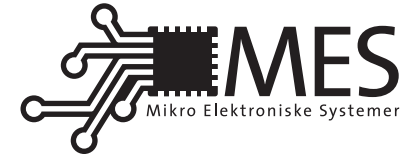




UNIVERSITY  
OF OSLO

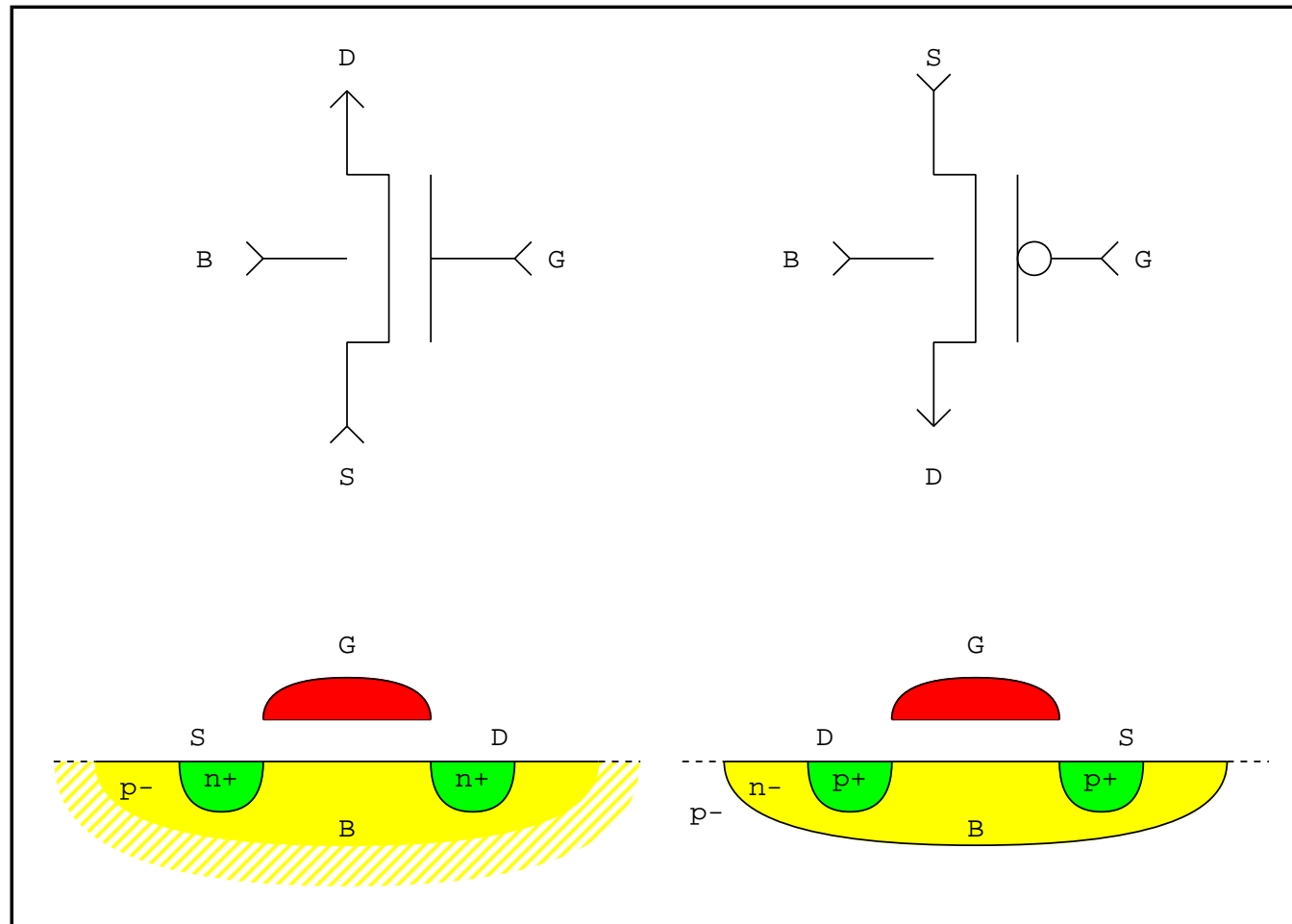


---

# Neuromorphic Electronics

## Basic Analog CMOS

# NFET symbol and cross section





## NFET formulae (1/2)

$$I_{DS} = I_F - I_R$$

$$I_{F(R)} = I_S \ln^2 \left[ 1 + e^{\frac{V_G - V_{T0} - nV_{S(D)}}{2nU_T}} \right]$$

$I_F \gg I_R$ : in saturation, else: triode region/linear region.



