

INF3580/4580 – Semantic Technologies – Spring 2017

Lecture 11: OWL 2

Leif Harald Karlsen

27th March 2017



DEPARTMENT OF
INFORMATICS



UNIVERSITY OF
OSLO

Outline

- 1 Reminder: \mathcal{ALC}
- 2 Important assumptions
- 3 OWL 2
 - Axioms and assertions using individuals
 - Restrictions on roles
 - Modelling problems
 - Roles
 - Datatypes

The \mathcal{ALC} Description Logic

Vocabulary

Fix a set of *atomic concepts* $\{A_1, A_2, \dots\}$, *roles* $\{R_1, R_2, \dots\}$ and *individuals* $\{a_1, a_2, \dots\}$.

The \mathcal{ALC} Description Logic

Vocabulary

Fix a set of *atomic concepts* $\{A_1, A_2, \dots\}$, *roles* $\{R_1, R_2, \dots\}$ and *individuals* $\{a_1, a_2, \dots\}$.

\mathcal{ALC} concept descriptions

$C, D \rightarrow$	A_i		(atomic concept)
	\top		(universal concept)
	\perp		(bottom concept)

The \mathcal{ALC} Description Logic

Vocabulary

Fix a set of *atomic concepts* $\{A_1, A_2, \dots\}$, *roles* $\{R_1, R_2, \dots\}$ and *individuals* $\{a_1, a_2, \dots\}$.

\mathcal{ALC} concept descriptions

$C, D \rightarrow$	A_i		(atomic concept)
	\top		(universal concept)
	\perp		(bottom concept)
	$\neg C$		(negation)
	$C \sqcap D$		(intersection)
	$C \sqcup D$		(union)

The \mathcal{ALC} Description Logic

Vocabulary

Fix a set of *atomic concepts* $\{A_1, A_2, \dots\}$, *roles* $\{R_1, R_2, \dots\}$ and *individuals* $\{a_1, a_2, \dots\}$.

\mathcal{ALC} concept descriptions

$C, D \rightarrow$	A_i		(atomic concept)
	\top		(universal concept)
	\perp		(bottom concept)
	$\neg C$		(negation)
	$C \sqcap D$		(intersection)
	$C \sqcup D$		(union)
	$\forall R_i.C$		(value restriction)
	$\exists R_i.C$		(existential restriction)

The \mathcal{ALC} Description Logic

Vocabulary

Fix a set of *atomic concepts* $\{A_1, A_2, \dots\}$, *roles* $\{R_1, R_2, \dots\}$ and *individuals* $\{a_1, a_2, \dots\}$.

\mathcal{ALC} concept descriptions

$C, D \rightarrow$	A_i		(atomic concept)
	\top		(universal concept)
	\perp		(bottom concept)
	$\neg C$		(negation)
	$C \sqcap D$		(intersection)
	$C \sqcup D$		(union)
	$\forall R_i.C$		(value restriction)
	$\exists R_i.C$		(existential restriction)

Axioms

- $C \sqsubseteq D$ and $C \equiv D$ for concept descriptions D and C .
- $C(a)$ and $R(a, b)$ for concept description C , atomic role R and individuals a, b .

\mathcal{ALC} Semantics

Interpretation

An interpretation \mathcal{I} fixes a set $\Delta^{\mathcal{I}}$, the *domain*, $A^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}}$ for each atomic concept A , $R^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$ for each role R , and $a^{\mathcal{I}} \in \Delta^{\mathcal{I}}$ for each individual a .

\mathcal{ALC} Semantics

Interpretation

An interpretation \mathcal{I} fixes a set $\Delta^{\mathcal{I}}$, the *domain*, $A^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}}$ for each atomic concept A , $R^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$ for each role R , and $a^{\mathcal{I}} \in \Delta^{\mathcal{I}}$ for each individual a .

Interpretation of concept descriptions

$$\begin{aligned}\top^{\mathcal{I}} &= \Delta^{\mathcal{I}} \\ \perp^{\mathcal{I}} &= \emptyset\end{aligned}$$

\mathcal{ALC} Semantics

Interpretation

An interpretation \mathcal{I} fixes a set $\Delta^{\mathcal{I}}$, the *domain*, $A^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}}$ for each atomic concept A , $R^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$ for each role R , and $a^{\mathcal{I}} \in \Delta^{\mathcal{I}}$ for each individual a .

Interpretation of concept descriptions

$$\begin{aligned}
 \top^{\mathcal{I}} &= \Delta^{\mathcal{I}} \\
 \perp^{\mathcal{I}} &= \emptyset \\
 (\neg C)^{\mathcal{I}} &= \Delta^{\mathcal{I}} \setminus C^{\mathcal{I}} \\
 (C \sqcap D)^{\mathcal{I}} &= C^{\mathcal{I}} \cap D^{\mathcal{I}} \\
 (C \sqcup D)^{\mathcal{I}} &= C^{\mathcal{I}} \cup D^{\mathcal{I}}
 \end{aligned}$$

\mathcal{ALC} Semantics

Interpretation

An interpretation \mathcal{I} fixes a set $\Delta^{\mathcal{I}}$, the *domain*, $A^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}}$ for each atomic concept A , $R^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$ for each role R , and $a^{\mathcal{I}} \in \Delta^{\mathcal{I}}$ for each individual a .

Interpretation of concept descriptions

$$\begin{aligned}
 \top^{\mathcal{I}} &= \Delta^{\mathcal{I}} \\
 \perp^{\mathcal{I}} &= \emptyset \\
 (\neg C)^{\mathcal{I}} &= \Delta^{\mathcal{I}} \setminus C^{\mathcal{I}} \\
 (C \sqcap D)^{\mathcal{I}} &= C^{\mathcal{I}} \cap D^{\mathcal{I}} \\
 (C \sqcup D)^{\mathcal{I}} &= C^{\mathcal{I}} \cup D^{\mathcal{I}} \\
 (\forall R.C)^{\mathcal{I}} &= \{a \in \Delta^{\mathcal{I}} \mid \text{for all } b, \text{ if } \langle a, b \rangle \in R^{\mathcal{I}} \text{ then } b \in C^{\mathcal{I}}\} \\
 (\exists R.C)^{\mathcal{I}} &= \{a \in \Delta^{\mathcal{I}} \mid \text{there is a } b \text{ where } \langle a, b \rangle \in R^{\mathcal{I}} \text{ and } b \in C^{\mathcal{I}}\}
 \end{aligned}$$

\mathcal{ALC} Semantics

Interpretation

An interpretation \mathcal{I} fixes a set $\Delta^{\mathcal{I}}$, the *domain*, $A^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}}$ for each atomic concept A , $R^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$ for each role R , and $a^{\mathcal{I}} \in \Delta^{\mathcal{I}}$ for each individual a .

Interpretation of concept descriptions

$$\begin{aligned}
 \top^{\mathcal{I}} &= \Delta^{\mathcal{I}} \\
 \perp^{\mathcal{I}} &= \emptyset \\
 (\neg C)^{\mathcal{I}} &= \Delta^{\mathcal{I}} \setminus C^{\mathcal{I}} \\
 (C \sqcap D)^{\mathcal{I}} &= C^{\mathcal{I}} \cap D^{\mathcal{I}} \\
 (C \sqcup D)^{\mathcal{I}} &= C^{\mathcal{I}} \cup D^{\mathcal{I}} \\
 (\forall R.C)^{\mathcal{I}} &= \{a \in \Delta^{\mathcal{I}} \mid \text{for all } b, \text{ if } \langle a, b \rangle \in R^{\mathcal{I}} \text{ then } b \in C^{\mathcal{I}}\} \\
 (\exists R.C)^{\mathcal{I}} &= \{a \in \Delta^{\mathcal{I}} \mid \text{there is a } b \text{ where } \langle a, b \rangle \in R^{\mathcal{I}} \text{ and } b \in C^{\mathcal{I}}\}
 \end{aligned}$$

Interpretation of Axioms

- $\mathcal{I} \models C \sqsubseteq D$ if $C^{\mathcal{I}} \subseteq D^{\mathcal{I}}$ and $\mathcal{I} \models C \equiv D$ if $C^{\mathcal{I}} = D^{\mathcal{I}}$
- $\mathcal{I} \models C(a)$ if $a^{\mathcal{I}} \in C^{\mathcal{I}}$ and $\mathcal{I} \models R(a, b)$ if $\langle a^{\mathcal{I}}, b^{\mathcal{I}} \rangle \in R^{\mathcal{I}}$.

\mathcal{ALC} Examples

Let \mathcal{K} be the following set of axioms:

$$Penguin \sqsubseteq Animal \sqcap \forall eats.Fish$$

$$Penguin \sqcap Fish \sqsubseteq \perp$$

$$Penguin(a)$$

$$Fish \sqsubseteq Animal$$

$$Animal \sqsubseteq \exists eats.T$$

$$eats(a, b)$$

\mathcal{ALC} Examples

Let \mathcal{K} be the following set of axioms:

$$Penguin \sqsubseteq Animal \sqcap \forall eats.Fish$$

$$Penguin \sqcap Fish \sqsubseteq \perp$$

$$Penguin(a)$$

$$Fish \sqsubseteq Animal$$

$$Animal \sqsubseteq \exists eats.\top$$

$$eats(a, b)$$

Let \mathcal{I} be an interpretation such that

$$\Delta^{\mathcal{I}} = \top^{\mathcal{I}} = \{tweety, terry, carl\}, \quad \perp^{\mathcal{I}} = \emptyset, \quad a^{\mathcal{I}} = tweety, \quad b^{\mathcal{I}} = terry$$

