

INF 5490 RF MEMS

LN12: RF MEMS inductors

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Today's lecture

- What is an inductor?
- MEMS inductors
 - Modeling
- Different types of RF MEMS inductors
 - **Horizontal plane** inductors
 - Real **solenoids**
- How to increase performance
 - Q-value, Inductance (L), Self resonance frequency (f_{\max})
- Elevated inductors
- Inductor banks

What is an inductor?

- Inductor = a component with interaction between **magnetic** and **electric flux**
 - Magnetic field \leftrightarrow current
- Two basic laws
 - Faraday's law
 - Varying **magnetic field** induces **current**
 - Ampere's law
 - **Current** flowing sets up a **magnetic field**

Faraday's law

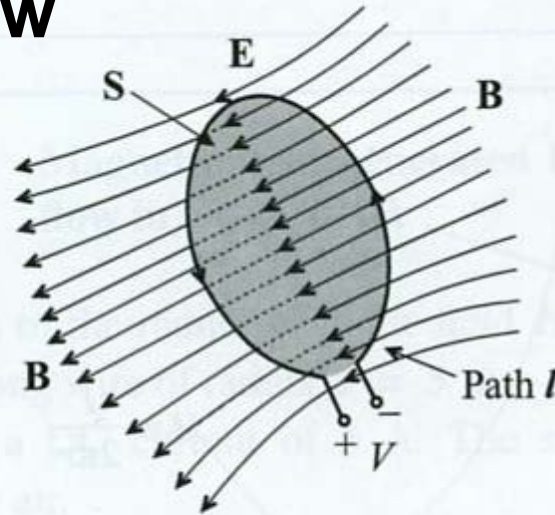


Figure 2-15 The time rate of change of the magnetic flux density induces a voltage.

$$\oint \vec{E} \cdot d\vec{l} = - \frac{d}{dt} \iint \vec{B} \cdot d\vec{S}$$

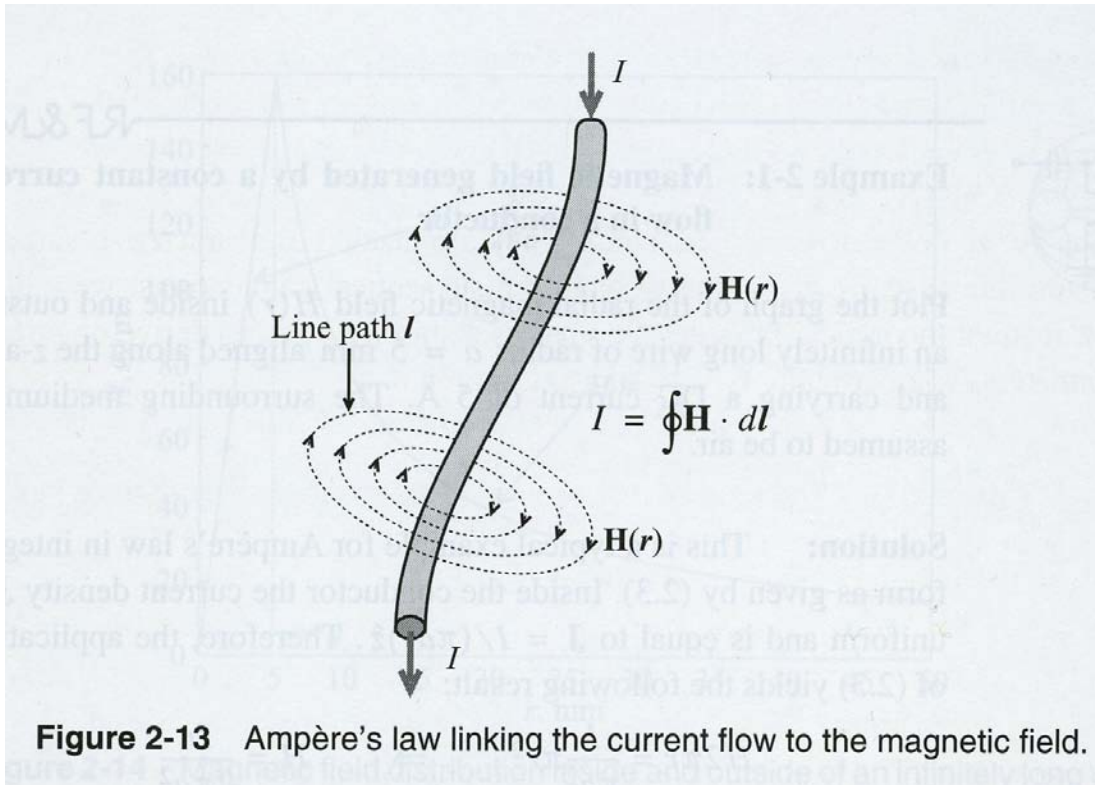
\vec{B} = magnetisk flukso-tetthet magnetic flux density

$$\vec{B} = \mu \cdot \vec{H}$$

μ = permeabilitet = $\mu_0 \cdot \mu_r$ permeability

\vec{H} = magnet felt magnetic field

Ampere's law



$$I = \oint \vec{H} \cdot d\vec{l} = \iint \vec{J} \cdot d\vec{S}$$

Inductors follow **Faraday's/Ampere's laws**

- Change of current in inductor →
- Change of magnetic field (Ampere's law) →
- Electric field induced (Faraday's law) →
- The induced electric field opposes further change in current (Lenz law)
 - **Inertia** with respect to variation: **"reactance"**
 - Mechanical analogy: **mass!**

Inductors

- Generally implemented as **solenoids**
 - 2D (in plane) or 3D
 - Several turns used to increase magnetic flux density
 - May give large inductance, L , for a small area/volume
- Basic equations
 - $V = L \, di/dt$
 - $V = L_s * I$ (Laplace)
- Solenoids in **plane** are typical for IC and MEMS

metal
dielectric
substrate

Any reason for RF MEMS inductors?

- Micromachined inductors should have better performance than today's CMOS inductors
 - MEMS may give **higher Q-values!**
 - **Q>30**
 - MEMS may give higher **L** and self resonance-frequency
- Should be CMOS compatible
 - F.ex. post processing CMOS
- Micromachined inductances not yet a commercial product

L → L, C, R -circuit

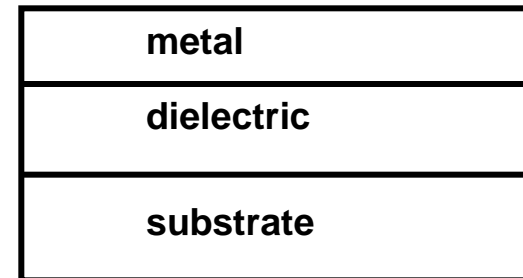


RF MEMS inductors

- Two-dimensional (planar) inductors
- Three-dimensional inductors, solenoids
- Only fixed-value inductors can be implemented
 - No practical implementation of tunable inductors exist
- Variable inductance values: implemented as an inductor bank
 - Many inductors with fixed, high Q-values
 - In combination with MEMS contact switches

