INF3580/4580 - Semantic Technologies - Spring 2018 Lecture 4: The SPARQL Query Language

Ernesto Jimenez-Ruiz 6th February 2018





Outline 1 Introduction 2 Recap: RDF 3 SPARQL by Example 4 SPARQL Systematically 5 Executing SPARQL Queries in Jena 6 Wrap-up

Today's Plan

- Introduction
- 2 Recap: RDF
- 3 SPARQL by Example
- 4 SPARQL Systematically
- 5 Executing SPARQL Queries in Jena
- 6 Wrap-up

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Introduction

Introduction

Today's lecturer



Office hours: from 9:00 to 16:00 at OJD 8165

- Lessons
 - February 6th: SPARQL 1.0
 - April 3rd: More OWL
 - April 24th: More SPARQL (SPARQL 1.1 and entailment regimes)
 - May 8th: OBDA: Ontology Based Data Access

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SPARQL

- SPARQL Protocol And RDF Query Language
- Standard language to query graph data represented as RDF triples
- W3C Recommendations
 - SPARQL 1.0: W3C Recommendation 15 January 2008
 - **SPARQL 1.1**: W3C Recommendation 21 March 2013
- This lecture is about SPARQL 1.0.
- Documentation:
 - Syntax and semantics of the SPARQL query language for RDF. http://www.w3.org/TR/rdf-sparql-query/

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Recap: RDF

Recap: RDF triples

- The W3C representation of knowledge in the Semantic Web is RDF (Resource Description Framework)
- RDF talks about *resources* identified by URIs.
- In RDF, all knowledge is represented by triples (aka statements or facts)
- A triple consists of *subject*, *predicate*, and *object*
- The *subject* maybe a resource or a blank node
- The *predicate* must be a resource
- The *object* can be a resource, a blank node, or a literal

Outline

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4 SPARQL Systematically
5 Executing SPARQL Queries in Jena
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Recap: RDF

Recap: RDF Literals

- Can only appear as object in the *object* in the triple.
- Literals can be
 - Plain, without language tag: geo:berlin geo:name "Berlin" .
 - Plain, with language tag:
 geo:germany geo:name "Deutschland"@de .
 geo:germany geo:name "Germany"@en .
 - Typed, with a URI indicating the type: geo:berlin geo:population "3431700"^^xsd:integer .

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```
Recap: RDF Blank Nodes

Blank nodes are like resources without a URI

There is a city in Germany called Berlin

.:x a geo:City .

.:x geo:containedIn geo:germany .

.:x geo:name "Berlin" .

geo:germany

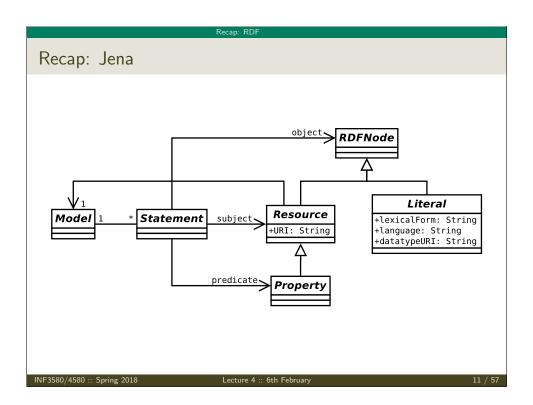
geo:City

Berlin

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```



Recap: Jena

- Jena is a Semantic Web programming framework for Java.
- Open source.
- API to extract data from and write to RDF graphs.
- Includes an engine to query RDF graphs through SPARQL.
- Interfaces for main RDF elements Resource, Property, Literal, Statement, Model
- The RDF graphs are represented as an abstract Model.

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Recap: RE

Recap: Vocabularies

- Best Practices: Reuse vocabularies to ease interoperability.
 - People are more familiar with them
 - Can be queried more easily
 - \bullet The semantics must be clear, shouldn't twist the meaning too much.
- Good starting point:
 - Linked Open Vocabularies: http://lov.okfn.org/
 - Schema.org: https://schema.org

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Recap: RDF

Recap: RDF and RDFS Vocabularies

- Prefix rdf:<http://www.w3.org/1999/02/22-rdf-syntax-ns#>
- Prefix rdfs:<http://www.w3.org/2000/01/rdf-schema#>
- They need to be declared like all others.
- Examples:

```
geo:berlin rdf:type geo:City .
geo:containedIn a rdf:Property .
geo:berlin rdfs:label geo:City .
```

• Note that the keyword "a" is an alternative for rdf:type.