\mathcal{ALC} Examples

Let \mathcal{K} be the following set of axioms:

$$Penguin \sqsubseteq Animal \sqcap \forall eats.Fish$$

$$Penguin \sqcap Fish \sqsubseteq \perp$$

$$Penguin(a)$$

$$Fish \sqsubseteq Animal$$

$$Animal \sqsubseteq \exists eats.\top$$

$$eats(a, b)$$

Let \mathcal{I} be an interpretation such that

$$\Delta^{\mathcal{I}} = \top^{\mathcal{I}} = \{tweety, terry, carl\}, \quad \perp^{\mathcal{I}} = \emptyset, \quad a^{\mathcal{I}} = tweety, \quad b^{\mathcal{I}} = terry$$

$$Penguin^{\mathcal{I}} = \{a^{\mathcal{I}}\}$$

\mathcal{ALC} Examples

Let \mathcal{K} be the following set of axioms:

$$Penguin \sqsubseteq Animal \sqcap \forall eats.Fish$$

$$Penguin \sqcap Fish \sqsubseteq \perp$$

$$Penguin(a)$$

$$Fish \sqsubseteq Animal$$

$$Animal \sqsubseteq \exists eats.\top$$

$$eats(a, b)$$

Let \mathcal{I} be an interpretation such that

$$\Delta^{\mathcal{I}} = \top^{\mathcal{I}} = \{tweety, terry, carl\}, \quad \perp^{\mathcal{I}} = \emptyset, \quad a^{\mathcal{I}} = tweety, \quad b^{\mathcal{I}} = terry$$

$$Penguin^{\mathcal{I}} = \{a^{\mathcal{I}}\}$$

$$eats^{\mathcal{I}} = \{\langle a^{\mathcal{I}}, b^{\mathcal{I}} \rangle\},$$

\mathcal{ALC} Examples

Let \mathcal{K} be the following set of axioms:

$$Penguin \sqsubseteq Animal \sqcap \forall eats.Fish$$

$$Penguin \sqcap Fish \sqsubseteq \perp$$

$$Penguin(a)$$

$$Fish \sqsubseteq Animal$$

$$Animal \sqsubseteq \exists eats.\top$$

$$eats(a, b)$$

Let \mathcal{I} be an interpretation such that

$$\Delta^{\mathcal{I}} = \top^{\mathcal{I}} = \{tweety, terry, carl\}, \quad \perp^{\mathcal{I}} = \emptyset, \quad a^{\mathcal{I}} = tweety, \quad b^{\mathcal{I}} = terry$$

$$Penguin^{\mathcal{I}} = \{a^{\mathcal{I}}\}$$

$$eats^{\mathcal{I}} = \{\langle a^{\mathcal{I}}, b^{\mathcal{I}} \rangle\},$$

$$Fish^{\mathcal{I}} = \{b^{\mathcal{I}}\}$$

\mathcal{ALC} Examples

Let \mathcal{K} be the following set of axioms:

$$Penguin \sqsubseteq Animal \sqcap \forall eats.Fish$$

$$Penguin \sqcap Fish \sqsubseteq \perp$$

$$Penguin(a)$$

$$Fish \sqsubseteq Animal$$

$$Animal \sqsubseteq \exists eats.\top$$

$$eats(a, b)$$

Let \mathcal{I} be an interpretation such that

$$\Delta^{\mathcal{I}} = \top^{\mathcal{I}} = \{tweety, terry, carl\}, \quad \perp^{\mathcal{I}} = \emptyset, \quad a^{\mathcal{I}} = tweety, \quad b^{\mathcal{I}} = terry$$

$$Penguin^{\mathcal{I}} = \{a^{\mathcal{I}}\}$$

$$eats^{\mathcal{I}} = \{\langle a^{\mathcal{I}}, b^{\mathcal{I}} \rangle\},$$

$$Fish^{\mathcal{I}} = \{b^{\mathcal{I}}\}$$

$$Animal^{\mathcal{I}} = \{a^{\mathcal{I}}, b^{\mathcal{I}}\}$$

\mathcal{ALC} Examples

Let \mathcal{K} be the following set of axioms:

$$Penguin \sqsubseteq Animal \sqcap \forall eats.Fish$$

$$Penguin \sqcap Fish \sqsubseteq \perp$$

$$Penguin(a)$$

$$Fish \sqsubseteq Animal$$

$$Animal \sqsubseteq \exists eats.\top$$

$$eats(a, b)$$

Let \mathcal{I} be an interpretation such that

$$\Delta^{\mathcal{I}} = \top^{\mathcal{I}} = \{tweety, terry, carl\}, \quad \perp^{\mathcal{I}} = \emptyset, \quad a^{\mathcal{I}} = tweety, \quad b^{\mathcal{I}} = terry$$

$$Penguin^{\mathcal{I}} = \{a^{\mathcal{I}}\}$$

$$eats^{\mathcal{I}} = \{\langle a^{\mathcal{I}}, b^{\mathcal{I}} \rangle, \langle b^{\mathcal{I}}, carl \rangle\}$$

$$Fish^{\mathcal{I}} = \{b^{\mathcal{I}}\}$$

$$Animal^{\mathcal{I}} = \{a^{\mathcal{I}}, b^{\mathcal{I}}\}$$

\mathcal{ALC} Examples

Let \mathcal{K} be the following set of axioms:

$$Penguin \sqsubseteq Animal \sqcap \forall eats.Fish$$

$$Penguin \sqcap Fish \sqsubseteq \perp$$

$$Penguin(a)$$

$$Fish \sqsubseteq Animal$$

$$Animal \sqsubseteq \exists eats.\top$$

$$eats(a, b)$$

Let \mathcal{I} be an interpretation such that

$$\Delta^{\mathcal{I}} = \top^{\mathcal{I}} = \{tweety, terry, carl\}, \quad \perp^{\mathcal{I}} = \emptyset, \quad a^{\mathcal{I}} = tweety, \quad b^{\mathcal{I}} = terry$$

$$Penguin^{\mathcal{I}} = \{a^{\mathcal{I}}\}$$

$$eats^{\mathcal{I}} = \{\langle a^{\mathcal{I}}, b^{\mathcal{I}} \rangle, \langle b^{\mathcal{I}}, carl \rangle\} = \{\langle tweety, terry \rangle, \langle terry, carl \rangle\}$$

$$Fish^{\mathcal{I}} = \{b^{\mathcal{I}}\}$$

$$Animal^{\mathcal{I}} = \{a^{\mathcal{I}}, b^{\mathcal{I}}\}$$

\mathcal{ALC} Examples

Let \mathcal{K} be the following set of axioms:

$$Penguin \sqsubseteq Animal \sqcap \forall eats.Fish$$

$$Penguin \sqcap Fish \sqsubseteq \perp$$

$$Penguin(a)$$

$$Fish \sqsubseteq Animal$$

$$Animal \sqsubseteq \exists eats.\top$$

$$eats(a, b)$$

Let \mathcal{I} be an interpretation such that

$$\Delta^{\mathcal{I}} = \top^{\mathcal{I}} = \{tweety, terry, carl\}, \quad \perp^{\mathcal{I}} = \emptyset, \quad a^{\mathcal{I}} = tweety, \quad b^{\mathcal{I}} = terry$$

$$Penguin^{\mathcal{I}} = \{a^{\mathcal{I}}\} = \{tweety\}$$

$$eats^{\mathcal{I}} = \{\langle a^{\mathcal{I}}, b^{\mathcal{I}} \rangle, \langle b^{\mathcal{I}}, carl \rangle\} = \{\langle tweety, terry \rangle, \langle terry, carl \rangle\}$$

$$Fish^{\mathcal{I}} = \{b^{\mathcal{I}}\} = \{terry\}$$

$$Animal^{\mathcal{I}} = \{a^{\mathcal{I}}, b^{\mathcal{I}}\}$$

\mathcal{ALC} Examples

Let \mathcal{K} be the following set of axioms:

$$Penguin \sqsubseteq Animal \sqcap \forall eats.Fish$$

$$Penguin \sqcap Fish \sqsubseteq \perp$$

$$Penguin(a)$$

$$Fish \sqsubseteq Animal$$

$$Animal \sqsubseteq \exists eats.\top$$

$$eats(a, b)$$

Let \mathcal{I} be an interpretation such that

$$\Delta^{\mathcal{I}} = \top^{\mathcal{I}} = \{tweety, terry, carl\}, \quad \perp^{\mathcal{I}} = \emptyset, \quad a^{\mathcal{I}} = tweety, \quad b^{\mathcal{I}} = terry$$

$$Penguin^{\mathcal{I}} = \{a^{\mathcal{I}}\} = \{tweety\}$$

$$eats^{\mathcal{I}} = \{\langle a^{\mathcal{I}}, b^{\mathcal{I}} \rangle, \langle b^{\mathcal{I}}, carl \rangle\} = \{\langle tweety, terry \rangle, \langle terry, carl \rangle\}$$

$$Fish^{\mathcal{I}} = \{b^{\mathcal{I}}\} = \{terry\}$$

$$Animal^{\mathcal{I}} = \{a^{\mathcal{I}}, b^{\mathcal{I}}\} = \{tweety, terry\}$$

\mathcal{ALC} Examples

Let \mathcal{K} be the following set of axioms:

$$Penguin \sqsubseteq Animal \sqcap \forall eats.Fish$$

$$Penguin \sqcap Fish \sqsubseteq \perp$$

$$Penguin(a)$$

$$Fish \sqsubseteq Animal$$

$$Animal \sqsubseteq \exists eats.\top$$

$$eats(a, b)$$

Let \mathcal{I} be an interpretation such that

$$\Delta^{\mathcal{I}} = \top^{\mathcal{I}} = \{tweety, terry, carl\}, \quad \perp^{\mathcal{I}} = \emptyset, \quad a^{\mathcal{I}} = tweety, \quad b^{\mathcal{I}} = terry$$

$$Penguin^{\mathcal{I}} = \{a^{\mathcal{I}}\} = \{tweety\}$$

$$eats^{\mathcal{I}} = \{\langle a^{\mathcal{I}}, b^{\mathcal{I}} \rangle, \langle b^{\mathcal{I}}, carl \rangle\} = \{\langle tweety, terry \rangle, \langle terry, carl \rangle\}$$

$$Fish^{\mathcal{I}} = \{b^{\mathcal{I}}\} = \{terry\}$$

$$Animal^{\mathcal{I}} = \{a^{\mathcal{I}}, b^{\mathcal{I}}\} = \{tweety, terry\}$$

Now $\mathcal{I} \models \mathcal{K}$.