Planar inductors, in general

- Implemented in a single plane
- One **metal layer** patterned by etching
- Inductor rests on a **substrate** covered by a **dielectric**
- **Loss** in inductor due to:
 - Finite metal conductivity
 - Loss in dielectric
 - Loss in substrate
- Area limitations for RF
 - Total length of an inductor has to be significantly shorter than the wavelength
 - This will give negligible phase shift of signal



Contribution to inductance

- **Self inductance** from its own winding
- **Mutual inductance** from neighbouring windings
 - Mutual coupling between neighbour lines
- Total inductance is the sum of self inductance and mutual inductance
 - In some elements current flows in the **same** direction, in others **opposite**

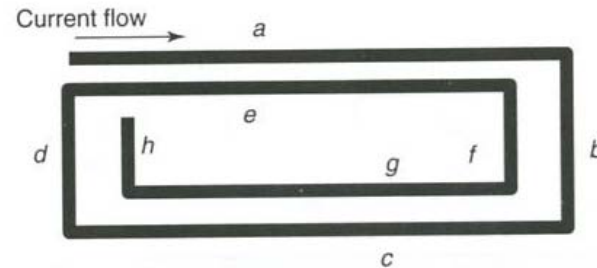


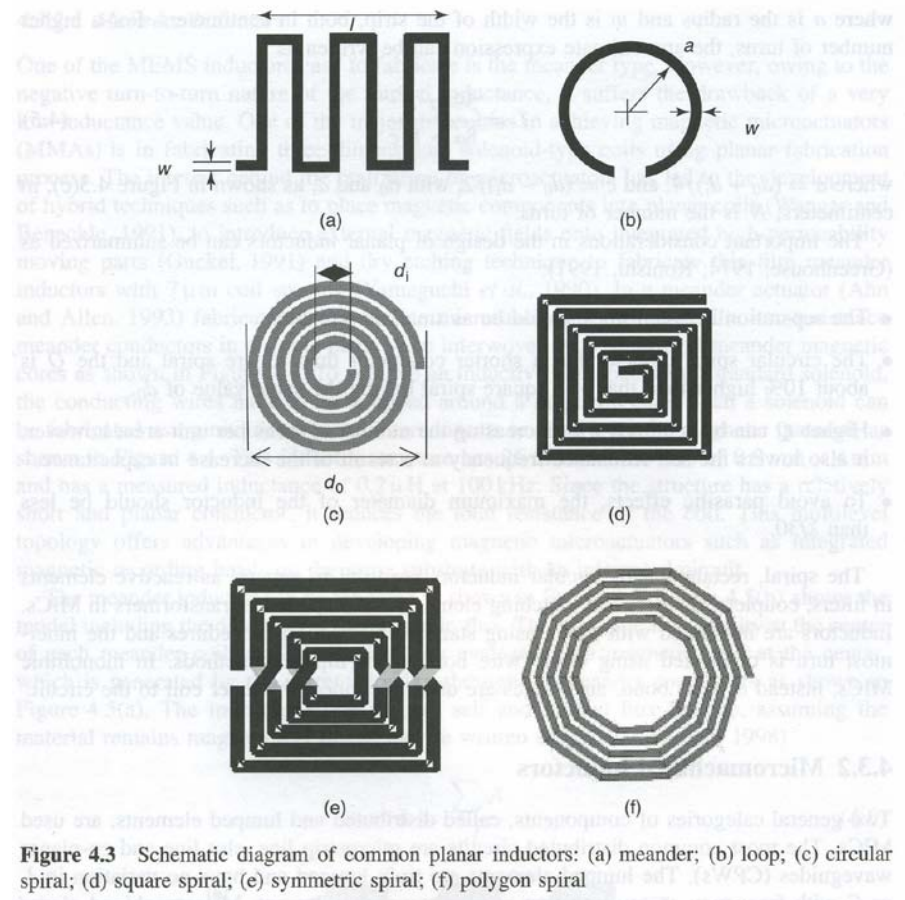
Figure 4.2 Spiral inductor and the effect of current flow in nearby segments

Different planar geometries

- Simple **line sections**
 - Each one has a low inductance value, nH
- **Meander**
 - Coupling by negative mutual inductances
- **Spiral inductors**
 - Increasing inductance, L
 - **Problem:** connecting to the **inner winding**
 - Wire bonding
 - Separate structure layer
 - Flip-chip bonding methods

Different planar geometries

- Distance between lines is critical
- Circular spiral has a shorter length than a quadratic spiral
 - \rightarrow Lower R
 - Q is about 10% higher with same "diameter", d_0
- Higher Q achieved by increasing number of turns per area
 - Self resonance frequency decreases due to the increase in capacitance \rightarrow limits the region of use



General **model** for a planar inductor

L_s is low frequency inductance

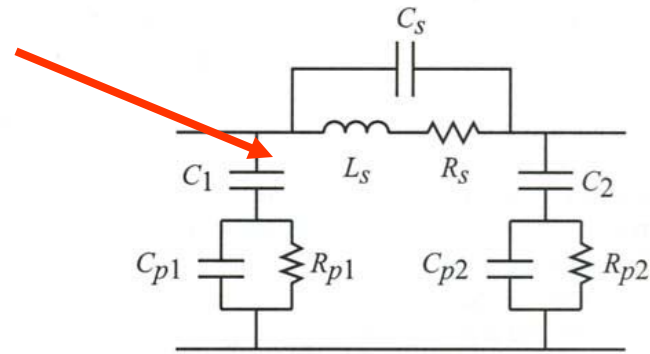
R_s is series resistance

C_s is capacitance between windings

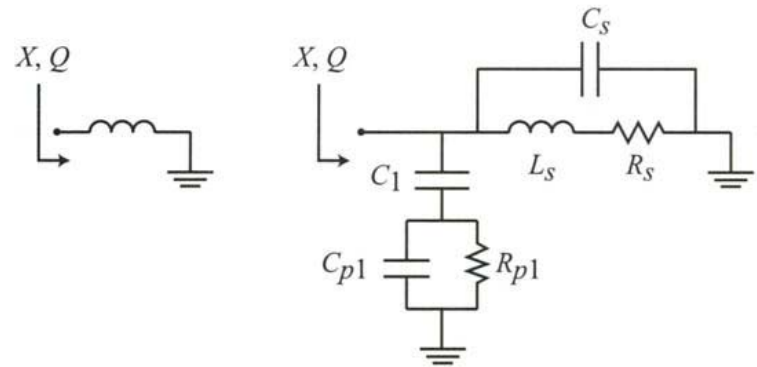
C_1 is capacitance in oxide layer between inductor and substrate

C_p is capacitance to ground through substrate

R_p is **"eddy current"** loss in substrate



(a)



(b)

Figure 12.1. (a) The equivalent LRC model of a planar inductor. (b) A short-circuited inductor model typically used in S -parameter and Q measurements. C_{p1} and C_{p2} are often assumed identical and equal to C_p .

