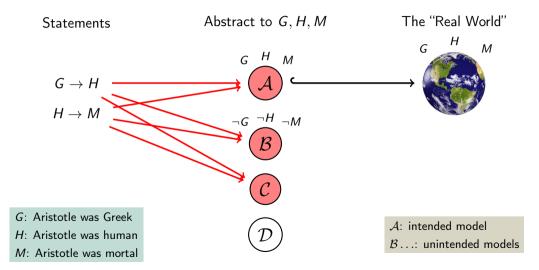
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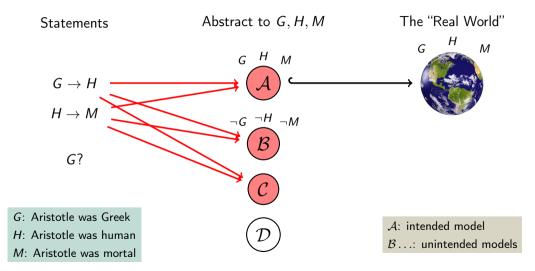
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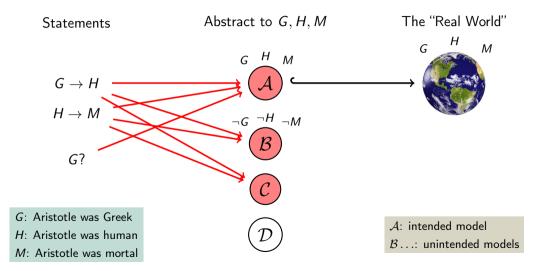
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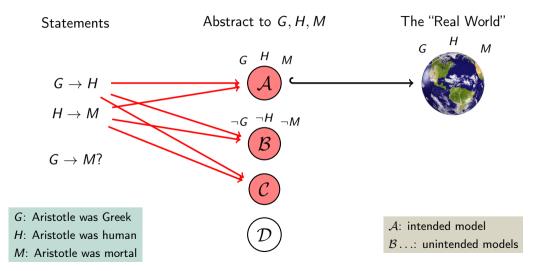
 $\mathcal{A}$ : intended model  $\mathcal{B}$ ...: unintended models

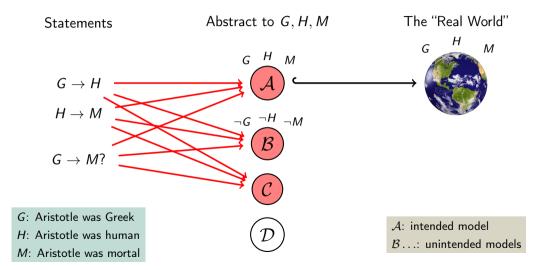


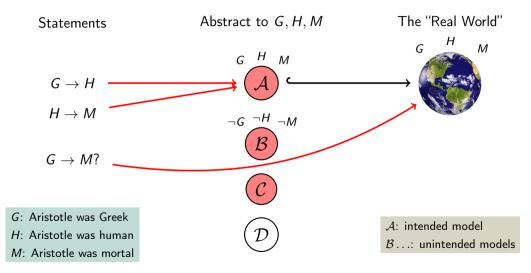












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- Whatever these models all share can be said to be entailed by those features.

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## Propositional Logic: Formulas

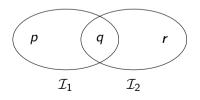
- Formulas are defined "by induction" or "recursively":
- 1 Any letter  $p, q, r, \ldots$  is a formula
- 2 if A and B are formulas, then
  - $(A \land B)$  is also a formula (read: "A and B")
  - $(A \lor B)$  is also a formula (read: "A or B")
  - $\neg A$  is also a formula (read: "not A")
- Nothing else is. Only what rules [1] and [2] say is a formula.
- Examples of formulae:  $p (p \land \neg r) (q \land \neg q) ((p \lor \neg q) \land \neg p)$
- Formulas are just a kind of strings until now:
  - no meaning
  - but every formula can be "parsed" uniquely.

$$((q \land p) \lor (p \land q))$$

$$\begin{array}{c} & & \\ & &$$

#### Interpretations

- Logic is about truth and falsity
- Truth of compound formulas depends on truth of letters.
- Idea: put all letters that are "true" into a set!
- $\bullet$  Define: An interpretation  ${\mathcal I}$  is a set of letters.
- Letter p is true in interpretation  $\mathcal{I}$  if  $p \in \mathcal{I}$ .
- E.g., in  $\mathcal{I}_1 = \{p, q\}$ , p is true, but r is false.