## NFET formulae (2/2)

$I_F \ll I_S$  ( $V_G < V_{T0} + nV_S$ ): weak inversion/subthreshold

simplifies to:  $I_F = I_S e^{\frac{V_G - V_{T0} - nV_S}{nU_T}}$

$I_F \gg I_S$  ( $V_G > V_{T0} + nV_S$ ): strong inversion/above threshold

simplifies to:  $I_{F(R)} = \frac{I_S}{4} \left( \frac{V_G - V_{T0} - nV_{S(D)}}{nU_T} \right)^2$

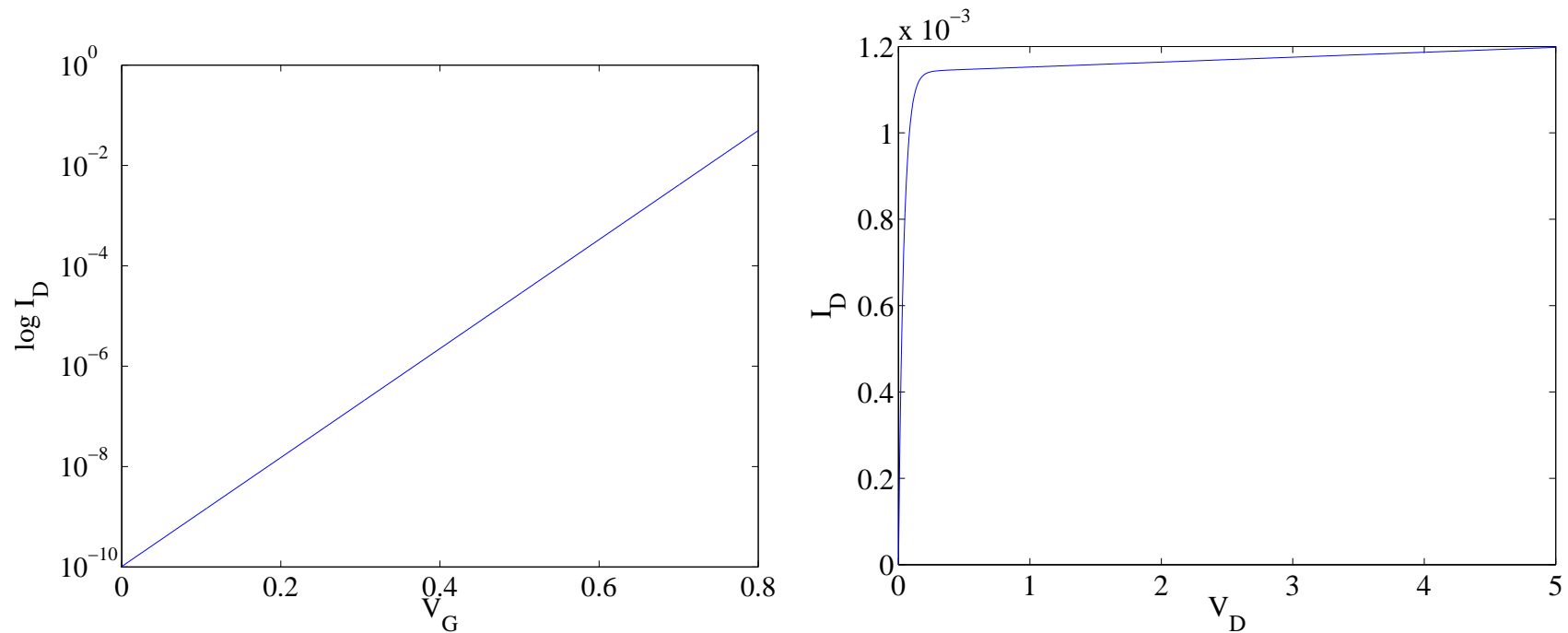


## NFET Early effect

$$I_F = \frac{V_D + V_{Early}}{V_{Early}} I_F$$



