## INF5490 RF MEMS

#### L17: Summary, repetition

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## Overview

- Motivation
- Micromachining
- Modeling
- Specific features for RF systems
- Q-factor
- RF MEMS components
  - Switches
  - Phase shifters
  - Resonators
  - Micromechanical filters
  - Capacitors
  - Inductors
- Integration and packaging
- RF MEMS in wireless systems
- Conclusion and future prospects

#### Choice of focus $\rightarrow$ RF MEMS

- MEMS is a <u>broad</u> field of research
   Need of focus in NANO group → RF MEMS!
- "RF MEMS refers to the design and fabrication of dedicated MEMS for RF (integrated) circuits"
  - 1a) Components operate micromechanical and/or
  - 1b) Components fabricated using micromachining
  - 2) Components are used in RF systems

# Typical RF MEMS components

- Switches
- Variable capacitors
- Inductors
- Resonators
- Micromechanical filters
- Phase shifters





Figure 4.1. Illustration of a typical MEMS shunt switch shown in cross section and plan view. The equivalent circuit is also shown [6] (Copyright IEEE).







# Typical RF MEMS components

- Switches
- Variable capacitors
- Inductors
- Resonators
- Micromechanical filters
- Phase shifters

- Focus on real vibrating structures →
  - May be used to implement
    - oscillators
    - filters
    - "mixer with filter"

## **Benefits of RF MEMS**

#### Higher performance

- Increased selectivity: sharp filters
- Increased Q-factor: stable "tank" frequency
- Reduced loss
- Higher isolation, reduced cross talk
- Reduced signal distortion
- Larger bandwidth
- Lower power consumption
- Reduced cost
  - Batch processing
- Circuit and system miniaturization
  - System integration (µelectronics + MEMS)
    - Packaging: Multi-chip module
    - Monolithic integration: SoC (System-on-Chip)

## Micromachining

• Micromachining, definition:

 Accurately, to define and implement any microscopic mechanical structure out of or on a material

#### Silicon micromachining is mature

- Si processes also used by IC industry
  - "grown out of" IC-processing
- New specific MEMS processes also developed
  - A lot of variants, few standards!

## Important process steps

- Define patterns
   *Photolithography*
- Modify semiconductor material properties
   *Diffusion*
- Remove material

- Ething

Adding material – build structures
 – *Deposition*

## Bulk micromachining

- Selective etching and diffusion into well defined areas of a substrate
  - Etching of the substrate  $\rightarrow$  membranes
  - Etching from back side (wet etching: liquid is used)
  - Possibly combined with <u>dry etching</u> on the front side
- More mature than surface micromachining
- Typical examples
  - Pressure sensor, accelerometer
- "Wafer-bonding" may be necessary
  - Interconnect whole wafers

### Cross section overview



## Surface micromachining

- "Surface" micromachining
  - Deposit layers
    - Structural layer
    - **Sacrificial layer** = "distance-keeping" layer
  - Selective etching of structural layers
    Removing sacrificial layers



#### Srinivasan

## Additive process steps

#### Techniques

- a. Epitaxial growth
- b. Oxidation
- c. Vaporization
- d. CVD, Chemical Vapor Deposition
- e. Sputtering
- f. Moulding
- When depositing, stress may be built into the structures

#### **Residual Stress in Thin Films**

#### Residual film stress

- Microstructure
- Thermal mismatch





Under compressive stress, film wants to expand. Constrained to substrate, bends it in convex way.



Under tensile stress, film wants to shrink Constrained to substrate, bends it in concave way.

Srinivasan

## Removing material: Etching

- Wet-etching or dry-etching
- Wet-etching
  - Deep etching of Si is essential in micromachining
  - Using liquids
  - Depends of:
    - Concentration of liquid, time, temperature
  - Low cost batch processing
  - Both isotropic or anisotropic

## Wet-etching

- Isotropic = uniform etching in all directions
  - HF or blends are usual
  - 0.1 100  $\mu$ m/min etch speed
- Anisotropic = etching faster along some directions
  - Etch speed depends of crystal orientation
  - NaOH, KOH used
  - Silicon nitride used as mask for KOH

## **RIE - DRIE**

- **DRIE** Deep Reactive Ion Etching (1995-)
  - Vertical etching
  - Can etch deep holes (> 500  $\mu$ m) with almost perfect vertical sidewalls
  - Bosch-process
    - Figure  $\rightarrow$
    - High "aspect-ratio"
    - Etching and deposition every second • step
      - etch: SF6, mostly at the bottom!
      - deposit: C4F8, polymer





## Transducers for (RF) MEMS

- Electromechanical transducers
  - − Transforming
     electrical energy ← → mechanical energy
- Transducer principles
  - Electrostatic
  - Electromagnetic
  - Electro thermal
  - Piezoelectric

#### Methods for modeling RF MEMS

- 1. Simple mathematical models

   Ex. parallel plate capacitor
- 2. Converting to electrical equivalents

 3. Analysis using Finite Element Methods

#### **Parallel plate capacitor**



Attractive force between plates

$$F = -\frac{\partial U}{\partial d} = -\frac{\partial}{\partial d} \left(\frac{\varepsilon A}{2d}V^2\right) = \frac{\varepsilon A V^2}{2d^2}$$

#### **Force balance**



k = spring constant

deflection from start position

d0 = gap at 0V and zero spring straind = d0 - zz=d0 - d

Force on upper plate at V and d:

$$F_{nef} = -\frac{\varepsilon A V^2}{2 d^2} + k (d_0 - d) = 0 \text{ at equilibrium}$$

#### Two equilibrium positions



*Figure 6.7.* Electrical and spring forces for the voltage-controlled parallel-plate electrostatic actuator, plotted for  $V/V_{PI} = 0.8$ .

