INF3580/4580 – Semantic Technologies – Spring 2018

Lecture 8: RDF and RDFS semantics

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Oblig 5

- Published today
- First delivery due 21 March
- Final delivery 2 weeks after feedback
- Extra question for INF4580 students
- "Real" semantics of RDF and RDFS
- Foundations book: Section 3.2
- Still OK to ignore some complications, see oblig text
- We provide an excerpt of Sect. 3.2 with unimportant parts removed.
- Go to group sessions!

Today's Plan

1. Why we need semantics
2. Model-theoretic semantics from a birds-eye perspective
3. Repetition: Propositional Logic
4. Simplified RDF semantics

Outline

Semantics—why do we need it?

A formal semantics for RDFS became necessary because

1. the previous informal specification
2. left plenty of room for interpretation of conclusions, whence
3. triple stores sometimes answered queries differently, thereby
4. obstructing interoperability and interchangeability.
5. The information content of data once more came to depend on applications

But RDF was supposed to be the **data liberation movement**

Another look at the Semantic Web cake

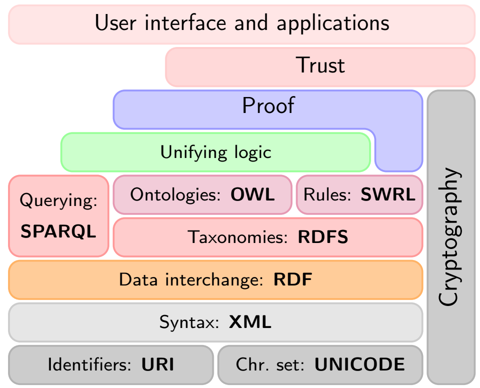


Figure: Semantic Web Stack

Absolute precisision required

RDF is to serve as the foundation of the entire Semantic Web tower.

- It must therefore be sufficiently clear to sustain advanced reasoning, e.g.:
  - type propagation/inheritance,
    - "Tweety is a penguin and a penguin is a bird, so..."
  - domain and range restrictions,
    - "Martin has a birthdate, and only people have birthdates, so..."
  - existential restrictions.
    - "all persons have parents, and Martin is a person, so..."

  ...to which we shall return in later lectures

To ensure that infinitely many conclusions will be agreed upon,

- RDF must be furnished with a model-theory
- that specifies how the different node types should be interpreted
- and in particular what entailment should be taken to mean.

Example: What is the meaning of blank nodes?

Co-authors of Paul Erdős:

```
SELECT DISTINCT ?name WHERE {
    _:pub dc:creator [foaf:name "Paul Erdős"] , [foaf:name ?name] .
}
```

SPARQL must

- match the query to graph patterns
- which involves assigning values to variables and blank nodes

But,

- which values are to count?
- the problem becomes more acute under reasoning.
- Should a value for `foaf:familyname` match a query for `foaf:name`?
- Are blanks in SPARQL the same as blanks in RDF?

Outline

Formal semantics

- The study of how to model the meaning of a logical calculus.
- A logical calculus consists of:
  - A finite set of symbols,
  - a grammar, which specifies the formulae,
  - a set of axioms and inference rules from which we construct proofs.
- A logical calculus can be defined apart from any interpretation.
- A calculus that has not been furnished with a formal semantics,
  - is a 'blind' machine, a mere symbol manipulator,
  - the only criterion of correctness is provability.