\mathcal{ALC} Examples

Let \mathcal{K} be the following set of axioms:

$$Penguin \sqsubseteq Animal \sqcap \forall eats.Fish$$

$$Penguin \sqcap Fish \sqsubseteq \perp$$

$$Penguin(a)$$

$$Fish \sqsubseteq Animal$$

$$Animal \sqsubseteq \exists eats.T$$

$$eats(a, b)$$

Let \mathcal{J} be an interpretation such that

\mathcal{ALC} Examples

Let \mathcal{K} be the following set of axioms:

$$Penguin \sqsubseteq Animal \sqcap \forall eats.Fish$$

$$Penguin \sqcap Fish \sqsubseteq \perp$$

$$Penguin(a)$$

$$Fish \sqsubseteq Animal$$

$$Animal \sqsubseteq \exists eats.\top$$

$$eats(a, b)$$

Let \mathcal{J} be an interpretation such that

$$\Delta^{\mathcal{J}} = \top^{\mathcal{J}} = \{tweety\}, \quad \perp^{\mathcal{J}} = \emptyset, \quad a^{\mathcal{J}} = tweety, b^{\mathcal{J}} = tweety$$

$$Animal^{\mathcal{J}} = \{a^{\mathcal{J}}, b^{\mathcal{J}}\} = \{tweety\},$$

$$Penguin^{\mathcal{J}} = \{a^{\mathcal{J}}\} = \{tweety\},$$

$$Fish^{\mathcal{J}} = \{b^{\mathcal{J}}\} = \{tweety\}$$

$$eats^{\mathcal{J}} = \{\langle a^{\mathcal{J}}, b^{\mathcal{J}} \rangle, \langle b^{\mathcal{J}}, a^{\mathcal{J}} \rangle\} = \{\langle tweety, tweety \rangle\}$$

\mathcal{ALC} Examples

Let \mathcal{K} be the following set of axioms:

$$Penguin \sqsubseteq Animal \sqcap \forall eats.Fish$$

$$Penguin \sqcap Fish \sqsubseteq \perp$$

$$Penguin(a)$$

$$Fish \sqsubseteq Animal$$

$$Animal \sqsubseteq \exists eats.\top$$

$$eats(a, b)$$

Let \mathcal{J} be an interpretation such that

$$\Delta^{\mathcal{J}} = \top^{\mathcal{J}} = \{tweety\}, \quad \perp^{\mathcal{J}} = \emptyset, \quad a^{\mathcal{J}} = tweety, b^{\mathcal{J}} = tweety$$

$$Animal^{\mathcal{J}} = \{a^{\mathcal{J}}, b^{\mathcal{J}}\} = \{tweety\},$$

$$Penguin^{\mathcal{J}} = \{a^{\mathcal{J}}\} = \{tweety\},$$

$$Fish^{\mathcal{J}} = \{b^{\mathcal{J}}\} = \{tweety\}$$

$$eats^{\mathcal{J}} = \{\langle a^{\mathcal{J}}, b^{\mathcal{J}} \rangle, \langle b^{\mathcal{J}}, a^{\mathcal{J}} \rangle\} = \{\langle tweety, tweety \rangle\}$$

Now $\mathcal{J} \not\models \mathcal{K}$ since $\mathcal{J} \not\models Penguin \sqcap Fish \sqsubseteq \perp$.

Modelling patterns

So, what can we say with ACC ?

- ✓ Every person has a mother.
- ✓ Penguins eats only fish. Horses eats only chocolate.
- ✗ Every nuclear family has two parents, at least two children and a dog.
- ✓ No smoker is a non-smoker (and vice versa).
- ✗ Everybody loves Mary.
- ✗ Adam is not Eve (and vice versa).
- ✓ Everything is black or white.
- ✓ There is no such thing as a free lunch.
- ✗ Brothers of fathers are uncles.
- ✗ My friend's friends are also my friends.
- ✗ If Homer is married to Marge, then Marge is married to Homer.
- ✗ If Homer is a parent of Bart, then Bart is a child of Homer.

Today we'll learn how to say more.

Outline

- 1 Reminder: *ALC*
- 2 Important assumptions
- 3 OWL 2
 - Axioms and assertions using individuals
 - Restrictions on roles
 - Modelling problems
 - Roles
 - Datatypes

World assumptions

- Closed World Assumption (CWA)
- Open World Assumption (OWA)

CWA:

- Complete knowledge.
- Any statement that is not known to be true is false. (*)
- Typical semantics for database systems.

OWA:

- Potential incomplete knowledge.
- (*) does not hold.
- Typical semantics for logic-based systems.

Name assumptions

- Unique name assumption (UNA)
- Non-unique name assumption (NUNA)
- Under any assumption, equal names (read: individual URIs, DB constants) always denote the same “thing” (obviously).
 - E.g., cannot have $a^I \neq a^I$.
- Under UNA, different names *always* denote different things.
 - E.g., $a^I \neq b^I$.
 - common in relational databases.
- Under NUNA, different names *need not* denote different things.
 - Can have , $a^I = b^I$, or
 - $\text{dbpedia:0slo}^I = \text{geo:34521}^I$.

Outline

- 1 Reminder: *ALC*
- 2 Important assumptions
- 3 OWL 2
 - Axioms and assertions using individuals
 - Restrictions on roles
 - Modelling problems
 - Roles
 - Datatypes

$SHOIN(\mathcal{D})$ and OWL 2

- OWL 2 is based on the DL $SHOIN(\mathcal{D})$:
 - \mathcal{S} for \mathcal{ALC}^1 plus role transitivity,
 - \mathcal{H} for roles hierarchies,
 - \mathcal{O} for closed classes,
 - \mathcal{I} for inverse roles,
 - \mathcal{N} for cardinality restrictions, and
 - \mathcal{D} for datatypes.

¹Attributive Concept Language with Complements

$SHOIN(\mathcal{D})$ and OWL 2

- OWL 2 is based on the DL $SHOIN(\mathcal{D})$:
 - \mathcal{S} for \mathcal{ALC}^1 plus role transitivity,
 - \mathcal{H} for roles hierarchies,
 - \mathcal{O} for closed classes,
 - \mathcal{I} for inverse roles,
 - \mathcal{N} for cardinality restrictions, and
 - \mathcal{D} for datatypes.
- So, today we'll see:
 - new concept and role builders,
 - new TBox axioms,
 - new ABox axioms,
 - new RBox axioms, and
 - datatypes.

¹Attributive Concept Language with Complements

Individual identity

- New ABox axioms.
- Express equality and non-equality between individuals.

Individual identity

- New ABox axioms.
- Express equality and non-equality between individuals.
- Syntax:
 - DL: $a = b$, $a \neq b$;
 - RDF/OWL: `:a owl:sameAs :b`, `:a owl:differentFrom :b`,
 - Manchester: `SameAs`, `DifferentFrom`.

Individual identity

- New ABox axioms.
- Express equality and non-equality between individuals.
- Syntax:
 - DL: $a = b$, $a \neq b$;
 - RDF/OWL: `:a owl:sameAs :b`, `:a owl:differentFrom :b`,
 - Manchester: `SameAs`, `DifferentFrom`.
- Semantics:
 - $\mathcal{I} \models a = b$ iff $a^{\mathcal{I}} = b^{\mathcal{I}}$
 - $\mathcal{I} \models a \neq b$ iff $a^{\mathcal{I}} \neq b^{\mathcal{I}}$

Individual identity

- New ABox axioms.
- Express equality and non-equality between individuals.
- Syntax:
 - DL: $a = b$, $a \neq b$;
 - RDF/OWL: `:a owl:sameAs :b`, `:a owl:differentFrom :b`,
 - Manchester: `SameAs`, `DifferentFrom`.
- Semantics:
 - $\mathcal{I} \models a = b$ iff $a^{\mathcal{I}} = b^{\mathcal{I}}$
 - $\mathcal{I} \models a \neq b$ iff $a^{\mathcal{I}} \neq b^{\mathcal{I}}$
- Examples:
 - `sim:Bart owl:sameAs dbpedia:Bart_Simpson`,
 - `sim:Bart owl:differentFrom sim:Homer`.

Individual identity

- New ABox axioms.
- Express equality and non-equality between individuals.
- Syntax:
 - DL: $a = b$, $a \neq b$;
 - RDF/OWL: `:a owl:sameAs :b`, `:a owl:differentFrom :b`,
 - Manchester: `SameAs`, `DifferentFrom`.
- Semantics:
 - $\mathcal{I} \models a = b$ iff $a^{\mathcal{I}} = b^{\mathcal{I}}$
 - $\mathcal{I} \models a \neq b$ iff $a^{\mathcal{I}} \neq b^{\mathcal{I}}$
- Examples:
 - `sim:Bart owl:sameAs dbpedia:Bart_Simpson`,
 - `sim:Bart owl:differentFrom sim:Homer`.
- Remember:
 - Non unique name assumption (NUNA) in Sem. Web,
 - must sometimes use `=` and `≠` to get expected results.

Creating concepts using individuals

- New concept builder.

Creating concepts using individuals

- New concept builder.
- Create (anonymous) concepts by explicitly listing all members.

Creating concepts using individuals

- New concept builder.
- Create (anonymous) concepts by explicitly listing all members.
- Called *closed classes* in OWL.

Creating concepts using individuals

- New concept builder.
- Create (anonymous) concepts by explicitly listing all members.
- Called *closed classes* in OWL.
- Syntax:
 - DL: $\{a, b, \dots\}$
 - RDF/OWL: `owl:oneOf + rdf:List++`
 - Manchester: $\{a, b, \dots\}$

Creating concepts using individuals

- New concept builder.
- Create (anonymous) concepts by explicitly listing all members.
- Called *closed classes* in OWL.
- Syntax:
 - DL: $\{a, b, \dots\}$
 - RDF/OWL: `owl:oneOf + rdf:List++`
 - Manchester: $\{a, b, \dots\}$
- Example:
 - $SimpsonFamily \equiv \{Homer, Marge, Bart, Lisa, Maggie\}$
 - `:SimpsonFamily owl:equivalentClass [owl:oneOf (:Homer :Marge :Bart :Lisa :Maggie)] .`

Creating concepts using individuals

- New concept builder.
- Create (anonymous) concepts by explicitly listing all members.
- Called *closed classes* in OWL.
- Syntax:
 - DL: $\{a, b, \dots\}$
 - RDF/OWL: `owl:oneOf + rdf:List++`
 - Manchester: $\{a, b, \dots\}$
- Example:
 - $SimpsonFamily \equiv \{Homer, Marge, Bart, Lisa, Maggie\}$
 - `:SimpsonFamily owl:equivalentClass [owl:oneOf (:Homer :Marge :Bart :Lisa :Maggie)] .`
- Note:
 - The individuals does not necessarily represent different objects,
 - we still need $=$ and \neq to say that members are the same/different.
 - “Closed classes of data values” are *datatypes*.

Axioms involving individuals: Negative Property Assertions

- New ABox axiom.
- Syntax:
 - DL: $\neg R(a, b)$,
 - RDF/OWL: `owl:NegativePropertyAssertion` (Class of assertions/triples)
 - Manchester: `a not R b`.