 $\varsigma = 1 - d/d0$  Senturia

#### **Pull-in**

 $F_{net} = 0$   $\frac{\mathcal{E}A V_{PI}^{2}}{2 d_{PI}^{2}} = k \left( d_{o} - d_{PI} \right)$   $1 = \frac{\mathcal{E}A V_{PI}^{2}}{4 d_{o}^{3}}$  $d_{PI} = \frac{2}{3} d_o$ Pull-in when: 8 k do 3 ⊲

# 2. Converting to electrical equivalents

- Mechanical behavior can be modeled using electrical circuit elements
  - Mechanical structure → simplifications → equivalent electrical circuit
    - ex. spring/mass  $\rightarrow$  R, C, L
  - Possible to "interconnect" electrical and mechanical energy domains
    - Simplified modeling and co-simulation of electronic and mechanical parts of the system
  - Proper analysis-tools can be used
    - Ex. SPICE

#### $e \rightarrow V$ - convention

- Senturia and Tilmans use the e→V –convention
- Ex. electrical and mechanical circuits
  - $-e \rightarrow V$  (voltage) equivalent to F (force)
  - $f \rightarrow I$  (current) equivalent to v (velocity)
  - $-q \rightarrow Q$  (charge) equivalent to x (position)
  - e \* f = "power" injected into the element

H. Tilmans, Equivalent circuit representation of electromagnetical transducers:

I. Lumped-parameter systems, J. Micromech. Microeng., Vol. 6, pp 157-176, 1996

### Interconnecting elements

- $e \rightarrow V$  follows two basic principles
  - Elements that share a common flow , and hence a common variation of displacement, are connected in series
  - Elements that share a common effort are connected in parallel

#### **Ex. of interconnection:**

#### "Direct transformation"



Figure 5.9. Translating mechanical to electrical representations.

#### **Mechanical / Electrical Systems**





Input : external force F Output : displacement x  $m\ddot{x}(t) + b\dot{x}(t) + Kx(t) = F$ m mass, b damping, K stiffness Transfer function :

$$H(s) = \frac{x}{F} = \frac{\frac{1}{m}}{s^2 + \frac{b}{m}s + \frac{K}{m}}$$

Input : voltage  $V_i$ Output : voltage  $V_o$   $L\ddot{q}(t) + R\dot{q}(t) + \frac{1}{C}q(t) = V_i$ L induct., R resist., C capacit. Transfer function :  $V_0 = \frac{1}{V_0}$ 

$$H(s) = \frac{V_o}{V_i} = \frac{\frac{1}{LC}}{s^2 + \frac{R}{L}s + \frac{1}{LC}}$$

Texas Christian University

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Ed Kolesar

#### **Resonators**

- Analogy between mechanical and electrical system:
  - Mass *m* inductivity *L*
  - Spring *K* capacitance *C*
  - Damping b resistance R (depending where R is placed in circuit)
- Solution to 2nd order differential equation:

$$H(s) = \frac{\omega_0^2}{s^2 + \frac{\omega_0}{Q}s + \omega_0^2}$$
  

$$\omega_0 = 2\pi f_0 \text{ natural frequency}$$
  

$$\omega_0 = \sqrt{\frac{K}{m}} \text{ mechanical system, } \omega_0 = \sqrt{\frac{1}{LC}} \text{ electrical system}$$
  
 $Q \text{ quality factor}$ 

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#### Frequency and wavelength

• In vacuum:  $\lambda * f = c$ 

Increasing frequency → decreasing wavelength

• At high frequencies (RF) is the wavelength comparable to the circuit dimensions

## Skin depth

- Resistance R increases towards centre of conductor
  - Current close to surface at increasing frequency
  - Formula: "skin-depth" →
    - Current density reduced by a factor 1/e

 $\delta = (\pi f \mu \sigma_{\rm cond})^{-1/2}$ 

• What does this mean for practical designs?



## **Transmission line**

• A conductor has to be modeled as a transmission line



**Figure 2-3** Partitioning an electric line into small elements  $\Delta z$  over which Kirchhoff's laws of constant voltage and current can be applied.

## Solution: 2 waves

 The solution is waves in a positive and negative direction

 $V(z) = V^{+}e^{-kz} + V^{-}e^{+kz}$   $I(z) = I^{+}e^{-kz} + I^{-}e^{+kz}$ (2.34)
(2.35)

$$I(z) = \frac{k}{(R+j\omega L)} (V^{+}e^{-kz} - V^{-}e^{+kz})$$
 (2.36) (Jmfr.2.27)

**Characteristic line-impedance:**  $Z_0 = \frac{V^+}{I^+} = -\frac{V^-}{I^-}$ 

$$Z_0 = \frac{(R + j\omega L)}{k} = \sqrt{\frac{(R + j\omega L)}{(G + j\omega C)}}$$

(2.37)

#### Impedance for lossless transmission line

$$Z_0 = \sqrt{L/C}$$



**Figure 2-23** Terminated transmission line at location z = 0.

How to avoid reflections and have good signal propagation?