Derivations

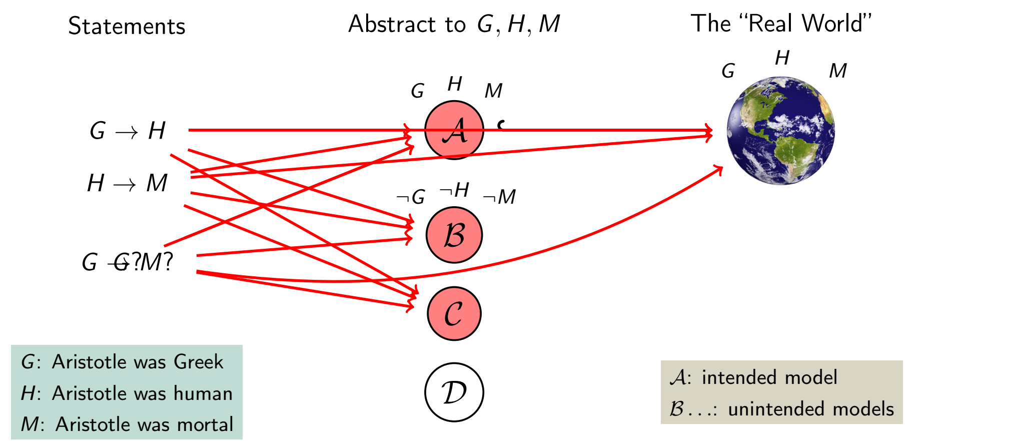
A proof typically looks something like this:

$$\dfrac{\dfrac{\dfrac{P \vdash Q, P \qquad Q, P \vdash Q}{P \to Q, P \vdash Q} \qquad \dfrac{R \vdash Q, P \qquad Q, R \vdash Q}{P \to Q, R \vdash Q}}{P \to Q, P \lor R \vdash Q}}{P \to Q \vdash (P \lor R) \to Q}$$

Where each line represents an application of an inference rule.

- How do we know that the inference rules are well-chosen?
- Which manipulations derive conclusions that hold in the real world?

Finding out stuff about the World



Model-theoretic semantics

Basic idea: Asserting a sentence makes a claim about the world:

- A formula therefore limits the set of worlds that are possible.
- We can therefore encode meaning/logical content
  - by describing models of these worlds.
  - thus making *certain aspects* of meaning mathematically tractable
- The exact makeup of models varies from logic to logic, but they all
  - express a view on what kinds of things there are,
  - and the basic relations between these things
- By selecting a class of models one selects the basic features of the world
  - as one chooses to see it.
- Whatever these models all share can be said to be entailed by those features.

Outline

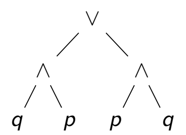
Propositional Logic: Formulas

- Formulas are defined "by induction" or "recursively":

1 Any letter p, q, r, . . . is a formula
2 *if* A and B are formulas, *then*
  - $(A \wedge B)$ is also a formula (read: "A and B")
  - $(A \vee B)$ is also a formula (read: "A or B")
  - $\neg A$ is also a formula (read: "not A")

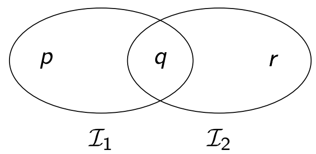
- Nothing else is. Only what rules [1] and [2] say is a formula.
- Examples of formulae: $p \quad (p \wedge \neg r) \quad (q \wedge \neg q) \quad ((p \vee \neg q) \wedge \neg p)$
- Formulas are just a kind of strings until now:
  - no meaning
  - but every formula can be "parsed" uniquely.

$((q \wedge p) \vee (p \wedge q))$



Interpretations

- Logic is about truth and falsity
- Truth of compound formulas depends on truth of letters.
- Idea: put all letters that are "true" into a set!
- Define: An *interpretation* $\mathcal{I}$ is a set of letters.
- Letter p is true in interpretation $\mathcal{I}$ if $p \in \mathcal{I}$.
- E.g., in $\mathcal{I}_1 = \{p, q\}$, p is true, but r is false.



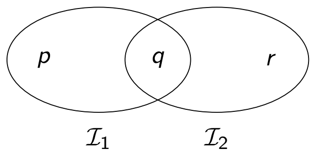
- But in $\mathcal{I}_2 = \{q, r\}$, p is false, but r is true.