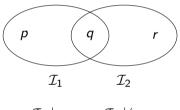
• But in  $\mathcal{I}_2 = \{q, r\}$ , p is false, but r is true.

# Semantic Validity $\models$

• To say that p is true in  $\mathcal{I}$ , write

 $\mathcal{I}\models p$ 

• For instance



$$\mathcal{I}_1 \models p \qquad \mathcal{I}_2 \not\models p$$

• In other words, for all letters *p*:

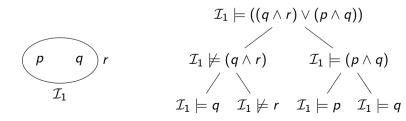
$$\mathcal{I} \models p$$
 if and only if  $p \in \mathcal{I}$ 

# Validity of Compound Formulas

- Is  $((q \land r) \lor (p \land q))$  true in  $\mathcal{I}$ ?
- Idea: apply our rule recursively
- For any formulas A and B,...
- $\bullet$  . . . and any interpretation  $\mathcal{I},\ldots$ 
  - $\ldots \mathcal{I} \models A \land B$  if and only if  $\mathcal{I} \models A$  and  $\mathcal{I} \models B$
  - ...  $\mathcal{I} \models A \lor B$  if and only if  $\mathcal{I} \models A$  or  $\mathcal{I} \models B$  (or both)

• 
$$\ldots \mathcal{I} \models \neg A$$
 if and only if  $\mathcal{I} \not\models A$ .

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## Truth Table

• Semantics of  $\neg$ ,  $\land$ ,  $\lor$  often given as *truth table*:

Α	В	$\neg A$	$A \wedge B$	$A \lor B$
f	f	t	f	f
f	t	t	f	t
t	f	f	f	t
t	t	f	t	t

## Tautologies

- A formula A that is true in all interpretations is called a tautology
- also logically valid
- also a *theorem* (of propositional logic)
- written:

# $\models A$

- $(p \lor \neg p)$  is a tautology
- True whatever *p* means:
  - The sky is blue or the sky is not blue.
  - P.N. will win the 50km in 2016 or P.N. will not win the 50km in 2016.
  - The slithy toves gyre or the slithy toves do not gyre.
- Possible to derive true statements mechanically...
- ... without understanding their meaning!
- $\bullet$  ...e.g. using truth tables for small cases.

## Entailment

- Tautologies are true in all interpretations
- Some formulas are true only under certain assumptions
- A entails B, written  $A \models B$  if

 $\mathcal{I} \models B$ 

for all interpretations  $\mathcal{I}$  with  $\mathcal{I} \models A$ 

- Also: "B is a logical consequence of A"
- Whenever A holds, also B holds
- For instance:

$$p \wedge q \models p$$

- Independent of meaning of *p* and *q*:
  - If it rains and the sky is blue, then it rains
  - $\bullet\,$  If P.N. wins the race and the world ends, then P.N. wins the race
  - If 'tis brillig and the slythy toves do gyre, then 'tis brillig
- Also entailment can be checked mechanically, without knowing the meaning of words.

#### Question

#### Given the letters

- P Ola answers none of the questions correctly
- Q Ola fails the exam
- Which of the following are tautologies of propositional logic?
  - 0 Q
  - **2** ¬*Q*

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Triples are true or false on the basis of what each part refers to.

Simplified RDF semantics

#### On what there is: Resources, Properties, Literals

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The semantics of typed and language tagged literals is considerably more complex.

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• Forget blank nodes and literals for a while!

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indi rdf:type class .	$C(i_1)$
<pre>class rdfs:subClassOf class .</pre>	$C \sqsubseteq D$
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- This is called "Description Logic" (DL) Syntax
- Used much in particular for OWL



• Triples:

