

INF1400- Uke 03

Folkens, her kommer det en del oppgaver som skal gi dere god trening innen det å bruke Karnaugh-diagram til forkortning av uttrykk. Løs også alle oppgave som står i boka i slutten av kapittel 3.

1. Simplify the following boolean expressions using a Karnaugh-diagram:

a): $BA + D'B' + DB'A$

b): $CZ + Z'W + CW' + C'ZW$

c): $B'A' + D'A' + DB'A$

2. Simplify the following Boolean functions F

a): $F(W,X,Y,Z) = \text{Sum } m(0, 2, 3, 4, 8, 9, 10, 14)$

b): $F(A,B,C,D) = \text{Sum } m(3, 6, 7, 8, 10, 11, 13, 14, 15)$

c): $F(W,X,Y,Z) = \text{Sum } m(0, 1, 2, 5, 6, 7, 8, 9, 10, 13, 14, 15)$

3. Simplify the following Boolean functions F together with the don't-care conditions

a): $F(A,B,C,D) = \text{Sum } m(3, 6, 7, 10, 14, 15)$, don't-care conditions: $d(A,B,C,D) = \text{Sum } m(9, 11, 12, 13)$

b): $F(A,B,C,D) = \text{Sum } m(1, 2, 7, 9, 15)$, don't-care conditions: $d(A,B,C,D) = \text{Sum } m(5, 11, 13)$

c): $F(W,X,Y,Z) = \text{Sum } m(9, 11, 13, 15)$, don't-care conditions: $d(W,X,Y,Z) = \text{Sum } m(0, 2, 3, 5, 7, 8, 10, 14)$

4. Simplify the following Boolean expressions, using four-variable maps:

$$F = wxy + yz + xy'z + x'y$$

5. Simplify the following Boolean function by first finding the essential prime implicants:

$$F(A, B, C, D) = \Sigma (0, 2, 3, 5, 7, 8, 10, 11, 14, 15).$$

6. Simplify the following Boolean function, using five-variable maps:

$$F(A, B, C, D, E) = \Sigma (0, 1, 4, 5, 16, 17, 21, 25, 29)$$

7. Simplify the following Boolean function F , together with the don't-care conditions d , and then express the simplified function in sum of minterms:

$$F(x, y, z) = \Sigma (0, 1, 2, 4, 5)$$

$$d(x, y, z) = \Sigma (3, 6, 7).$$

8. Given

$$F(A, B, C, D) = \Sigma(0, 4, 5, 7, 8, 12, 13, 15)$$

$$G(A, B, C, D) = \Pi(0, 1, 7, 8, 9, 10, 11, 12, 15)$$

Use 4-variable maps to find

a) Simplified $F \cdot G$

b) Simplified $F + G$

9. Draw the multiple-level NOR circuit for the following expression:

$$F = w(x + y + z) + xyz.$$

10. Design a combinational circuit with three inputs x , y and z , and three outputs A , B and C . When the binary input is 0, 1, 2 and 3, the binary output is one greater than the input. When the binary input is 4, 5, 6 and 7, the binary output is one less than the input.