Semantic Validity $\models$

- To say that p is true in $\mathcal{I}$, write

$$\mathcal{I} \models p$$

- For instance



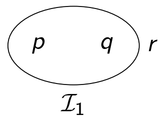
$$\mathcal{I}_1 \models p \qquad \mathcal{I}_2 \not\models p$$

- In other words, for all letters p:

$$\mathcal{I} \models p \quad \text{if and only if} \quad p \in \mathcal{I}$$

Validity of Compound Formulas

- Is $((q \land r) \lor (p \land q))$ true in $\mathcal{I}$?
- Idea: apply our rule recursively
- For any formulas A and B,...
- ...and any interpretation $\mathcal{I}$,...
  - ...$\mathcal{I} \models A \land B$ if and only if $\mathcal{I} \models A$ and $\mathcal{I} \models B$
  - ...$\mathcal{I} \models A \lor B$ if and only if $\mathcal{I} \models A$ or $\mathcal{I} \models B$ (or both)
  - ...$\mathcal{I} \models \neg A$ if and only if $\mathcal{I} \not\models A$.
- For instance



$$\mathcal{I}_1 \models ((q \land r) \lor (p \land q))$$

$$\mathcal{I}_1 \not\models (q \land r) \qquad \mathcal{I}_1 \models (p \land q)$$

$$\mathcal{I}_1 \models q \quad \mathcal{I}_1 \not\models r \quad \mathcal{I}_1 \models p \quad \mathcal{I}_1 \models q$$

Truth Table

- Semantics of $\neg$, $\land$, $\lor$ often given as *truth table*:

A	B	$\neg A$	$A \land B$	$A \lor B$
f	f	t	f	f
f	t	t	f	t
t	f	f	f	t
t	t	f	t	t

Tautologies

- A formula A that is true in *all* interpretations is called a *tautology*
- also *logically valid*
- also a *theorem* (of propositional logic)
- written:

$$\models A$$

- $(p \lor \neg p)$ is a tautology
- True whatever p means:
  - The sky is blue or the sky is not blue.
  - P.N. will win the 50km in 2016 or P.N. will not win the 50km in 2016.
  - The slithy toves gyre or the slithy toves do not gyre.
- Possible to derive true statements mechanically...
- ...without understanding their meaning!
- ...e.g. using truth tables for small cases.

Entailment

- Tautologies are true in all interpretations
- Some formulas are true only under certain assumptions
- *A entails B*, written $A \models B$ if
  $\mathcal{I} \models B$
  for all interpretations $\mathcal{I}$ with $\mathcal{I} \models A$
- Also: "B is a logical consequence of A"
- Whenever A holds, also B holds
- For instance:
  $$p \wedge q \models p$$
- Independent of meaning of p and q:
  - If it rains and the sky is blue, then it rains
  - If P.N. wins the race and the world ends, then P.N. wins the race
  - If 'tis brillig and the slythy toves do gyre, then 'tis brillig
- Also entailment can be checked mechanically, without knowing the meaning of words.

Question

Given the letters

P – Ola answers none of the questions correctly

Q – Ola fails the exam

Which of the following are tautologies of propositional logic?

1. Q
2. $\neg Q$
3. $P \rightarrow Q$
4. $Q \rightarrow (P \rightarrow Q)$

Outline

Taking the structure of triples into account

Unlike propositions, triples have parts, namely:

- subject
- predicates, and
- objects

Less abstractly, these may be:

- URI references
- literal values, and
- blank nodes

Triples are true or false on the basis of what each part refers to.

On what there is: Resources, Properties, Literals

The RDF data model consists of three object types; resources, properties and literals values:

Resources: All things described by RDF are called resources. Resources are identified by URIs

Properties: A property is a specific aspect, characteristic, attribute or relation used to describe a resource. Properties are also resources, and therefore identified by URIs.

Literals: A literal value is a concrete data item, such as an integer or a string. String literals name themselves, i.e.

- "Julius Ceasar" names the string "Julius Ceasar"
- "42" names the string "42"

The semantics of typed and language tagged literals is considerably more complex.

Restricting RDF/RDFS

- We will simplify things by only looking at certain kinds of RDF graphs.
- No triples "about" properties, classes, etc., except RDFS
- Assume Resources are divided into four disjoint kinds:
  - *Properties* like `foaf:knows`, `dc:title`
  - *Classes* like `foaf:Person`
  - *Built-ins*, a fixed set including `rdf:type`, `rdfs:domain`, etc.
  - *Individuals* (all the rest, "usual" resources)
- All triples have one of the forms:

```
individual property individual .
individual rdf:type class .

class rdfs:subClassOf class .
property rdfs:subPropertyOf property .
property rdfs:domain class .
property rdfs:range class .
```

- Forget blank nodes and literals for a while!