### Example

Triples:

ws:romeo ws:loves ws:juliet .
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• DL syntax, without namespaces:

```
loves(romeo, juliet)
Lady(juliet)
Lady ⊑ Person
loves ⊑ knows
dom(loves, Lover)
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- Given these, it will be possible to say whether a triple holds or not.

Simplified RDF semantics

• 
$$\Delta^{\mathcal{I}_1} = \left\{ \left| \left| \left| \left| \right\rangle \right| \right\rangle, \left| \left| \left| \right\rangle \right| \right\rangle \right\} \right\}$$

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$$\Delta^{\mathcal{I}_1} = \left\{ \overbrace{\begin{subarray}{c} \\ \hline \end{array}, \overbrace{\begin{subarray}{c} \end{array}, \overbrace{\begin{subarray}{c} \end{array}, \overbrace{\begin{subarray}{c} \end{array}, \overbrace{\begin{subarray}{c} \end{array}, \overbrace{\begin{subarray}{c} \end{array}, \rule \\ \hline \begin{subarray}{c} \end{array}, \rule \\ \hline \begin{subarray}{c} \end{array}, \rule \\ \begin{subarray}{c} \end{array}, \rule \begin{subarray}{c} \end{array}, \rule$$

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•  $romeo^{\mathcal{I}_1} = \left| \left| \left| \left| \right| \right| \right| \right| \left| \left| \left| \left| \left| \left| \left| \left| \right| \right| \right| \right| \right| \right| \right| \right\}$   
•  $Lady^{\mathcal{I}_1} = \left\{ \left| \left| \left| \left| \left| \right| \right| \right| \right\} \right\}$   $Person^{\mathcal{I}_1} = \Delta^{\mathcal{I}_1}$   
 $Lover^{\mathcal{I}_1} = Beloved^{\mathcal{I}_1} = \left\{ \left| \left| \left| \left| \left| \left| \right| \right| \right| \right\} \right\}$ 

• 
$$\Delta^{\mathcal{I}_{1}} = \left\{ \left| \overbrace{}^{\mathcal{I}_{1}}, \overbrace{}^{\mathcal{I}_{1}}, \overbrace{}^{\mathcal{I}_{2}}, \overbrace{}^{\mathcal{I}_{2}} \right| \right\}$$
  
•  $romeo^{\mathcal{I}_{1}} = \left| \overbrace{}^{\mathcal{I}_{2}} \right| \quad person^{\mathcal{I}_{1}} = \Delta^{\mathcal{I}_{1}}$   
•  $Lady^{\mathcal{I}_{1}} = \left\{ \left| \overbrace{}^{\mathcal{I}_{2}} \right| \right\} \quad Person^{\mathcal{I}_{1}} = \Delta^{\mathcal{I}_{1}}$   
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•  $loves^{\mathcal{I}_{1}} = \left\{ \left\langle \left| \overbrace{}^{\mathcal{I}_{2}} \right|, \overbrace{}^{\mathcal{I}_{2}} \right\rangle, \left\langle \left| \overbrace{}^{\mathcal{I}_{2}} \right|, \overbrace{}^{\mathcal{I}_{2}} \right\rangle \right\}$ 

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$$loves^{\mathcal{I}_2} = <= \{ \langle x, y \rangle \mid x < y \}$$
  
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- Just because names (URIs) look familiar, they don't need to denote what we think!

#### An example "non-intended" interpretation

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- $loves^{\mathcal{I}_2} = <= \{ \langle x, y \rangle \mid x < y \}$  $knows^{\mathcal{I}_2} = \le= \{ \langle x, y \rangle \mid x \le y \}$
