







### The approach we choose

- 1. Mathematical morphology can be explained from very mathematical standpoint.
- 2. We will not choose that approach, rather we will focus on how these operators work from a visual point of view and how they can be implemented on a computer.
- 3. This avoids us a lot of gory mathematical detail.
- 4. If you want more details then consider INF5300.

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# The structuring element

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- 1. The fundamental tool in mathematical morphology is the structuring element.
- The structuring element is a (small) group of pixels. One of these pixels is designated as the origin of the structuring element.
- 3. The relation between this small group of pixels and the foreground pixels in the image to be analyzed is what we use to define the morphological operators.

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Erosion	
1. Matlab example.	
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# Geodesic operators One very important class of morphological operators are the so called geodesic operators. They are based on simple erosions and dilations, but operate on two images, the input image and a mask. The operator is applied to the input image, but the effect of the operator on the input image is limited by the mask.

### **Geodesic erosion Geodesic dilation** 1. Consider two binary images, f and g. 1. Consider two binary images, f and g. 2. We will consider f the input image and g the mask. 2. We will consider f the input image and g the mask. 3. A geodesic erosion of f over the mask g is simply 3. A geodesic dilation of f under the mask g is simply the following: the following: a. Erode f by your structuring element. a. Dilate f by your structuring element. b. Perform a pixelwise maximum operation using the b. Perform a pixelwise minimum operation using the eroded f and the mask g as input. dialted f and the mask g as input. NR Regnesentral www.nr.no NR Regnesentral www.nr.no





# Morphological reconstruction (by dilation) of the input image f under the mask g consists in repeating a geodesic dilation of f under the mask g until idempotence (that is, until no further change). Matlab example.

# <section-header><list-item> The extension to gray level images 1. The formal definition for morphological operations on gray level images can be quite confusing. 2. We will consider a slightly simplified definition, based on the assumption that the structuring element is "flat". 3. In that case, the basic mathematical operations of erosion and dilation are reduced to local min and max operations over the structuring element as it is "moved" over the image.





# Gray level erosion

- 1. Remember: This is **nothing else** than a calculation of local minima values.
- 2. The **only** difference with what you would typically consider a local minimum calculation is that the **shape** of the region over which you calculate the minimum is defined by the shape of the structuring element.

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### **Gray level erosion**

- 1. Consider the following image showing carbon fibers embedded in a special glue (epoxy).
- 2. Such carbon fiber matrices make very light but







## **Gray level dilation**

- 1. Dilating a gray level image with this structuring element is also very simple:
  - a. Move the origin of the structuring element from pixel to pixel in the input image.
  - b. Select the local maximum over the region defined by the structuring element.
  - c. Write this maximum value to the same pixel position in the output image.

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## **Gray level dilation** 1. Again: This is nothing else than a calculation of local maxima values. 2. The only difference with what you would typically consider a local maximum calculation is that the shape of the region over which you calculate the maximum is defined by the shape of the structuring element.

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## The top hat transforms

Consider this image that we have already looked at earlier. We have already observed that there is no single, global threshold that will succeed in separating text from background. So far we have seen how this can be solved using local thresholding algorithms. But can anything be done in order to compensate for the uneven illumination.

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 The top hat transforms

 1. Matlab example.