#### **Reflection coefficient**

z = -l

Z,

Impedance for z = 0:

$$Z(0) = \frac{V(0)}{I(0)} = Z_0 \frac{1 + \Gamma_0}{1 - \Gamma_0} = Z_L \quad = \text{load impedance}$$
$$\Gamma_0 = \frac{Z_L - Z_0}{Z_L + Z_0}$$

#### Various terminations

$$\Gamma_0 = \frac{Z_L - Z_0}{Z_L + Z_0}$$

Open line → reflection with equal polarity

$$Z_L = \infty \Longrightarrow \Gamma_0 = 1$$

#### **Short circuit**

 $\rightarrow$  Reflection with inverse polarity

$$Z_L = 0 \Longrightarrow \Gamma_0 = -1$$

No reflection when:

$$Z_0 = Z_L \Longrightarrow \Gamma_0 = 0$$

→ "MATCHING"
# Interpretation of S-parameters



<i>S</i> <sub>11</sub>	=	$\frac{b_1}{a_1}\Big _{a_2 = 0} = \frac{\text{reflected power wave at port 1}}{\text{incident power wave at port 1}}$	(4.42a)
<i>S</i> <sub>21</sub>	=	$\frac{b_2}{a_1}\Big _{a_2 = 0} \equiv \frac{\text{transmitted power wave at port 2}}{\text{incident power wave at port 1}}$	(4.42b)
<i>S</i> <sub>22</sub>	=	$\frac{b_2}{a_2}\Big _{a_1 = 0} \equiv \frac{\text{reflected power wave at port 2}}{\text{incident power wave at port 2}}$	(4.42c)
<i>S</i> <sub>12</sub>	Ξ	$\left. \frac{b_1}{a_2} \right _{a_1 = 0} \equiv \frac{\text{transmitted power wave at port 1}}{\text{incident power wave at port 2}} \right.$	(4.42d)

### Q-value

- Q-factor characterizes loss due to power dissipation in elements
- Q should be as high as possible to reduce Insertion loss
  - Quality factor fundamentals (definition)

$$Q = 2\pi \frac{\text{max imum ins tan t energy stored in circuit}}{\text{energy dissipated per cycle}}$$

Characterize power loss due to dissipation mechanisms in reactive elements.



#### Relation between Q-factor and oscillator stability

• Q-factor is critical for RF circuit performance!



#### Benefits and typical characteristics of RF MEMS switches



### Two basic switch configurations



Varadan fig. 3.2

# **Basic switch structures**

### Series switch

- Contact switch, ohmic (relay) \*
  - Cantilever beam
- Capacitive switch ("contact less")
  - RF-signals short-circuited via C ( Z=1/j $\omega$ C )
    - Impedance depends on value of C

### Shunt switch

- Shunt capacitive switch \*
  - clamped-clamped beam (c-c beam)
- Shunt contact switch

### Series switch



Rebeiz fig.2.12

## Typical shunt switch





Figure 4.1. Illustration of a typical MEMS shunt switch shown in cross section and plan view. The equivalent circuit is also shown [6] (Copyright IEEE).



## **Electromechanical operation**

- The operation is based on the **pull-in** effect
  - Characteristics at pull-in
    - Membrane/beam pulls in at 1/3 of gap
    - Pull-in voltage:

$$V_{PI} = \sqrt{\frac{8K}{27\varepsilon_0 Ww}} g_0^3$$

- Definition of parameters:
  - K spring constant
  - g0 initial gap
  - A=W\*w = area

# Hysteresis

 A capacitive switch shows hysteresis when being switched on/off



# Deflection of beam

- Suppose the following approximations:
  - Actuation electrode is not deflected
  - Electrostatic force concentrated at the end of the flexible beam with length L



$$w(x) = \frac{FL}{2EI} x^{2} \left(1 - \frac{x}{3L}\right)$$

Max. deflection at x = L

$$w(L) = \frac{L^3}{3EI} \cdot F$$

Beam stiffness represents a spring with spring constant k\_cantilever

Compare with

$$F = k_{cantilum} \cdot \Delta W$$

$$w_{max}$$

$$k_{cantilum} = \frac{F}{W(L)} = \frac{3EI}{L^3} \cdot \frac{1}{4} E \cdot W \left(\frac{H}{L}\right)^3$$

# Switch speed and damping

- Switch speed depends of damping
  - Air, gas must be pushed/pulled
  - "squeezed-film damping"
  - Method of modeling from fluid dynamics
- How to reduce damping?
  - Operate in vacuum
    - Hermetic sealed packages
  - Make holes in membrane
    - Perforated membrane

# Switch speed

- Damping influences Q-factor
- Switch-speed depends of Q-factor
  - High Q-factor means small damping
    - $\rightarrow$  increased switch speed
  - Low Q-factor means large damping
    - System is damping-limited when Q ≤ 0.5 [Castaner and Senturia]

### Gap vs. Time for various Q-factors



Figure 3.3. Pull-down simulations for the Au and Al beams of Table 3.1 for an applied voltage of 42 V ( $V_s = 1.4V_p$ ).

### Acceleration limited switch



Figure 3.5. Simulated switching times for the Au beam given in Table 3.1. "AL" means acceleration-limited and is given by Eq. (3.23).

Note: The system becomes more acceleration limited when damping decreases (eg. Q-factor increases). High Vs/Vp is good.

# Switch speed for increased Vs

- Switch-speed strongly depends on actuation voltage, Vs
  - Vs is usually larger than Vpi
  - Vs = const \* Vpi (pullin) = ("actuation voltage")
  - Larger voltage gives larger electrostatic force
    - → increased switch speed



Figure 3.4. Pull-down simulations for the Au beam of Table 3.1 versus the applied voltage, and Q = 1.