- Just because names (URIs) look familiar, they don't need to denote what we think!
- In fact, there is no way of ensuring they denote only what we think!

• Given an interpretation  $\mathcal{I}$ , define  $\models$  as follows:

- Given an interpretation *I*, define ⊨ as follows: *I* ⊨ *r*(*i*<sub>1</sub>, *i*<sub>2</sub>) iff ⟨*i*<sub>1</sub><sup>*T*</sup>, *i*<sub>2</sub><sup>*T*</sup>⟩ ∈ *r*<sup>*T*</sup>

- Given an interpretation  $\mathcal{I}$ , define  $\models$  as follows:
- $\mathcal{I} \models r(i_1, i_2)$  iff  $\langle i_1^{\mathcal{I}}, i_2^{\mathcal{I}} \rangle \in r^{\mathcal{I}}$   $\mathcal{I} \models C(i)$  iff  $i^{\mathcal{I}} \in C^{\mathcal{I}}$

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•  $\mathcal{I}_1 \models \textit{Person(romeo)}$  because

$$romeo^{\mathcal{I}_1} = egin{matrix} \mathcal{I}_1 \ \mathcal{I}_2 \ \mathcal{I}_1 \ \mathcal{I}_1$$

- $\mathcal{I}_2 \not\models loves(juliet, romeo)$  because  $loves^{\mathcal{I}_2} = < and juliet^{\mathcal{I}_2} = 32 \not< romeo^{\mathcal{I}_2} = 17$
- $\mathcal{I}_2 \not\models Person(romeo)$  because
- romeo<sup> $\mathcal{I}_2$ </sup> = 17  $\notin$  Person<sup> $\mathcal{I}_2$ </sup> = {2, 4, 6, 8, 10, ...}

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$$Lover^{\mathcal{I}_1} = \left\{ \bigotimes_{i=1}^{\infty}, \bigotimes_{i=1}^{\infty} \right\} \subseteq Person^{\mathcal{I}_1} = \left\{ \bigotimes_{i=1}^{\infty}, \bigotimes_{i=1}^{\infty}, \bigotimes_{i=1}^{\infty} \right\}$$

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- Examples:

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$$\mathcal{I}_1 \models Lover \sqsubseteq Person \text{ because}$$
  
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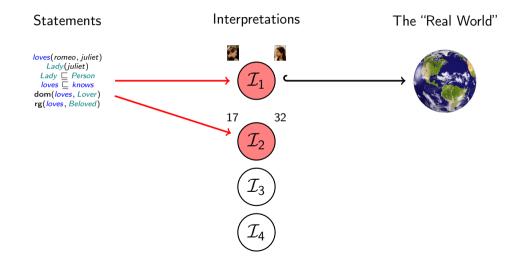
•  $\mathcal{I}_2 \not\models \textit{Lover} \sqsubseteq \textit{Person}$  because

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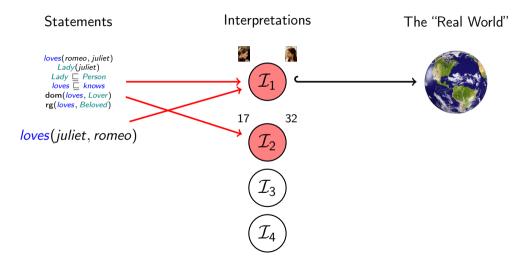
•  $\mathcal{I}_2 \not\models Lover \sqsubseteq Person$  because  $Lover^{\mathcal{I}_2} = \mathbb{N}$  and  $Person^{\mathcal{I}_2} = \{2, 4, 6, 8, 10, \ldots\}$  Simplified RDF semantics

### Finding out stuff about Romeo and Juliet



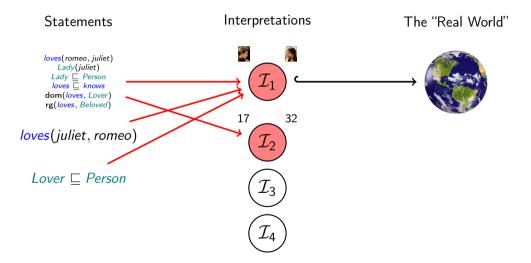
Simplified RDF semantics

### Finding out stuff about Romeo and Juliet



Simplified RDF semantics

### Finding out stuff about Romeo and Juliet



 $\mathcal{I}_2 \models \mathsf{dom}(\mathit{knows}, \mathit{Beloved})$ 

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and for any x and y with

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and for any x and y with

$$\langle x, y \rangle \in knows^{\mathcal{I}_2}, \quad \text{i.e.} \quad x \leq y,$$

we also have

$$x \in \mathbb{N}$$
 i.e.  $x \in Beloved^{\mathcal{I}_2}$ 

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$$\mathcal{A} = \{ loves(romeo, juliet), \ Lady(juliet), \ Lady \sqsubseteq Person, \\ loves \sqsubseteq knows, \ dom(loves, Lover), \ rg(loves, Beloved) \}$$