# NFET characteristics



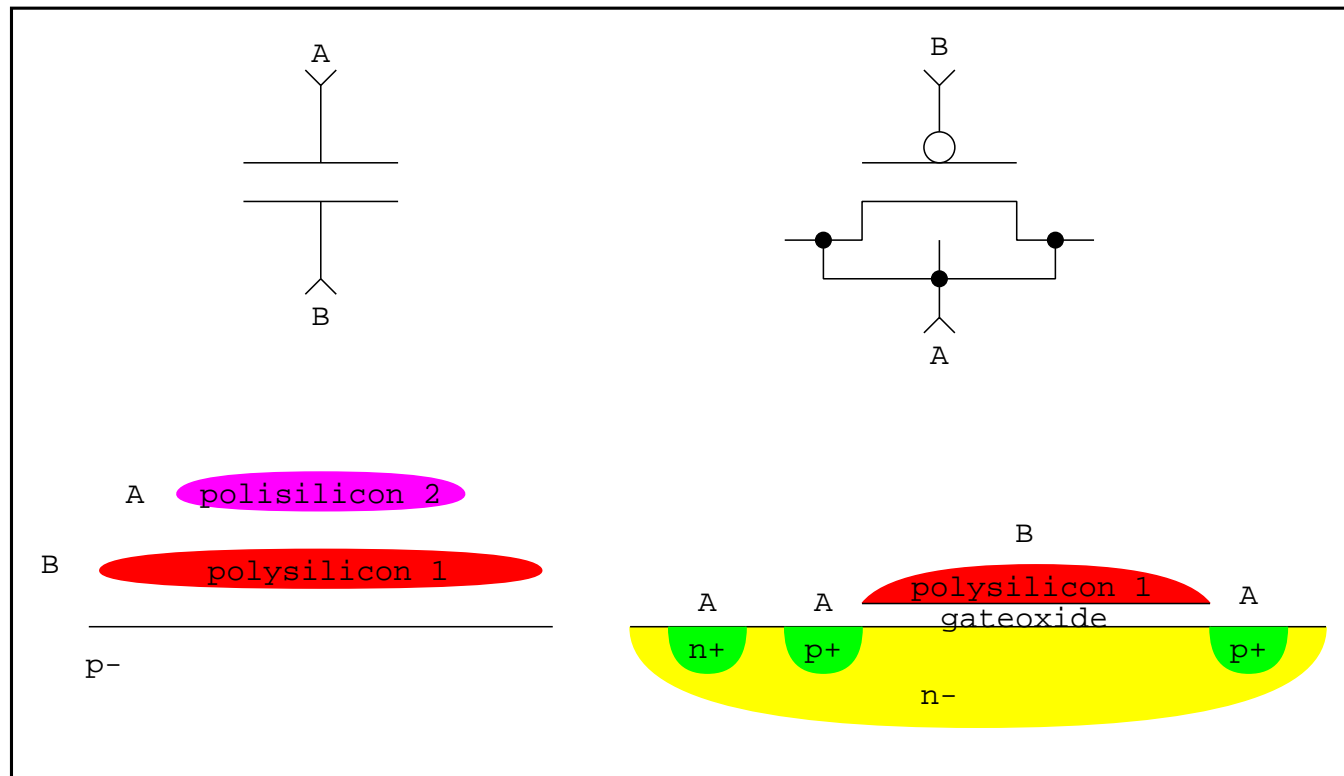


## Briefly Mentioned: Gate Leakage/Direct Tunneling

$$t_{ox} \leq 2 - 3 \text{ nm}$$

$$J_g = \begin{cases} A \frac{V_{ox}^2}{t_{ox}^2} e^{-\frac{B \left( 1 - \left( 1 - \frac{V_{ox} q_e}{\phi_{ox}} \right)^{\frac{2}{3}} \right)}{\frac{V_{ox}}{t_{ox}}}} & \text{if } V_{ox} < \frac{\phi_{ox}}{q_e} \\ A \frac{V_{ox}^2}{t_{ox}^2} e^{-\frac{B}{\frac{V_{ox}}{t_{ox}}}} & \text{if } V_{ox} < \frac{\phi_{ox}}{q_e} \end{cases} \quad (1)$$