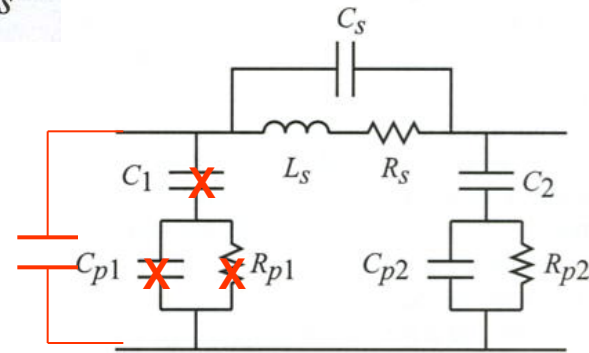
Frequency response for a planar inductor

- At low frequencies we have

$$Z = R_s + j\omega L_s \quad (12.1)$$

- At high frequencies:

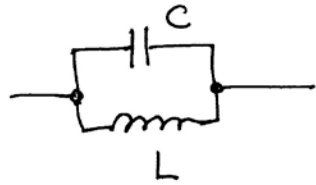
- R_{p1} is negligible
- C_1 and C_{p1} combined $\rightarrow C_p$



$$Z = (R_s + j\omega L_s) \parallel \left(\frac{1}{\omega C_s} \right) \parallel \left\{ \frac{1}{\omega C_1} + \left(\frac{1}{\omega C_{p1}} \parallel R_{p1} \right) \right\} \quad (12.2)$$

Parallel resonator

Parallell resonans



$$Z = \frac{\frac{1}{j\omega C} \cdot j\omega L}{\frac{1}{j\omega C} + j\omega L}$$

Resonans när

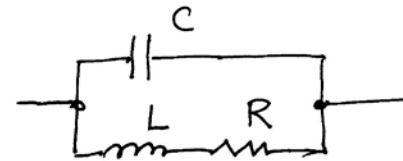
$$\frac{1}{\omega C} = \omega L$$

$$\frac{1}{j\omega C} + j\omega L = 0$$

$$Z = \infty$$

Due to parasitic capacitances a specific self resonance frequency is obtained

$$Q_{ind} = \omega L / R$$



$$Z = \frac{\frac{1}{j\omega C} \cdot (R + j\omega L)}{\frac{1}{j\omega C} + R + j\omega L} = \frac{-j\omega L (R + j\omega L)}{R}$$

$$\approx -j\omega L$$

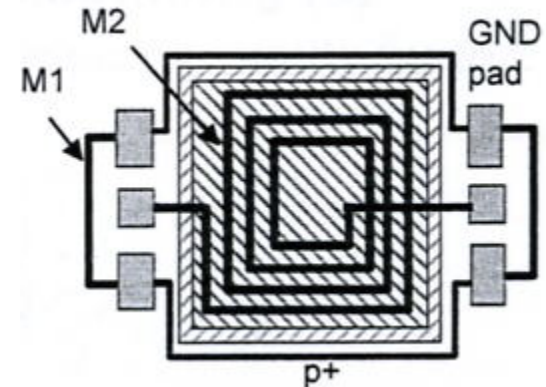
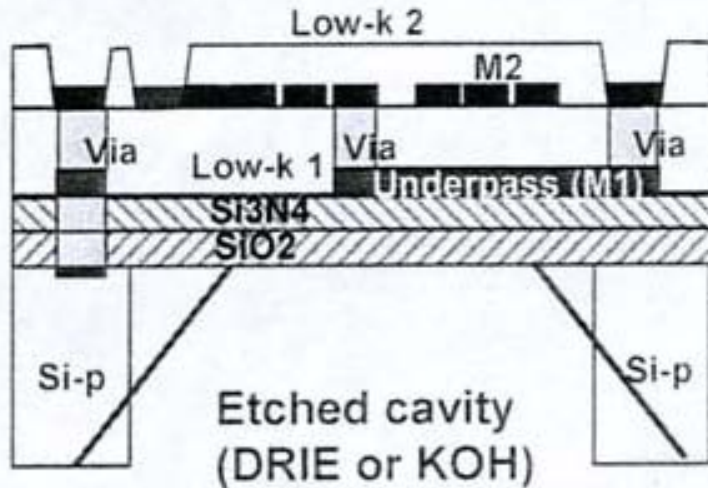
At resonance:

$$Z = \frac{\omega^2 L^2}{R} - j\omega L \approx \frac{\omega^2 L^2}{R}$$

Example: Thick copper/polyimide **horizontal-plane** inductor

Process (EPF Lausanne, WIDE-RF):

- 4-8 μm electroplated Cu in polyimide mold using Ta barriers



”Form” (”mold”) of organic material

Ex. Spiral inductor (Ahn & Allen)

- Two solenoids
- **Magnetic core** used for trapping magnetic flux
 - Must be a high permeability material
 - Ex. Varadan fig. 4.7 (Ahn & Allen) →
- Conductor from centre needed!

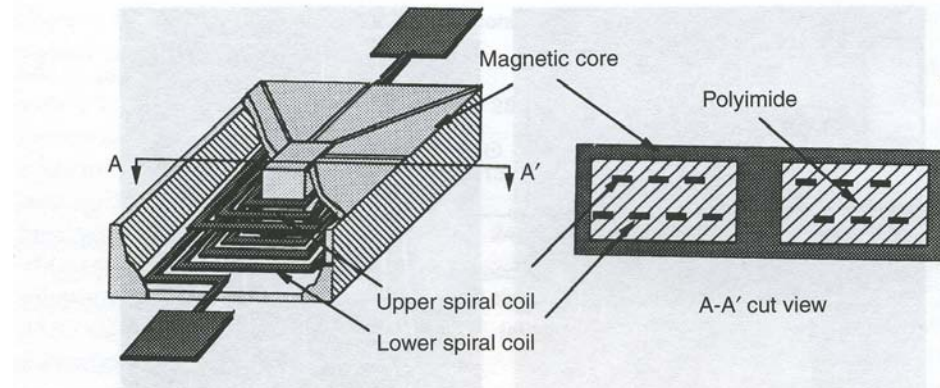


Figure 4.7 Schematic diagram of a micromachined spiral inductor. Reproduced from C.H. Ahn and M.G. Allen, 1993, 'A planar micromachined spiral inductor for integrated magnetic microactuator applications', *Journal of Micromechanics Microengineering* 3: 37–44, by permission of the Institute of Physics