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Recap: RDF

Recap: Dublin Core

- Metadata for documents, see http://dublincore.org/.
- Prefix dc:<http://purl.org/dc/terms/>
- Important elements:

```
creator a document's main author
created the creation date
title title of document
description a natural language description
```

• Examples:

```
Recap: R
```

Recap: Friend Of A Friend

- People, personal information, friends, see http://www.foaf-project.org/
- Prefix foaf:<http://xmlns.com/foaf/0.1/>
- Important elements:

```
Person a person, alive, dead, real, imaginary name name of a person (also firstName, familyName) mbox mailbox URL of a person knows a person knows another
```

• Examples:

```
<https://w3id.org/scholarlydata/person/ernesto-jimenez-ruiz>
    a foaf:Person ;
    foaf:name "Ernesto Jiménez-Ruiz" ;
    foaf:mbox <mailto:ernestoj@ifi.uio.no> ;
    foaf:knows <http://heim.ifi.uio.no/martingi/foaf#me> .
```

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SPARQL by Example

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```
SPARQL by Example
```

SPARQL by Example

- SPARQL Protocol And RDF Query Language
- Try it out:

```
https://www.w3.org/wiki/SparqlEndpoints
DBLP http://dblp.13s.de/d2r/snorql/
DBpedia http://dbpedia.org/sparql
Lenka http://data.lenka.no/sparql
EBI https://www.ebi.ac.uk/rdf/
```

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SPARQL by Example

Simple Examples (cont.)

```
Publications by people called "Ernesto Jimenez-Ruiz"
```

Answer:

?pub

<http://dblp.13s.de/d2r/resource/publications/journals/ijdsn/MartiSMJ12>
<http://dblp.13s.de/d2r/resource/publications/journals/biomedsem/Jimenez-RuizGHL11>
<http://dblp.13s.de/d2r/resource/publications/journals/dke/Jimenez-RuizGHL11>

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SPARQL by Examp

Simple Examples

- DBLP contains computer science publications: http://dblp.uni-trier.de/
- Vocabulary of RDF (con)version: dc:creator, dc:title, foaf:name, etc.
- Web service: http://dblp.13s.de/d2r/snorql/
- Endpoint: http://dblp.13s.de/d2r/sparql

Answer:

```
?ejr
```

<http://dblp.13s.de/d2r/resource/authors/Ernesto_Jimenez-Ruiz>

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SPARQL by Example

Simple Examples (cont.)

```
Titles of publications by people called "Ernesto Jimenez-Ruiz"
```

```
SELECT ?title WHERE {
    ?ejr foaf:name "Ernesto Jimenez-Ruiz" .
    ?pub dc:creator ?ejr .
    ?pub dc:title ?title .
}
```

Answer:

?title

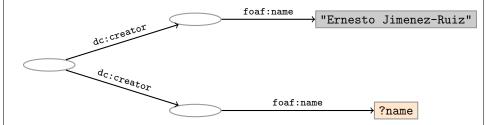
"Localization of Mobile Sensors and Actuators for Intervention in Low-Visibility Conditions"^^xsd:string
"Logic-based assessment of the compatibility of UMLS ontology sources."^^xsd:string
"Supporting concurrent ontology development: Framework, algorithms and tool."^^xsd:string

. . .

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Graph with blank nodes

Variables not SELECTed can equivalently be blank:



Pattern matching: assign values to variables and blank nodes to make this a sub-graph of the RDF graph!

Graph Patterns

The previous SPARQL query as a graph:

?ejr foaf:name "Ernesto Jimenez-Ruiz"
?pub dc:creator ?other foaf:name ?name

Pattern matching: assign values to variables to make this a sub-graph of the RDF graph!

SPARQL Systematically

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- **(5)** Executing SPARQL Queries in Jena
- 6 Wrap-up

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SPARQL Systematically

Types of Queries