# Capacitor symbol and cross section







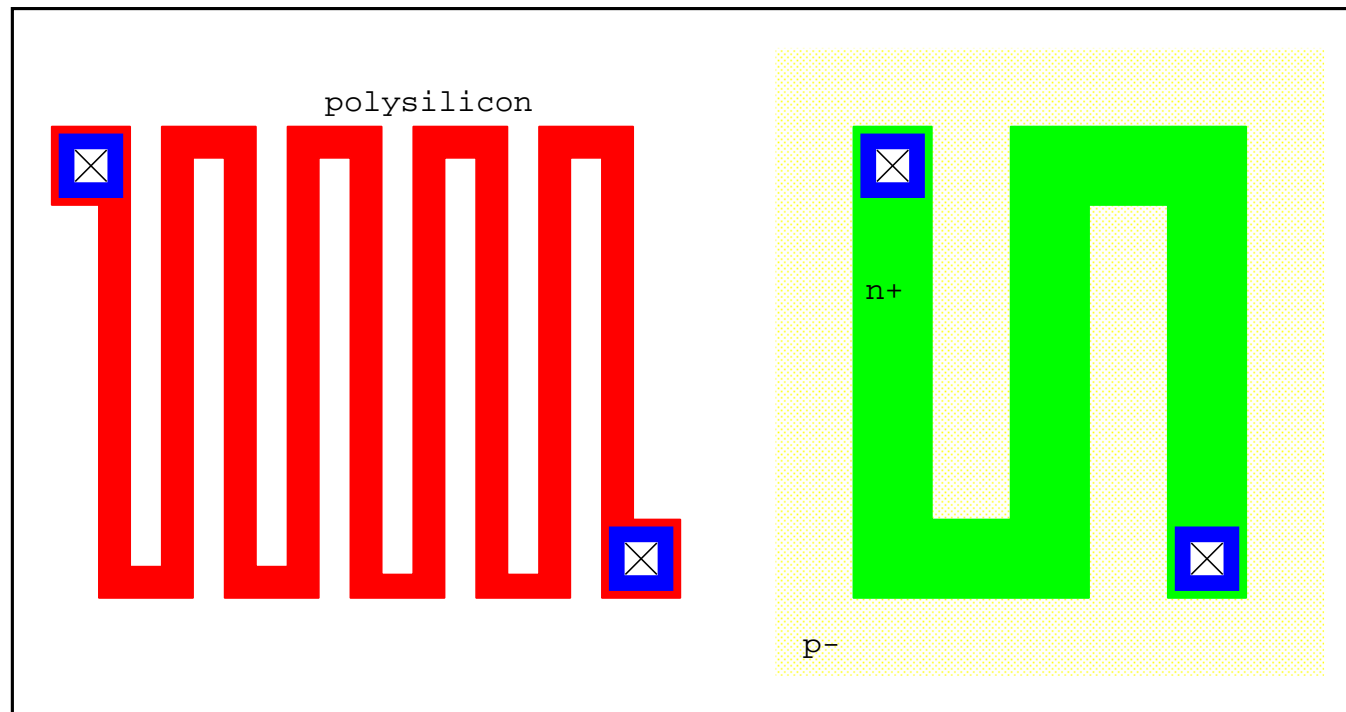
## Capacitor formulae

$$V = \frac{1}{C}Q$$

$$\frac{\delta V}{\delta t} = \frac{1}{C}I$$



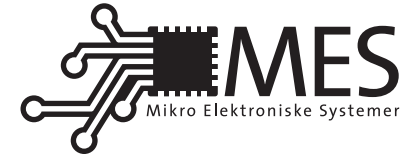
# Resistor layout





UNIVERSITY  
OF OSLO

Atoms

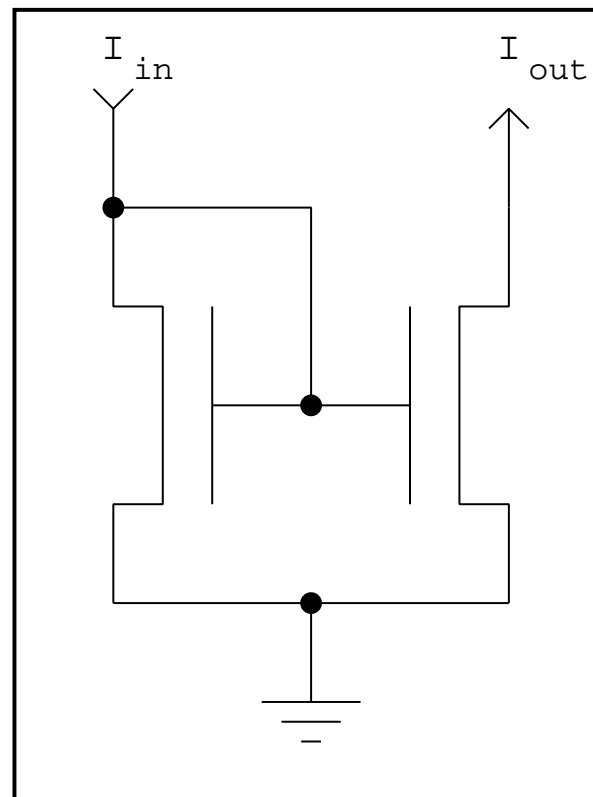


## Resistor formulae

$$V = RI$$



# Current Mirror Schematics



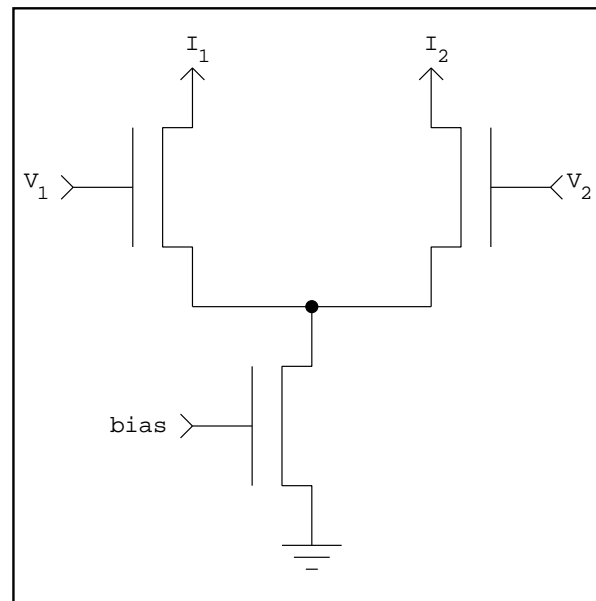


## Current Mirror formulae

$I_{out} = I_{in}$  (if both transistors are in saturation, and have the same W/L ratio, and neglecting the Early effect)



