UNIVERSITY OF OSLO

Faculty of Mathematics and Natural Sciences

Exam: **INF 4300 / INF 9305 – Digital image analysis**
Date: **Monday December 16, 2013**
Exam hours: **14.30-18.30 (4 hours)**
Number of pages: **5 pages**
Enclosures: **None**
Allowed aid: **Calculator**

- Read the entire exercise text before you start solving the exercises. Please check that the exam paper is complete. If you lack information in the exam text or think that some information is missing, you may make your own assumptions, as long as they are not contradictory to the "spirit" of the exercise. In such a case, you should make it clear what assumptions you have made.

- You should spend your time in such a manner that you get to answer all exercises. If you get stuck on one question, move on to the next question.

- Your answers should be **short**, typically a few sentences and / or a sketch should be sufficient.

Good luck!!

Exercise 1: Texture

You are given an image with a periodic texture in a sinusoidal pattern as given below. The image was created as a 1D sinus signal f(x)=100sin(20πx)+100; so the amplitude varies gradually between 0 and 200 (not as abrupt as the image figure might indicate).
For simplicity, in this exercise we will use number of gray levels G=200.
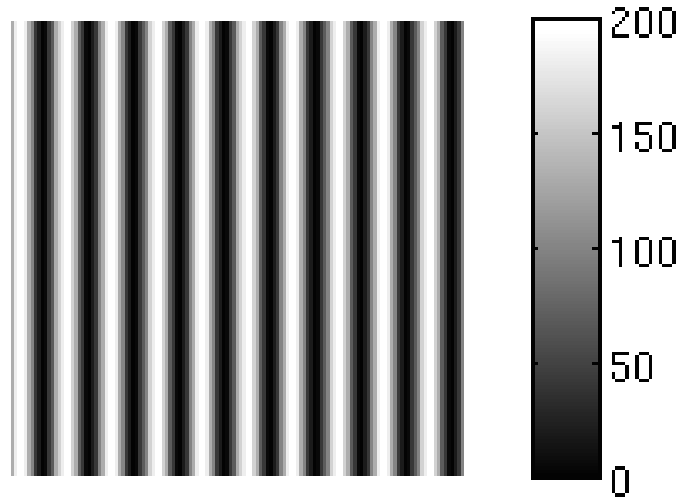
A profile of the gray levels along a horisontal line in the in the image is also given:
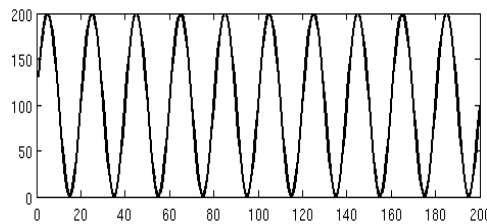
a) If you create a GLCM matrix with an offset Δx=0 and offset Δy=10, what would the shape of the pattern that will appear in the GLCM matrix look like? Please make a simple sketch of the GLCM matrix including the axes of the coordinate system. Will it change with a different Δy offset if Δx=0? Please explain!

b) This image is periodic in the horisontal direction with a period of x=20. What will the GLCM matrix look like with Δx=20 and offset Δy=0? Explain!

c) Sketch the shape of the GLCM matrix with Δx=10 and offset Δy=0, and explain your reasoning.

d) PHD students only:
As Δx goes from 0 to 5, discuss how the shape of the GLCM matrix will change.

Exercise 2: Texture

You are given an isotropic normalized Gray Level Cooccurrence Matrix computed with G=32.
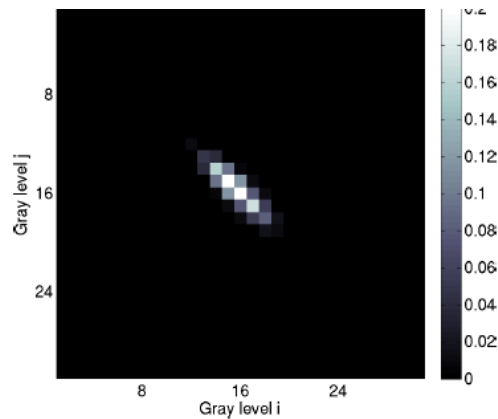
a) What can you say about the range of gray levels that theoriginal image contains?

b) Discuss what you know about the texture in the image, how do you think the original image looks?

c) There are several possible features that may be extracted from the GLCM. Which of the two features below will give a high feature value for the given GLCM? Entropy:

$$E = - \sum_{i=0}^{G-1} \sum_{j=0}^{G-1} P(i,j) \times log(P(i,j))$$

Inverse difference moment:

$$IDM = \sum_{i=0}^{G-1} \sum_{j=0}^{G-1} \frac{1}{1 + (i-j)^2} P(i,j)$$

Please explain your reasoning.

Exercise 3: Discrimination of objects based on chain codes

You are given a set of objects. The absolute chain code for each object is given as:
Object 1: 1 7 4 4
Object 2: 1 7 5 3
Object 3: 0 5 3 0
Object 4: 6 6 4 4 2 2 0 0
Object 5: 2 0 6 4
Object 6: 7 7 5 5 2 2 2 2

a) Draw the objects in a simple sketch. Which shapes do the objects represent?

b) What kind of chain code would you use to best discriminate between the object types? Justify you answer. Can you use chain code to separate the two shapes classes perfectly?

c) Phd students only:
    From the chain code, can you derive a new feature that is also invariant to object size?