```
SELECT Compute table of bindings for variables

SELECT ?a ?b WHERE {

        [ dc:creator ?a ;

            dc:creator ?b ]
     }

CONSTRUCT Use bindings to construct a new RDF graph

CONSTRUCT {
        ?a foaf:knows ?b .
     } WHERE {
        [ dc:creator ?a ;
            dc:creator ?b ]
     }
```

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SPARQL Systematicall

Components of an SPARQL query

Prologue: prefix definitions Results form specification: (1) variable list, (2) type of query (SELECT, ASK, CONSTRUCT, DESCRIBE), (3) remove duplicates (DISTINCT, REDUCED) Dataset specification Query pattern: graph pattern to be matched Solution modifiers: ORDER BY, LIMIT, OFFSET

SPARQL Systematically

Types of Queries (cont.)

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SPARQL Systematically

Solution Sequences and Modifiers

- Permitted to SELECT queries only
- SELECT treats solutions as a sequence (solution sequence)
- Query patterns generate an unordered collection of solutions
- Sequence modifiers can modify the solution sequence (not the solution itself):
 - Order
 - Projection
 - Distinct
 - Reduced
 - Offset
 - Limit
- Applied in this order.

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SPARQL Systematically

Projection, DISTINCT, REDUCED

- Projection means that only some variables are part of the solution
 - Done with SELECT ?x ?y WHERE {?x ?y ?z...}
- DISTINCT eliminates (all) duplicate solutions:
 - \bullet Done with SELECT DISTINCT ?x ?y WHERE {?x ?y ?z...}
 - A solution is a duplicate if it assigns the same RDF terms to all variables as another solution.
- REDUCED allows to remove some or all duplicate solutions
 - Done with SELECT REDUCED ?x ?y WHERE {?x ?y ?z...}
 - Motivation: Can be expensive to find and remove all duplicates
 - Leaves amount of removal to implementation (e.g. consecutive occurrences)
 - Rarely used...

SPARQL Systematical

ORDER BY

- Used to sort the solution sequence in a given way:
- SELECT ... WHERE ... ORDER BY ...
- ASC for ascending order (default) and DESC for descending order
- E.g.

```
SELECT ?city ?pop WHERE {
    ?city geo:containedIn ?country ;
        geo:population ?pop .
} ORDER BY ?country ?city DESC(?pop)
```

- Standard defines sorting conventions for literals, URIs, etc.
- Not all "sorting" variables are required to appear in the solution

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OFFSET and LIMIT

- LIMIT: limits the number of results
- OFFSET: position/index of the first returned result
- Useful for paging through a large set of solutions
- ...but not useful for implementing paging in applications.
- Can compute solutions number 51 to 60
- Done with SELECT ... WHERE {...} ORDER BY ... LIMIT 10 OFFSET 50
- LIMIT and OFFSET can be used separately
- OFFSET not meaningful without ORDER BY.

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Query patterns

- Different types of *graph patterns* for the query pattern (WHERE clause):
 - Basic Graph Patterns (BGP)
 - Group Graph Patterns
 - Filters or Constraints (FILTER)
 - Optional Graph Patterns (OPTIONAL)
 - Union Graph Patterns (UNION, Matching Alternatives)
 - Graph Graph Patterns (RDF Datasets)

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SPARQL Systematically

Group Graph Patterns

- Group several patterns with { and }.
- A group containing *one* basic graph pattern:

```
{
   _:pub dc:creator ?ejr .
   _:pub dc:creator ?other .
}
```

• Two groups with one basic grapg pattern each:

```
{
    { _:pub1 dc:creator ?ejr . }
    { _:pub2 dc:creator ?other . }
}
```

- Note: Same name for two different blank nodes not allowed!
- The scope of a FILTER constraint is the group where the filter appears.

SPARQL Systematica

Basic Graph Patterns (BGP)

- A Basic Graph Pattern is a set of triple patterns.
- e.g.