## Interpretation of Sets of Triples

- $\bullet$  Given an interpretation  ${\cal I}$
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 $\bullet \ \, {\sf Then} \ \, {\cal I}_1 \models {\cal A} \ {\sf and} \ \, {\cal I}_2 \models {\cal A}$ 

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  - $\bullet~$  For any interpretation  $\mathcal I$  with  $\mathcal I \models \mathcal A$
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- $\mathcal{A} \models \mathcal{B}$  iff  $\mathcal{I} \models \mathcal{B}$  for all  $\mathcal{I}$  with  $\mathcal{I} \models \mathcal{A}$

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- Example:
- $\mathcal{A} = \{\dots, Lady(juliet), Lady \sqsubseteq Person, \dots\}$  as before

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- $\mathcal{A} \models Person(juliet)$  because...

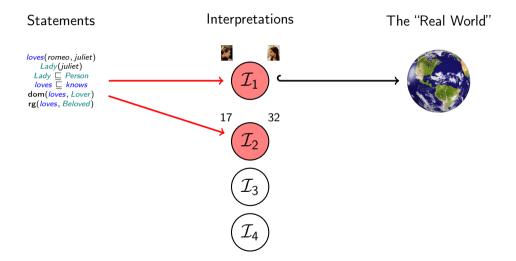
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- $A = \{\dots, Lady(juliet), Lady \sqsubseteq Person, \dots\}$  as before
- $\mathcal{A} \models Person(juliet)$  because...
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- in *any* interpretation  $\mathcal{I}$ ...
- if  $juliet^{\mathcal{I}} \in Lady^{\mathcal{I}}$  and  $Lady^{\mathcal{I}} \subseteq Person^{\mathcal{I}} \dots$
- $\bullet$  then by set theory  $\textit{juliet}^\mathcal{I} \in \textit{Person}^\mathcal{I}$

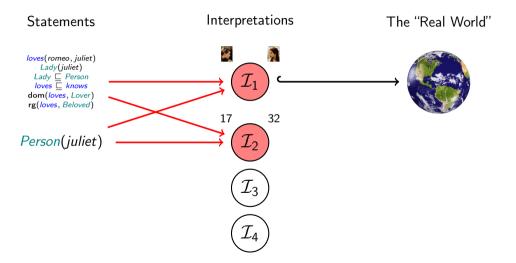
Simplified RDF semantics

# Finding out stuff about Romeo and Juliet



Simplified RDF semantics

# Finding out stuff about Romeo and Juliet



## Countermodels

- If  $\mathcal{A} \not\models \mathcal{T}, \ldots$
- $\bullet\,$  then there is an  ${\cal I}$  with
  - $\mathcal{I} \models \mathcal{A}$
  - $\mathcal{I} \not\models T$
- Vice-versa: if  $\mathcal{I} \models \mathcal{A}$  and  $\mathcal{I} \not\models \mathcal{T}$ , then  $\mathcal{A} \not\models \mathcal{T}$
- Such an  $\mathcal{I}$  is called a *counter-model* (for the assumption that  $\mathcal{A}$  entails  $\mathcal{T}$ )
- To show that  $\mathcal{A} \models \mathcal{T}$  does *not* hold:
  - Describe an interpretation  $\mathcal{I}$  (using your fantasy)
  - Prove that  $\mathcal{I} \models \mathcal{A}$  (using the semantics)
  - Prove that  $\mathcal{I} \not\models \mathcal{T}$  (using the semantics)

$$\mathcal{A} = \{ loves(romeo, juliet), Lady(juliet), Lady \sqsubseteq Person, \\ loves \sqsubseteq knows, dom(loves, Lover), rg(loves, Beloved) \}$$

•  $\mathcal{A}$  as before:

$$\mathcal{A} = \{ loves(romeo, juliet), Lady(juliet), Lady \sqsubseteq Person, \\ loves \sqsubseteq knows, dom(loves, Lover), rg(loves, Beloved) \}$$

• Does  $\mathcal{A} \models Lover \sqsubseteq Beloved$ ?

$$\mathcal{A} = \{ loves(romeo, juliet), Lady(juliet), Lady \sqsubseteq Person, \\ loves \sqsubseteq knows, dom(loves, Lover), rg(loves, Beloved) \}$$

- Does  $\mathcal{A} \models Lover \sqsubseteq Beloved$ ?
- Holds in  $\mathcal{I}_1$  and  $\mathcal{I}_2$ .