Short Forms

- Resources and Triples are no longer all alike
- No need to use the same general triple notation
- Use alternative notation

Triples	Abbreviation
`indi prop indi .`	$r(i_1, i_2)$
`indi rdf:type class .`	$C(i_1)$
`class rdfs:subClassOf class .`	$C \sqsubseteq D$
`prop rdfs:subPropOf prop .`	$r \sqsubseteq s$
`prop rdfs:domain class .`	$\mathrm{dom}(r, C)$
`prop rdfs:range class .`	$\mathrm{rg}(r, C)$

- This is called "Description Logic" (DL) Syntax
- Used much in particular for OWL

Example

- Triples:

```
ws:romeo ws:loves ws:juliet .
ws:juliet rdf:type ws:Lady .
ws:Lady rdfs:subClassOf foaf:Person .
ws:loves rdfs:subPropertyOf foaf:knows .
ws:loves rdfs:domain ws:Lover .
ws:loves rdfs:range ws:Beloved .
```

- DL syntax, without namespaces:

$loves(romeo, juliet)$
$Lady(juliet)$

$Lady \sqsubseteq Person$
$loves \sqsubseteq knows$
$\mathrm{dom}(loves, Lover)$
$\mathrm{rg}(loves, Beloved)$

Interpretations for RDF

- To interpret propositional formulas, we need to know how to interpret
  - Letters
- To interpret the six kinds of triples, we need to know how to interpret
  - *Individual URIs* as real or imagined objects
  - *Class URIs* as sets of such objects
  - *Property URIs* as relations between these objects
- A *DL-interpretation* $\mathcal{I}$ consists of
  - A set $\Delta^{\mathcal{I}}$, called the *domain* (sorry!) of $\mathcal{I}$
  - For each individual URI i, an element $i^{\mathcal{I}} \in \Delta^{\mathcal{I}}$
  - For each class URI C, a subset $C^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}}$
  - For each property URI r, a relation $r^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$
- Given these, it will be possible to say whether a triple holds or not.

An example "intended" interpretation

- $\Delta^{\mathcal{I}_1} = \{$  $\}$
- $romeo^{\mathcal{I}_1} =$  $juliet^{\mathcal{I}_1} =$ 
- $Lady^{\mathcal{I}_1} = \{$  $\}$ $Person^{\mathcal{I}_1} = \Delta^{\mathcal{I}_1}$

  $Lover^{\mathcal{I}_1} = Beloved^{\mathcal{I}_1} = \{$  $\}$
- $loves^{\mathcal{I}_1} = \{$  $\}$

  $knows^{\mathcal{I}_1} = \Delta^{\mathcal{I}_1} \times \Delta^{\mathcal{I}_1}$

An example "non-intended" interpretation

- $\Delta^{\mathcal{I}_2} = \mathbb{N} = \{1, 2, 3, 4, \ldots\}$
- $romeo^{\mathcal{I}_2} = 17$

  $juliet^{\mathcal{I}_2} = 32$
- $Lady^{\mathcal{I}_2} = \{2^n \mid n \in \mathbb{N}\} = \{2, 4, 8, 16, 32, \ldots\}$

  $Person^{\mathcal{I}_2} = \{2n \mid n \in \mathbb{N}\} = \{2, 4, 6, 8, 10, \ldots\}$

  $Lover^{\mathcal{I}_2} = Beloved^{\mathcal{I}_2} = \mathbb{N}$
- $loves^{\mathcal{I}_2} = <= \{\langle x, y\rangle \mid x < y\}$

  $knows^{\mathcal{I}_2} = \leq = \{\langle x, y\rangle \mid x \leq y\}$
- Just because names (URIs) look familiar, they don't need to denote what we think!
- In fact, there is *no way* of ensuring they denote only what we think!