#### **RF** modeling: Shunt configuration



 $S_{II} = S_{22} = \Gamma = \frac{Z_L - Z_0}{Z_L + Z_0} = \frac{Z_s / Z_0 - Z_0}{Z_s / Z_0 + Z_0} = \frac{-Z_0}{2Z_s + Z_0}$ 

 $S_{12} = S_{21} = 1 + i7 = 1 + \frac{-Z_0}{2Z_s + Z_0} = \frac{2Z_s}{2Z_s + Z_0}$ 

$$\frac{Shunt suitch}{Return loss} (up-otate) \qquad Z_{s} \approx \frac{1}{jwc}$$

$$S_{II} = \frac{-Z_{o}}{2Z_{s} + Z_{o}} = \frac{-Z_{o}}{2 \cdot \frac{1}{jwc} + Z_{o}} = \frac{-jwCZ_{o}}{2 + jwCZ_{o}}$$

$$|S_{II}|^{2} = S_{II} \cdot S_{II}^{*} = \frac{(wCZ_{o})^{2}}{4 + (wCZ_{o})^{2}}$$

$$\frac{Return loss}{2S_{s} + Z_{o}} = \frac{-Z_{o}}{2(R+jwL+\frac{1}{jwc}) + Z_{o}} = \frac{-jwCZ_{o}}{(2-2w^{2}Lc) + jw(2R+CZ_{o})}$$

$$|S_{II}|^{2} = S_{II} \cdot S_{II}^{*} = \frac{(wCZ_{o})^{2}}{(2-2w^{2}Lc) + jw(2R+CZ_{o})^{2}}$$

Series contact caphilever suitch  

$$OFF (up-state)$$

$$= \frac{\int_{z_{o}}^{L} \int_{z_{o}}^{C_{1}} \int_{z_{o}}^{C_{1}} Z_{s} = jwL + \frac{1}{jwc}$$

$$S_{II} = S_{22} = \Pi = \frac{Z_{L} - Z_{o}}{Z_{L} + Z_{o}} = \frac{(Z_{s} + Z_{o}) - Z_{o}}{(Z_{s} + Z_{o}) + Z_{o}} = \frac{Z_{s}}{2Z_{o} + Z_{s}}$$

$$S_{12} = S_{21} = 1 - P = 1 - \frac{Z_s}{2Z_0 + Z_s} = \frac{2Z_0}{2Z_0 + Z_s}$$

# Phase shifter

• A phase shifter is a 2-port



- Output signal is delayed relative to the input signal
- The effective "path-length" of the transmission line can be changed
  - Signal propagates a longer distance → "delayed" → phase change
  - Phase difference can be controlled by a DC bias

# Analog phase shifters

Phase velocity for a transmission line

$$v_p = \frac{1}{\sqrt{L_t \cdot C_t}}$$

- Variables are inductance and capacitance per unit length
- Idea: C-value can be controlled by a bias voltage
  - For example by shunt capacitive loaded line



Figure 5.1 Schematic of analog phase shifter.

De Los Santos

Ct = line capacitance

#### Digital phase shifters with series-switches



- Working principle
  - Different line paths connected in/out
  - Interconnections through switches
- Switches for "180°, 90°, 45°, 22.5°, 11.25° -sections in a cascade arrangement
- Several bits used
  - Controlling line sections individually
  - F.ex. 3 bits:  $45/90/180^{\circ}$  give phase shift 0, 45, 90, 135, ...,  $315^{\circ}$
  - 3 bit and 4 bit phase shifters have been demonstrated

### Reflection type phase shifter, N-bit



(a)



Figure 9.1. A reflect-line N-bit phase shifter using (a) shunt and (b) series switches.

# Vibrating MEMS resonators

- Vibrating resonators can be scaled down to micrometer lengths
  - Analogy with IC-technology
- Reduced dimensions give mass reduction and increased spring constant → increased resonance frequency
- Vibrating MEMS resonators can give high Q-factor
  - Reduced insertion loss (BP-filters)
  - Reasons for Q degradation for MEMS resonators
    - Energy loss to substrate via anchors
    - Air/gas damping
    - Intrinsic friction
    - Small dimensions (low stored energy compared to energy loss)

### **Comb-resonator**

- Fixed comb + movable, suspended comb
- Using folded springs, compact layout
- Total capacitance between combs can be varied
- Applied voltage (+ or -) generates electrostatic force between left anchor comb and "shuttle"-comb. Plate pulled left laterally controlled by drive voltage



**Figure 7.9** Illustration of a micromachined folded-beam comb-drive resonator. The left comb drive actuates the device at a variable frequency  $\omega$ . The right capacitive-sense-comb structure measures the corresponding displacement by turning the varying capacitance into a current, which generates a voltage across the output resistor. There is a peak in displacement, current, and output voltage at the resonant frequency.

# Comb-resonator, summary

- Summary of modeling:
- Force: Fe = <sup>1</sup>/<sub>2</sub> dC/dx V <sup>2</sup> (force is always attractive)
  - Input signal Va \* cos ( $\omega$ t)
  - Fe ~ Va<sup>2</sup> \* ½ [1 + cos (2ωt)]
  - Driving force is 2x input frequency + DC: NOT DESIRABLE
- Add DC bias, Vd
  - Fe ~ Vd ^2 + 2 Vd \* Va \*  $\cos \omega t$  + negligible term (2 $\omega t$ )
  - Linear AC force-component ~ Vd \* Va, has same frequency as Va: ω. Is emphasized!
- C increases when finger-overlap increases
  - $\epsilon * A/d$  (A = comb thickness \* overlap-length)
- dC/dx = constant for a given design (linear change, C is proportional to length variation)

## Feedback $\rightarrow$ oscillator

- Structure can have
   2 output ports
  - Feedback is isolated from any variation of output load
  - Ex. 16.5 kHz
    oscillator, Q =
    50.000 in vacuum



Fig. 8: System level schematic for the µresonator oscillator.



