

# UNIVERSITY OF OSLO

## Faculty of Mathematics and Natural Sciences

Examination in: INF4140 — Models of Concurrency

Day of examination: 17. December 2012

Examination hours: 14.30–18.30

This problem set consists of 0 pages.

Appendices: Inference Rules for program verification

Permitted aids: None

Please make sure that your copy of the problem set is complete before you attempt to answer anything.

Some general advice and remarks:

- This problem set consists of two independent problems and one optional extra problem which gives you extra points.
- The points from problems one and two sum up to a total of 100 points. The number of points stated on each part indicates the weight of that part.
- Problem three is optional and can give you extra points on top of your final score.
- Use your time wisely and take into consideration the weight of each question.
- You should read the whole problem set before you start solving the problems.
- You can make your own clarifications if you find the examination text ambiguous or imprecise. Such clarifications must be written clearly in the delivered answer.
- Make short and clear explanations!

Good Luck and Merry Christmas!

*(Continued on page 2.)*

## Problem 1 Shared variables: Santa's Factory (weight 50)

### The Snow-globe Production:

We here consider the following description of the snow-globe production as a synchronization problem:

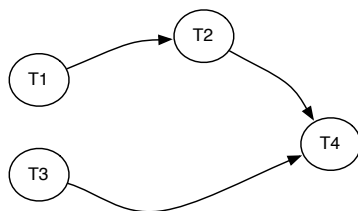
In Santa's Factory the elves are going to start the production of snow-globes. They divide the production in different tasks:

Some elves are in charge of collecting the different materials and organizing them in different groups (each group contains glass, fake snow and ceramic).



Some other elves are in charge of assembling the snow-globes and for that they take a group of materials and hand-make a snow-globe. Other elves are in charge of hand-making boxes for the different snow-globes. Finally some elves are in charge of wrapping the snow-globes in the boxes.

The assembling of a snow-globe has the following precedence graph:



Where:

T1: collect a group of materials

T2: hand-make a snow-globe

T3: hand-make a box

T4: wrap a snow-globe

Figure 1: Precedence graph

Note that many snow-globes may be assembled concurrently.

### 1a Semaphore Solution (weight 18)

Implement the synchronization part of the snow-globe production by extending the sketch below. Fill in code for the dots where needed. Use semaphores for synchronization. Remember to declare and initialize the semaphores.

```

process MaterialCollector[i=1 to N]{
  while (true){
    ...
    ‘‘collect a group of materials (glass, fake snow and ceramic)’’
    ...
  }
}

```

(Continued on page 3.)

```
process GiftAssembler[i=1 to N]{
  while (true){
    ...
    ‘‘hand-make a snow-globe’’
    ...
  }
}

process BoxMaker[i=1 to N]{
  while (true){
    ...
    ‘‘hand-make a box’’
    ...
  }
}

process GiftWrapper[i=1 to N]{
  while (true){
    ...
    ‘‘wrap a snow-globe’’
    ...
  }
}
```

### 1b Safety (weight 3)

Explain briefly why your implementation (from exercise 1a) is safe, i.e., why a snow-globe is only wrapped in a box after both the box and the snow-globe have been made, and why a `GiftAssembler` will only start making a snow-globe when there is a group of materials that he can use.

### 1c Binary semaphores (weight 3)

Does your solution (from exercise 1a) use binary semaphores? Explain briefly.

(Continued on page 4.)

## Gift Storage:

In Santa's factory there are some elves in charge of organizing the gifts for transporting into the storage room. There are  $N$  `GiftOrganizer` elves and one `Transporter` elf. They share a common sledge. Each `GiftOrganizer` elf repeatedly gathers one gift and puts it into the sledge, the sledge can hold  $G$  gifts and it is initially empty.



When the sledge is full the `Transporter` elf moves the sledge with the gifts into the storage room (which means that the `GiftOrganizer` elves have to take a break until the sledge is back), downloads the gifts in one empty bag, closes the bag, and returns with an empty sledge.

### 1d Monitor Solution (weight 20)

Given the following implementation of the `GiftOrganizers` and `Transporter` elves as processes:

```
process GiftOrganizer[i=1 to N] {
  while (true) call Gift_Storage.put();
}

process Transporter{
  while (true) call Gift_Storage.transport();
}
```

Extend the sketch below of the monitor. Fill in code for the dots where needed. Use the Signal and Continue discipline and assume there is an infinite supply of gifts.

```
monitor Gift_Storage {
  int g = G; # capacity of the sledge
  int counter = 0; # number of gifts in the sledge
  ...
  procedure put() {
    ...
    'Put gift into the sledge'
    ...
  }

  procedure transport() {
    ...
    'move sledge into the storage room, download gifts
    and return'
    ...
  }
}
```

(Continued on page 5.)

```
monitor Gift_Storage {
  int g = G; # capacity of the sledge
  int counter = 0; # number of gifts in the sledge
  ...
  procedure put() {
    ...
    'Put gift into the sledge'
    ...
  }

  procedure transport() {
    ...
    'move sledge into the storage room, download gifts and return'
    ...
  }
}
```

### 1e Java (weight 3)

Can your monitor solution from exercise 1d easily translate into a monitor in Java using the built-in statements `wait`, `notify` and `notifyAll`? Explain briefly. (The Java implementation code is not needed)

**Hint:** How many condition variables are you using in your solution from exercise 1d?

### 1f Signaling Disciplines (weight 3)

What is the difference between the Signal and Continue discipline and the Signal and Wait discipline? Does your monitor implementation from exercise 1d work correctly with the Signal and Wait discipline? Explain briefly.