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- Holds in  $\mathcal{I}_1$  and  $\mathcal{I}_2$ .
- Try to find an interpretaion with  $\Delta^{\mathcal{I}} = \{a, b\}, a \neq b$ .

$$\mathcal{A} = \{ loves(romeo, juliet), Lady(juliet), Lady \sqsubseteq Person, \\ loves \sqsubseteq knows, dom(loves, Lover), rg(loves, Beloved) \}$$

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- Interpret  $\textit{romeo}^{\mathcal{I}} = a$  and  $\textit{juliet}^{\mathcal{I}} = b$

$$\mathcal{A} = \{ loves(romeo, juliet), Lady(juliet), Lady \sqsubseteq Person, \\ loves \sqsubseteq knows, dom(loves, Lover), rg(loves, Beloved) \}$$

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- Interpret  $romeo^{\mathcal{I}} = a$  and  $juliet^{\mathcal{I}} = b$
- Then  $\langle a, b \rangle \in loves^{\mathcal{I}}$ ,  $a \in Lover^{\mathcal{I}}$ ,  $b \in Beloved^{\mathcal{I}}$ .

•  $\mathcal{A}$  as before:

 $\mathcal{A} = \{ \text{loves}(\text{romeo}, \text{juliet}), \text{ Lady}(\text{juliet}), \text{ Lady} \sqsubseteq \text{Person}, \\ \text{loves} \sqsubseteq \text{knows}, \text{ dom}(\text{loves}, \text{Lover}), \text{ rg}(\text{loves}, \text{Beloved}) \}$ 

- Does  $\mathcal{A} \models Lover \sqsubseteq Beloved$ ?
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- Then  $\langle a, b \rangle \in loves^{\mathcal{I}}$ ,  $a \in Lover^{\mathcal{I}}$ ,  $b \in Beloved^{\mathcal{I}}$ .
- With  $Lover^{\mathcal{I}} = \{a\}$  and  $Beloved^{\mathcal{I}} = \{b\}$ ,  $\mathcal{I} \not\models Lover \sqsubseteq Beloved!$

•  $\mathcal{A}$  as before:

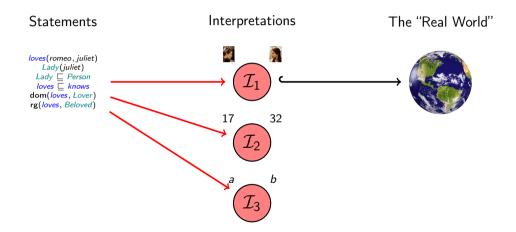
 $\mathcal{A} = \{ \textit{loves}(\textit{romeo}, \textit{juliet}), \textit{Lady}(\textit{juliet}), \textit{Lady} \sqsubseteq \textit{Person}, \\ \textit{loves} \sqsubseteq \textit{knows}, \textit{dom}(\textit{loves}, \textit{Lover}), \textit{rg}(\textit{loves}, \textit{Beloved}) \}$ 

- Does  $\mathcal{A} \models Lover \sqsubseteq Beloved$ ?
- Holds in  $\mathcal{I}_1$  and  $\mathcal{I}_2$ .
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- Interpret  $romeo^{\mathcal{I}} = a$  and  $juliet^{\mathcal{I}} = b$
- Then  $\langle a, b \rangle \in \mathit{loves}^{\mathcal{I}}$ ,  $a \in \mathit{Lover}^{\mathcal{I}}$ ,  $b \in \mathit{Beloved}^{\mathcal{I}}$ .
- With  $Lover^{\mathcal{I}} = \{a\}$  and  $Beloved^{\mathcal{I}} = \{b\}$ ,  $\mathcal{I} \not\models Lover \sqsubseteq Beloved!$
- Choose

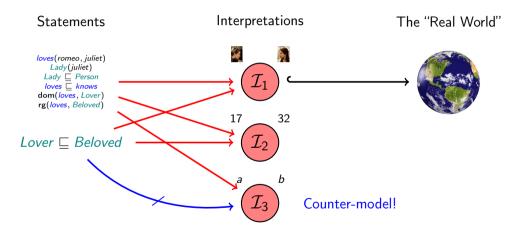
$$\textit{loves}^{\mathcal{I}} = \textit{knows}^{\mathcal{I}} = \{ \langle a, b \rangle \} \qquad \textit{Lady}^{\mathcal{I}} = \textit{Person}^{\mathcal{I}} = \{ b \}$$

to complete the counter-model while satisfying  $\mathcal{I} \models \mathcal{A}$ 

# Countermodels about Romeo and Juliet



# Countermodels about Romeo and Juliet





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Supplementary reading on RDF and RDFS semantics:

- http://www.w3.org/TR/rdf-mt/
- Section 3.2 in Foundations of SW Technologies