Axioms involving individuals: Negative Property Assertions

- New ABox axiom.
- Syntax:
 - DL: $\neg R(a, b)$,
 - RDF/OWL: `owl:NegativePropertyAssertion` (Class of assertions/triples)
 - Manchester: `a not R b`.
- Semantics:
 - $\mathcal{I} \models \neg R(a, b)$ iff $\langle a^{\mathcal{I}}, b^{\mathcal{I}} \rangle \notin R^{\mathcal{I}}$,

Axioms involving individuals: Negative Property Assertions

- New ABox axiom.
- Syntax:
 - DL: $\neg R(a, b)$,
 - RDF/OWL: `owl:NegativePropertyAssertion` (Class of assertions/triples)
 - Manchester: `a not R b`.
- Semantics:
 - $\mathcal{I} \models \neg R(a, b)$ iff $\langle a^{\mathcal{I}}, b^{\mathcal{I}} \rangle \notin R^{\mathcal{I}}$,
- Notes:
 - Works both for object properties and datatype properties.

Axioms involving individuals: Negative Property Assertions

- New ABox axiom.
- Syntax:
 - DL: $\neg R(a, b)$,
 - RDF/OWL: `owl:NegativePropertyAssertion` (Class of assertions/triples)
 - Manchester: `a not R b`.
- Semantics:
 - $\mathcal{I} \models \neg R(a, b)$ iff $\langle a^{\mathcal{I}}, b^{\mathcal{I}} \rangle \notin R^{\mathcal{I}}$,
- Notes:
 - Works both for object properties and datatype properties.
- Examples:
 - `:Bart not :hasFather :NedFlanders`
 - `:Bart not :hasAge "2"^^xsd:int`

Recap of existential and universal restrictions

- Existential restrictions
 - have the form $\exists R.D$,
 - typically used to connect classes,
 - $C \sqsubseteq \exists R.D$: A C is R -related to (at least) *some* D :
 - Example: A person has a female parent: $Person \sqsubseteq \exists hasParent.Woman$.
 - Note that C -objects can be R -related to other things:
 - A person may have other parents who are not women—but there must be one who's a woman.

Recap of existential and universal restrictions

- Existential restrictions
 - have the form $\exists R.D$,
 - typically used to connect classes,
 - $C \sqsubseteq \exists R.D$: A C is R -related to (at least) *some* D :
 - Example: A person has a female parent: $Person \sqsubseteq \exists hasParent.Woman$.
 - Note that C -objects can be R -related to other things:
 - A person may have other parents who are not women—but there must be one who's a woman.
- Universal restrictions
 - have the form $\forall R.D$,
 - restrict the things a type of object can be connected to,
 - $C \sqsubseteq \forall R.D$: C is R -related to D 's *only*:
 - Example: A horse eats only chocolate: $Horse \sqsubseteq \forall eats.Chocolate$.
 - Note that C -objects may not be R -related to anything at all:
 - A horse does not have to eat anything—but if it does it must be chocolate.

Cardinality restrictions

- New concept builder.
- Syntax:
 - DL: $\leq_n R.D$ and $\geq_n R.D$ (and $=_n R.D$).
 - RDF/OWL: `owl:minCardinality`, `owl:maxCardinality`, `owl:cardinality`.
 - Manchester: `min`, `max`, `exactly`.

Cardinality restrictions

- New concept builder.
- Syntax:
 - DL: $\leq_n R.D$ and $\geq_n R.D$ (and $=_n R.D$).
 - RDF/OWL: `owl:minCardinality`, `owl:maxCardinality`, `owl:cardinality`.
 - Manchester: `min`, `max`, `exactly`.
- Semantics:
 - $(\leq_n R.D)^{\mathcal{I}} = \{a \in \Delta^{\mathcal{I}} : |\{b : \langle a, b \rangle \in R^{\mathcal{I}} \wedge b \in D^{\mathcal{I}}\}| \leq n\}$
 - $(\geq_n R.D)^{\mathcal{I}} = \{a \in \Delta^{\mathcal{I}} : |\{b : \langle a, b \rangle \in R^{\mathcal{I}} \wedge b \in D^{\mathcal{I}}\}| \geq n\}$
- Restricts the number of relations a type of object can/must have.

Cardinality restrictions

- New concept builder.
- Syntax:
 - DL: $\leq_n R.D$ and $\geq_n R.D$ (and $=_n R.D$).
 - RDF/OWL: `owl:minCardinality`, `owl:maxCardinality`, `owl:cardinality`.
 - Manchester: `min`, `max`, `exactly`.
- Semantics:
 - $(\leq_n R.D)^{\mathcal{I}} = \{a \in \Delta^{\mathcal{I}} : |\{b : \langle a, b \rangle \in R^{\mathcal{I}} \wedge b \in D^{\mathcal{I}}\}| \leq n\}$
 - $(\geq_n R.D)^{\mathcal{I}} = \{a \in \Delta^{\mathcal{I}} : |\{b : \langle a, b \rangle \in R^{\mathcal{I}} \wedge b \in D^{\mathcal{I}}\}| \geq n\}$
- Restricts the number of relations a type of object can/must have.
- TBox axioms read:
 - $C \sqsubseteq \square_n R.D$: "A C is R-related to n number of D's."
 - \leq : *at most*
 - \geq : *at least*
 - $=$: *exactly*

Example cardinality restriction

- $Car \sqsubseteq \leq_2 driveAxle.\top$
 - “A car has at most two drive axles.”

Example cardinality restriction

- $Car \sqsubseteq \leq_2 driveAxle.\top$
 - “A car has at most two drive axles.”
- $RangeRover \sqsubseteq =_1 driveAxle.FrontAxle \sqcap =_1 driveAxle.RearAxle$
 - “A Range Rover has one front axle as drive axle and one rear axle as drive axle”.

Example cardinality restriction

- $Car \sqsubseteq \leq_2 driveAxle.\top$
 - “A car has at most two drive axles.”
- $RangeRover \sqsubseteq =_1 driveAxle.FrontAxle \sqcap =_1 driveAxle.RearAxle$
 - “A Range Rover has one front axle as drive axle and one rear axle as drive axle”.
- $Human \sqsubseteq =_2 hasBiologicalParent.\top$
 - “A human has two biological parents.”

Example cardinality restriction

- $Car \sqsubseteq \leq_2 driveAxle.\top$
 - “A car has at most two drive axles.”
- $RangeRover \sqsubseteq =_1 driveAxle.FrontAxle \sqcap =_1 driveAxle.RearAxle$
 - “A Range Rover has one front axle as drive axle and one rear axle as drive axle”.
- $Human \sqsubseteq =_2 hasBiologicalParent.\top$
 - “A human has two biological parents.”
- $Mammal \sqsubseteq =_1 hasParent.Female \sqcap =_1 hasParent.Male$
 - “A mammal has one parent that is a female and one parent that is a male.”

Example cardinality restriction

- $Car \sqsubseteq \leq_2 driveAxle.\top$
 - “A car has at most two drive axles.”
- $RangeRover \sqsubseteq =_1 driveAxle.FrontAxle \sqcap =_1 driveAxle.RearAxle$
 - “A Range Rover has one front axle as drive axle and one rear axle as drive axle”.
- $Human \sqsubseteq =_2 hasBiologicalParent.\top$
 - “A human has two biological parents.”
- $Mammal \sqsubseteq =_1 hasParent.Female \sqcap =_1 hasParent.Male$
 - “A mammal has one parent that is a female and one parent that is a male.”
- $\geq_2 owns.Houses \sqcup \geq_5 own.Car \sqsubseteq Rich$
 - “Everyone who owns more than two houses or five cars is rich.”

One more value restriction

- Restrictions of the form $\forall R.D$, $\exists R.D$, $\leq_n R.D$, $\geq_n R.D$ are called *qualified* when D is not \top .
- We can also qualify with a closed class.

One more value restriction

- Restrictions of the form $\forall R.D$, $\exists R.D$, $\leq_n R.D$, $\geq_n R.D$ are called *qualified* when D is not \top .
- We can also qualify with a closed class.
- Syntax:
 - RDF/OWL: `hasValue`,
 - DL, Manchester: just use: `{...}`.

One more value restriction

- Restrictions of the form $\forall R.D$, $\exists R.D$, $\leq_n R.D$, $\geq_n R.D$ are called *qualified* when D is not \top .
- We can also qualify with a closed class.
- Syntax:
 - RDF/OWL: `hasValue`,
 - DL, Manchester: just use: `{...}`.
- Example:
 - $Bieberette \equiv Girl \sqcap \exists loves.\{J.Bieber\}$
 - $\top \sqsubseteq \exists loves.\{Mary\}$
 - $Norwegian \equiv Person \sqcap \exists citizenOf.\{Norway\}$

Self restriction

- New construct builder.
- Local reflexivity restriction. Restricts to objects which are related to themselves.
- Syntax:
 - DL: $\exists R.\textit{Self}$
 - RDF/OWL: `owl:hasSelf`,
 - Manchester: `Self`

Self restriction

- New construct builder.
- Local reflexivity restriction. Restricts to objects which are related to themselves.
- Syntax:
 - DL: $\exists R.Self$
 - RDF/OWL: `owl:hasSelf`,
 - Manchester: `Self`
- Semantics:
 - $(\exists R.Self)^{\mathcal{I}} = \{x \in \Delta^{\mathcal{I}} \mid \langle x, x \rangle \in R^{\mathcal{I}}\}$

Self restriction

- New construct builder.
- Local reflexivity restriction. Restricts to objects which are related to themselves.
- Syntax:
 - DL: $\exists R.Self$
 - RDF/OWL: `owl:hasSelf`,
 - Manchester: `Self`
- Semantics:
 - $(\exists R.Self)^{\mathcal{I}} = \{x \in \Delta^{\mathcal{I}} \mid \langle x, x \rangle \in R^{\mathcal{I}}\}$
- Examples:
 - $AutoregulatingProcess \sqsubseteq \exists regulate.Self$
 - $\exists hasBoss.Self \sqsubseteq SelfEmployed$

Restrictions, non-unique names and open worlds

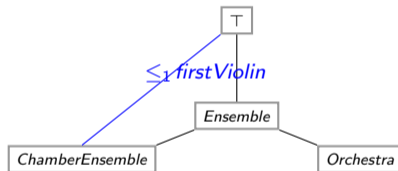
Restrictions + the OWA and the NUNA can be tricky, consider:

TBox:

$Orchestra \sqsubseteq Ensemble$

$ChamberEnsemble \sqsubseteq Ensemble$

$ChamberEnsemble \sqsubseteq \leq_1 firstViolin.T$



Restrictions, non-unique names and open worlds

Restrictions + the OWA and the NUNA can be tricky, consider:

TBox:

$Orchestra \sqsubseteq Ensemble$

$ChamberEnsemble \sqsubseteq Ensemble$

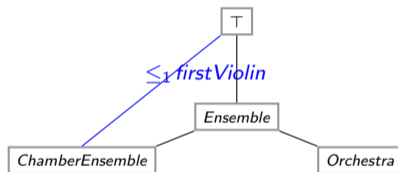
$ChamberEnsemble \sqsubseteq \leq_1 firstViolin.T$

ABox:

`Ensemble(oslo)`

`firstViolin(oslo, skolem)`

`firstViolin(oslo, lie)`



Restrictions, non-unique names and open worlds

Restrictions + the OWA and the NUNA can be tricky, consider:

TBox:

$Orchestra \sqsubseteq Ensemble$

$ChamberEnsemble \sqsubseteq Ensemble$

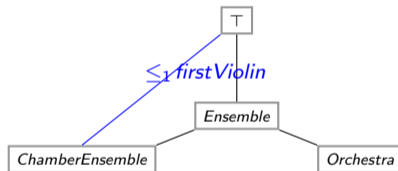
$ChamberEnsemble \sqsubseteq \leq_1 firstViolin.T$

ABox:

`Ensemble(oslo)`

`firstViolin(oslo, skolem)`

`firstViolin(oslo, lie)`



- Orchestras and Chamber ensembles are Ensembles.
- Chamber ensembles have only one instrument on each voice,
- in particular, only one first violin.

