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*INF5390 – Kunstig intelligens*

# **Agents That Learn**

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# Outline

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- General model
- Types of learning
- Learning decision trees
- Learning logical descriptions
- Other knowledge-based methods
- Summary

Extracts from

AIMA Chapter 18: Learning From Examples

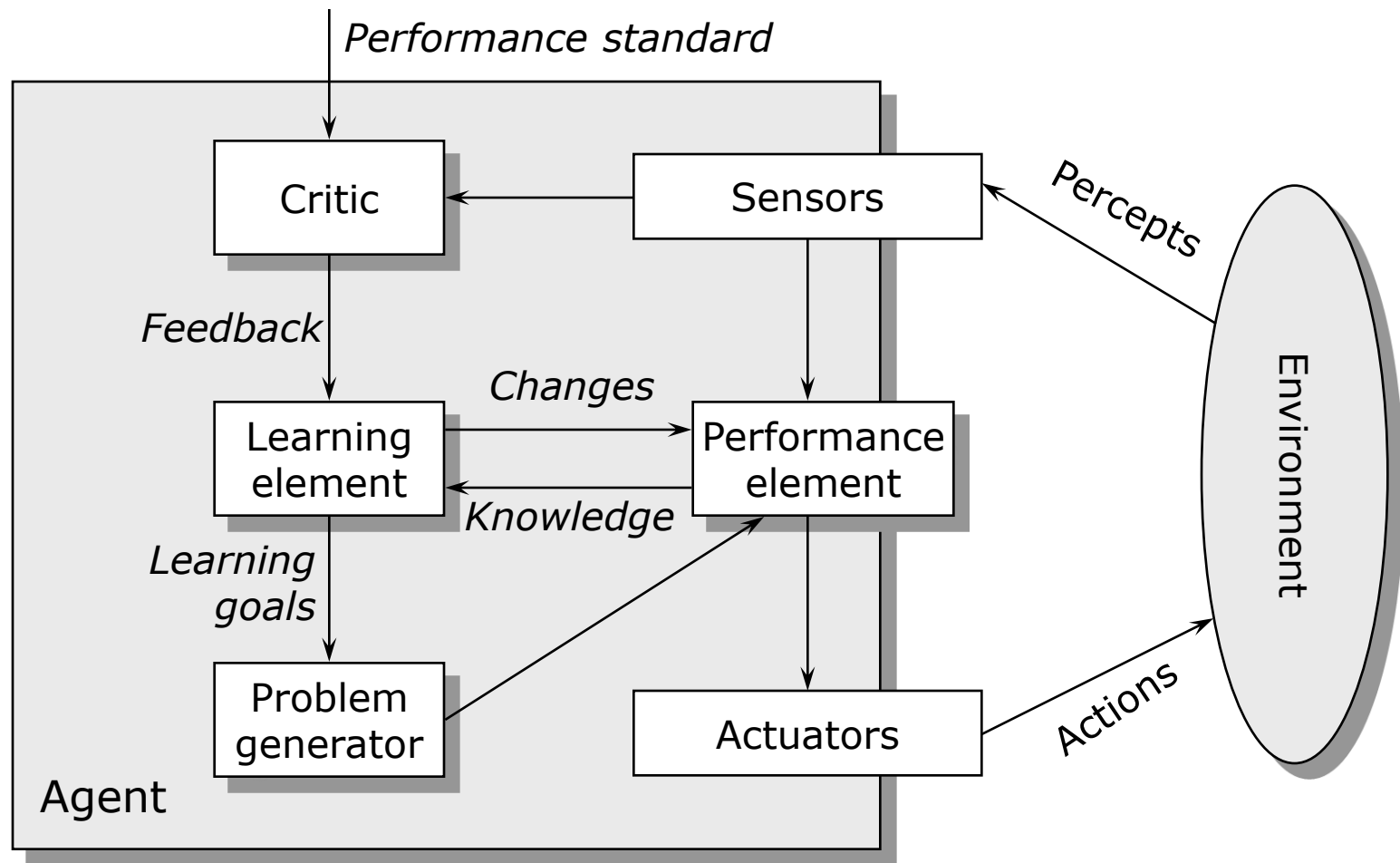
AIMA Chapter 19: Knowledge in Learning

# Why should agents learn?

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- Agents in previous lectures have assumed “built-in” knowledge, provided by designers
- In order to handle incomplete knowledge and changing knowledge requirements, agents must *learn*
- Learning is a way of achieving agent *autonomy* and the ability to *improve performance* over time
- The field in AI that deals with learning is called *machine learning*, and is very active