## Problem 2 Asynchronous Communication: Santa's Factory (weight 50)

We here consider asynchronous message passing using the language with **send** and **await** statements, and the following variation of the snow-globe production from Problem 1.

In this case, we have a total of four agents in the system:

- One `MaterialCollector` agent,
- One `GiftAssembler` agent,
- One `BoxMaker` agent, and
- One `GiftWrapper` agent.

The agents follow the precedence graph from Figure 1 in page 2, which means: The `MaterialCollector` notifies the `GiftAssembler` agent every time it finishes to collect a group of materials, the `GiftAssembler` agent notifies the `GiftWrapper` agent every time it finishes to hand-make a snow-globe, and the `BoxMaker` agent also notifies the `GiftWrapper` agent every time it finishes to hand-make a box.

Consider the following implementation of the `GiftAssembler` agents:

```
X : Agent; // assumed initialized to the MaterialCollector
Y : Agent; // assumed initialized to the GiftWrapper
```

```
while true do
  await X:materialIsCollected;
  // 'hand-make a snow-globe'
  send Y:giftIsAssembled;
od
```

You may assume that no communication occurs during the snow-globe production.

### 2a Loop invariant (weight 5)

Consider a `GiftAssembler` agent  $A$  implemented as above.

The function *isBeingAssembled* is defined over the local history of  $A$  to calculate the number of snow-globes which are in production but not complete.

$$\begin{aligned} \textit{isBeingAssembled}(\varepsilon) &= 0 \\ \textit{isBeingAssembled}(h; X \downarrow A : \textit{materialIsCollected}) &= \textit{isBeingAssembled}(h) + 1 \\ \textit{isBeingAssembled}(h; A \uparrow Y : \textit{giftIsAssembled}) &= \textit{isBeingAssembled}(h) - 1 \end{aligned}$$

Formulate a loop invariant of  $A$  using the *isBeingAssembled* function.

(Continued on page 7.)

**2b Program Analysis** (weight 15)

Use Hoare Logic to verify your loop invariant from exercise 2a (In the Appendix you can find a list of rules for program verification), and explain briefly why this is a suitable loop invariant.

**2c History Invariant** (weight 10)

Using the *isBeingAssembled* function formulate an invariant for *A* over its local history *h*, which always holds, and show formally or informally that this invariant holds after each interaction point in the implementation.

**2d Implementation** (weight 15)

Provide an implementation of the `GiftWrapper`. This agent should repeatedly try to wrap the snow-globes, but it must wait for the arrival of one snow-globe and one box before wrapping it. The implementation should allow `GiftWrapper` to receive a snow-globe and a box in a random order. Extend the program sketch below. Fill in code for the dots where needed.

```
while true do
  ...
  // ‘‘wrap a snow-globe’’
  ...
od
```

**2e Local Histories** (weight 5)

Give two examples of possible local histories of the `GiftWrapper` agent.

### Problem 3 Extra points (optional question): Program Verification (weight 10 )

#### IMPORTANT NOTE:

This question is optional, you can solve this question if you wish to get extra points added on top of your final score.

#### The Factorial function:

In mathematics, the factorial of a non-negative integer  $n$ , denoted by  $n!$ , is the product of all positive integers less than or equal to  $n$ . For example,

$$5! == 5 * 4 * 3 * 2 * 1 == 120.$$

Let  $n$  be a positive integer,  $\text{fac}(n)$  calculates the factorial of  $n$  and is implemented as follows:

```
x = n;  y = 1;  z = 0;

while (z != x) {
  z = z + 1;  y = y * z;
}
```

Use program logic (In the Appendix you can find a list of rules for program verification) to prove the following triple:

$$\{\text{True}\} \text{ fac}(n) \{y = x!\}$$

Use  $y = z!$  as loop invariant.

Additionally, you may assume the following properties for the factorial:

$$0! == 1$$

$$(n + 1)! == (n)! * (n+1)$$

(Continued on page 9.)



## Appendix: Inference Rules

### Assignment

$$\{P_{x \leftarrow e}\}x = e\{P\}$$

### Composition

$$\frac{\{P\}S_1\{Q\} \quad \{Q\}S_2\{R\}}{\{P\}S_1; S_2\{R\}}$$

### While

$$\frac{\{I \wedge B\}S\{I\}}{\{I\}\text{while } (B) S; \{I \wedge \neg B\}}$$

### Consequence

$$\frac{(P' \Rightarrow P) \quad \{P\}S\{Q\} \quad (Q \Rightarrow Q')}{\{P'\}S\{Q'\}}$$

### Non-deterministic choice ( $\square$ )

$$\frac{\{P_1\}S_1\{Q\} \quad \{P_2\}S_2\{Q\}}{\{P_1 \wedge P_2\}(S_1 \square S_2)\{Q\}}$$

### Send

$$\{Q_{h \leftarrow h; A \uparrow B : m}\} \text{send } B : m \{Q\}$$

### Receive

$$\{Q_{h \leftarrow h; B \downarrow A : m}\} \text{await } B : m \{Q\}$$