Effect of magnetic core

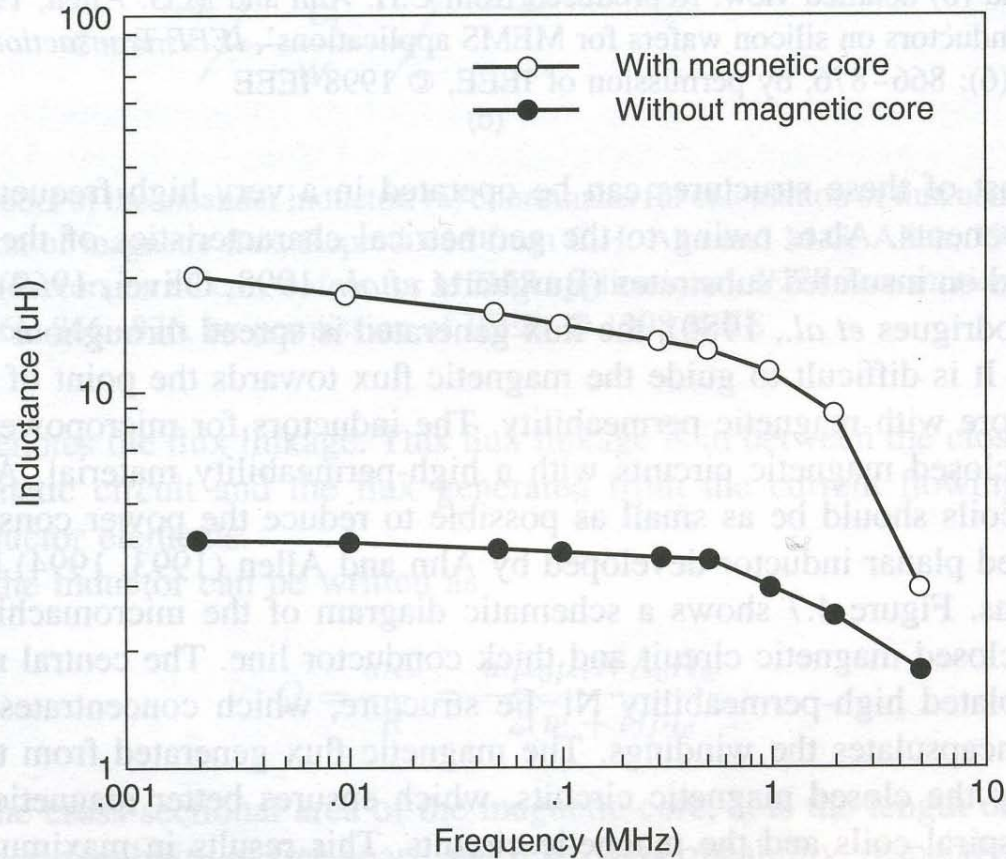


Figure 4.8 Measured inductance with and without magnetic core. Reproduced from C.H. Ahn and M.G. Allen, 1993, 'A planar micromachined spiral inductor for integrated magnetic microactuator applications', *Journal of Micromechanics Microengineering* **3**: 37–44, by permission of the Institute of Physics

Meander inductors

- Meander has lower inductance than spiral inductor
- Meander fabricated by surface processing
 - a) Metal conductor in one layer
 - Penetrated by multilevel magnetic core
 - b) Schematic of principle →
 - A magnetic core in one layer surrounded by metal turns

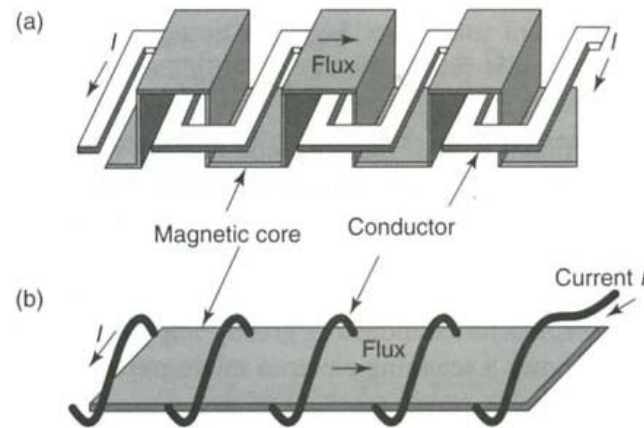


Figure 4.4 Schematic diagram of the micromachined multilevel meander inductor. Reproduced from C.H. Ahn and M.G. Allen, 1998, 'A fully integrated surface micromachined microactuator with a multilevel meander magnetic core', *Journal of Microelectromechanical Systems* 2(1): 15–22, by permission of IEEE, © 1998 IEEE

Meander fabricated (SEM picture)

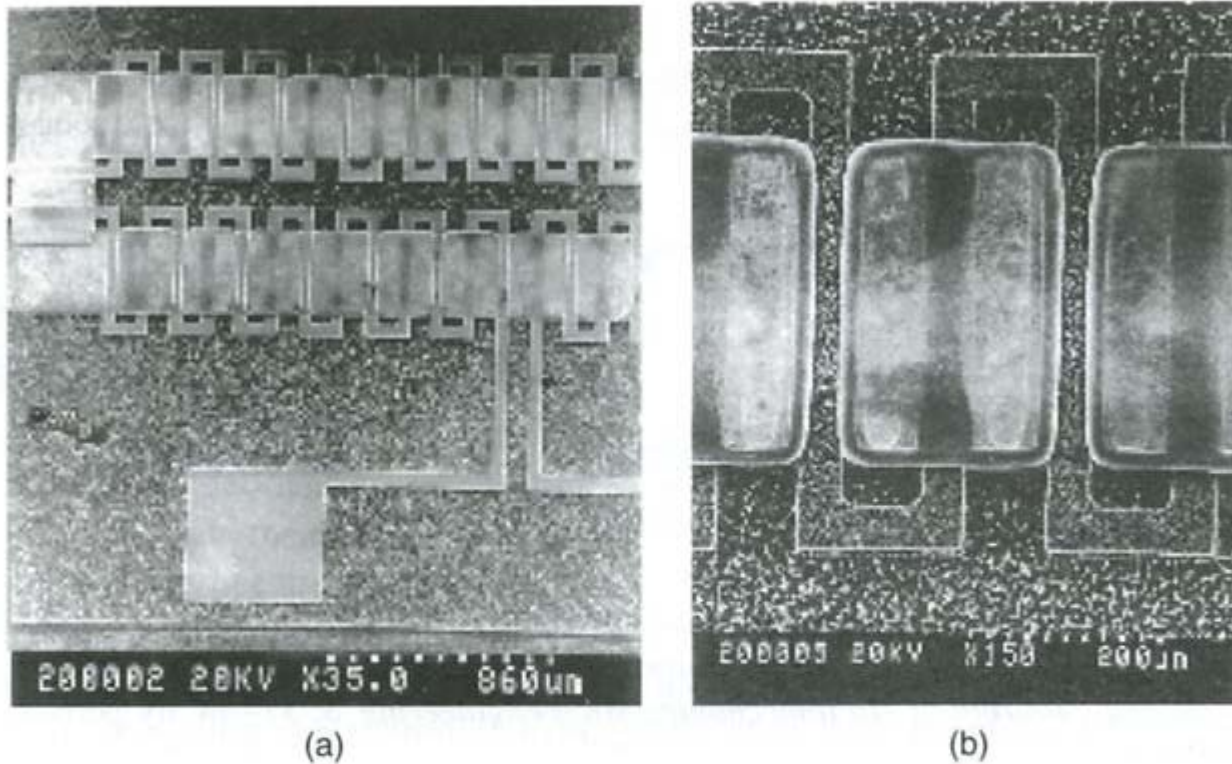


Figure 4.6 Scanning electron micrograph of the fabricated toroidal-meander inductor: (a) half of the inductor and (b) detailed view. Reproduced from C.H. Ahn and M.G. Allen, 1998, 'Micromachined planar inductors on silicon wafers for MEMS applications', *IEEE Transactions on Industrial Electronics* **45**(6): 866–876, by permission of IEEE, © 1998 IEEE

