

INF5410 Signal processing in space and time

Sverre Holm

DEPARTMENT OF INFORMATICS



INF5410 - What will you learn?

The course gives an introduction to spatial signal processing, with emphasis on the differences compared to time domain signal processing.

The course will also give an understanding of basic terminology in acoustics and electro magnetics required to master theory and realization of imaging systems based on signal processing.

DEPARTMENT OF INFORMATICS



INF5410 builds on

- INF3470 Signal Processing
- STK1100 Probability and statistical modeling
- MAT1120 Linear algebra

DEPARTMENT OF INFORMATICS

3



Estimation Theory

- · Needed for chapter 7
- If you lack a background in it, follow lectures in INF 4480 Signal Processing II
 - Stochastic Processes
 - Estimation Theory

DEPARTMENT OF INFORMATICS



Signal processing in space and time

- Home page: INF5410
 - Wednesday 12.15-14.00:
 - Thursday 13.15-15.00
 - » The two-three first hours will be used for new material
 - » The last hour will be used for problem solving
 - Curriculum
 - Plan
 - Lecturers
- Home page, IFI: <u>INF5410</u>
 - History back to the start in 1993

DEPARTMENT OF INFORMATICS

5



PhD course INF9410

- Extra curriculum: 4-5 papers from our research
- Mandatory exercises: all problems, even voluntary ones, must be answered

DEPARTMENT OF INFORMATICS

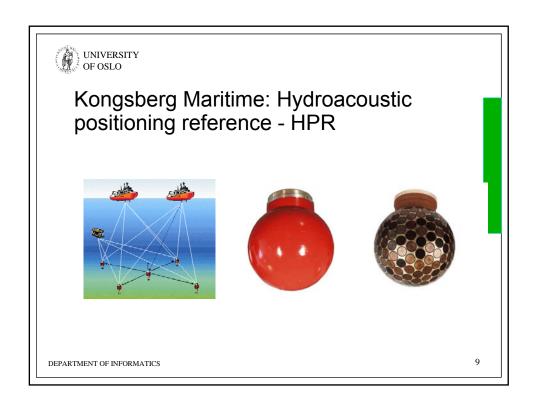


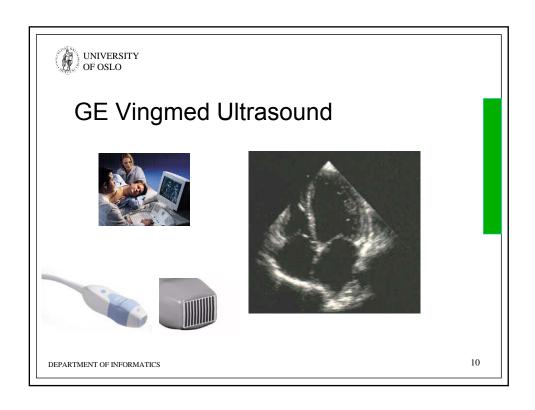
Applications

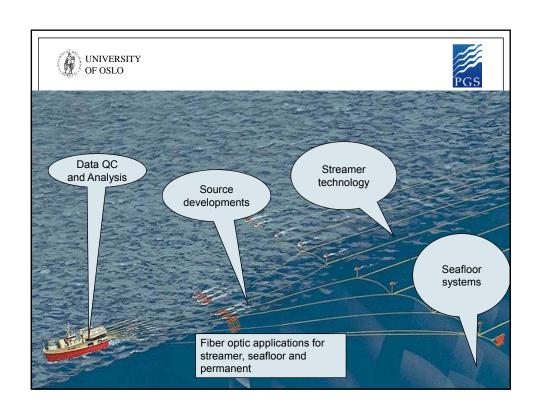
- Underwater Acoustics
- Medical Ultrasound
- Seismics
- Audio
- Radar
- · Radio Astronomy

DEPARTMENT OF INFORMATICS

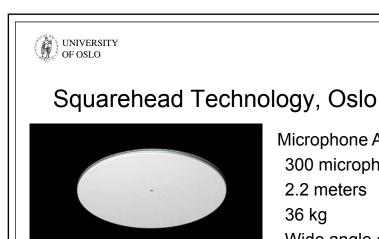












Microphone Array 300 microphones 2.2 meters 36 kg Wide angle camera

DEPARTMENT OF INFORMATICS





Constructive or destructive interference?