Validity in Interpretations (RDF)

- Given an interpretation $\mathcal{I}$, define $\models$ as follows:
- $\mathcal{I} \models r(i_1, i_2)$ iff $\langle i_1^{\mathcal{I}}, i_2^{\mathcal{I}}\rangle \in r^{\mathcal{I}}$
- $\mathcal{I} \models C(i)$ iff $i^{\mathcal{I}} \in C^{\mathcal{I}}$
- Examples:
  - $\mathcal{I}_1 \models loves(juliet, romeo)$ because

     $\in loves^{\mathcal{I}_1} = \{$  $\}$
  - $\mathcal{I}_1 \models Person(romeo)$ because

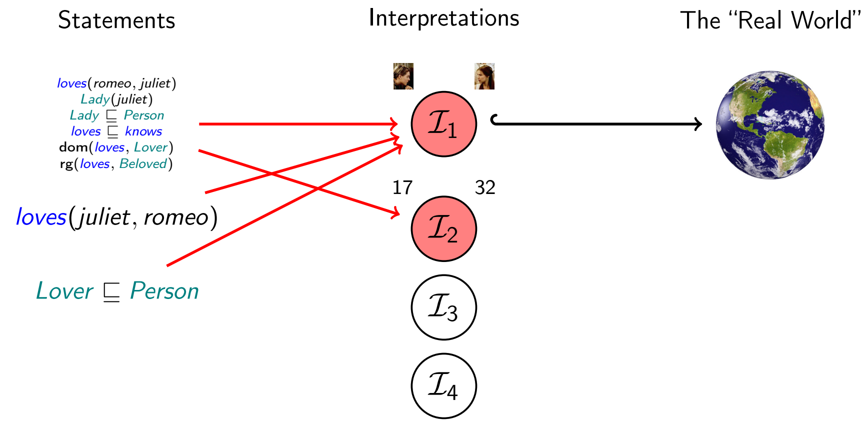
    $romeo^{\mathcal{I}_1} =$  $\in Person^{\mathcal{I}_1} = \Delta^{\mathcal{I}_1}$
  - $\mathcal{I}_2 \not\models loves(juliet, romeo)$ because

    $loves^{\mathcal{I}_2} = <$ and $juliet^{\mathcal{I}_2} = 32 \not< romeo^{\mathcal{I}_2} = 17$
  - $\mathcal{I}_2 \not\models Person(romeo)$ because
  - $romeo^{\mathcal{I}_2} = 17 \notin Person^{\mathcal{I}_2} = \{2, 4, 6, 8, 10, \ldots\}$

Validity in Interpretations, cont. (RDFS)

- Given an interpretation $\mathcal{I}$, define $\models$ as follows:
- $\mathcal{I} \models C \sqsubseteq D$ iff $C^{\mathcal{I}} \subseteq D^{\mathcal{I}}$
- $\mathcal{I} \models r \sqsubseteq s$ iff $r^{\mathcal{I}} \subseteq s^{\mathcal{I}}$
- $\mathcal{I} \models \mathrm{dom}(r, C)$ iff for all $\langle x, y\rangle \in r^{\mathcal{I}}$, we have $x \in C^{\mathcal{I}}$
- $\mathcal{I} \models \mathrm{rg}(r, C)$ iff for all $\langle x, y\rangle \in r^{\mathcal{I}}$, we have $y \in C^{\mathcal{I}}$
- Examples:
  - $\mathcal{I}_1 \models Lover \sqsubseteq Person$ because
    $Lover^{\mathcal{I}_1} =$  $\subseteq Person^{\mathcal{I}_1} =$ 
  - $\mathcal{I}_2 \not\models Lover \sqsubseteq Person$ because
    $Lover^{\mathcal{I}_2} = \mathbb{N}$ and $Person^{\mathcal{I}_2} = \{2, 4, 6, 8, 10, \ldots\}$

Finding out stuff about Romeo and Juliet



Example: Range/Domain semantics

$$\mathcal{I}_2 \models \mathrm{dom}(knows, Beloved)$$

because. . .