# General model of learning agents



# Elements of the general model

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- Performance element
  - ✓ Carries out the task of the agent, i.e. processes percepts and decides on actions
- Learning element
  - ✓ Proposes improvements of the performance element, based on previous knowledge and feedback
- Critic
  - ✓ Evaluates performance element by comparing results of its actions with imposed performance standards
- Problem generator
  - ✓ Proposes exploratory actions to increase knowledge

# Aspects of the learning element

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- Which *components* of the performance element are to be improved
  - ✓ Which parts of the agent's knowledge base is targeted
- What *feedback* is available
  - ✓ Supervised, unsupervised or reinforcement learning differ in type of feedback agent receives
- What *representation* is used for the components
  - ✓ E.g. logic sentences, belief networks, utility functions, etc.
- What *prior information (knowledge)* is available

# Performance element components

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- Possible components that can be improved
  - ✓ Direct mapping from states to actions
  - ✓ Means to infer world properties from percept sequences
  - ✓ Information about how the world evolves
  - ✓ Information about the results of possible actions
  - ✓ Utility information about the desirability of world states
  - ✓ Desirability of specific actions in specific states
  - ✓ Goals describing states that maximize utility
- In each case, learning can be seen as learning an unknown *function*  $y = f(x)$

# Hypothesis space H

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- H: the set of hypothesis functions  $h$  to be considered in searching for  $f(x)$
- *Consistent* hypothesis: Fits with all data
  - ✓ If several consistent hypotheses – choose simplest one! (Occam's razor)
- *Realizability* of learning problem:
  - ✓ *Realizable* if H contains the "true" function
  - ✓ *Unrealizable* if not
  - ✓ We do normally know what the true function is
- Why not choose H as large as possible?
  - ✓ May be very inefficient in learning and in applying



# Types of learning - Knowledge

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- *Inductive* learning
  - ✓ Given a collection of *examples*  $(x, f(x))$
  - ✓ Return a function  $h$  that approximates  $f$
  - ✓ Does not rely on prior knowledge (“just data”)
- *Deductive* (or analytical) learning
  - ✓ Going from known general  $f$  to a new  $f'$  that is logically entailed
  - ✓ Based on prior knowledge (“data+knowledge”)
  - ✓ Resemble more human learning

# Types of learning - Feedback

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- *Unsupervised* learning
  - ✓ Agent learns patterns in data even though no feedback is given, e.g. via clustering
- *Reinforcement* learning
  - ✓ Agent gets reward or punishment at the end, but is not told which particular action led to the result
- *Supervised* learning
  - ✓ Agent receives learning examples and is explicitly told what the correct answer is for each case
- Mixed modes, e.g. *semi-supervised* learning
  - ✓ Correct answers for some but not all examples