- The PA system, assembled for Iron Maiden, represented state-of-the-art technology in the late 70s $\,$
- It consists of folded horn bass, horn loaded midrange and bi-radial horn high frequency elements thrown into a big pile. What it lacked in sonic uniformity it made up for in sound pressure level; which was pretty impressive.

 Nobody apart from a few heavy duty math freaks had heard of interference effect or line (source) arrays at that time.

DEPARTMENT OF INFORMATICS

15

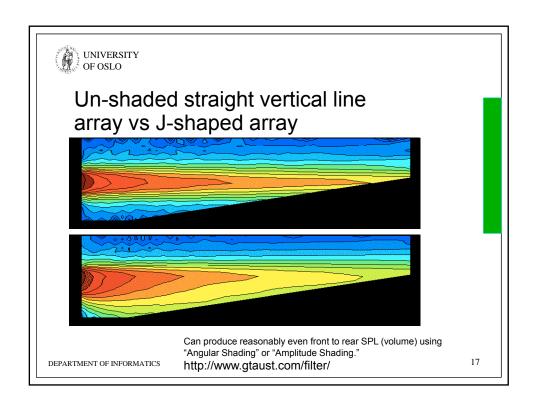


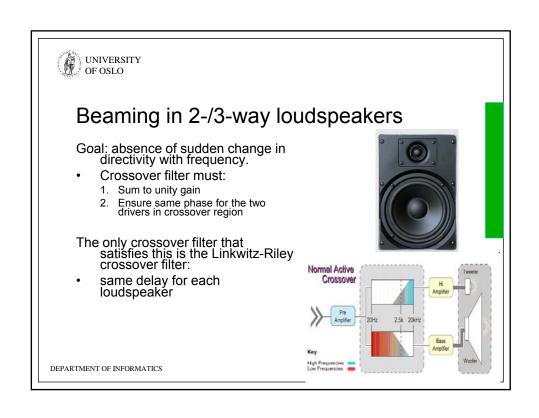
J-arrays: Physically smaller compared to the stack of the 70/80s

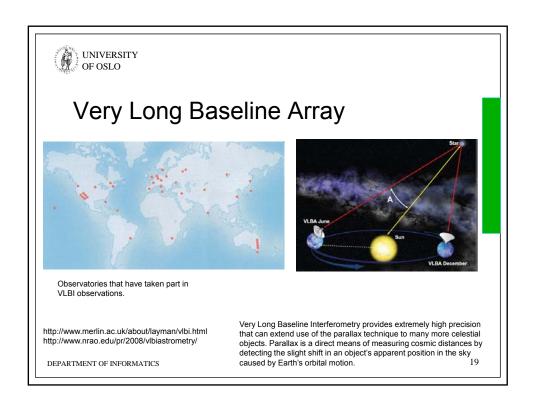


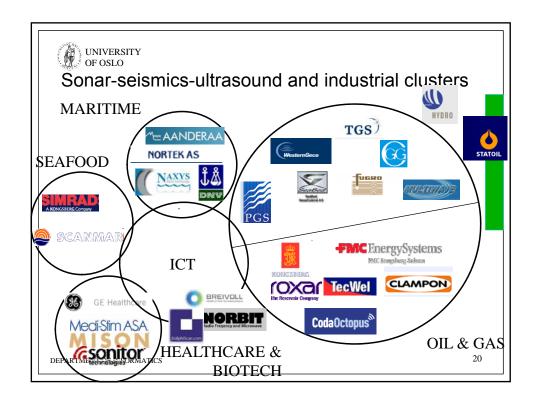


DEPARTMENT OF INFORMATICS











Centre of Imaging

- · Established Jan 2006
- Department of Informatics
 - Digital signal processing and image analysis (DSB)
- · Department of Geosciences

DEPARTMENT OF INFORMATICS

21



Johnson & Dudgeon

- Goal of book: Give a strong foundation for approaching problems in
 - Acoustic signal processing
 - Sonar
 - Radar
- To a lesser extent:
 - Geophysical processing
 - Tomography
 - Computed imaging
 - Ultrasonic imaging
 - Communications

DEPARTMENT OF INFORMATICS



Chapters in Johnson & Dungeon

- Ch. 1: Introduction.
- · Ch. 2: Signals in Space and Time.
 - Physics: Waves and wave equation.
 - » c, λ , f, ω , k vector,...
 - » Ideal and "real" conditions
- · Ch. 3: Apertures and Arrays.
- · Ch. 4: Beamforming.
 - Classical, time and frequency domain algorithms.
- · Ch. 7: Estimation Theory
 - Assumed known: otherwise follow lectures in INF4480 in Stochastic processes and Estimation Theory
- · Ch. 7: Adaptive Array Processing.

