# UNIVERSITY OF OSLO

# Faculty of Mathematics and Natural Sciences

Examination in:	INF9145 — Models of Concurrency
Day of examination:	17. December 2012
Examination hours:	14.30-18.30
This problem set consists of 0 pages.	
Appendices:	Inference Rules for program verification
Permitted aids:	None

Please make sure that your copy of the problem set is complete before you attempt to answer anything.

Some general advice and remarks:

- This problem set consists of three independent problems and one optional extra problem which gives you extra points.
- The points from problems one, two and three sum up to a total of 100 points. The number of points stated on each part indicates the weight of that part.
- Problem four is optional and can give you extra points on top of your final score.
- Use your time wisely and take into consideration the weight of each question.
- You should read the whole problem set before you start solving the problems.
- You can make your own clarifications if you find the examination text ambiguous or imprecise. Such clarifications must be written clearly in the delivered answer.
- Make short and clear explanations!

Good Luck and Merry Christmas!

# Problem 1 Shared variables: Santa's Factory (weight 40)

### The Snow-globe Production:

We here consider the following description of the snow-globe production as a synchronization problem:

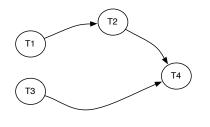
In Santa's Factory the elves are going to start the production of snow-globes. They divide the production in different tasks:

Some elves are in charge of collecting the different materials and organizing them in different groups (each group contains glass, fake snow and ceramic).



Some other elves are in charge of assembling the snow-globes and for that they take a group of materials and hand-make a snow-globe. Other elves are in charge of hand-making boxes for the different snow-globes. Finally some elves are in charge of wrapping the snow-globes in the boxes.

The assembling of a snow-globe has the following precedence graph:



Where: T1: collect a group of materials T2: hand-make a snow-globe T3: hand-make a box T4: wrap a snow-globe

Figure 1: Precedence graph

Note that many snow-globes may be assembled concurrently.

# **1a** Semaphore Solution (weight 13)

Implement the synchronization part of the snow-globe production by extending the sketch below. Fill in code for the dots where needed. Use semaphores for synchronization. Remember to declare and initialize the semaphores.

```
process MaterialCollector[i=1 to N]{
    while (true){
        ...
        ''collect a group of materials (glass, fake snow and ceramic)''
        ...
    }
}
(Continued on page 3.)
```

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```
process GiftAssembler[i=1 to N]{
  while (true){
    . . .
    ''hand-make a snow-globe''
    . . .
  }
}
process BoxMaker[i=1 to N]{
  while (true){
     . . .
    ''hand-make a box''
    . . .
  }
}
process GiftWrapper[i=1 to N]{
  while (true){
     . . .
    ''wrap a snow-globe''
  }
}
```

### 1b Safety (weight 3)

Explain briefly why your implementation (from exercise 1a) is safe, i.e., why a snow-globe is only wrapped in a box after both the box and the snow-globe have been made, and why a GiftAssembler will only start making a snow-globe when there is a group of materials that he can use.

# 1c Binary semaphores (weight 3)

Does your solution (from exercise 1a) use binary semaphores? Explain briefly.

### Gift Storage:

In Santa's factory there are some elves in charge of organizing the gifts for transporting into the storage room. There are N GiftOrganizer elves and one Transporter elf. They share a common sledge. Each GiftOrganizer elf repeatedly gathers one gift and puts it into the sledge, the sledge can hold G gifts and it is initially empty.



When the sledge is full the Transporter elf moves the sledge with the gifts into the storage room (which means that the GiftOrganizer elves have to take a break until the sledge is back), downloads the gifts in one empty bag, closes the bag, and returns with an empty sledge.

# 1d Monitor Solution (weight 15)

Given the following implementation of the GiftOrganizers and Transporter elves as processes:

```
process GiftOrganizer[i=1 to N] {
  while (true) call Gift_Storage.put();
}
process Transporter{
  while (true) call Gift_Storage.transport();
}
```

Extend the sketch below of the monitor. Fill in code for the dots where needed. Use the Signal and Continue discipline and assume there is an infinite supply of gifts.

code/giftstorage-skeleton.code