Restrictions, non-unique names and open worlds

Restrictions + the OWA and the NUNA can be tricky, consider:

TBox:

$Orchestra \sqsubseteq Ensemble$

$ChamberEnsemble \sqsubseteq Ensemble$

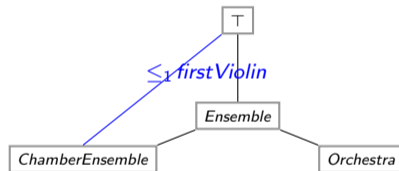
$ChamberEnsemble \sqsubseteq \leq_1 firstViolin.T$

ABox:

`Ensemble(oslo)`

`firstViolin(oslo, skolem)`

`firstViolin(oslo, lie)`



- Orchestras and Chamber ensembles are Ensembles.
- Chamber ensembles have only one instrument on each voice, in particular, only one first violin.
- oslo has two first violins; is oslo an Orchestra?

Unexpected (non-)results

It does not follow from $TBox + ABox$ that `oslo` is an *Orchestra*:

- An ensemble need neither be an orchestra nor a chamber ensemble, its “just” an ensemble.
- Add “covering axiom” $Ensemble \sqsubseteq Orchestra \sqcup ChamberEnsemble$:
 - An ensemble is an orchestra or a chamber ensemble.

Unexpected (non-)results

It does not follow from $TBox + ABox$ that `oslo` is an *Orchestra*:

- An ensemble need neither be an orchestra nor a chamber ensemble, its “just” an ensemble.
- Add “covering axiom” $Ensemble \sqsubseteq Orchestra \sqcup ChamberEnsemble$:
 - An ensemble is an orchestra or a chamber ensemble.

It still does not follow that `oslo` is an *Orchestra*:

- This is due to the NUNA.
- We cannot assume that `skolem` and `lie` are distinct.
- The statement `skolem owl:differentFrom lie`, i.e., $skolem \neq lie$, makes `oslo` an orchestra.

Unexpected (non-)results

It does not follow from TBox + ABox that oslo is an *Orchestra*:

- An ensemble need neither be an orchestra nor a chamber ensemble, its “just” an ensemble.
- Add “covering axiom” $Ensemble \sqsubseteq Orchestra \sqcup ChamberEnsemble$:
 - An ensemble is an orchestra or a chamber ensemble.

It still does not follow that oslo is an *Orchestra*:

- This is due to the NUNA.
- We cannot assume that skolem and lie are distinct.
- The statement `skolem owl:differentFrom lie`, i.e., $skolem \neq lie$, makes oslo an orchestra.

If we remove `firstViolin(oslo, lie)`, is oslo a *ChamberEnsemble*?

Unexpected (non-)results

It does not follow from TBox + ABox that oslo is an *Orchestra*:

- An ensemble need neither be an orchestra nor a chamber ensemble, its “just” an ensemble.
- Add “covering axiom” $Ensemble \sqsubseteq Orchestra \sqcup ChamberEnsemble$:
 - An ensemble is an orchestra or a chamber ensemble.

It still does not follow that oslo is an *Orchestra*:

- This is due to the NUNA.
- We cannot assume that skolem and lie are distinct.
- The statement `skolem owl:differentFrom lie`, i.e., $skolem \neq lie$, makes oslo an orchestra.

If we remove `firstViolin(oslo, lie)`, is oslo a *ChamberEnsemble*?

- it does not follow that oslo is a *ChamberEnsemble*.
- This is due to the OWA:
- oslo may have other first violinists.

Protégé demo of previous slide

- Make class Ensemble.
- Make subclass Orchestra.
- Make subclass ChamberEnsemble.
- Make object property firstViolin.
- Make `firstViolin` `max 1` superclass of ChamberEnsemble.
- Make an Ensemble `oslo`
- Make a Thing `skolem`
- Make a Thing `lie`
- Add `firstViolin` `skolem` to `oslo`
- Add `firstViolin` `lie` to `oslo`
- Classify! Nothing happens.
- Add covering axiom: `Orchestra` or `ChamberEnsemble` superclass of `Ensemble`.
- Classify! Nothing happens.
- `skolem` is different from `lie`
- Classify! Bingo! `oslo` is an `Orchestra`!

Role characteristics and relationships (RBox)

Vocabulary

Given the *roles* $\{R_1, R_2, \dots\}$

Role characteristics and relationships (RBox)

Vocabulary

Given the *roles* $\{R_1, R_2, \dots\}$

Role descriptions

$R, S \rightarrow$	R_i		(atomic role)
	\top_{role}		(universal role)
	\perp_{role}		(bottom role)

Role characteristics and relationships (RBox)

Vocabulary

Given the *roles* $\{R_1, R_2, \dots\}$

Role descriptions

$R, S \rightarrow$	R_i		(atomic role)
	\top_{role}		(universal role)
	\perp_{role}		(bottom role)
	$\neg R$		(complement role)
	R^-		(inverse role)
	$R \sqcap S$		(role intersection)
	$R \circ S$		(role chain)

Rbox (cont.)

- Role axioms: Let R and S be roles, then we can assert
 - subsumption: $R \sqsubseteq S$ $(R^{\mathcal{I}} \subseteq S^{\mathcal{I}})$,
 - equivalence: $R \equiv S$ $(R^{\mathcal{I}} = S^{\mathcal{I}})$,
 - disjointness: $R \sqcap S \sqsubseteq \perp_{\text{role}}$ $(R^{\mathcal{I}} \cap S^{\mathcal{I}} \subseteq \emptyset)$,
 - key: R is a key for concept C .

²Restrictions apply

Rbox (cont.)

- Role axioms: Let R and S be roles, then we can assert
 - subsumption: $R \sqsubseteq S$ $(R^{\mathcal{I}} \subseteq S^{\mathcal{I}})$,
 - equivalence: $R \equiv S$ $(R^{\mathcal{I}} = S^{\mathcal{I}})$,
 - disjointness: $R \sqcap S \sqsubseteq \perp_{\text{role}}$ $(R^{\mathcal{I}} \cap S^{\mathcal{I}} \subseteq \emptyset)$,
 - key: R is a key for concept C .
- A role can have the characteristics (axioms):
 - reflexive, irreflexive,
 - symmetric, asymmetric,
 - transitive, or/and²
 - functional, inverse functional.

²Restrictions apply

New roles

- The universal role, and the empty role—for both object roles and data roles.
- Syntax:
 - (DL: U (universal object role), D (universal data value role))
 - RDF/OWL, Manchester: `owl:topObjectProperty`, `owl:topDataProperty`,
`owl:bottomObjectProperty`, `owl:bottomDataProperty`

New roles

- The universal role, and the empty role—for both object roles and data roles.
- Syntax:
 - (DL: U (universal object role), D (universal data value role))
 - RDF/OWL, Manchester: `owl:topObjectProperty`, `owl:topDataProperty`,
`owl:bottomObjectProperty`, `owl:bottomDataProperty`
- Semantics:
 - $U^{\mathcal{I}} = \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$
 - $\mathcal{D}^{\mathcal{I}} = \Delta^{\mathcal{I}} \times \Lambda$

New roles

- The universal role, and the empty role—for both object roles and data roles.
- Syntax:
 - (DL: U (universal object role), D (universal data value role))
 - RDF/OWL, Manchester: `owl:topObjectProperty`, `owl:topDataProperty`, `owl:bottomObjectProperty`, `owl:bottomDataProperty`
- Semantics:
 - $U^{\mathcal{I}} = \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$
 - $D^{\mathcal{I}} = \Delta^{\mathcal{I}} \times \Lambda$
- Reads:
 - all pairs of individuals are connected by `owl:topObjectProperty`,
 - no individuals are connected by `owl:bottomObjectProperty`.
 - all possible individuals are connected with all literals by `owl:topDataProperty`,
 - no individual is connected by `owl:bottomDataProperty` to a literal.

Corresponding mathematical properties and operations

If R and S are binary relations on X then

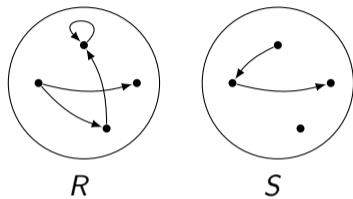
- $(R^-)^I = \{\langle a^I, b^I \rangle \mid \langle b^I, a^I \rangle \in R^I\}$

Corresponding mathematical properties and operations

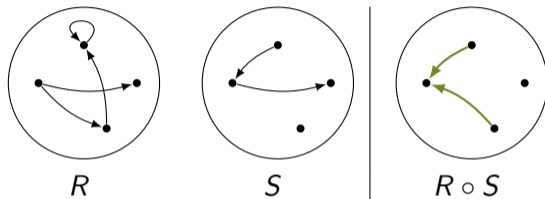
If R and S are binary relations on X then

- $(R^-)^{\mathcal{I}} = \{\langle a^{\mathcal{I}}, b^{\mathcal{I}} \rangle \mid \langle b^{\mathcal{I}}, a^{\mathcal{I}} \rangle \in R^{\mathcal{I}}\}$
- $(R \circ S)^{\mathcal{I}} = \{\langle a^{\mathcal{I}}, c^{\mathcal{I}} \rangle \mid \langle a^{\mathcal{I}}, b^{\mathcal{I}} \rangle \in R^{\mathcal{I}}, \langle b^{\mathcal{I}}, c^{\mathcal{I}} \rangle \in S^{\mathcal{I}}\}$