DEPARTMENT OF INFORMATICS

23



Ch. 1: Introduction: Array signal processing

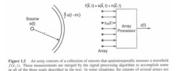
- Goal of signal processing: To extract as much information as possible from our environment.
- Array Signal Processing: Branch of signal processing; focusing on signals conveyed by propagating waves.
- Array: a group of sensors located at distinct spatial locations.

= Gruppeantenne

DEPARTMENT OF INFORMATICS



Goals of array processing



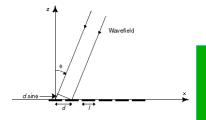
- · Detection: To enhance the signal-tonoise ratio beyond that of a single sensor's output (problem 1.1).
- Signal characterization:
 - Directions to sources or its dual: speed of propagation = Imaging
 - The number of sources
 - Waveforms, temporal and spatial spectra
- Tracking:
 - Track the energy sources as they move in
 - E.g. ships approaching a harbour

DEPARTMENT OF INFORMATICS

25



Array pattern = spatial frequency response



• Frequency response:

$$H(e^{j\omega T}) = \sum_{m=0}^{M-1} h_m e^{-jm\omega T}$$

 Aperture smoothing function ($u=\sin \phi$):

$$H(e^{j\omega T}) = \sum_{m=0}^{M-1} h_m e^{-jm\omega T}$$
 $W(u) = \sum_{m=0}^{M-1} w_m e^{-jm2\pi(u/\lambda)d}$

· Sampling theorem:

$$\omega \cdot T < \pi$$

· To avoid aliasing:

$$2\pi \frac{|u|}{\lambda}d = |k_x| \cdot d \le \pi \Leftrightarrow d \le \frac{\lambda}{2|\sin\phi|}$$

DEPARTMENT OF INFORMATICS



Array pattern for a regular 1-d array and a filter's frequency response

$$\begin{array}{ccc} \omega & \leftrightarrow & k_x = 2\pi \frac{\sin \phi}{\lambda} \\ T & \leftrightarrow & d \\ h_m & \leftrightarrow & w_m \end{array}$$

• The time-frequency sampling theorem T < π / ω_{max} translates into the spatial sampling theorem d < λ_{min} /2.

DEPARTMENT OF INFORMATICS

27



Signal processing

Johnson & Dudgeon, preface:

 We firmly believe that mathematics should be used to support and verify intuition, not substitute for it.

DEPARTMENT OF INFORMATICS



Signal Processing: Where physics and mathematics meet

Simon Haykin, IEEE Signal Processing Magazine, July 2001

Signal processing is at its best when it successfully combines ...

- the unique ability of mathematics to generalize ...
- with both the insight and prior information gained from the underlying physics of the problem at hand; ...
- the combination should lead to reliable algorithms that make a practical difference.

DEPARTMENT OF INFORMATICS

29

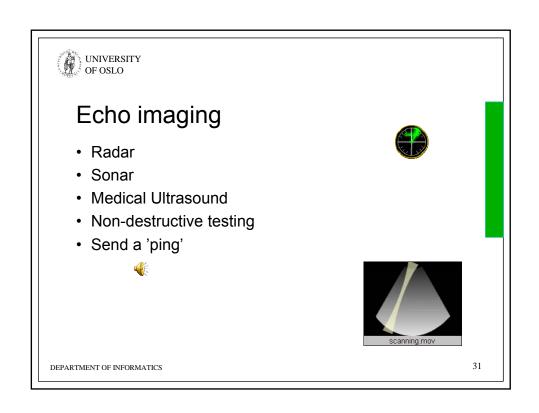


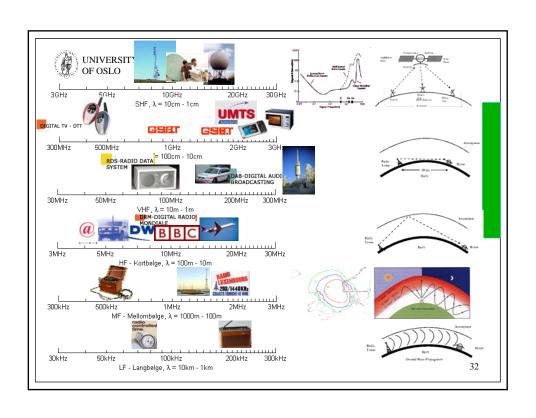
Signal Processing: Where physics and mathematics meet