Fig. 9: SEM of a fully monolithic high-Q CMOS micromechanical resonator oscillator.









## Conversion between energy domains

 Both vertical and lateral resonator structures may be described by a generalized non-linear capacitance, C, interconnecting energydomains

Electrical domain



Mechanical domain

Interconnecting where there is **no energy loss** 

#### Interconnecting different energy domains

- 1. Each energy domain is transformed to its electrical equivalent
- 2. Domains are interconnected by a generalized nonlinear capacitance, C
- 3. Transformer and gyrator may be used for interconnecting if a linear relationship exists between the power-variables!
  - Problem: Transducer C is generally **NOT** a linear 2-port
- 4. Must linearize the 2-port transducer to be able to substitute it with a transformer
- 5. The transformer can "be removed" by recalculating the component **values** to **new** ones
  - − → Electromechanical coupling coefficient used! = turn ratio
  - $\rightarrow$  Results in a common circuit diagram




#### Similarly for relationship between FLOWS:



flow (electrical domain) = - const. \* flow (mechanical domain)





#### Both methods result in the same equivalent circuit:



### Beam resonator

- How to obtain a higher resonance frequency than that which is possible with the comb-structure?
  - Mass should be reduced more -> beam resonator
- Beam resonator benefits
  - Smaller dimensions
  - Higher resonance frequency
  - Simple
  - Many frequency references on a single chip
  - Frequency variation versus temperature is more linear over a broader temperature range
  - Integration with electronics possible  $\rightarrow$  lower cost

### Beam-resonator, contd.

- Electrode under beam, electrostatic actuation
- Plate attracted for both positive and negative wave. Actuated with double frequency
  - $\rightarrow$  Need a polarization voltage, Vd, between beam and actuation electrode
  - As for "lateral shuttle": When Vd is combined with ac-signal, then beam oscillates with same frequency as ac signal
  - At resonance the amplitude is maximum



**Figure 7.10** Illustration of a beam resonator and a typical circuit to measure the signal. The beam is clamped on both ends by anchors to the substrate. The capacitance between the resonant beam and the drive electrode varies with the deflection.

### Clamped-clamped beam



Figure 12.4. Perspective-view schematic of a clamped-clamped beam µmechanical resonator in a general bias and excitation configuration.

Then

$$F_{d} = \left(\frac{1}{2}V_{p}^{2} - V_{p}V_{i}\cos\omega_{i}t + \frac{1}{2}\frac{V_{i}^{2}}{2} + \frac{1}{2}\frac{V_{i}^{2}}{2}\cos 2\omega_{i}t\right)\frac{\partial C}{\partial x}$$
$$F_{d} = \frac{\partial C}{\partial x}\left(\frac{V_{p}^{2}}{2} + \frac{V_{i}^{2}}{4}\right) - V_{p}\frac{\partial C}{\partial x}V_{i}\cos\omega_{i}t + \frac{\partial C}{\partial x}\frac{V_{i}^{2}}{4}\cos 2\omega_{i}t$$

Off-resonance DC force Static bending of beam

Force driven by the input frequency, amplified by  $V_P$ 



Ε.

# Topology



Figure 12.9. Resonator cross-sectional schematic for frequency-pulling and impedance analysis.

#### Simplification (De Los Santos):

Assume that the beam is flat over the electrode

Potential energy

 $U_1 = \frac{1}{2} C V_p^2$ 

Work being done to move the beam a distance g AGAINST the force due to the electrical beam stiffness k\_e (The spring stiffness is now considered to be CONSTANT in each pont y')

$$U_2 = \int_0^g k_e \cdot x \cdot dx = \frac{1}{2}k_e \cdot g^2$$

The energies can be set equal

Simplified expression for the electrical beam stiffness

$$\frac{1}{2}k_e \cdot g^2 = \frac{1}{2}C \cdot V_p^2$$
$$k_e = \frac{C \cdot V_p^2}{g^2}$$

#### Simplified expression for frequency

$$f = \frac{1}{2\pi} \sqrt{\frac{k_m - k_e}{m_r}} = \frac{1}{2\pi} \sqrt{\frac{k_m}{m_r}} \left(1 - \frac{k_e}{k_m}\right)$$
$$= \frac{1}{2\pi} \sqrt{\frac{k_m}{m_r}} \cdot \sqrt{1 - \frac{k_e}{k_m}} = f_{nom} \cdot \sqrt{1 - \frac{C \cdot V_p^2}{k_m \cdot g^2}}$$

Substitute for C:

$$C = \varepsilon_0 \cdot \frac{A}{g}$$
$$f = f_{nom} \cdot \sqrt{1 - \frac{\varepsilon_0 \cdot A \cdot V_p^2}{k_m \cdot g^3}}$$

## **Beam-softening**

Resonance frequency decreases by

$$\sqrt{1-C_0\cdot V_P^2/(k_m\cdot g^2)}$$

# - → resonance frequency may be tuned electrically!

$$f_o = \frac{1}{2\pi} \sqrt{\frac{k_r}{m_r}} = 1.03 \kappa \sqrt{\frac{E}{\rho}} \frac{h}{L_r^2} [1 - g(V_P)]^{1/2}, \qquad (12.2)$$

## "free-free-beam"

- f-f-beam is suspended with 4 support-beams in widthdirection
  - Torsion-springs
  - Suspension points at nodes for beam "flexural mode"
- Support-dimension is a quarter-wavelength of f-fbeam resonance frequency
  - The impedance seen at the nodes is infinite preventing energy propagating along the beam to the anchor
  - Beam is free to vibrate as it was not anchored
  - Beneficial for reducing energy loss via anchors to substrate



Fig. 29. SEM of free-free beam virtually levitated micromechanical resonator with relevant dimensions for  $f_o = 71$  MHz.