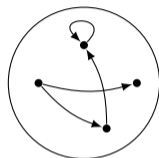
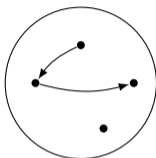
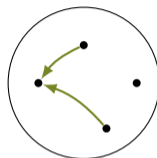
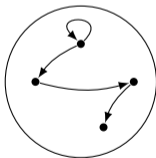
Role chaining and inverses illustrated



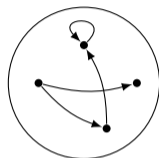
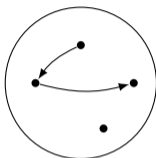
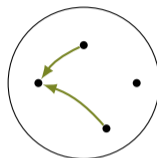
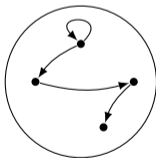
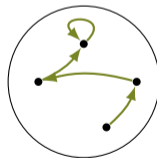
Role chaining and inverses illustrated



Role chaining and inverses illustrated

 R  S  $R \circ S$  T

Role chaining and inverses illustrated

 R  S  $R \circ S$  T  T^-

Common properties of roles

A relation R over a set X ($R \subseteq X \times X$) is

Reflexive: if $\langle a, a \rangle \in R$ for all $a \in X$ ($X \sqsubseteq \exists R. \text{Self}$)

Common properties of roles

A relation R over a set X ($R \subseteq X \times X$) is

Reflexive: if $\langle a, a \rangle \in R$ for all $a \in X$

$(X \sqsubseteq \exists R.Self)$

Irreflexive: if $\langle a, a \rangle \notin R$ for all $a \in X$

$(X \sqsubseteq \neg \exists R.Self)$

Common properties of roles

A relation R over a set X ($R \subseteq X \times X$) is

Reflexive:	if $\langle a, a \rangle \in R$ for all $a \in X$	$(X \sqsubseteq \exists R.Self)$
Irreflexive:	if $\langle a, a \rangle \notin R$ for all $a \in X$	$(X \sqsubseteq \neg \exists R.Self)$
Symmetric:	if $\langle a, b \rangle \in R$ implies $\langle b, a \rangle \in R$	$(R^- \sqsubseteq R)$

Common properties of roles

A relation R over a set X ($R \subseteq X \times X$) is

Reflexive:	if $\langle a, a \rangle \in R$ for all $a \in X$	$(X \sqsubseteq \exists R. Self)$
Irreflexive:	if $\langle a, a \rangle \notin R$ for all $a \in X$	$(X \sqsubseteq \neg \exists R. Self)$
Symmetric:	if $\langle a, b \rangle \in R$ implies $\langle b, a \rangle \in R$	$(R^- \sqsubseteq R)$
Asymmetric:	if $\langle a, b \rangle \in R$ implies $\langle b, a \rangle \notin R$	$(R^- \sqsubseteq \neg R)$

Common properties of roles

A relation R over a set X ($R \subseteq X \times X$) is

Reflexive:	if $\langle a, a \rangle \in R$ for all $a \in X$	$(X \sqsubseteq \exists R. Self)$
Irreflexive:	if $\langle a, a \rangle \notin R$ for all $a \in X$	$(X \sqsubseteq \neg \exists R. Self)$
Symmetric:	if $\langle a, b \rangle \in R$ implies $\langle b, a \rangle \in R$	$(R^- \sqsubseteq R)$
Asymmetric:	if $\langle a, b \rangle \in R$ implies $\langle b, a \rangle \notin R$	$(R^- \sqsubseteq \neg R)$
Transitive:	if $\langle a, b \rangle, \langle b, c \rangle \in R$ implies $\langle a, c \rangle \in R$	$(R \circ R \sqsubseteq R)$

Common properties of roles

A relation R over a set X ($R \subseteq X \times X$) is

Reflexive:	if $\langle a, a \rangle \in R$ for all $a \in X$	$(X \sqsubseteq \exists R. Self)$
Irreflexive:	if $\langle a, a \rangle \notin R$ for all $a \in X$	$(X \sqsubseteq \neg \exists R. Self)$
Symmetric:	if $\langle a, b \rangle \in R$ implies $\langle b, a \rangle \in R$	$(R^- \sqsubseteq R)$
Asymmetric:	if $\langle a, b \rangle \in R$ implies $\langle b, a \rangle \notin R$	$(R^- \sqsubseteq \neg R)$
Transitive:	if $\langle a, b \rangle, \langle b, c \rangle \in R$ implies $\langle a, c \rangle \in R$	$(R \circ R \sqsubseteq R)$
Functional:	if $\langle a, b \rangle, \langle a, c \rangle \in R$ implies $b = c$	$(\top \sqsubseteq \leq_1 R. \top)$

Common properties of roles

A relation R over a set X ($R \subseteq X \times X$) is

Reflexive:	if $\langle a, a \rangle \in R$ for all $a \in X$	$(X \sqsubseteq \exists R. Self)$
Irreflexive:	if $\langle a, a \rangle \notin R$ for all $a \in X$	$(X \sqsubseteq \neg \exists R. Self)$
Symmetric:	if $\langle a, b \rangle \in R$ implies $\langle b, a \rangle \in R$	$(R^- \sqsubseteq R)$
Asymmetric:	if $\langle a, b \rangle \in R$ implies $\langle b, a \rangle \notin R$	$(R^- \sqsubseteq \neg R)$
Transitive:	if $\langle a, b \rangle, \langle b, c \rangle \in R$ implies $\langle a, c \rangle \in R$	$(R \circ R \sqsubseteq R)$
Functional:	if $\langle a, b \rangle, \langle a, c \rangle \in R$ implies $b = c$	$(\top \sqsubseteq \leq_1 R. \top)$
Inverse functional:	if $\langle a, b \rangle, \langle c, b \rangle \in R$ implies $a = c$	$(\top \sqsubseteq \leq_1 R^- . \top)$

Properties in OWL

Remember: three kinds of *mutually disjoint* properties in OWL:

- ① `owl:DatatypeProperty`
 - link individuals to data values, e.g., `xsd:string`.
 - Examples: `:hasAge`, `:hasSurname`.
- ② `owl:ObjectProperty`
 - link individuals to individuals.
 - Example: `:hasFather`, `:driveAxle`.
- ③ `owl:AnnotationProperty`
 - has no logical implication, ignored by reasoners.
 - Examples: `rdfs:label`, `dc:creator`.

Characteristics of OWL properties

- Object properties link individuals to individuals, so all characteristics and operations are defined for them.

Characteristics of OWL properties

- Object properties link individuals to individuals, so all characteristics and operations are defined for them.
- Datatype properties link individuals to data values, so they cannot be
 - reflexive—or they would not be datatype properties,

Characteristics of OWL properties

- Object properties link individuals to individuals, so all characteristics and operations are defined for them.
- Datatype properties link individuals to data values, so they cannot be
 - reflexive—or they would not be datatype properties,
 - transitive—since no property takes data values in 1. position,

Characteristics of OWL properties

- Object properties link individuals to individuals, so all characteristics and operations are defined for them.
- Datatype properties link individuals to data values, so they cannot be
 - reflexive—or they would not be datatype properties,
 - transitive—since no property takes data values in 1. position,
 - symmetric—as above,

Characteristics of OWL properties

- Object properties link individuals to individuals, so all characteristics and operations are defined for them.
- Datatype properties link individuals to data values, so they cannot be
 - reflexive—or they would not be datatype properties,
 - transitive—since no property takes data values in 1. position,
 - symmetric—as above,
 - inverses—as above,

Characteristics of OWL properties

- Object properties link individuals to individuals, so all characteristics and operations are defined for them.
- Datatype properties link individuals to data values, so they cannot be
 - reflexive—or they would not be datatype properties,
 - transitive—since no property takes data values in 1. position,
 - symmetric—as above,
 - inverses—as above,
 - inverse functional—for computational reasons,

Characteristics of OWL properties

- Object properties link individuals to individuals, so all characteristics and operations are defined for them.
- Datatype properties link individuals to data values, so they cannot be
 - reflexive—or they would not be datatype properties,
 - transitive—since no property takes data values in 1. position,
 - symmetric—as above,
 - inverses—as above,
 - inverse functional—for computational reasons,
 - part of chains—as above,

Characteristics of OWL properties

- Object properties link individuals to individuals, so all characteristics and operations are defined for them.
- Datatype properties link individuals to data values, so they cannot be
 - reflexive—or they would not be datatype properties,
 - transitive—since no property takes data values in 1. position,
 - symmetric—as above,
 - inverses—as above,
 - inverse functional—for computational reasons,
 - part of chains—as above,
 - so, what remains is: functionality,

Characteristics of OWL properties

- Object properties link individuals to individuals, so all characteristics and operations are defined for them.
- Datatype properties link individuals to data values, so they cannot be
 - reflexive—or they would not be datatype properties,
 - transitive—since no property takes data values in 1. position,
 - symmetric—as above,
 - inverses—as above,
 - inverse functional—for computational reasons,
 - part of chains—as above,
 - so, what remains is: functionality,
 - (and subsumption, equivalence and disjointness).

Characteristics of OWL properties

- Object properties link individuals to individuals, so all characteristics and operations are defined for them.
- Datatype properties link individuals to data values, so they cannot be
 - reflexive—or they would not be datatype properties,
 - transitive—since no property takes data values in 1. position,
 - symmetric—as above,
 - inverses—as above,
 - inverse functional—for computational reasons,
 - part of chains—as above,
 - so, what remains is: functionality,
 - (and subsumption, equivalence and disjointness).

Characteristics of OWL properties

- Object properties link individuals to individuals, so all characteristics and operations are defined for them.
- Datatype properties link individuals to data values, so they cannot be
 - reflexive—or they would not be datatype properties,
 - transitive—since no property takes data values in 1. position,
 - symmetric—as above,
 - inverses—as above,
 - inverse functional—for computational reasons,
 - part of chains—as above,
 - so, what remains is: functionality,
 - (and subsumption, equivalence and disjointness).
- (Annotation properties have no logical implication, so nothing can be said about them.)