# Differential Pair Schematics





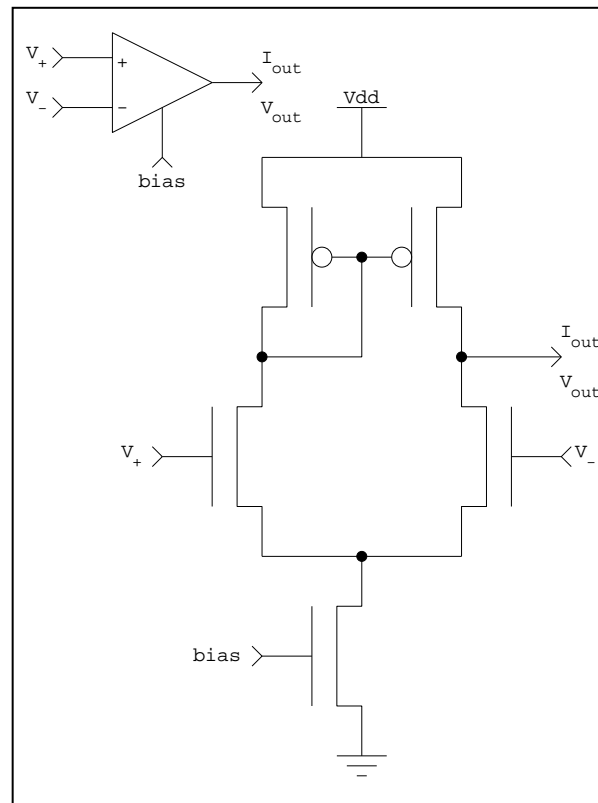
## Differential Pair Formulae

$$I_b = I_1 + I_2 = I_S e^{\frac{-V_{T0} - V_C}{nU_T}} \left( e^{\frac{V_1}{nU_T}} + e^{\frac{V_2}{nU_T}} \right)$$

$$\frac{I_1}{I_2} = \frac{I_1}{I_b - I_1} = e^{\frac{V_1 - V_2}{nU_T}}$$



# Transconductance Amplifier Schematics





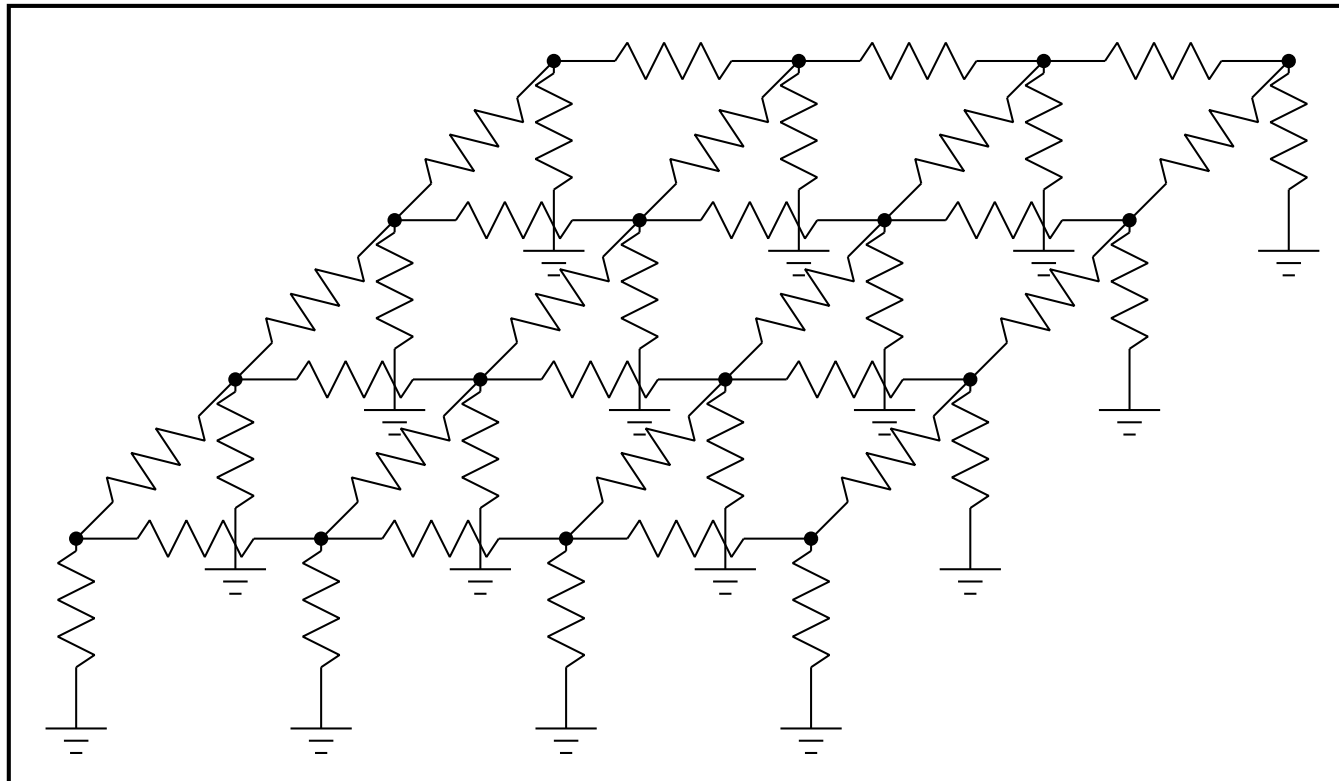


## Transconductance Amplifier Formulae

$$I_{out} = I_b \frac{e^{\frac{V_+}{nU_T}} - e^{\frac{V_-}{nU_T}}}{e^{\frac{V_+}{nU_T}} + e^{\frac{V_-}{nU_T}}} = I_b \tanh \frac{V_+ - V_-}{2nU_T}$$