# Learning decision trees

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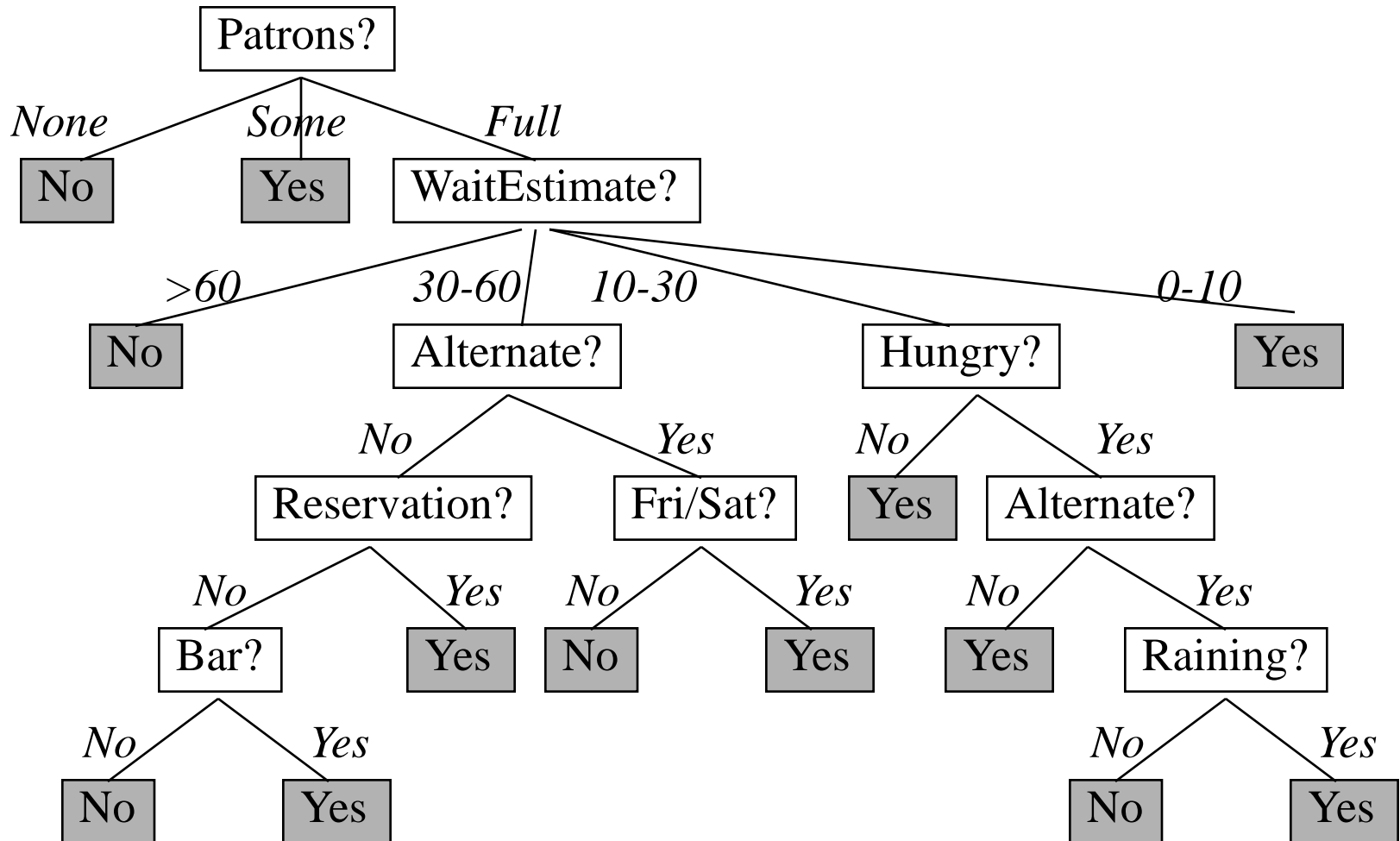
- A *decision situation* can be described by
  - ✓ A number of *attributes*, each with a set of possible values
  - ✓ A *decision* which may be Boolean (yes/no) or multivalued
- A *decision tree* is a tree structure where
  - ✓ Each internal node represents a *test* of the value of an attribute, with one branch for each possible attribute value
  - ✓ Each leaf node represents the value of the *decision* if that node is reached
- *Decision tree learning* is one of simplest and most successful forms of machine learning
- An example of *inductive* and *supervised* learning

# Example: Wait for restaurant table

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- Goal predicate: *WillWait* (for restaurant table)
- Domain attributes
  - Alternate (other restaurants nearby)
  - Bar (to wait in)
  - Fri/Sat (day of week)
  - Hungry (yes/no)
  - Patrons (none, some, full)
  - Price (range)
  - Raining (outside)
  - Reservation (made before)
  - Type (French, Italian, ..)
  - WaitEstimate (minutes)

# One decision tree for the example



# Expressiveness of decision trees

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- The tree is equivalent to a conjunction of implications  
 $\forall r \text{Patrons}(r, \text{Full}) \wedge \text{WaitEstimate}(r, 10 - 30) \wedge \text{Hungry}(r, \text{No}) \Rightarrow \text{WillWait}(r)$
- Cannot represent tests on two or more objects, restricted to testing attributes of one object
- Fully expressive as propositional language, e.g. any Boolean function can be written as a decision tree
- For some functions, exponentially large decision trees are required
- E.g. decision trees are good for some functions and bad for others