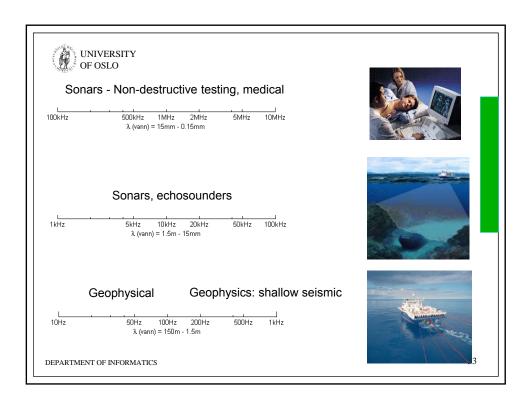
Five ingredients essential for satisfactory performance:

- 1. Prior information
 - Understand the physical laws that govern the generation of the signals
- 2. Regularization
 - Embed prior information into algorithm design so as to stabilize the solution
- 3. Adaptivity
 - Learn from the operational environment so as to account for unknown statistics and nonstationary behavior
- 4. Robustness
 - Unavoidable disturbances are not magnified by the algorithm
- 5. Feedback
 - Powerful engineering principle with many beneficial effects: improved convergence, improved robustness, ...

DEPARTMENT OF INFORMATICS









Narrowband - wideband

- Definition: Narrowband \Leftrightarrow relative bandwidth, B/f₀ < 10% of center frequency
- Most radio-based systems are narrowband
 - c is large, so frequency is high for reasonable λ , c= λ ·f

 - Therefore B is high even if B/f is small
 E.g. remote sensing radar: 19 MHz/5.3 GHz = 0.35%
 Exception: UWB Ultra wide band, B>500 MHz (last ~5 10 years)
- Most acoustic systems are wideband
 - Hearing: 20 20 kHz ⇔ 3 decades
 - Medical ultrasound: 50 100% relative bandwidth centered on 2-10 MHz
 - Sonar is traditionally narrowband, is getting more wideband
- · Consequence: time-delay or phase delay beamformers

DEPARTMENT OF INFORMATICS



Near field - farfield

- Important applications operate in the near field.
 - Medical ultrasound
 - Seismics
 - Synthetic aperture radar and sonar
- Rule-of-thumb: Nearfield is characterized by a resolution which is smaller than the antenna

DEPARTMENT OF INFORMATICS

35



Approximations (1) – must know!

McLaurin series:

- $\sin\theta = \theta 1/3! \theta^3 + 1/5! \theta^5 ...$
- $\cos \theta = 1 1/2! \theta^2 + 1/4! \theta^4 ...$
- $\tan \theta = \theta + 1/3 \theta^3 + 2/15 \theta^5 + ...$

Small angle approximation – extensively used in mathematical physics:

- $\sin\theta \approx \tan\theta \approx \theta$
- $\cos\theta \approx 1$
- E.g. argument θ < 0.2 rad \approx 11.5 0 =>
 - error in $sin\theta$ is less than 0.7%
 - error in tanθ less than 1.4%
 - error in cosθ is less than 2%

DEPARTMENT OF INFORMATICS



Approximations (2) – must know!

• $(1+x)^{m/n} = 1+(n/m)\cdot x - n(m-n)/2!m^2\cdot x^2 + n(m-n)(2m-n)/3!m^3\cdot x^3 - ...$

Approximations for x << 1:

- $1/(1+x) = (1+x)^{-1} \approx 1 x$
- $\sqrt{(1+x)} = (1+x)^{1/2} \approx 1 + x/2$
- $1/\sqrt{(1+x)} = (1+x)^{-1/2} \approx 1 x/2$

DEPARTMENT OF INFORMATICS