# Resistive Net

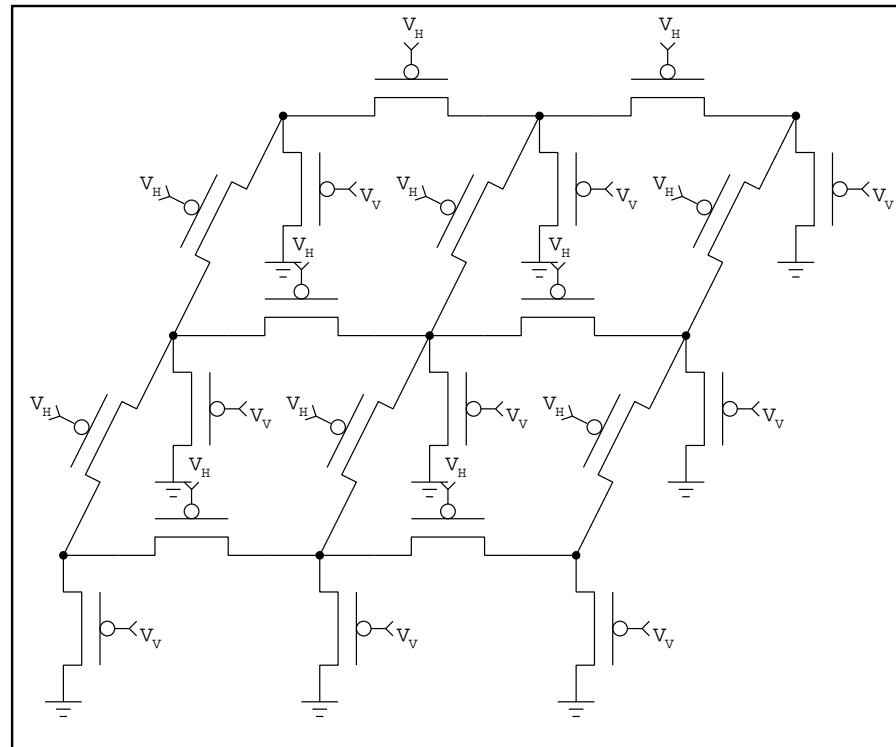




## Resistive Net Formulae

$$\frac{V}{R_V} = \frac{\delta^2}{\delta x^2 \delta y^2} \frac{V}{R_H}$$

# Diffuser Net





## Diffuser Net Formulae

$$\frac{V^*}{R_V^*} = \frac{\delta^2}{\delta x^2 \delta y^2} \frac{V^*}{R_H^*}$$

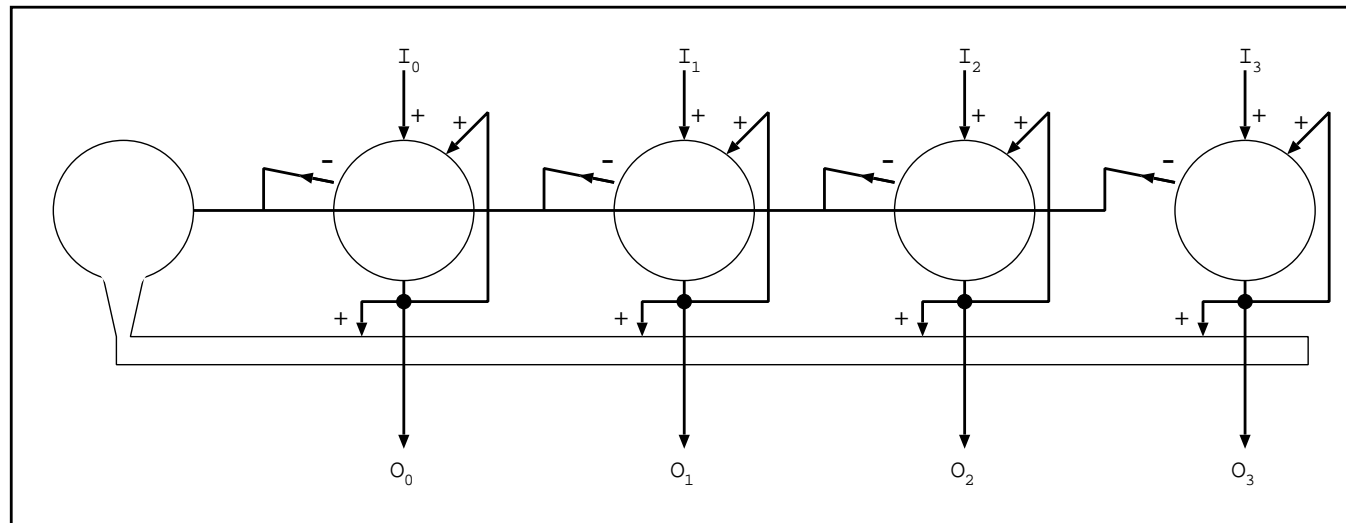
$$V^* = -e \frac{-V}{U_T}$$

$$\frac{1}{R^*} = g^* = I_S e^{\frac{V_G - V_{T0}}{nU_T}}$$

Attention: transistors must be in subthreshold for this to be applicable!