Some relations from ordinary language

- Symmetric relations:

Some relations from ordinary language

- Symmetric relations:
 - *hasSibling*

Some relations from ordinary language

- Symmetric relations:
 - *hasSibling*
 - *differentFrom*

Some relations from ordinary language

- Symmetric relations:
 - *hasSibling*
 - *differentFrom*
- *Non-symmetric* relations:

Some relations from ordinary language

- Symmetric relations:
 - *hasSibling*
 - *differentFrom*
- Non-symmetric relations:
 - *hasBrother*

Some relations from ordinary language

- Symmetric relations:
 - *hasSibling*
 - *differentFrom*
- Non-symmetric relations:
 - *hasBrother*
- Asymmetric relations:

Some relations from ordinary language

- Symmetric relations:
 - *hasSibling*
 - *differentFrom*
- Non-symmetric relations:
 - *hasBrother*
- Asymmetric relations:
 - *olderThan*

Some relations from ordinary language

- Symmetric relations:
 - *hasSibling*
 - *differentFrom*
- Non-symmetric relations:
 - *hasBrother*
- Asymmetric relations:
 - *olderThan*
 - *memberOf*

Some relations from ordinary language

- Symmetric relations:
 - *hasSibling*
 - *differentFrom*
- *Non-symmetric* relations:
 - *hasBrother*
- Asymmetric relations:
 - *olderThan*
 - *memberOf*
- Transitive relations:

Some relations from ordinary language

- Symmetric relations:
 - *hasSibling*
 - *differentFrom*
- Non-symmetric relations:
 - *hasBrother*
- Asymmetric relations:
 - *olderThan*
 - *memberOf*
- Transitive relations:
 - *olderThan*

Some relations from ordinary language

- Symmetric relations:
 - *hasSibling*
 - *differentFrom*
- Non-symmetric relations:
 - *hasBrother*
- Asymmetric relations:
 - *olderThan*
 - *memberOf*
- Transitive relations:
 - *olderThan*
 - *hasSibling*

Some relations from ordinary language

- Symmetric relations:
 - *hasSibling*
 - *differentFrom*
- Non-symmetric relations:
 - *hasBrother*
- Asymmetric relations:
 - *olderThan*
 - *memberOf*
- Transitive relations:
 - *olderThan*
 - *hasSibling*
- Functional relations:

Some relations from ordinary language

- Symmetric relations:
 - *hasSibling*
 - *differentFrom*
- Non-symmetric relations:
 - *hasBrother*
- Asymmetric relations:
 - *olderThan*
 - *memberOf*
- Transitive relations:
 - *olderThan*
 - *hasSibling*
- Functional relations:
 - *hasBiologicalMother*

Some relations from ordinary language

- Symmetric relations:
 - *hasSibling*
 - *differentFrom*
- Non-symmetric relations:
 - *hasBrother*
- Asymmetric relations:
 - *olderThan*
 - *memberOf*
- Transitive relations:
 - *olderThan*
 - *hasSibling*
- Functional relations:
 - *hasBiologicalMother*
- Inverse functional relations:

Some relations from ordinary language

- Symmetric relations:
 - *hasSibling*
 - *differentFrom*
- Non-symmetric relations:
 - *hasBrother*
- Asymmetric relations:
 - *olderThan*
 - *memberOf*
- Transitive relations:
 - *olderThan*
 - *hasSibling*
- Functional relations:
 - *hasBiologicalMother*
- Inverse functional relations:
 - *gaveBirthTo*

Examples inverses and chains

Some inverses:

- $hasParent \equiv hasChild^{-}$
- $hasBiologicalMother \equiv gaveBirthTo^{-}$
- $olderThan \equiv youngerThan^{-}$



Examples inverses and chains

Some inverses:

- $hasParent \equiv hasChild^{-}$
- $hasBiologicalMother \equiv gaveBirthTo^{-}$
- $olderThan \equiv youngerThan^{-}$

Some role chains:

- $hasParent \circ hasParent \sqsubseteq hasGrandParent$
- $hasAncestor \circ hasAncestor \sqsubseteq hasAncestor$
- $hasParent \circ hasBrother \sqsubseteq hasUncle$



Quirks

Role modelling in OWL 2 can get excessively complicated.

- For instance:
 - transitive roles cannot be irreflexive or asymmetric,

Quirks

Role modelling in OWL 2 can get excessively complicated.

- For instance:
 - transitive roles cannot be irreflexive or asymmetric,
 - role inclusions are not allowed to cycle, i.e. not

`hasParent o hasHusband \sqsubseteq hasFather`

`hasFather \sqsubseteq hasParent.`

Quirks

Role modelling in OWL 2 can get excessively complicated.

- For instance:
 - transitive roles cannot be irreflexive or asymmetric,
 - role inclusions are not allowed to cycle, i.e. not
$$\begin{aligned} \text{hasParent} \circ \text{hasHusband} &\sqsubseteq \text{hasFather} \\ \text{hasFather} &\sqsubseteq \text{hasParent}. \end{aligned}$$
 - transitive roles R and S cannot be declared disjoint

Quirks

Role modelling in OWL 2 can get excessively complicated.

- For instance:
 - transitive roles cannot be irreflexive or asymmetric,
 - role inclusions are not allowed to cycle, i.e. not
$$\begin{aligned} \text{hasParent} \circ \text{hasHusband} &\sqsubseteq \text{hasFather} \\ \text{hasFather} &\sqsubseteq \text{hasParent}. \end{aligned}$$
 - transitive roles R and S cannot be declared disjoint
- Note:
 - these restrictions can be hard to keep track of
 - the reason they exist are computational, not logical

Quirks

Role modelling in OWL 2 can get excessively complicated.

- For instance:
 - transitive roles cannot be irreflexive or asymmetric,
 - role inclusions are not allowed to cycle, i.e. not
$$\begin{aligned} \text{hasParent} \circ \text{hasHusband} &\sqsubseteq \text{hasFather} \\ \text{hasFather} &\sqsubseteq \text{hasParent}. \end{aligned}$$
 - transitive roles R and S cannot be declared disjoint
- Note:
 - these restrictions can be hard to keep track of
 - the reason they exist are computational, not logical
- Fortunately:
 - There are also *simple* patterns
 - that are quite useful.

Creating datatypes

- Many predefined datatypes are available in OWL:
 - all common XSD datatypes: `xsd:string`, `xsd:int`, ...
 - a few from RDF: `rdf:PlainLiteral`,
 - and a few of their own: `owl:real` and `owl:rational`.

Creating datatypes

- Many predefined datatypes are available in OWL:
 - all common XSD datatypes: `xsd:string`, `xsd:int`, ...
 - a few from RDF: `rdf:PlainLiteral`,
 - and a few of their own: `owl:real` and `owl:rational`.
- New datatypes can be defined by boolean operations: \neg , \sqcap , \sqcup :
 - `owl:datatypeComplementOf`, `owl:intersectionOf`, `owl:unionOf`.

Creating datatypes

- Many predefined datatypes are available in OWL:
 - all common XSD datatypes: `xsd:string`, `xsd:int`, ...
 - a few from RDF: `rdf:PlainLiteral`,
 - and a few of their own: `owl:real` and `owl:rational`.
- New datatypes can be defined by boolean operations: \neg , \sqcap , \sqcup :
 - `owl:datatypeComplementOf`, `owl:intersectionOf`, `owl:unionOf`.
- Datatypes may be restricted with *constraining facets*, borrowed from XML Schema.
 - For numeric datatypes: `xsd:minInclusive`, `xsd:maxInclusive`
 - For string datatypes: `xsd:minLength`, `xsd:maxLength`, `xsd:pattern`.

Creating datatypes

- Many predefined datatypes are available in OWL:
 - all common XSD datatypes: `xsd:string`, `xsd:int`, ...
 - a few from RDF: `rdf:PlainLiteral`,
 - and a few of their own: `owl:real` and `owl:rational`.
- New datatypes can be defined by boolean operations: \neg , \sqcap , \sqcup :
 - `owl:datatypeComplementOf`, `owl:intersectionOf`, `owl:unionOf`.
- Datatypes may be restricted with *constraining facets*, borrowed from XML Schema.
 - For numeric datatypes: `xsd:minInclusive`, `xsd:maxInclusive`
 - For string datatypes: `xsd:minLength`, `xsd:maxLength`, `xsd:pattern`.
- Example:
 - Teenager is equivalent to: (Manchester Person and (age some positiveInteger[\geq 13, \leq 19]))
 - “A teenager is a person of age 13 to 19.”

Modelling patterns

So, what can we say now?

- ✓ A person has a mother.
- ✓ A penguin eats only fish. A horse eats only chocolate.
- ✓ A nuclear family has two parents, at least two children and a dog.

Modelling patterns

So, what can we say now?

- ✓ A person has a mother.
- ✓ A penguin eats only fish. A horse eats only chocolate.
- ✓ A nuclear family has two parents, at least two children and a dog.

(*NuclearFam* $\sqsubseteq =_2$ *hasMember.Parent* $\sqcap \geq_2$ *hasMember.Child* $\sqcap \exists$ *hasMember.Dog*)

Modelling patterns

So, what can we say now?

- ✓ A person has a mother.
- ✓ A penguin eats only fish. A horse eats only chocolate.
- ✓ A nuclear family has two parents, at least two children and a dog.
($NuclearFam \sqsubseteq =_2 hasMember.Parent \sqcap \geq_2 hasMember.Child \sqcap \exists hasMember.Dog$)
- ✓ A smoker is not a non-smoker (and vice versa).

Modelling patterns

So, what can we say now?

- ✓ A person has a mother.
- ✓ A penguin eats only fish. A horse eats only chocolate.
- ✓ A nuclear family has two parents, at least two children and a dog.
($NuclearFam \sqsubseteq =_2 hasMember.Parent \sqcap \geq_2 hasMember.Child \sqcap \exists hasMember.Dog$)
- ✓ A smoker is not a non-smoker (and vice versa).
- ✓ Everybody loves Mary.

Modelling patterns

So, what can we say now?

- ✓ A person has a mother.
- ✓ A penguin eats only fish. A horse eats only chocolate.
- ✓ A nuclear family has two parents, at least two children and a dog.
($NuclearFam \sqsubseteq =_2 hasMember.Parent \sqcap \geq_2 hasMember.Child \sqcap \exists hasMember.Dog$)
- ✓ A smoker is not a non-smoker (and vice versa).
- ✓ Everybody loves Mary. ($\top \sqsubseteq \exists loves.\{mary\}$ or $Person \sqsubseteq \exists loves.\{mary\}$)

Modelling patterns

So, what can we say now?

- ✓ A person has a mother.
- ✓ A penguin eats only fish. A horse eats only chocolate.
- ✓ A nuclear family has two parents, at least two children and a dog.
($NuclearFam \sqsubseteq =_2 hasMember.Parent \sqcap \geq_2 hasMember.Child \sqcap \exists hasMember.Dog$)
- ✓ A smoker is not a non-smoker (and vice versa).
- ✓ Everybody loves Mary. ($\top \sqsubseteq \exists loves.\{mary\}$ or $Person \sqsubseteq \exists loves.\{mary\}$)
- ✓ Adam is not Eve (and vice versa).