# Inducing decision trees from examples

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- Terminology
  - ✓ *Example* - Specific values for all attributes, plus goal predicate
  - ✓ *Classification* - Value of goal predicate of the example
  - ✓ *Positive/negative example* - Goal predicate is true/false
  - ✓ *Training set* - Complete set of examples
- The task of inducing a decision tree from a training set is to *find the simplest tree that agrees with the examples*
- The resulting tree should be more *compact* and *general* than the training set itself

# A training set for the restaurant example

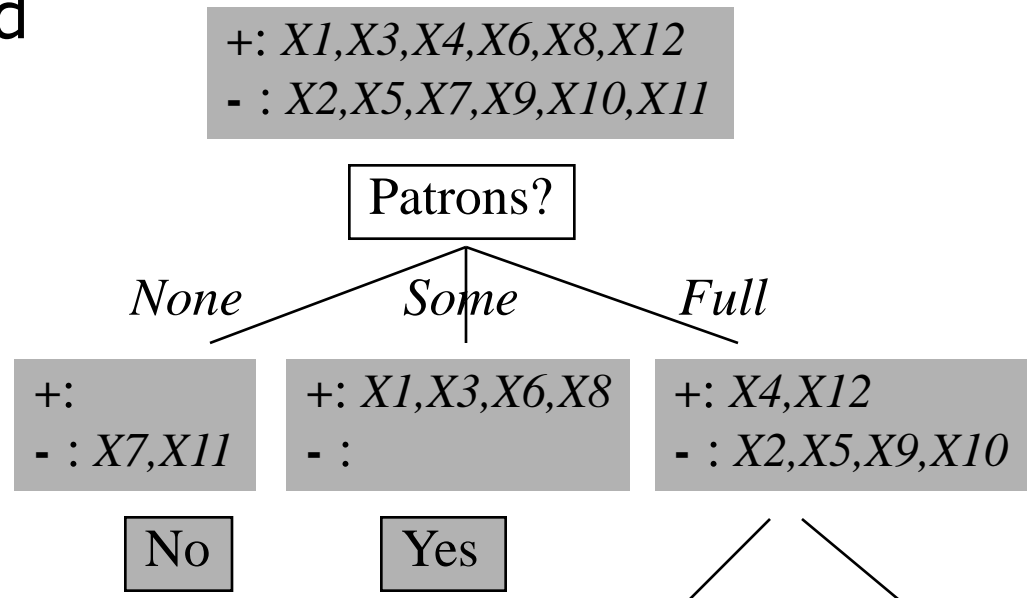
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Example	Attributes										Will wait
	<i>Alt</i>	<i>Bar</i>	<i>Fri</i>	<i>Hun</i>	<i>Pat</i>	<i>Price</i>	<i>Rain</i>	<i>Res</i>	<i>Type</i>	<i>Est</i>	
X1	Yes	No	No	Yes	Some	\$\$\$	No	Yes	French	0-10	Yes
X2	Yes	No	No	Yes	Full	\$	No	No	Thai	30-60	No
X3	No	Yes	No	No	Some	\$	No	No	Burger	0-10	Yes
X4	Yes	No	Yes	Yes	Full	\$	No	No	Thai	10-30	Yes
X5											
X6											
X7											
X8						ETC.					
X9											
X10											
X11											
X12											



# General idea of induction algorithm

- Test the most important attribute first, i.e. the one that makes the most difference to the classification
- *Patrons?* is a good choice for the first attribute, because it allows early decisions
- Apply same principle recursively