$$knows^{\mathcal{I}_2} = \leq = \{\langle x, y\rangle \mid x \leq y\}$$
$$Beloved^{\mathcal{I}_2} = \mathbb{N}$$

and for any x and y with

$$\langle x, y\rangle \in knows^{\mathcal{I}_2}, \quad \text{i.e.} \quad x \leq y,$$

we also have

$$x \in \mathbb{N} \quad \text{i.e.} \quad x \in Beloved^{\mathcal{I}_2}$$

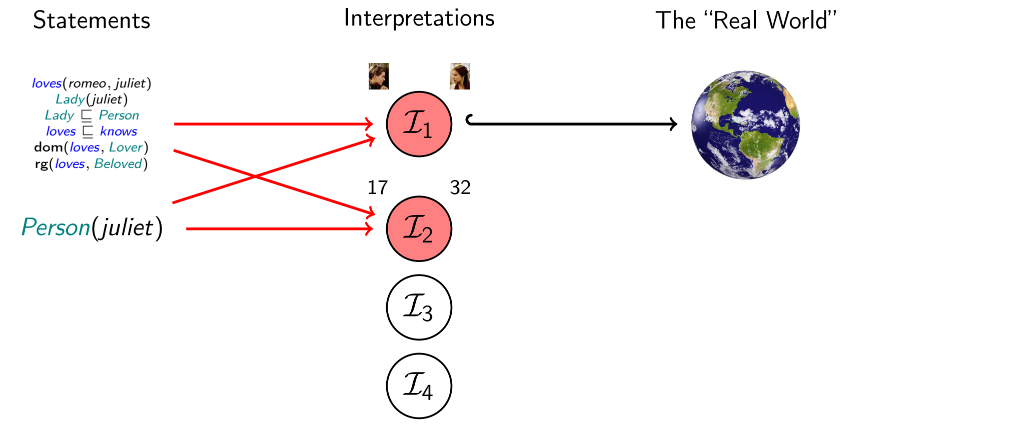
Interpretation of Sets of Triples

- Given an interpretation $\mathcal{I}$
- And a set of triples $\mathcal{A}$ (any of the six kinds)
- $\mathcal{A}$ is valid in $\mathcal{I}$, written
  $$\mathcal{I} \models \mathcal{A}$$
- iff $\mathcal{I} \models A$ for all $A \in \mathcal{A}$.
- Then $\mathcal{I}$ is also called a model of $\mathcal{A}$.
- Examples:
  $$\mathcal{A} = \{loves(romeo, juliet),\ Lady(juliet),\ Lady \sqsubseteq Person,\ loves \sqsubseteq knows,\ \mathrm{dom}(loves, Lover),\ \mathrm{rg}(loves, Beloved)\}$$
- Then $\mathcal{I}_1 \models \mathcal{A}$ and $\mathcal{I}_2 \models \mathcal{A}$

Entailment

- Given a set of triples $\mathcal{A}$ (any of the six kinds)
- And a further triple T (also any kind)
- T is entailed by $\mathcal{A}$, written $\mathcal{A} \models T$
- iff
  - For any interpretation $\mathcal{I}$ with $\mathcal{I} \models \mathcal{A}$
  - $\mathcal{I} \models T$.
- $\mathcal{A} \models \mathcal{B}$ iff $\mathcal{I} \models \mathcal{B}$ for all $\mathcal{I}$ with $\mathcal{I} \models \mathcal{A}$
- Example:
- $\mathcal{A} = \{\ldots, \mathit{Lady}(\mathit{juliet}),\ \mathit{Lady} \sqsubseteq \mathit{Person}, \ldots\}$ as before
- $\mathcal{A} \models \mathit{Person}(\mathit{juliet})$ because...
- in *any* interpretation $\mathcal{I}$ with $\mathcal{I} \models \mathcal{A}$...
- $\mathit{juliet}^{\mathcal{I}} \in \mathit{Lady}^{\mathcal{I}}$ and $\mathit{Lady}^{\mathcal{I}} \subseteq \mathit{Person}^{\mathcal{I}}, \ldots$
- so by set theory $\mathit{juliet}^{\mathcal{I}} \in \mathit{Person}^{\mathcal{I}}$...
- and therefore $\mathcal{I} \models \mathit{Person}(\mathit{juliet})$