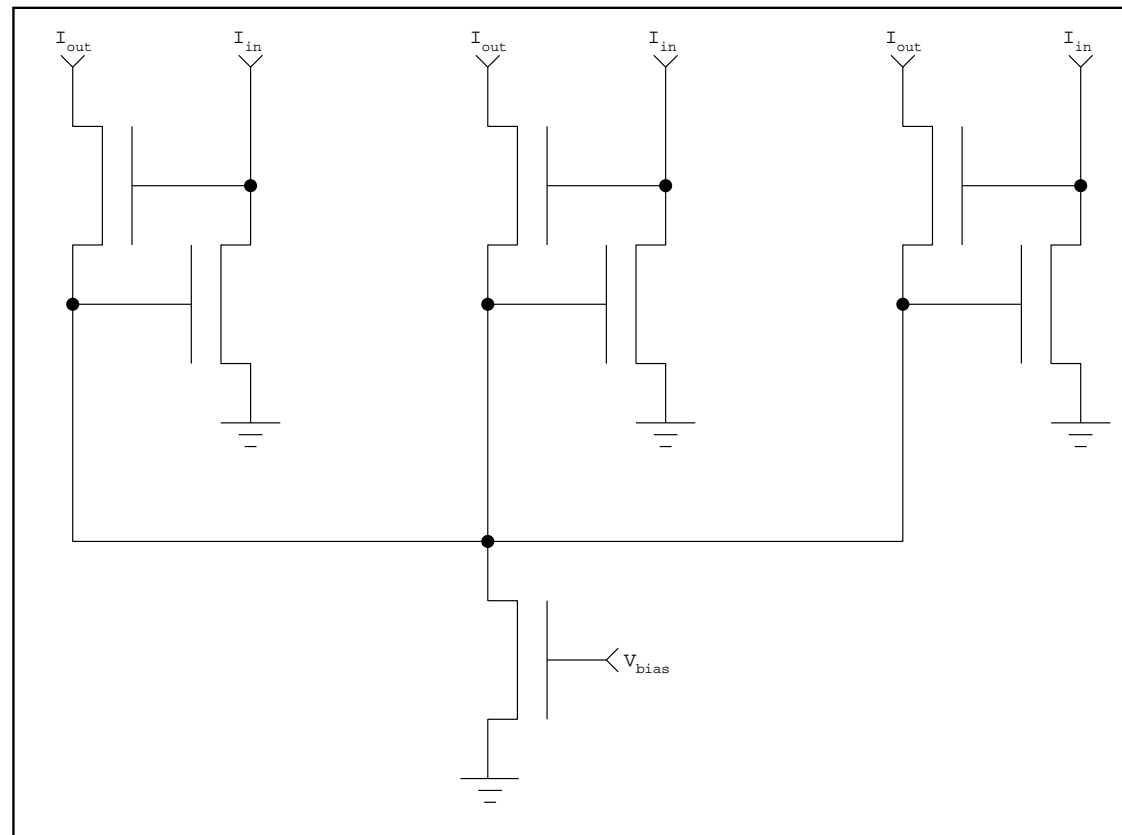


# Winner Take All Principle



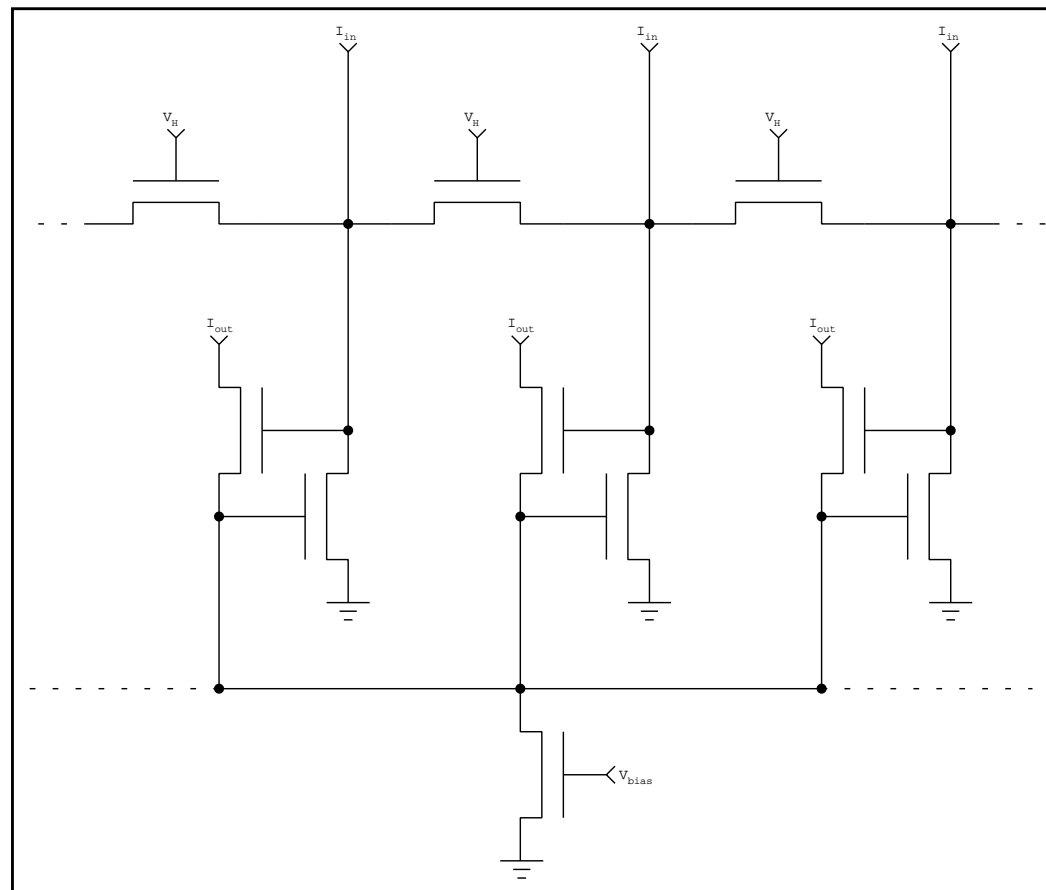


# Winner Take All Basic Circuit

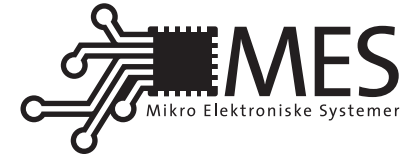