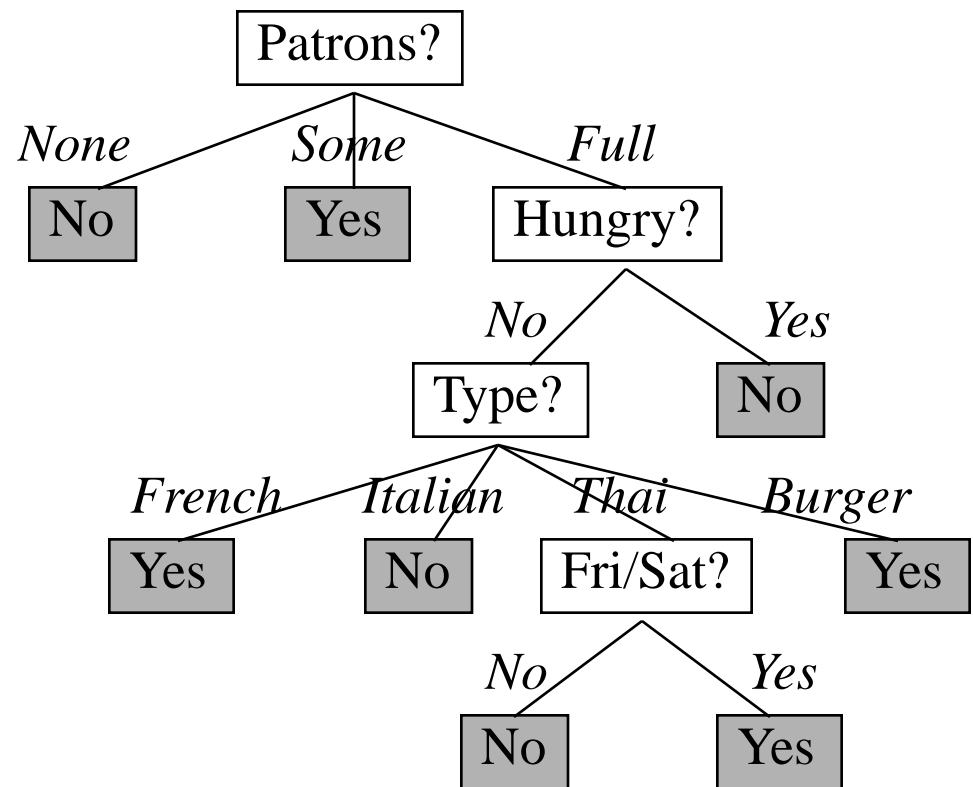
# Recursive step of induction algorithm

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- The attribute test splits the tree into smaller decision trees, with fewer examples and one attribute less
- Four cases to consider for the smaller trees
  - ✓ If some positive and some negative examples, choose best attribute to split them
  - ✓ If examples are all positive (negative), answer *Yes (No)*
  - ✓ If no examples left, return a default value (no example observed for this case)
  - ✓ If no attributes left, but both positive and negative examples: Problem! (same description, different classifications - *noise*)

# Induced tree for the example set

- The induced tree is *simpler* than the original “manual” tree
- It captures some *regularities* that the original creator was unaware of



# Broaden applicability of decision trees

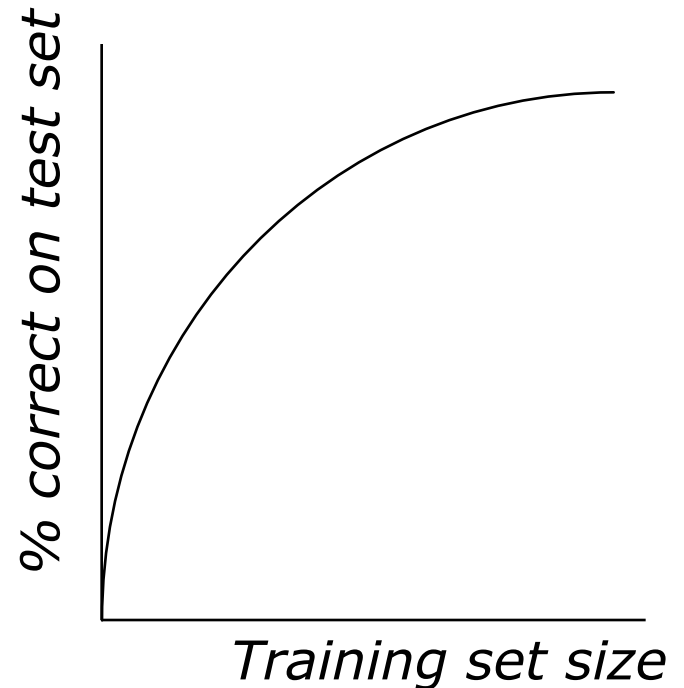
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- Missing data
  - ✓ How to handle training samples with partially missing attribute values
- Multi/many-valued attributes
  - ✓ How to treat attributes with many possible values
- Continuous or integer-valued input attributes
  - ✓ How to branch the decision tree when attribute has a continuous value range
- Continuous-valued output attributes
  - ✓ Requires *regression tree* rather than a decision tree, i.e. output value is a linear function of input variables rather than a point value