Finding out stuff about Romeo and Juliet



Countermodels

- If $\mathcal{A} \not\models T, \ldots$
- then there is an $\mathcal{I}$ with
  - $\mathcal{I} \models \mathcal{A}$
  - $\mathcal{I} \not\models T$
- Vice-versa: if $\mathcal{I} \models \mathcal{A}$ and $\mathcal{I} \not\models T$, then $\mathcal{A} \not\models T$
- Such an $\mathcal{I}$ is called a *counter-model* (for the assumption that $\mathcal{A}$ entails T)
- To show that $\mathcal{A} \models T$ does *not* hold:
  - Describe an interpretation $\mathcal{I}$ (using your fantasy)
  - Prove that $\mathcal{I} \models \mathcal{A}$ (using the semantics)
  - Prove that $\mathcal{I} \not\models T$ (using the semantics)

Countermodel Example

- $\mathcal{A}$ as before:

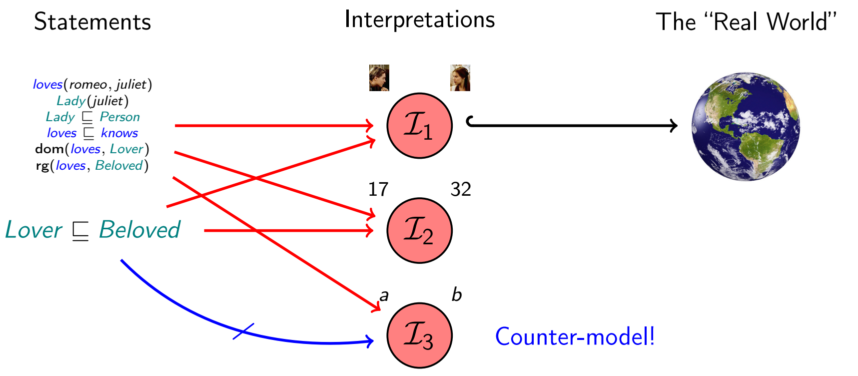
$$\mathcal{A} = \{\mathit{loves}(\mathit{romeo}, \mathit{juliet}),\ \mathit{Lady}(\mathit{juliet}),\ \mathit{Lady} \sqsubseteq \mathit{Person},\ \mathit{loves} \sqsubseteq \mathit{knows},\ \mathrm{dom}(\mathit{loves}, \mathit{Lover}),\ \mathrm{rg}(\mathit{loves}, \mathit{Beloved})\}$$

- Does $\mathcal{A} \models \mathit{Lover} \sqsubseteq \mathit{Beloved}$?
- Holds in $\mathcal{I}_1$ and $\mathcal{I}_2$.
- Try to find an interpretaion with $\Delta^{\mathcal{I}} = \{a, b\}$, $a \neq b$.
- Interpret $\mathit{romeo}^{\mathcal{I}} = a$ and $\mathit{juliet}^{\mathcal{I}} = b$
- Then $\langle a, b\rangle \in \mathit{loves}^{\mathcal{I}}$, $a \in \mathit{Lover}^{\mathcal{I}}$, $b \in \mathit{Beloved}^{\mathcal{I}}$.
- With $\mathit{Lover}^{\mathcal{I}} = \{a\}$ and $\mathit{Beloved}^{\mathcal{I}} = \{b\}$, $\mathcal{I} \not\models \mathit{Lover} \sqsubseteq \mathit{Beloved}$!
- Choose

$$\mathit{loves}^{\mathcal{I}} = \mathit{knows}^{\mathcal{I}} = \{\langle a, b\rangle\} \qquad \mathit{Lady}^{\mathcal{I}} = \mathit{Person}^{\mathcal{I}} = \{b\}$$

to complete the counter-model while satisfying $\mathcal{I} \models \mathcal{A}$

Countermodels about Romeo and Juliet



Take aways

1. Model-theoretic semantics yields an unambigous notion of entailment,
2. which is necessary in order to liberate data from applications.
3. Shown today: A simplified semantics for parts of RDF
   1. Only RDF/RDFS vocabulary to talk "about" predicates and classes
   2. Literals and blank nodes next time

Supplementary reading on RDF and RDFS semantics:

- `http://www.w3.org/TR/rdf-mt/`
- Section 3.2 in Foundations of SW Technologies