```
?ejr foaf:name "Ernesto Jimenez-Ruiz" .
_:pub dc:creator ?ejr .
_:pub dc:creator ?other .
```

- Scope of blank node labels is the BGP
- Basically: A match is a function that maps
 - every variable and every blank node in the pattern
 - to a resource, a blank node, or a literal in the RDF graph (an "RDF term")

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Filters

- Groups may include constraints or filters
- Reduces matches of surrounding group where filter applies

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SPARQL Systematically

Filters: Functions and Operators

- Usual binary operators: ||, &&, =, !=, <, >, <=, >=, +, -, *, /.
- Usual unary operators: !, +, -.
- Unary tests: bound(?var), isURI(?var), isBlank(?var), isLiteral(?var).
- Accessors: str(?var), lang(?var), datatype(?var)
- regex is used to match a variable with a regular expression. *Always* use with str(?var). E.g.: regex(str(?name), "Os").

Read the spec for details!

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SPARQL Systematically

Optional Patterns: Negation as Failure

- Testing if a graph pattern is not expressed...
- ... by specifying an OPTIONAL graph pattern that introduces a variable.
- and testing if the variable is not bound.
- Called **Negation as Failure** in logic programming

SPARQL Systematical

Optional Patterns

- Allows a match to leave some variables unbound (e.g. no data was available)
- A partial function from variables to RDF terms
- Groups may include optional parts

- ?x and ?date bound in every match, ?abs bound if there is a Norwegian abstract
- Groups can contain several optional parts, evaluated separately

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Matching Alternatives (UNION)

- A UNION pattern matches if any of some alternatives matches

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Graph Graph Patterns (RDF datasets)

- SPARQL queries are executed against an RDF dataset
- An RDF dataset comprises
 - One **default graph** (unnamed) graph.
 - Zero or more named graphs identified by an URI
- FROM and FROM NAMED keywords allows to select an RDF dataset by reference
 - The **default graph** will consist of the RDF merge of the graphs referred to in the FROM clauses,
 - FROM NAMED clauses will define the different named graphs.
 - Note that, if there is no FROM clause, but there are FROM NAMED clauses, the default graph will be empty.
- Keyword GRAPH makes the named graphs the active graph for pattern matching
 - A specific (named) graph can be used as active graph if its IRI is provided.

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SPARQL Systematically

Named graph example 1

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Default graph example

```
Add three RDF datasets to default graph

SELECT ?kname ?fname

FROM <a href="http://data.lenka.no/dumps/fylke-geonames.ttl">http://data.lenka.no/dumps/kommune-navn.ttl</a>

FROM <a href="http://.../dumps/kommunesentre-geonames.ttl">http://.../dumps/kommunesentre-geonames.ttl</a>

WHERE {

    ?fylke a gd:Fylke;
        gn:officialName ?fname;
        gn:childrenFeatures ?kommune.

    ?kommune a gd:Kommune;
        gn:officialName ?kname;

FILTER (langMatches(lang(?fname), 'no'))

FILTER (langMatches(lang(?kname), 'no'))
}
```

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Named graph example 2

```
Take coordinates from one source only
  FROM <a href="http://data.lenka.no/dumps/kommune-navn.ttl">http://data.lenka.no/dumps/kommune-navn.ttl</a>
   FROM <a href="http://data.lenka.no/dumps/kommunesentre-geonames.ttl">http://data.lenka.no/dumps/kommunesentre-geonames.ttl</a>
   FROM NAMED <a href="http://data.lenka.no/dumps/kommunesentre-geonames.ttl">http://data.lenka.no/dumps/kommunesentre-geonames.ttl</a>
   FROM NAMED <a href="http://sws.geonames.org/6453350/about.rdf">http://sws.geonames.org/6453350/about.rdf</a>
   WHERE {
        ?feature gn:officialName "Lillehammer"@no .
     } UNION {
        ?feature gn:name "Lillehammer" .
     OPTIONAL {
        GRAPH <http://data.lenka.no/dumps/kommunesentre-geonames.ttl> {
          ?feature pos:lat ?lat ;
                       pos:long ?long ;
                       owl:sameAs ?other
     OPTIONAL {
        ?feature gn:population ?pop .
```

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Executing SPARQL Queries in Jena

Outline

Introduction

2 Recap: RDF

3 SPARQL by Example

4 SPARQL Systematically

String qStr =

5 Executing SPARQL Queries in Jena

6 Wrap-up

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Executing SPARQL Queries in Jena

Constructing a Query and a QueryExecution

• Query objects are usually constructed by parsing:

```
"PREFIX foaf: <" + foafNS + ">"
+ "SELECT ?a ?b WHERE {"
+ " ?a foaf:knows ?b ."
+ "} ORDER BY ?a ?b";
```

Query q = QueryFactory.create(qStr);

- \bullet A Query can be used several times, on multiple models
- For each execution, a new QueryExecution is needed
- To produce a QueryExecution for a given Query and Model:
 QueryExecution qe =