Meander: effect of different line widths

- Influence of the **line width** (C vs width)
 - "sheet resistance" is inversely proportional to w → decreases!
 - Resistance decreases if w increases, but the **capacitance increases**

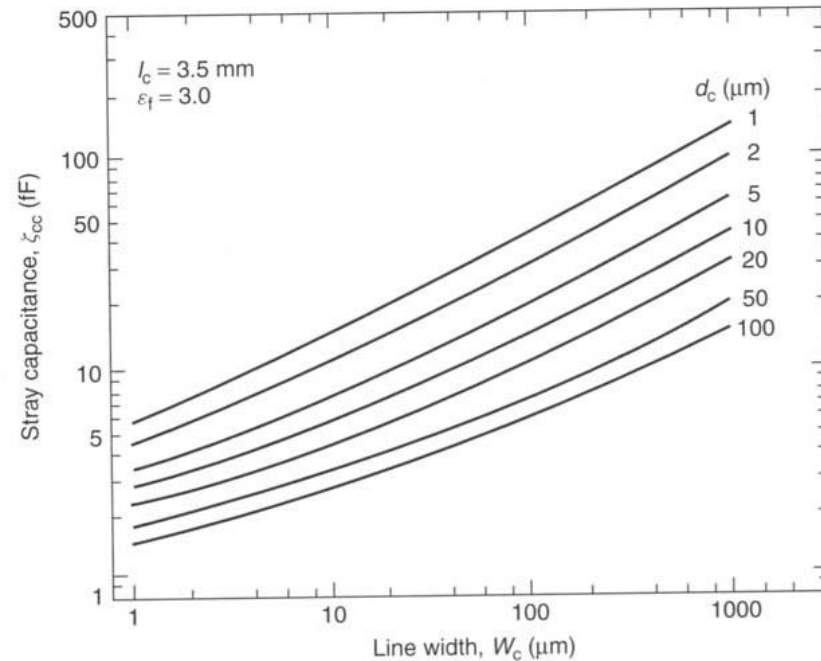
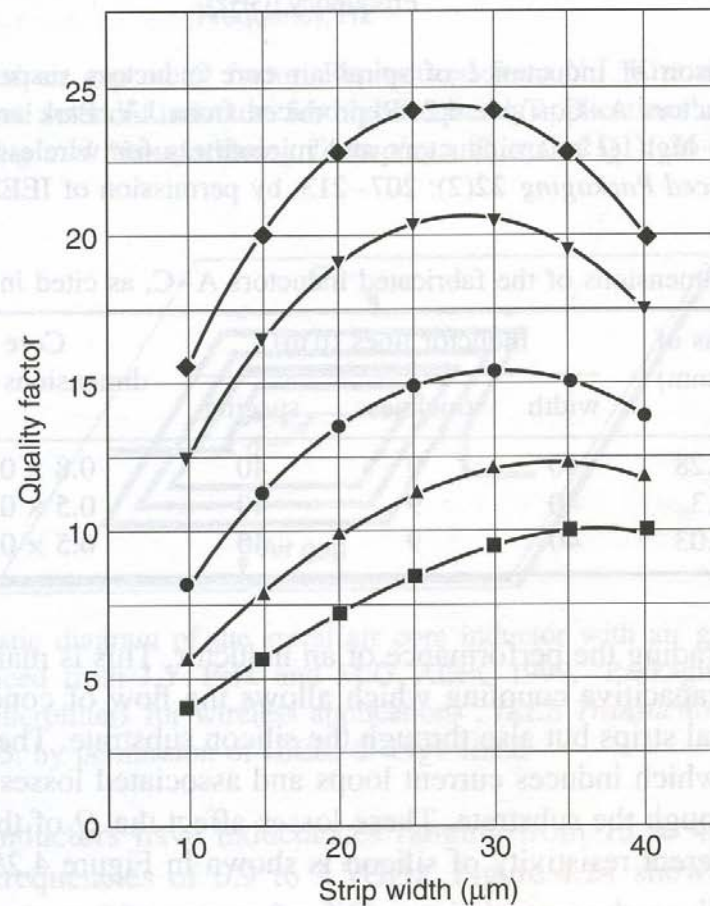


Figure 4.11 Computed stray capacitance due to change in line width W_c . Reproduced from M. Yamaguchi, M. Mastumo, H. Ohzeki and K.I. Arai, 1991, 'Analysis of the inductance and the stray capacitance of the dry-etched micro inductors', *IEEE Transactions on Magnetics* 27(6): 5274-5276, by permission of IEEE, © 1991 IEEE

d_c = distance between conductors (line spacing)

Effect of **stripe width w** on Q-factor



Optimal values of w exist for minimizing series resistance and maximizing Q

Figure 4.26 Change in Q due to change in strip width for 20-nH inductors for different frequencies: ■, 7 GHz; ▲, 1 GHz; ●, 1.5 GHz; ▼, 2.5 GHz; and ◆, 3.5 GHz. Reproduced from I.J. Bahl, 1999, 'Improved quality factor spiral inductors on GaAs substrates', *IEEE Microwave and Guided Wave Letters* 9(10): 398–400, by permission of IEEE, © 1999 IEEE

Effect of different implementations

- How **line spacing** influences L

Line spacing has different effect for spiral and meander: constructive versus destructive mutual inductance