Nguyen, 1999

#### **Increasing the Resonant Frequency**

option 2. spring rate  $\rightarrow \infty$ 



## **Disk resonators**

- Advantages of using disks compared to beams
  - Reduced air damping
    - Vacuum not needed to measure Q-factor
  - Higher stiffness
    - Higher frequency for given dimensions
  - Larger volume
    - Higher Q because more energy is stored
    - Less problems with thermal noise
- Periphery of the disk may have different motional patterns
  - Radial, wine-glass

### Micromechanical filter: 3 \* resonators



**Figure 12.12.** (a) Equivalent lumped-parameter mechanical circuit for a mechanical filter. (b) Corresponding equivalent *LCR* network.



### 2-resonator HF-VHF micromechanical filter



## Design

At centre frequency fo and bandwidth B, spring constants must fulfill

$$B = \left(\frac{f_0}{k_{ij}}\right) \cdot \left(\frac{k_{sij}}{k_r}\right)$$

- $k_{ij}$  = normalized coupling coefficient taken from filter cook books • Ratio  $\left(\frac{k_{sij}}{k_r}\right)$  important, NOT absolute values
- Theoretical design procedure \*
- (\* can not be implemented)
  - Determine  $f_0$  and  $k_r$  Choose  $k_{sij}$  for required B
  - I real life this procedure is modified

## Design procedures c-c beam filter

- A. Design resonators first
  - This will give constraints for selecting the stiffness of the coupling beam
  - $\rightarrow$  bandwidth B can not be chosen freely! or
- B. Design coupling beam spring constant
  - Determine the spring constant the resonator must have for a given B
  - $\rightarrow$  this determines the coupling point!

# Design procedure B

- B1. Use coupling points on the resonator to determine filter bandwidth
  - B determined by the ratio

$$\frac{k_{s12}}{k_{rc}}$$

- $k_{rc}$  is the value of k at the **coupling point!**
- $k_{rc}^{rc}$  position dependent, especially of the **speed** at the position
- $k_{rc}$  can be selected by choosing a proper coupling point of resonator beam!
- The dynamic spring constant  $k_{rc}$  for a c-c beam is largest nearby the anchors
  - $k_{rc}$  is larger for smaller speed of coupling point at resonance

### Position of coupling beam



Figure 12.15. Filter schematics showing (a) maximum velocity coupling to yield a large percent bandwidth and (b) low-velocity coupling to yield a smaller percent bandwidth.

#### **Mixer** -filter



Figure 12.18. (a) Simplified block diagram of a wireless receiver, indicating (with shading) the components replaceable by mixer-filter devices. (b) Schematic diagram of the described  $\mu$ mechanical mixer-filter, depicting the bias and excitation scheme needed for downconversion. (c) Equivalent block diagram of the mixer-filter scheme.

## Passive components in RF circuits

- $\rightarrow$  MEMS capacitors and inductors
  - Relevant as replacements for traditional "off-chip" passive components
  - Tuneability and programability are desired

#### MEMS capacitors

- Simple, tunable capacitances
  - = varactor ("variable reactor")
- Programable capacitance banks with fixed C

### MEMS inductors

- Simple, fixed inductors
- Programable inductance banks with fixed L

# **Tunable RF MEMS capacitors**

- Electrostatic actuation is a dominating mechanism for tuning
  - Low power consumption, simple
- Vertical electrostatic displacement
  - Tuning the gap (non-linear change) in parallel plate capacitor
    - 2-plate capacitance
    - 3-plate capacitance
    - Double air-gap capacitance
    - Other examples
- Horizontal (lateral) displacement
  - Tuning of area (linear change)
- Thermal tunable MEMS capacitance
- Piezoelectric actuator tunable capacitance
- Tuning by change of **dielectric** material

### Challenges for RF MEMS capacitors

- ÷ Tuning ratio for MEMS varactors is small
  - 1.2 2.5
  - For semiconductor varactors: 4 6
  - − → Obtain required Tuning Ratio (TR)
    - Definition TR:  $C_{\text{max}}/C_{\text{min}}$
    - Should be > 2
- HEMS is sensitive to various noise effects present for low spring constant, k
  - Low k is desired for 3 5 V applications
  - Is a challenge due to
    - Acceleration, RF power self actuation, noise effects

### Two-plate tunable MEMS capacitance

- Young & Boser, Berkeley
- Gap-tuning
- One plate can move by electrostatic actuation
- Equilibrium between elastic and electrical forces



### 3-plate tunable MEMS capacitance

- TR can be increased by introducing a 3rd plate
  - A. Dec & K. Suyama: "Micromachined Electro-Mechanically Tunable Capacitors and Their Applications to RF IC's" 1998.
     Columbia University



# Double air-gap capacitance

- J. Zou et al, 2000, Univ of Illinois
- Why double air-gap?
  - Increase TR
    - Eliminate pull-in effect
  - May deflect down to 1/3 d<sub>2</sub>
    before pull-in
  - TR may increase significantly if 1/3 \*d<sub>2</sub> > d<sub>1</sub>
    - Eg. centre electrode can be fully deflected without pull-in!