Modelling patterns

So, what can we say now?

- ✓ A person has a mother.
- ✓ A penguin eats only fish. A horse eats only chocolate.
- ✓ A nuclear family has two parents, at least two children and a dog.
($NuclearFam \sqsubseteq =_2 hasMember.Parent \sqcap \geq_2 hasMember.Child \sqcap \exists hasMember.Dog$)
- ✓ A smoker is not a non-smoker (and vice versa).
- ✓ Everybody loves Mary. ($\top \sqsubseteq \exists loves.\{mary\}$ or $Person \sqsubseteq \exists loves.\{mary\}$)
- ✓ Adam is not Eve (and vice versa). ($adam \neq eve$)

Modelling patterns

So, what can we say now?

- ✓ A person has a mother.
- ✓ A penguin eats only fish. A horse eats only chocolate.
- ✓ A nuclear family has two parents, at least two children and a dog.
($NuclearFam \sqsubseteq =_2 hasMember.Parent \sqcap \geq_2 hasMember.Child \sqcap \exists hasMember.Dog$)
- ✓ A smoker is not a non-smoker (and vice versa).
- ✓ Everybody loves Mary. ($\top \sqsubseteq \exists loves.\{mary\}$ or $Person \sqsubseteq \exists loves.\{mary\}$)
- ✓ Adam is not Eve (and vice versa). ($adam \neq eve$)
- ✓ Everything is black or white.

Modelling patterns

So, what can we say now?

- ✓ A person has a mother.
- ✓ A penguin eats only fish. A horse eats only chocolate.
- ✓ A nuclear family has two parents, at least two children and a dog.
($NuclearFam \sqsubseteq =_2 hasMember.Parent \sqcap \geq_2 hasMember.Child \sqcap \exists hasMember.Dog$)
- ✓ A smoker is not a non-smoker (and vice versa).
- ✓ Everybody loves Mary. ($\top \sqsubseteq \exists loves.\{mary\}$ or $Person \sqsubseteq \exists loves.\{mary\}$)
- ✓ Adam is not Eve (and vice versa). ($adam \neq eve$)
- ✓ Everything is black or white.
- ✓ The brother of my father is my uncle.

Modelling patterns

So, what can we say now?

- ✓ A person has a mother.
- ✓ A penguin eats only fish. A horse eats only chocolate.
- ✓ A nuclear family has two parents, at least two children and a dog.
($NuclearFam \sqsubseteq =_2 hasMember.Parent \sqcap \geq_2 hasMember.Child \sqcap \exists hasMember.Dog$)
- ✓ A smoker is not a non-smoker (and vice versa).
- ✓ Everybody loves Mary. ($\top \sqsubseteq \exists loves.\{mary\}$ or $Person \sqsubseteq \exists loves.\{mary\}$)
- ✓ Adam is not Eve (and vice versa). ($adam \neq eve$)
- ✓ Everything is black or white.
- ✓ The brother of my father is my uncle. ($hasFather \circ hasBrother \sqsubseteq hasUncle$)

Modelling patterns

So, what can we say now?

- ✓ A person has a mother.
- ✓ A penguin eats only fish. A horse eats only chocolate.
- ✓ A nuclear family has two parents, at least two children and a dog.
($NuclearFam \sqsubseteq =_2 hasMember.Parent \sqcap \geq_2 hasMember.Child \sqcap \exists hasMember.Dog$)
- ✓ A smoker is not a non-smoker (and vice versa).
- ✓ Everybody loves Mary. ($\top \sqsubseteq \exists loves.\{mary\}$ or $Person \sqsubseteq \exists loves.\{mary\}$)
- ✓ Adam is not Eve (and vice versa). ($adam \neq eve$)
- ✓ Everything is black or white.
- ✓ The brother of my father is my uncle. ($hasFather \circ hasBrother \sqsubseteq hasUncle$)
- ✓ My friend's friends are also my friends.

Modelling patterns

So, what can we say now?

- ✓ A person has a mother.
- ✓ A penguin eats only fish. A horse eats only chocolate.
- ✓ A nuclear family has two parents, at least two children and a dog.
($NuclearFam \sqsubseteq =_2 hasMember.Parent \sqcap \geq_2 hasMember.Child \sqcap \exists hasMember.Dog$)
- ✓ A smoker is not a non-smoker (and vice versa).
- ✓ Everybody loves Mary. ($\top \sqsubseteq \exists loves.\{mary\}$ or $Person \sqsubseteq \exists loves.\{mary\}$)
- ✓ Adam is not Eve (and vice versa). ($adam \neq eve$)
- ✓ Everything is black or white.
- ✓ The brother of my father is my uncle. ($hasFather \circ hasBrother \sqsubseteq hasUncle$)
- ✓ My friend's friends are also my friends. ($hasFriend \circ hasFriend \sqsubseteq hasFriend$)

Modelling patterns

So, what can we say now?

- ✓ A person has a mother.
- ✓ A penguin eats only fish. A horse eats only chocolate.
- ✓ A nuclear family has two parents, at least two children and a dog.
($NuclearFam \sqsubseteq =_2 hasMember.Parent \sqcap \geq_2 hasMember.Child \sqcap \exists hasMember.Dog$)
- ✓ A smoker is not a non-smoker (and vice versa).
- ✓ Everybody loves Mary. ($\top \sqsubseteq \exists loves.\{mary\}$ or $Person \sqsubseteq \exists loves.\{mary\}$)
- ✓ Adam is not Eve (and vice versa). ($adam \neq eve$)
- ✓ Everything is black or white.
- ✓ The brother of my father is my uncle. ($hasFather \circ hasBrother \sqsubseteq hasUncle$)
- ✓ My friend's friends are also my friends. ($hasFriend \circ hasFriend \sqsubseteq hasFriend$)
- ✓ If Homer is married to Marge, then Marge is married to Homer.

Modelling patterns

So, what can we say now?

- ✓ A person has a mother.
- ✓ A penguin eats only fish. A horse eats only chocolate.
- ✓ A nuclear family has two parents, at least two children and a dog.
($NuclearFam \sqsubseteq =_2 hasMember.Parent \sqcap \geq_2 hasMember.Child \sqcap \exists hasMember.Dog$)
- ✓ A smoker is not a non-smoker (and vice versa).
- ✓ Everybody loves Mary. ($\top \sqsubseteq \exists loves.\{mary\}$ or $Person \sqsubseteq \exists loves.\{mary\}$)
- ✓ Adam is not Eve (and vice versa). ($adam \neq eve$)
- ✓ Everything is black or white.
- ✓ The brother of my father is my uncle. ($hasFather \circ hasBrother \sqsubseteq hasUncle$)
- ✓ My friend's friends are also my friends. ($hasFriend \circ hasFriend \sqsubseteq hasFriend$)
- ✓ If Homer is married to Marge, then Marge is married to Homer. ($marriedTo^- \sqsubseteq marriedTo$)

Modelling patterns

So, what can we say now?

- ✓ A person has a mother.
- ✓ A penguin eats only fish. A horse eats only chocolate.
- ✓ A nuclear family has two parents, at least two children and a dog.
($NuclearFam \sqsubseteq =_2 hasMember.Parent \sqcap \geq_2 hasMember.Child \sqcap \exists hasMember.Dog$)
- ✓ A smoker is not a non-smoker (and vice versa).
- ✓ Everybody loves Mary. ($\top \sqsubseteq \exists loves.\{mary\}$ or $Person \sqsubseteq \exists loves.\{mary\}$)
- ✓ Adam is not Eve (and vice versa). ($adam \neq eve$)
- ✓ Everything is black or white.
- ✓ The brother of my father is my uncle. ($hasFather \circ hasBrother \sqsubseteq hasUncle$)
- ✓ My friend's friends are also my friends. ($hasFriend \circ hasFriend \sqsubseteq hasFriend$)
- ✓ If Homer is married to Marge, then Marge is married to Homer. ($marriedTo^- \sqsubseteq marriedTo$)
- ✓ If Homer is a parent of Bart, then Bart is a child of Homer.

Modelling patterns

So, what can we say now?

- ✓ A person has a mother.
- ✓ A penguin eats only fish. A horse eats only chocolate.
- ✓ A nuclear family has two parents, at least two children and a dog.
($NuclearFam \sqsubseteq =_2 hasMember.Parent \sqcap \geq_2 hasMember.Child \sqcap \exists hasMember.Dog$)
- ✓ A smoker is not a non-smoker (and vice versa).
- ✓ Everybody loves Mary. ($\top \sqsubseteq \exists loves.\{mary\}$ or $Person \sqsubseteq \exists loves.\{mary\}$)
- ✓ Adam is not Eve (and vice versa). ($adam \neq eve$)
- ✓ Everything is black or white.
- ✓ The brother of my father is my uncle. ($hasFather \circ hasBrother \sqsubseteq hasUncle$)
- ✓ My friend's friends are also my friends. ($hasFriend \circ hasFriend \sqsubseteq hasFriend$)
- ✓ If Homer is married to Marge, then Marge is married to Homer. ($marriedTo^- \sqsubseteq marriedTo$)
- ✓ If Homer is a parent of Bart, then Bart is a child of Homer. ($parentOf^- \sqsubseteq childOf$)

Modelling patterns

So, what can we say now?

- ✓ A person has a mother.
- ✓ A penguin eats only fish. A horse eats only chocolate.
- ✓ A nuclear family has two parents, at least two children and a dog.
($NuclearFam \sqsubseteq =_2 hasMember.Parent \sqcap \geq_2 hasMember.Child \sqcap \exists hasMember.Dog$)
- ✓ A smoker is not a non-smoker (and vice versa).
- ✓ Everybody loves Mary. ($\top \sqsubseteq \exists loves.\{mary\}$ or $Person \sqsubseteq \exists loves.\{mary\}$)
- ✓ Adam is not Eve (and vice versa). ($adam \neq eve$)
- ✓ Everything is black or white.
- ✓ The brother of my father is my uncle. ($hasFather \circ hasBrother \sqsubseteq hasUncle$)
- ✓ My friend's friends are also my friends. ($hasFriend \circ hasFriend \sqsubseteq hasFriend$)
- ✓ If Homer is married to Marge, then Marge is married to Homer. ($marriedTo^- \sqsubseteq marriedTo$)
- ✓ If Homer is a parent of Bart, then Bart is a child of Homer. ($parentOf^- \sqsubseteq childOf$)

... and more!

DL: Family of languages

`http://www.cs.man.ac.uk/~ezolin/dl/`

Next week

- More modelling with OWL/OWL 2.
- What cannot be expressed in OWL/OWL 2?