Exercise 4: Clustering and classification

You are given the following set of data points:
(15,7), (11,11), (13,11),(8,10),(9,9),(7,7), (7,5),(13,5),(14,4),(9,3), (11,3).
The points are plotted in the scatter plot below.
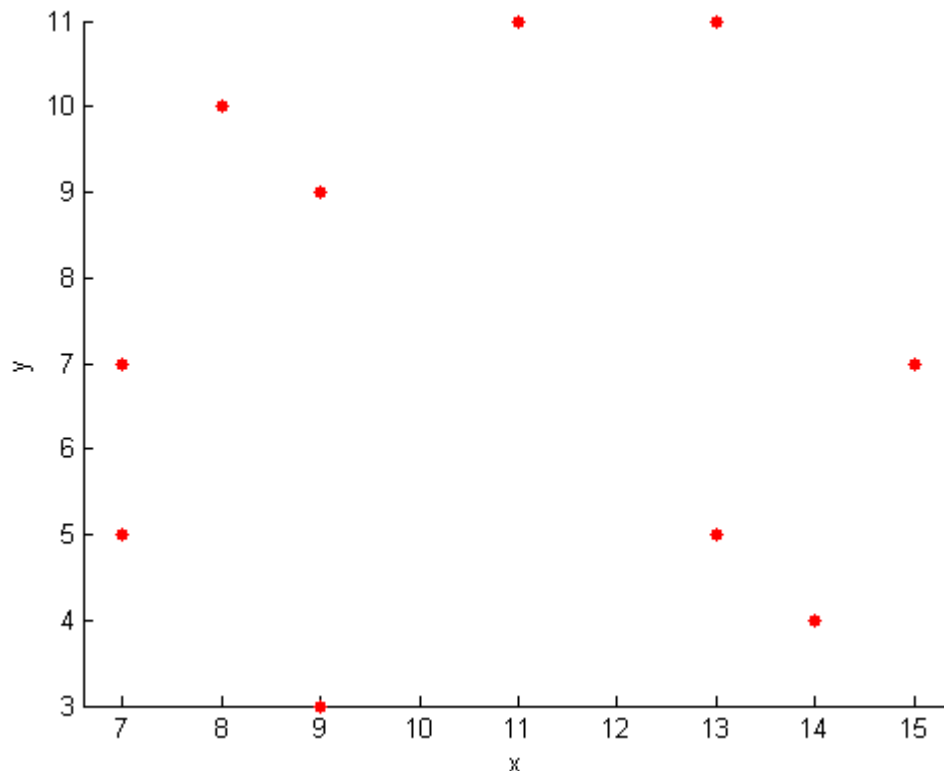
a) Perform a K-means clustering of the points with K=3 and starting with the cluster centers (7,5), (9,9) and (11,3). You can do the clustering either by computation or geometrically. Indicate the new cluster centers on the figure.
    List the clusters that each point will belong to.

    List the cluster centers after each iteration. How many iterations are necessary before no point will change cluster during a new iteration?

b) Assume now that you train a Gaussian classifier with equal diagonal covariance matrices with the end result from point a. Plot the resulting decision boundaries in the figure. Assume that the classes have equal prior probabilities.

c) What is the estimated classification accuracy on the training set if this is the training set for the Gaussian classifier with 3 classes and equal diagonal covariance matrices.

d) Consider now how the resulting classification would be if we removed one of the original cluster centers that you used in a). If you want a classification with only 2 remaining classes, and you want the resulting classes to be well described using a common covariance matrix, which cluster center would you remove?

e) Sketch the shape of the resulting two Gaussian classes with common covariance matrix on the plot in figure 2 in the enclosure.

Exercise 5: Mathematical morphology

a) Explain morphological opening of a binary image

b) Given the 10x10 binary image below

```
0 0 0 0 0 0 0 0 0 0
0 0 0 0 0 0 0 0 0 0
0 0 0 1 1 1 1 0 0 0
0 0 0 0 1 1 0 0 0 0
0 0 0 0 1 1 0 0 0 0
0 0 0 0 1 1 0 0 0 0
0 0 1 1 1 1 1 1 0 0
0 0 1 1 1 1 1 1 0 0
0 0 0 0 0 0 0 0 0 0
0 0 0 0 0 0 0 0 0 0
```

```
0 1 0
1 1 1
0 1 0
```

Show how the necessary steps to arrive at the **top-hat** transform of that image, using the structuring element to the right, having a centered origin.
What does the top-hat transform give you in this case?

Exercise 6: Object features – moments

a) How do we define the moments of inertia of an intensity distribution f(x,y)?

b) In terms of inertial moments, what is the requirement for a 2D object to exhibit a unique orientation?

c) Show the simple relationships between the two moments of inertia μ_{20} and μ_{02} of an image object f(x,y) about axes through its center of mass and the same moments of inertia about the parallel image coordinate axes (x=0 and y=0).

Good Luck!