Comb-like (inter-digital) tunable MEMS capacitors

Deflection: x = V<sup>2</sup> (dC/dx) / 2k

FSRM



#### Design and fabrication

(Rockwell Science Center):

- Comb-like structure using single mask process
- Deep anisotropic silicon etching technique in ICP (inductively coupled plasma) reactor
- Very flexible design: large range of C and TR

#### Figures of merit:

- TR= 200% C<sub>max</sub>=3.2pF, C<sub>min</sub>=6.44pF, V=5V
- Recent results show: Q > 40-160 @ 400-1600MHz

J.J. Yao, S. Park and J. DeNatale, Solid-State Sensor and Actuator Workshop, Hilton Head Island, SC, 1998, pp. 124-127.

Idea: area-tuning capacitor





Ionescu, EPFL

## **RF MEMS inductors**

- Two-dimensional (planar) inductors
- Three-dimensional inductors, solenoids
- Only fixed-value inductor can be implemented
  No practical implementation of tunable inductors exist
- Variable inductance values: implemented as inductor bank
  - Many inductors with fixed, high Q-value
  - In combination with MEMS contact switches

## Planar inductors, in general

- Implemented in a single plane
- One metal layer patterned by etching
- Inductor rest on a substrate covered by a dielectric
- Loss in inductor due to:
  - Finite metal conductivity
  - Loss in dielectric
  - Loss in substrate
- Area limitations for RF
  - Total length of an inductor has to be significantly shorter than the wavelength
    - Gives then negligible phase shift of signal

metal	
dielectric	
substrate	

### Different planar geometries

- Distance between lines is critical
- Circular spiral has a shorter length than a quadratic spiral
  - $\rightarrow$  Lower R
  - Q is about 10% higher with same "diameter", do
- Higher Q achieved by increasing number of turns per area
  - Self resonance frequency decreases due to the increase in capacitance → limits the region of use



**Figure 4.3** Schematic diagram of common planar inductors: (a) meander; (b) loop; (c) circular spiral; (d) square spiral; (e) symmetric spiral; (f) polygon spiral

### General model for a planar inductor

 $C_{p1}$ 

Ls is low frequency inductance

Rs is series resistance

Cs is capacitance between windings

C1 is capacitance in oxide layer between inductor and substrate

Cp is capacitance to ground through substrate

Rp is "eddy current" loss in substrate



 $C_{S}$ 

 $\leq R_{p1}$ 

Rs

 $C_{p2}$ 

 $\gtrsim R_{p2}$ 

**Figure 12.1.** (a) The equivalent LRC model of a planar inductor. (b) A short-circuited inductor model typically used in S-parameter and Q measurements.  $C_{p1}$  and  $C_{p2}$  are often assumed identical and equal to  $C_p$ .

## Various design parameters

- Structure – 2D or 3D, form
- Line spacing
- Line width
- Number of turns
- Magnetic core
- Metal thickness
- Sheet resistance
- Thickness of dielectrics
- Substrate resistivity
#### Summary: How to increase performance?

- Have thick metal layer with good conductivity
  To reduce series resistance
  - To reduce series resistance
- Use substrate etching

Reduce substrate parasitic capacitance

• Use **3-D** structures

- For vertical plane solenoids the L-value may increase

• Use of core material

#### Out of plane inductors

- Inductor can be elevated by "scratch actuators"
  - L. Fan et al, MEMS 1998
  - Elevated 250 µm over Si substrate
  - Resonance at 1.8 6.6 GHz after elevation of solenoid





**Figure 4.31** (a) Schematic diagram of the MESA micro-elevator by self-assembly structure; (b) the center platform can move upward or downward. Reproduced from L. Fan, R.T. Chen, A. Nepolsa and M.C. Wu, 1998, 'Universal MEMS platforms for passive RF components: suspended inductors and variable capacitors', in *Proceedings of 11th Annual International Workshop on MEMS '98*, IEEE, Washington, DC: 29–33, by permission of IEEE, © 1998 IEEE

#### Micromachining using self-assembly

Elevate inductor above substrate to reduce parasitic capacitance

Cr-Au layer over polylayer

Different residual **stress** in materials make the inductor "**curl**" above substrate

Anchor causes a significant parasitic capacitance



Figure 12.12. Picture (a) and measured Q (b) of a self-assembled 1.2-nH inductor [20] (Copyright IEEE).

#### Programmable inductor banks



# Purpose of packaging

- For secure and reliable interaction with environment packaging is needed
- Package:
  - Is a mechanical support
  - Has **signal connections** to the physical world
  - Provides heat transport
  - Gives environmental protection
  - Makes **contact** with environment possible
    - Pressure sensor
    - Liquid system

## Different packages used

- Important issues
  - Package size, form, number of pins
  - Package material
- Different package types
  - Ceramic packages
  - Metal packages
  - Polymer packages
- Package can be combined with a 1. level encapsulation
  - Die level encapsulation: "microcaps"
  - Interesting if MEMS does not need direct contact with liquids and gasses

## Integration of IC and MEMS

- Separate MEMS- and IC-dies can be impractical and costly
  - Often the only possibility
    - Due to different technology requirements
  - + MEMS and CMOS may then be individually optimized
  - Parasitic capacitances, impedances!
  - $\rightarrow$  One-chip solution desired! (monolithic integration)
- Technologies for monolithic integration
  - Pre-circuits (Pre-CMOS)
  - Mixed circuit- and micromechanics (Intermediate CMOS)
  - Post-circuits (Post-CMOS)

