UNIVERSITETET I OSLO Institutt for Informatikk



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## INF 5110: Compiler construction

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## Handout 2

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## Handout 2: Scanning etc.

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The handout collects definitions in connection with scanning resp. the underlying principles and definitions. They are shown in the slides, as well, but collected in this handout for easier reference.

**Definition 1 (Alpabet**  $\Sigma$ ) Finite set of elements called "letters" or "symbols" or "characters".

**Definition 2 (Words and languages)** Given an alphabet  $\Sigma$ , a *word* over  $\Sigma$  is a finite sequence of letters from  $\Sigma$ . A *language* over alphabet  $\Sigma$  is a *set* of finite *words* over  $\Sigma$ .

Definition 3 (Regular expressions) A regular expression is one of the following

- 1. a *basic* regular expression of the form **a** (with  $a \in \Sigma$ ), or  $\boldsymbol{\epsilon}$ , or  $\boldsymbol{\emptyset}$
- 2. an expression of the form  $r \mid s$ , where r and s are regular expressions.
- 3. an expression of the form rs, where r and s are regular expressions.
- 4. an expression of the form  $r^*$ , where r is a regular expression.

**Definition 4 (Regular expression)** Given an alphabet  $\Sigma$ . The meaning of a regexp r (written  $\mathcal{L}(r)$ ) over  $\Sigma$  is given by equation (1).

**Definition 5 (FSA)** A FSA  $\mathcal{A}$  over an alphabet  $\Sigma$  is a tuple  $(\Sigma, Q, I, F, \delta)$ 

- Q: finite set of states
- $I \subseteq Q, F \subseteq Q$ : initial and final states.
- $\delta \subseteq Q \times \Sigma \times Q$  transition relation

**Definition 6 (DFA)** A deterministic, finite automaton  $\mathcal{A}$  (DFA for short) over an alphabet  $\Sigma$  is a tuple  $(\Sigma, Q, I, F, \delta)$ 

- Q: finite set of states
- $I = \{i\} \subseteq Q, F \subseteq Q$ : initial and final states.
- $\delta: Q \times \Sigma \to Q$  transition function

**Definition 7 (Accepted words and language of an automaton)** A word  $c_1c_2...c_n$  with  $c_i \in \Sigma$  is *accepted* by automaton  $\mathcal{A}$  over  $\Sigma$ , if there exists states  $q_0, q_2, ..., q_n$  from Q such that

 $q_0 \xrightarrow{c_1} q_1 \xrightarrow{c_2} q_2 \xrightarrow{c_3} \dots q_{n-1} \xrightarrow{c_n} q_n$ 

and were  $q_0 \in I$  and  $q_n \in F$ . The *language* of an FSA  $\mathcal{A}$ , written  $\mathcal{L}(\mathcal{A})$ , is the set of all words that  $\mathcal{A}$  accepts.

**Definition 8 (NFA (with**  $\epsilon$  **transitions))** A *non-deterministic* finite-state automaton (NFA for short)  $\mathcal{A}$  over an alphabet  $\Sigma$  is a tuple  $(\Sigma, Q, I, F, \delta)$ , where

- Q: finite set of states
- $I \subseteq Q, F \subseteq Q$ : initial and final states.
- $\delta: Q \times \Sigma \to 2^Q$  transition function

In case, one uses the alphabet  $\Sigma + \{\epsilon\}$ , one speaks about an NFA with  $\epsilon$ -transitions.

**Definition 9 (Acceptance with**  $\epsilon$ **-transitions)** A word w over alphabet  $\Sigma$  is *accepted* by an NFA with  $\epsilon$ -transitions, if there exists a word w' which is accepted by the NFA with alphabet  $\Sigma + \{\epsilon\}$  according to Definition 7 and where w is w' with all occurrences of  $\epsilon$  removed.

**Definition 10 (** $\epsilon$ **-closure,** *a***-successors)** Given a state *q*, the  $\epsilon$ -closure of *q*, written  $close_{\epsilon}(q)$ , is the set of states reachable via zero, one, or more  $\epsilon$ -transitions. We write  $q_a$  for the set of states, reachable from *q* with one *a*-transition. Both definitions are used analogously for sets of states.