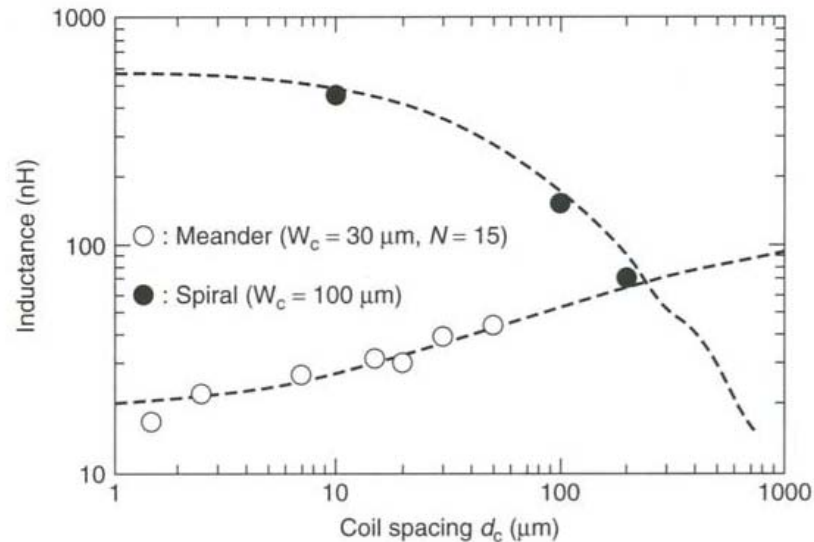
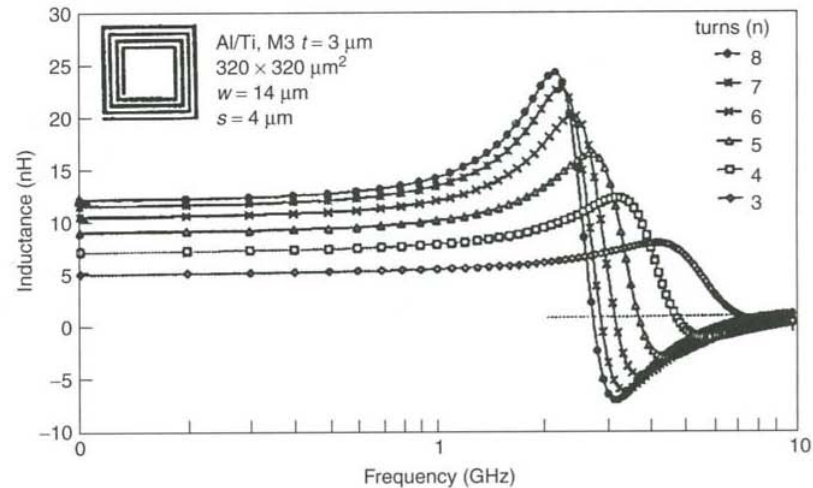
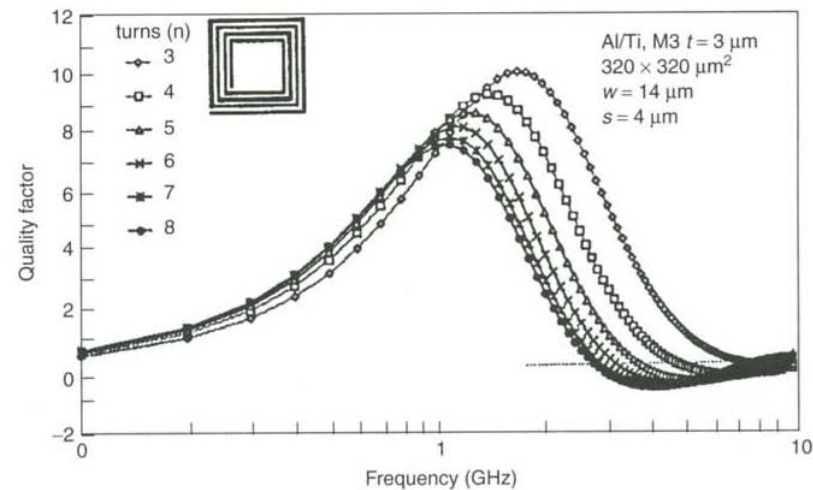


Figure 4.10 Change in inductance arising from changes in spacing between the conductors for meander and spiral inductors. Reproduced from M. Yamaguchi, M. Mastumo, H. Ohzeki and K.I. Arai, 1991, 'Analysis of the inductance and the stray capacitance of the dry-etched micro inductors', *IEEE Transactions on Magnetics* **27**(6): 5274–5276, by permission of IEEE, © 1991 IEEE

- Effect of number of turns on L and Q
- **Spiral** inductors with same dimensions
- n: 3 → 8:
 - L increases
 - Q decreases (due to increase in C)
 - f_{\max} decreases



(a)



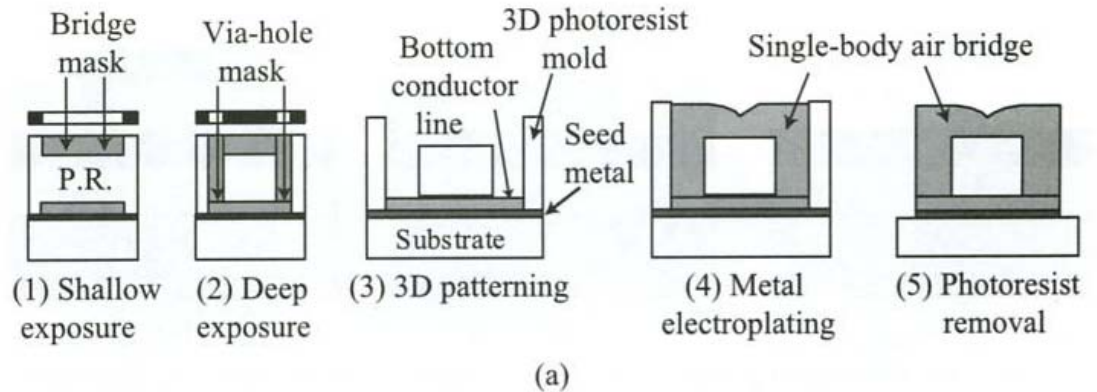
(b)

Figure 4.12 Effect of number of turns on (a) the inductance value and (b) Q factor. Reproduced from Y.K. Koutsoyannopoulos and Y. Papananos, 2000, 'Systematic analysis and modeling of integrated inductors and transformers in RF IC design', *IEEE Transactions on Circuits and Systems II* 47(8): 699–713, by permission of IEEE, © 2000 IEEE

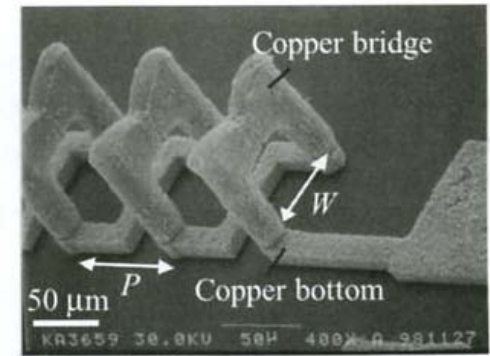
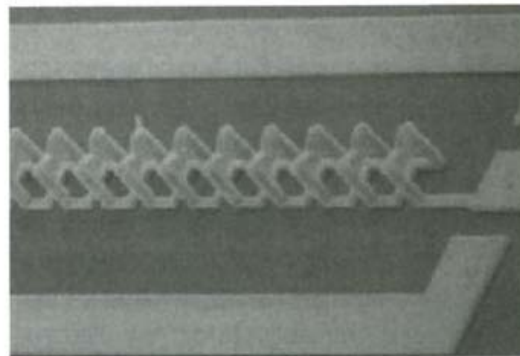
Solenoid-type inductors