## Pre-CMOS circuits

- Fabricate micromechanics first, then IC
- Benefits
  - May fabricate MEMS optimally
  - Only one passivation step needed after micromechanics processing
  - Upgrade each process module individually
- Drawbacks
  - Large topography variations present after MEMS (ex. of 9  $\mu$ m)
  - CMOS photo resist spinning and patterning become more difficult
    - Especially for submicron circuits
    - CMOS and MEMS have different minimum geometries!
  - Must make the surface planar before CMOS processing
  - CMOS foundry processes do not allow "dirty" MEMS wafers into the fabrication line

## Mixed circuit- and micromechanics

- IC and MEMS-processes integrated into one process
  - "MEMS in the middle"
- Drawbacks
  - Limitations on MEMS structures that can be fabricated
  - Many passivation layers needed
    - When switching between circuit and micromechanics process
  - Only custom CMOS-processes can be used
  - Total redesign of the whole process if one of the combined technologies ("modules") is changed
  - Ex. of a combination process  $\rightarrow$

## Post-CMOS circuits

- CMOS circuit processing performed **before** MEMS
  - Possibly the most promising procedure
  - Planarization not needed
  - May use advanced/standard IC foundries and succeeding micromechanical processing
  - Method gradually developed
- Drawbacks
  - Difficulties with CMOS Al-based metallization
    - Al can not withstand the high temperature steps needed for several micromechanical process steps
      - Especially those needed for high Q: f.ex. polySi deposition/annealing
  - Compromises must be done for one or both processes
    - Ex. MICS process: Tungsten ("wolfram") as CMOS metal
    - Ex. UoC Berkely: use SiGe as MEMS structure material

#### ASIMPS at CMU



micromachining; (b) CHF<sub>3</sub>/O<sub>2</sub> reactive-ion etch of dielectric stack down to the silicon substrate; (c) Deep reactive-ion etch of Si substrate (nominal 35 μm deep); and (d) Si undercut (nominal 15 μm undercut and 50 μm deep).

#### General communication system



Bit streams are modulated (coded) onto a carrier

Radio channel introduces noise, interference, disturbances

Receiver shapes the signal for demodulation

## Present technology

- Technology and components used today
  - **Discrete**, **passive** components with good properties
    - R, C, L
    - Ex. crystals, inductors
  - Such components needed due to high performance and precision requirements
  - Off-chip solutions are the result
    - PCB assembly
    - Systems take a lot of space
    - Integrated solutions not possible
  - Active components
    - Amplifiers, switches
    - GaAs, bipolar Si, CMOS Si, PIN-diodes



Itoh et al, fig 12.1

## **Benefits of MEMS substitutes**

- Reduction of dimensions
- Possible integration
  - Multi-chip
  - Monolithic
- Power reduction
- More flexibility for impedance matching of MEMS filters

- Termination impedance matched to the following LNA (Low Noise Amplifier)
  - "Higher" (than 50 Ω) LNA input impedance can be used → power reduction and reduced noise



# B. Special RF MEMS blocks

- Figure shows 3 basic blocks that are substituted by RF MEMS
  - B1. Switchable RF channel-select filter bank
  - B2. Switchable micromechanical frequency synthesizer
  - B3. Micromechanical mixer-filter block



Figure 12.21. System block diagram for an RF channel-select receiver architecture utilizing large numbers of micromechanical resonators in banks to trade Q for power consumption. (On-chip µmechanics are shaded.)

#### B1. Switchable RF channel-select filter bank

- Idea
  - Use many, simple, nontunable filters with high Q
  - One for each channel, switched on command
  - A communication standard needs 100 1000 of filters
- Block diagram
  - Common input and output
  - Controlled by Vp from decoder
    - With no Vp the outputs are effectively "open-circuited"



## **Relevant research topics**

- The architectures shown are to some extent based on resonators with performance not yet achieved
- Research topics
  - 1. Obtain required high Q at UHF
  - 2. Set specific impedance levels
  - 3. Good enough linearity and capability to sustain power
  - 4. Efficient integration methods

## Conclusion (source: Ionescu, EPFL)

- RF MEMS is a promising technology for communication applications
  - Miniaturisation of critical parts
  - Great potential for low cost
    - Co-integration with IC
  - Increased RF performance
  - Low power applications

# Conclusion, contd.

- Central features
  - Micro mechanical processing!
  - Co-design of "elektromechanical / IC" -components
  - Full circuit functionality (filtering og mixing) in one function block
  - High Q tunable passive components have been demonstrated
  - New functionality of RF circuits  $\rightarrow$  programmability
- RF IC with only MEMS components
  - Challenging goal for the research within the field
  - Vision: Low effect radio with RF MEMS blocks

## Future prospects for RF MEMS

(source: lonescu, EPFL)

- The success of RF MEMS is dependent of co-integration
  with more traditional IC technology
  - High performance and reconfigurable units can be achieved
  - SOI is promising for co-integration
- Passive RF MEMS components will probably be the first units to reach market
- RF MEMS switches will be used in more specific applications (niches)
  - Capacitive switches for > 10 GHz
  - Still much effort is needed to reach acceptable reliability and effective packaging

#### Future prospects for RF MEMS, contd.

- Resonators are very promising!
  - Such units can replace complete circuit functions
  - The technology is CMOS compatible and relatively scalable
- "Improvements in reliability and packaging during the next years will determine the impact RF MEMS will have!"