# Assessing learning performance

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- Collect large set of examples
- Divide into two disjoint sets, *training set* and *test set*
- Use learning algorithm on training set to generate hypothesis  $h$
- Measure percentage of examples in test set that are correctly classified by  $h$
- Repeat steps above for differently sized training sets



# PAC – The theory of learning

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- How can we be sure that the learning algorithm gives a function  $h$  that predicts correctly?
  - ✓ How many learning examples are needed?
  - ✓ What hypothesis space  $H$  should be used?
  - ✓ Etc.
- Computational learning theory tries to answer such questions
  - ✓ Underlying principle: Any  $h$  that is consistent with a sufficient large number of examples is *probably approximately correct* (PAC)
- PAC theory can be used to bound hypothesis space and size of example set

# A logical formulation of learning

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- Inductive learning can be seen as *searching for a good hypothesis* in a large search space
- The *hypothesis space* is defined by a particular representation language, e.g. logic
- Define learning in terms of logical connections between *hypotheses, examples, and goals*
- This approach enables extensions of simple inductive decision tree learning to applying full *logical inference*

# Hypothesis space

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- Let  $Q$  be a unary *goal predicate*, and  $C_i$  a *candidate definition*, i.e. a *hypothesis*  $H_i$  for classifying examples  $x$  correctly is that

$$\forall x Q(x) \Leftrightarrow C_i(x)$$

- Example: Induced decision tree is equivalent to

$$\forall r \text{ WillWait}(r) \Leftrightarrow \text{Patrons}(r, \text{Some})$$

$$\vee \text{Patrons}(r, \text{Full}) \wedge \neg \text{Hungry}(r) \wedge \text{Type}(r, \text{French})$$

$$\vee \text{Patrons}(r, \text{Full}) \wedge \neg \text{Hungry}(r) \wedge \text{Type}(r, \text{Thai}) \wedge \text{Fri} / \text{Sat}(r)$$

$$\vee \text{Patrons}(r, \text{Full}) \wedge \neg \text{Hungry}(r) \wedge \text{Type}(r, \text{Burger})$$

- *Hypothesis space* is the set  $\{H_1, \dots, H_n\}$ , of which one is believed to be correct:  $H_1 \vee H_2 \vee \dots \vee H_n$



# Examples for learning

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- An *example* is an object  $X_i$  to which the goal concept  $Q$  may or may not apply ( $Q(X_i)$  or  $\neg Q(X_i)$ ), and which has a logical description  $D_i(X_i)$
- E.g. first induction example  $X_1$   
 $Alternate(X_1) \wedge \neg Bar(X_1) \wedge \neg Fri / Sat(X_1) \wedge Hungry(X_1) \wedge \dots$   
with classification  $WillWait(X_1)$
- Complete *training set* is the conjunction of all  $X_i$
- A hypothesis agrees with all examples if and only if it is *logically consistent* with the training set

# False examples and inductive learning

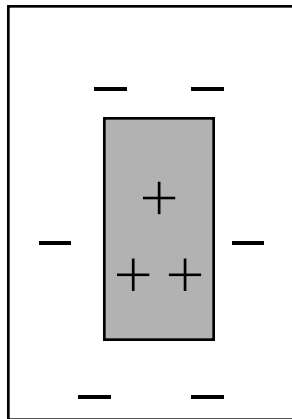
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- If a hypothesis  $H_i$  is consistent with the entire training set, it must be consistent with each example
- An example can be a *false negative* for the hypothesis, i.e.  $H_i$  says it should be negative but it is positive
- An example can be a *false positive* for the hypothesis, i.e.  $H_i$  says it should be positive but it is negative
- If the example is false negative or false positive, the example and hypothesis are *inconsistent*, and the hypothesis can be *ruled out*