- Classical example
- Process using thick **photoresist mold**

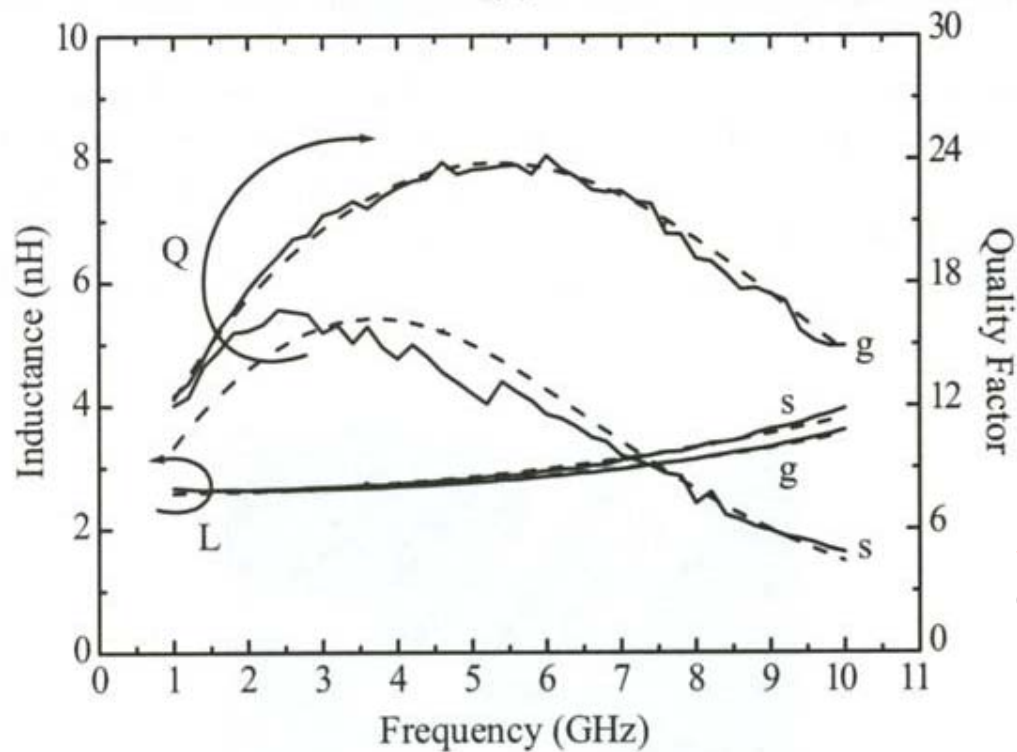
– 45 – 60 μm deep



- Top fabricated using copper: **electroplating**
 - seed + 20 – 30 μm copper layer plated on top
- Result: "loops" formed



Solenoid-type copper inductors



(c)

Figure 12.14. Fabrication process (a), picture (b), and measured performance (c) of a 2.4-nH all-copper solenoid inductor on silicon and glass substrates [24, 25] (Copyright IEEE).

Si or glass substrate give different values

Results from Yoon et al.

Example of 3-D structure

- Difficult to produce
 - Nickel-iron (permalloy) magnetic core
 - Multilevel copper + via-contacts
 - Contacts have high contact resistance
 - Need of many turns to get high L
 - More contacts → higher resistance
 - Electroplating of metal lines and via holes may reduce resistance and increase performance

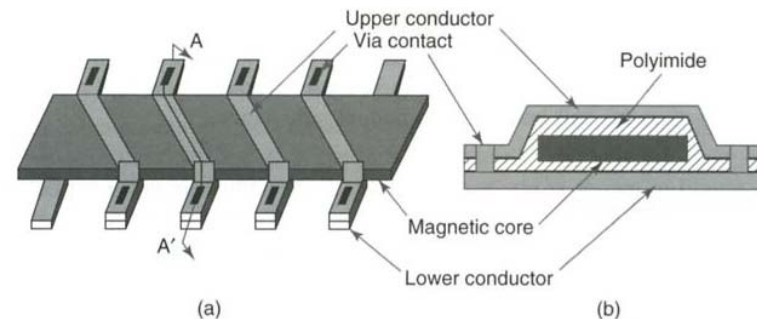


Figure 4.9 Schematic diagram of a solenoid-type inductor: (a) schematic view; (b) cross-sectional view at AA'. Reproduced from C.H. Ahn and M.G. Allen, 1998, 'Micromachined planar inductors on silicon wafers for MEMS applications', *IEEE Transactions on Industrial Electronics* 45(6): 866–876, by permission of IEEE, © 1998 IEEE

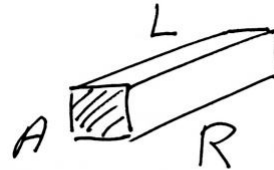
Ahn & Allen, 1998

Improving performance

- How to increase performance?
 - Q-value, Inductance (L), Self resonance frequency (f_{\max})
- Metallization is important!
 - Reduction of resistive loss!
 - Use metals with **higher conductivity**
 - Use copper, Cu, instead of Al
 - Use **thicker** structures

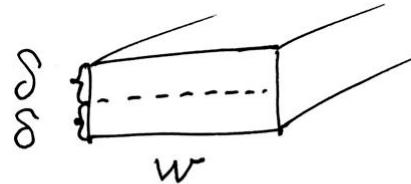
Effect of metal thickness

- Series resistance limits performance
- Simulations show that minimum thickness of **2 x "skin depth"** is needed to obtain minimum resistance



ρ = resistivity

$$R = \frac{\rho \cdot L}{A}$$



Resistance per length

$$\frac{R}{L} = \frac{\rho}{A} = \frac{\rho}{2\delta \cdot w}$$

skin depth = δ

$$\delta = \sqrt{\frac{\rho}{\pi \mu \cdot f}} \sim \frac{1}{\sqrt{f}}$$

μ = permeability
 ρ = resistivity

$$\frac{R}{L} \sim \frac{1}{\delta} \sim \sqrt{f}$$

Thick conductors needed

- For copper at 1 GHz: skin depth is about 2 μm
- One should have conductors of min 2 x skin depth thickness
 - E.g. about 4 - 5 μm for Cu
 - Thick layer!
 - Typically obtained by **electroplating**

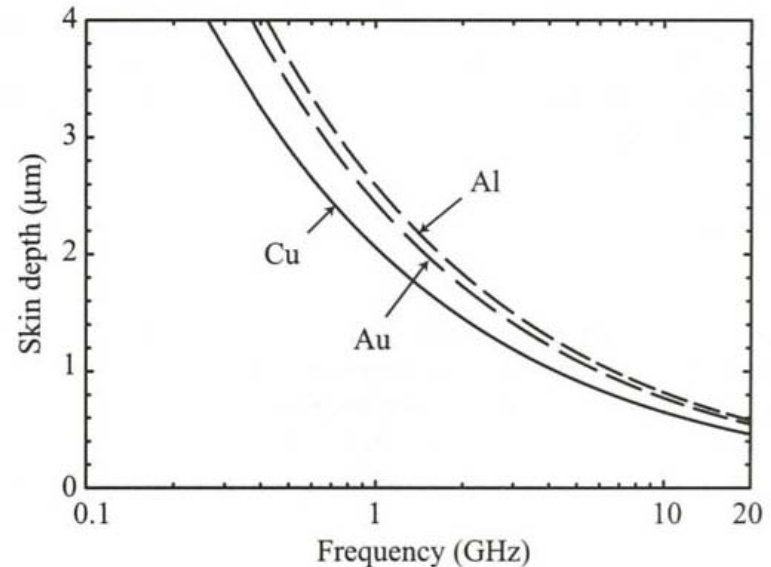


Figure 12.4. Skin depth versus frequency for copper, gold, and aluminum metal layer (bulk values of resistivities are assumed).