```
monitor Gift_Storage {
    int g = G; # capacity of the sledge
    int counter = 0; # number of gifts in the sledge
    ...
    procedure put() {
        ...
        ''Put gift into the sledge''
        ...
    }
    procedure transport() {
        ...
        ''move sledge into the storage room, download gifts and return''
    }
}
```

```
(Continued on page 5.)
```

```
...
}
}
```

#### 1e Java (weight 3)

Can your monitor solution from exercise 1d easily translate into a monitor in Java using the built-in statements wait, notify and notifyAll? Explain briefly. (The Java implementation code is not needed)

**Hint:** How many condition variables are you using in your solution from exercise 1d?

# 1f Signaling Disciplines (weight 3)

What is the difference between the Signal and Continue discipline and the Signal and Wait discipline? Does your monitor implementation from exercise 1d work correctly with the Signal and Wait discipline? Explain briefly.

# Problem 2 Asynchronous Communication: Santa's Factory (weight 40)

We here consider asynchronous message passing using the language with **send** and **await** statements, and the following variation of the snow-globe production from Problem 1.

In this case, we have a total of four agents in the system:

- One MaterialCollector agent,
- One GiftAssembler agent,
- One BoxMaker agent, and
- One GiftWrapper agent.

The agents follow the precedence graph from Figure 1 in page 2, which means: The MaterialCollector notifies the GiftAssembler agent every time it finishes to collect a group of materials, the GiftAssembler agent notifies the GiftWrapper agent every time it finishes to hand-make a snow-globe, and the BoxMaker agent also notifies the GiftWrapper agent every time it finishes to hand-make a box.

Consider the following implementation of the GiftAssembler agents:

```
X : Agent; // assumed initialized to the MaterialCollector
Y : Agent; // assumed initialized to the GiftWrapper
while true do
  await X:materialIsCollected;
  // ``hand-make a snow-globe''
  send Y:giftIsAssembled;
  od
```

You may assume that no communication occurs during the snow-globe production.

### **2a** Loop invariant (weight 4)

Consider a GiftAssembler agent A implemented as above. The function *isBeingAssembled* is defined over the local history of A to calculate the number of snow-globes which are in production but not complete.

