

Exercise 2.1 regular expressions

a) All strings of lowercase letters that begin and end in a

$a([a-z]^*a)?$

b) All strings of lowercase letters that either begin or end in a (or both)

$a[a-z]^* \mid [a-z]^*a$

c) All strings of digits that contain no leading zeroes

$\text{nonzero} = 1 \mid 2 \mid \dots \mid 9$

$\text{digit} = 0 \mid \text{nonzero}$

$\text{answer} = 0 \mid \text{nonzero digit}^*$

Exercise 2.1 regular expressions

d) All strings of digits that represent even numbers

$\text{even} = 0 \mid 2 \mid 4 \mid 6 \mid 8$
 $\text{answer} = \text{even} \mid [1-9] [0-9]^* \text{even}$

e) All strings of digits such that all the 2's occur before all the 9's

$\text{dignot9} = 0 \mid 1 \mid \dots \mid 8$
 $\text{dignot2} = 0 \mid 1 \mid 3 \mid 4 \mid \dots \mid 9$
 $\text{answer} = \text{dignot9}^+ \text{dignot2}^+$

f) All strings of a's and b's that contain no three consecutive b's

$(a \mid ba \mid bba)^* (e \mid b \mid bb)$

- g) All strings of a's and b's that contain an odd number of a's and an odd number of b's (or both)

$$b^*ab^*(ab^*ab^*)^* \mid a^*ba^*(ba^*ba^*)^*$$

- h) All strings of a's and b's with an even number of a's and an even number of b's

$$(aa \mid bb)^* ((ab \mid ba)(aa \mid bb)^* (ab \mid ba)(aa \mid bb)^*)^*$$