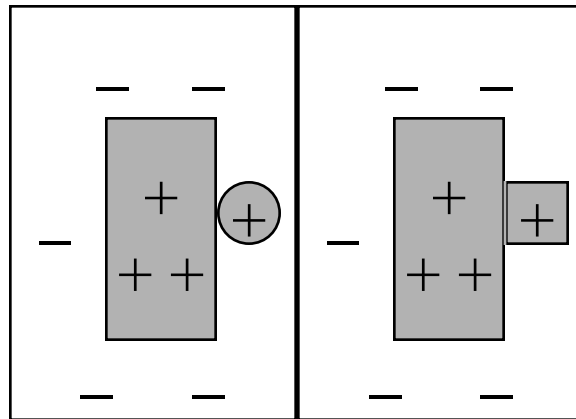
Inductive learning in a logical setting is the process of gradually eliminating hypotheses that are inconsistent with the examples

# Current-best-hypothesis search

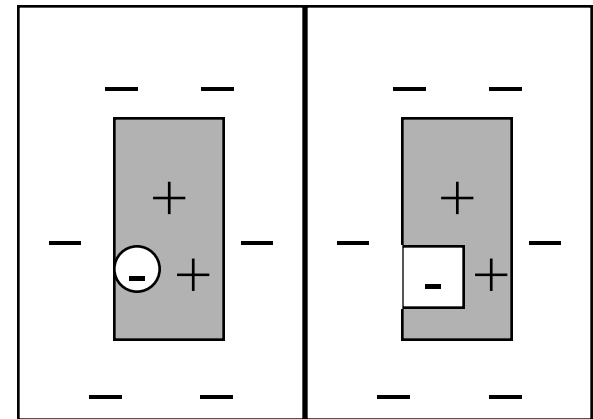
- *Current-best-hypothesis* search maintains a single hypothesis which is adjusted as new examples arrive to maintain consistency



*Consistent hypothesis*



*False negative hypothesis*



*False positive hypothesis*

# Generalizing and specializing hypotheses

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- If hypothesis H1 with definition C1 is a generalization of H2 with definition C2, then

$$\forall x C_2(x) \Rightarrow C_1(x)$$

- *Generalization* of a hypothesis can be achieved by *dropping conditions*

$$C_2(x) = \textit{Alternate}(x) \wedge \textit{Patrons}(x, \textit{Some}) \quad C_1(x) = \textit{Patrons}(x, \textit{Some})$$

- *Specialization* of a hypothesis can similarly be achieved by *adding conditions*
- Current-best-hypothesis search with generalization and specialization and backtracking has been used in many learning programs, but does not scale well

# Least commitment search

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- The current-best-hypothesis approach has to backtrack because it is forced to choose *one* hypothesis even if it does not have enough data
- A better approach is to keep all hypotheses consistent with data so far, and gradually remove hypotheses inconsistent with new examples
- Assuming that the right hypothesis is contained in the original set, it will still be in the reduced set (the *version space*)
- The algorithm is *incremental*, need not backtrack

# Other knowledge-based learning methods

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- EBL – Explanation-based learning
  - ✓ Extracts general rules from single examples accompanied by an explanation
- RBL – Relevance-based learning
  - ✓ Uses prior knowledge to identify relevant attributes thereby reducing hypothesis space
- KBIL – Knowledge-based inductive learning
  - ✓ Uses prior knowledge to find inductive hypotheses that explain sets of observations
- ILP – Inductive logic programming
  - ✓ Performs KBIL on knowledge expressed in first-order logic, and can learn relational knowledge

# Summary

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- Learning is an essential capability for agents in unknown or resource-constrained environments
- Learning agents have a *performance* element and a *learning* element
- The learning element tries to improve various parts of the performance element, generally seen as *functions*  $y = f(x)$
- Learning can be *inductive* (from examples) or *deductive* (based on knowledge)
- Differ in types of *feedback* to the agent: unsupervised, reinforcement or supervised learning

## Summary (cont.)

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- Learning a function from examples of inputs and outputs is an example of inductive/supervised learning, of which learning *decision trees* is a simple case
- A logical formulation of learning uses *current-best-hypothesis* approach to maintain a single hypothesis which is updated with new examples
- Other logical or knowledge-based learning methods include EBK, RBIL, KBIL and IPL