```
\label{eq:sembled} \begin{split} &isBeingAssembled(\varepsilon) = 0 \\ &isBeingAssembled(h; X \downarrow A: materialIsCollected) = isBeingAssembled(h) + 1 \\ &isBeingAssembled(h; A \uparrow Y: giftIsAssembled) = isBeingAssembled(h) - 1 \end{split}
```

Formulate a loop invariant of A using the isBeingAssembled function.

(Continued on page 7.)

# **2b Program Analysis** (weight 13)

Use Hoare Logic to verify your loop invariant from exercise 2a (In the Appendix you can find a list of rules for program verification), and explain briefly why this is a suitable loop invariant.

### **2c** History Invariant (weight 7)

Using the isBeingAssembled function formulate an invariant for A over its local history h, which always holds, and show formally or informally that this invariant holds after each interaction point in the implementation.

### **2d** Implementation (weight 12)

Provide an implementation of the GiftWrapper. This agent should repeatedly try to wrap the snow-globes, but it must wait for the arrival of one snowglobe and one box before wrapping it. The implementation should allow GiftWrapper to receive a snow-globe and a box in a random order. Extend the program sketch below. Fill in code for the dots where needed.

while true do

...
// ''wrap a snow-globe''
...
od

### **2e** Local Histories (weight 4)

Give two examples of possible local histories of the GiftWrapper agent.

# Problem 3 ABS Analysis (weight 20)

Consider the following ABS implementation of a class StorageRoom, providing the services for elves to store and remove gifts:

We here consider the following class invariant I for class StorageRoom:

 $I \triangleq (\text{counter} = total(\mathcal{H})) \land (\text{counter} >= 0)$ 

where  $\mathcal{H}$  is the local history variable of StorageRoom and *total* is a history function (see below).

#### **3a History Function** (weight 5)

Define inductively the history function  $total: Seq[Ev] \rightarrow Int$  which computes the number of current gifts in the storage room. **Hint:** The total function should be defined over the events shown in Figure 2.

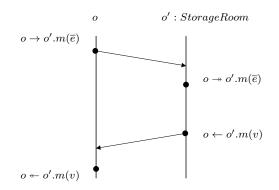


Figure 2: A method call cycle, where object o calls a method m on object o'. The arrows indicate message passing, and the bullets indicates **events**. Remark the events on the left hand side are visible to o, whereas the events on the right hand side are visible to o'.

#### **3b** Initialization (weight 5)

Argue informally that the invariant I is established by the initialization code of the class StorageRoom.

#### **3c** Analysis (weight 10)

Formulate the verification condition for proving that **remove** maintains the invariant I, and verify this condition. (You do not have to verify the **store** method.)

Hint: You may use the following Hoare axiom when reasoning about an **await** statement with boolean guard **b** and **return** statement with expression **e**, postcondition Q, and auxiliary variable return:

 $\{I\}$  await b $\{I \land b\}$  $\{Q_e^{\mathsf{return}}\}$  return e $\{Q\}$ 

**Hint:** In order to establish that some method  $\mathfrak{m}$ , defined by  $\mathfrak{m}(\overline{\mathbf{x}}) \{ \mathsf{Body} \}$ , maintains the invariant *I*, it suffices to verify the Hoare triple:

 $\{I\} \operatorname{Body} \{I^{\mathcal{H}}_{\mathcal{H} \vdash \operatorname{caller} \leftarrow \operatorname{this.m(return)}}\}$ 

# Problem 4 Extra points (optional question): Program Verification (weight 7)

#### **IMPORTANT NOTE:**

This question is optional, you can solve this question if you wish to get extra points added on top of your final score.

#### The Factorial function:

In mathematics, the factorial of a non-negative integer **n**, denoted by **n!**, is the product of all positive integers less than or equal to **n**. For example,

5! = 5 \* 4 \* 3 \* 2 \* 1 = 120.

Let n be a positive integer, fac(n) calculates the factorial of n and is implemented as follows:

x = n; y = 1; z = 0; while (z != x) { z = z + 1; y = y \* z; }

Use program logic (In the Appendix you can find a list of rules for program verification) to prove the following triple:

{True} fac(n) {
$$y = x!$$
}

Use  $\mathbf{y} = \mathbf{z}!$  as loop invariant.

Additionally, you may assume the following properties for the factorial:

$$0! == 1$$
  
(n + 1)! == (n)! \* (n+1)

# Appendix: Inference Rules

Assignment

$$\{P_{x \leftarrow e}\}$$
x = e $\{P\}$ 

Composition

$$\frac{\{P\}S_1\{Q\} \quad \{Q\}S_2\{R\}}{\{P\}S_1; \ S_2\{R\}}$$

While

$$\frac{\{I \land B\} \mathtt{S} \{I\}}{\{I\} \mathtt{while (B) S}; \{I \land \neg B\}}$$

Consequence

$$\frac{(P' \Rightarrow P) \quad \{P\} \mathtt{S}\{Q\} \quad (Q \Rightarrow Q')}{\{P'\} \mathtt{S}\{Q'\}}$$

Non-deterministic choice ([])

$$\frac{\{P_1\}\,\mathbf{S_1}\,\{Q\}}{\{P_1\wedge P_2\}\,(\mathbf{S_1}[]\mathbf{S_2})\,\{Q\}}$$

Send

 $\{Q_{h \leftarrow h; A \uparrow B:m}\}$  send  $B: m\{Q\}$ 

Receive

$$\{Q_{h\leftarrow h;B\downarrow A:m}\}$$
 await B : m  $\{Q\}$ 

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