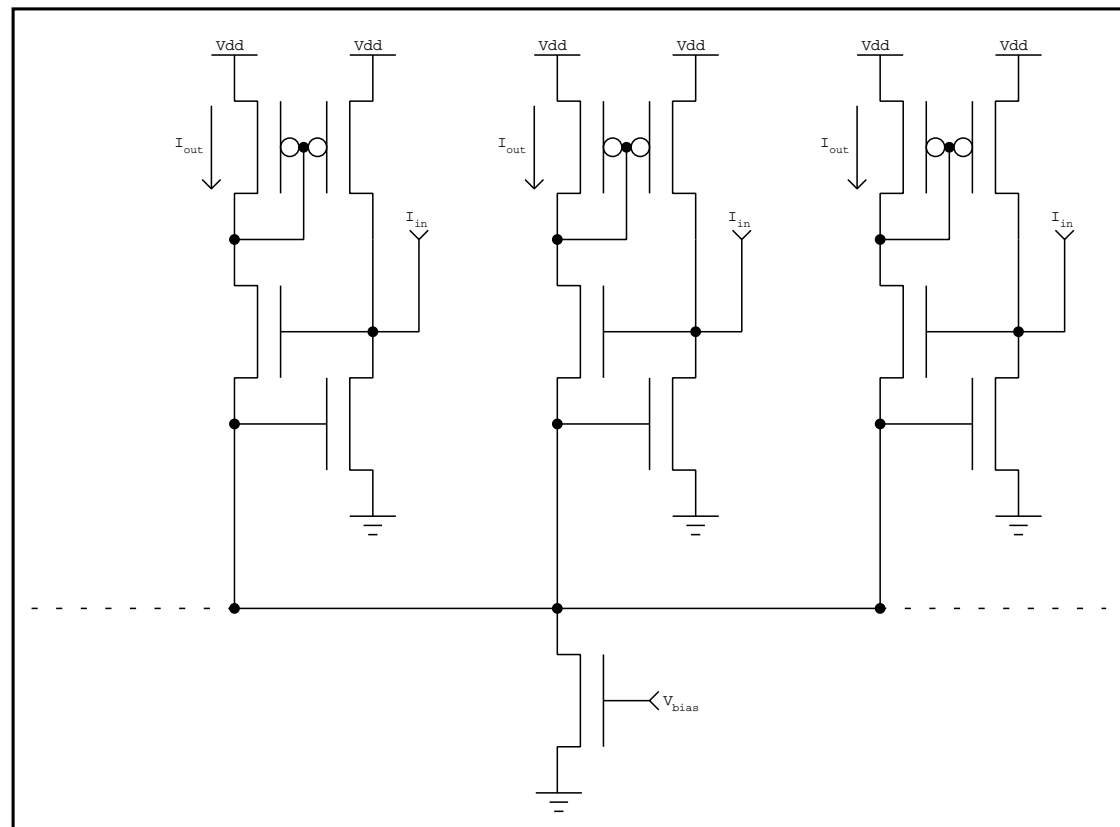
# Smooth Cooperative Winner Take All







# Hysteretic Winner Take All



# Local Winner Take All Principle