```
QueryExecutionFactory.create(q, model);
```

Executing SPARQL Queries in Jen

SPARQL in Jena

• SPARQL functionality bundled with Jena has separate Javadocs:

http://jena.apache.org/documentation/javadoc/arq/

- Main classes in package org.apache.jena.query
 - Query a SPARQL query
 - QueryFactory for creating queries in various ways
 - QueryExecution for the execution state of a query
 - QueryExecutionFactory for creating query executions (to get QueryExecution instances)
 - DatasetFactory for creating dataset instances
 - For SELECT queries:
 - QuerySolution, a single solution to the query.
 - ResultSet, all the QuerySolutions (an iterator)
 - ResultSetFormatter, turn a ResultSet into various forms: text, RDF graph (Model, in Jena terminology) or plain XML
 - CONSTRUCT and DESCRIBE return Models, ASK a Java boolean.

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Executing SPARQL Queries in Jena

Executing a Query

- QueryExecution contains methods to execute different kinds of queries (SELECT, CONSTRUCT, etc.)
- E.g. for a SELECT query:

 ResultSet res = qe.execSelect();
- E.g. for a CONSTRUCT query:
 Model construct_model = qe.execConstruct();
- ResultSet is a sub-interface of Iterator<QuerySolution>
- QuerySolution has methods to get list of variables, value of single variables, etc.
- Important to call close() on query executions when no longer needed.

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Example: SPARQL in Jena

```
String qStr = "SELECT ?a ?b ...";
Query q = QueryFactory.create(qStr);

QueryExecution qe =
    QueryExecutionFactory.create(q, model);

try {
    ResultSet res = qe.execSelect();
    while( res.hasNext()) {
        QuerySolution soln = res.next();
        RDFNode a = soln.get("?a");
        RDFNode b = soln.get("?b");
        System.out.println(""+a+" knows "+b);
    }
} finally {
    qe.close();
}
```

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Executing SPARQL Queries in Jena

Querying a Model, Dataset or Endpoint (cont.)

- Jena can also send SPARQL queries to a remote endpoint!
 - \bullet Use sparqlService in QueryExecutionFactory

```
E.g.
String endpoint = "http://dblp.13s.de/d2r/sparql";
String qStr = "SELECT ?a ?b ...";
Query q = QueryFactory.create(qStr);

QueryExecution qe =
    QueryExecutionFactory.sparqlService(endpoint,q);

try {
    ResultSet res = qe.execSelect();
    ...
} finally {
    qe.close();
}
```

Querying a Model, Dataset or Endpoint

• Querying a model:

```
Model model = ModelFactory.createDefaultModel();
model.read("http://heim.ifi.uio.no/martingi/foaf");
QueryExecutionFactory.create(q, model);
```

• Querying a Dataset:

```
Querying a Dataset:
    String dftGraphURI =
"http://heim.ifi.uio.no/martingi/foaf";
    List namedGraphURIs = new ArrayList();

namedGraphURIs.add("http://richard.cyganiak.de/foaf.rdf");
    namedGraphURIs.add("http://danbri.org/foaf.rdf");
    Dataset dataset = DatasetFactory.create(dftGraphURI,
namedGraphURIs);
    QueryExecutionFactory.create(q, dataset);
```

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Executing SPARQL Queries in Jena

SPARQL on the 'Net

- Many sites (DBLP, dbpedia, dbtunes,...) publish SPARQL endpoints
- I.e. SPARQL queries can be submitted to a database server that sends back the results
- Uses HTTP to submit URL-encoded queries to server GET /sparq1/?query=... HTTP/1.1
- Actually defined via W3C Web Services, see

http://www.w3.org/TR/rdf-sparql-protocol/

• Try it out:

```
https://www.w3.org/wiki/SparqlEndpoints
DBLP http://dblp.13s.de/d2r/snorql/
DBpedia http://dbpedia.org/sparql
Lenka http://data.lenka.no/sparql
EBI https://www.ebi.ac.uk/rdf/
```

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6 Wrap-up

Wrap-u

More to come: SPARQL 1.1

SPARQL 1.1 became W3C Recommendations 21 March 2013.

- Updates (add/delete triples)
- Service Descriptions
- Basic Federated query
- Subqueries.
- Property paths (to shorten common queries)
- Aggregate functions (count, sum, average,...)
- Negation, set difference, i.e. something is *not* in a graph
- Entailment regimes

Wrap-

Wrap-up

- SPARQL is a W3C-standardised query language for RDF graphs
- It is built about "graph patterns"
- Comes with a protocol to communicate with "endpoints"
- Can be conveniently used with Jena and tens of other systems.

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Wrap-up

Additional material

An Introduction to SPARQL by Olaf Hartig: http: //www.slideshare.net/olafhartig/an-introduction-to-sparql

SPARQL Query Language for RDF (SPARQL 1.0 W3C Recommendation): https://www.w3.org/TR/rdf-sparql-query/

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