Change of Q versus metal thickness

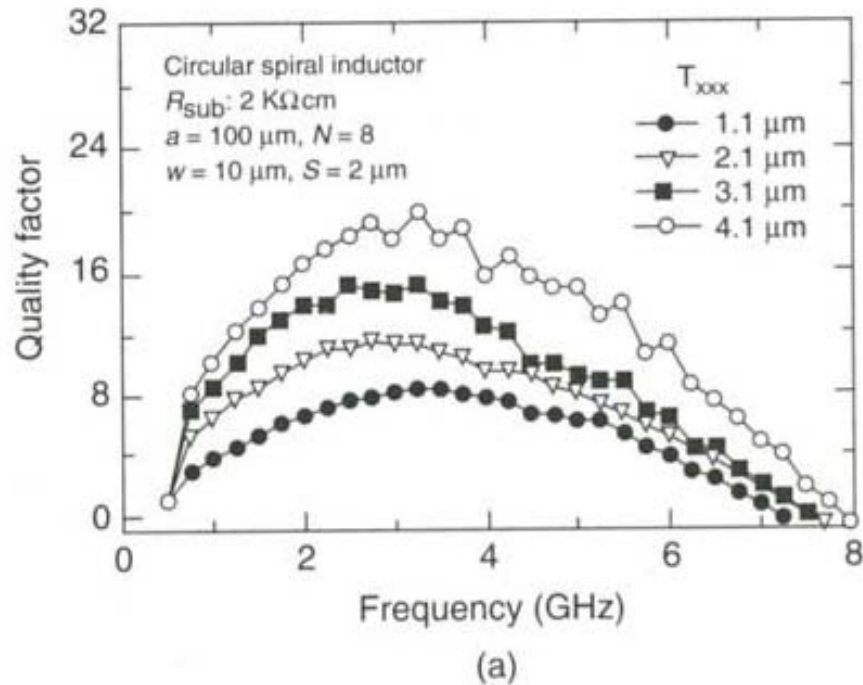
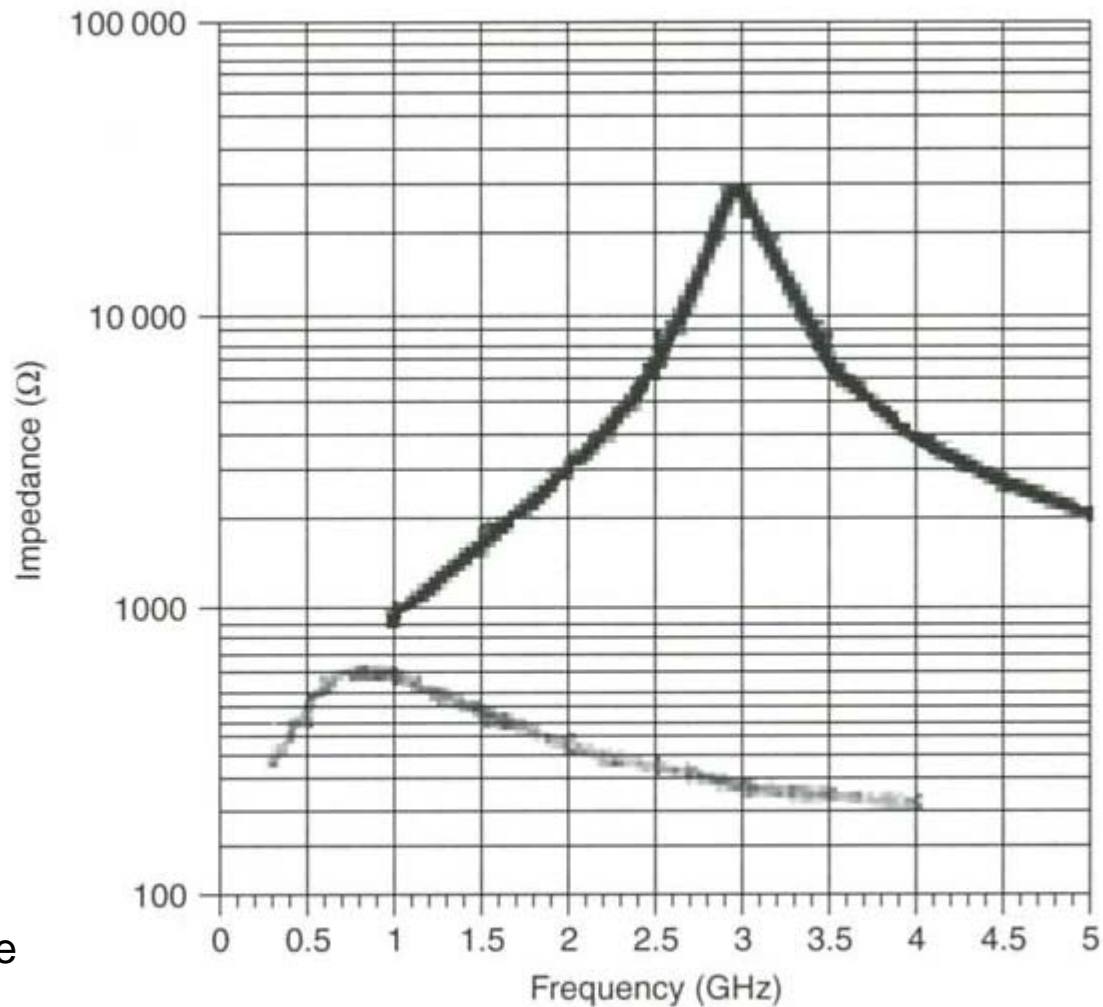


Figure 4.29 Change in Q of an inductor for (a) different metal thickness; (b) for substrates with different resistivity. Reproduced from M. Park, C.S. Kin, J.M. Park, H.K. Yu and K.S. Nam, 1997b, 'High Q microwave inductors in CMOS double metal technology and its substrate bias effects for 2 GHz RF IC application', in *Proceedings of IEDM 97*, IEEE, Washington, DC: 59–62, by permission of IEEE, © 1997 IEEE

Substrate etching

- Parasitic capacitance between inductor and ground plane is a problem
 - Depends on type and thickness of dielectric
 - Depends on type and thickness of substrate
- Solution: **etching of the underlying substrate**
 - Reduction of parasitic capacitance
 - Q increases
 - Resonance frequency is shifted to higher frequency
 - Increases the useful bandwidth of the inductor
 - High L can be implemented at the same time as avoiding a too low f_{\max}
- Alternative: elevation/suspension



With and without
underlying substrate

Figure 4.13 Simulated change in resonant frequency of 100 nH inductor with (gray) and without (black) underlying substrate. Reproduced from J.Y.-C. Chang, A.A. Abidi and M. Gaitan, 1993, 'Large suspended inductors on silicon and their use in a 2 mm CMOS RF amplifier', *IEEE Electron Device Letters* **14**(5): 246–248, by permission of IEEE, © 1993 IEEE

Ex.: Q for different etch depths

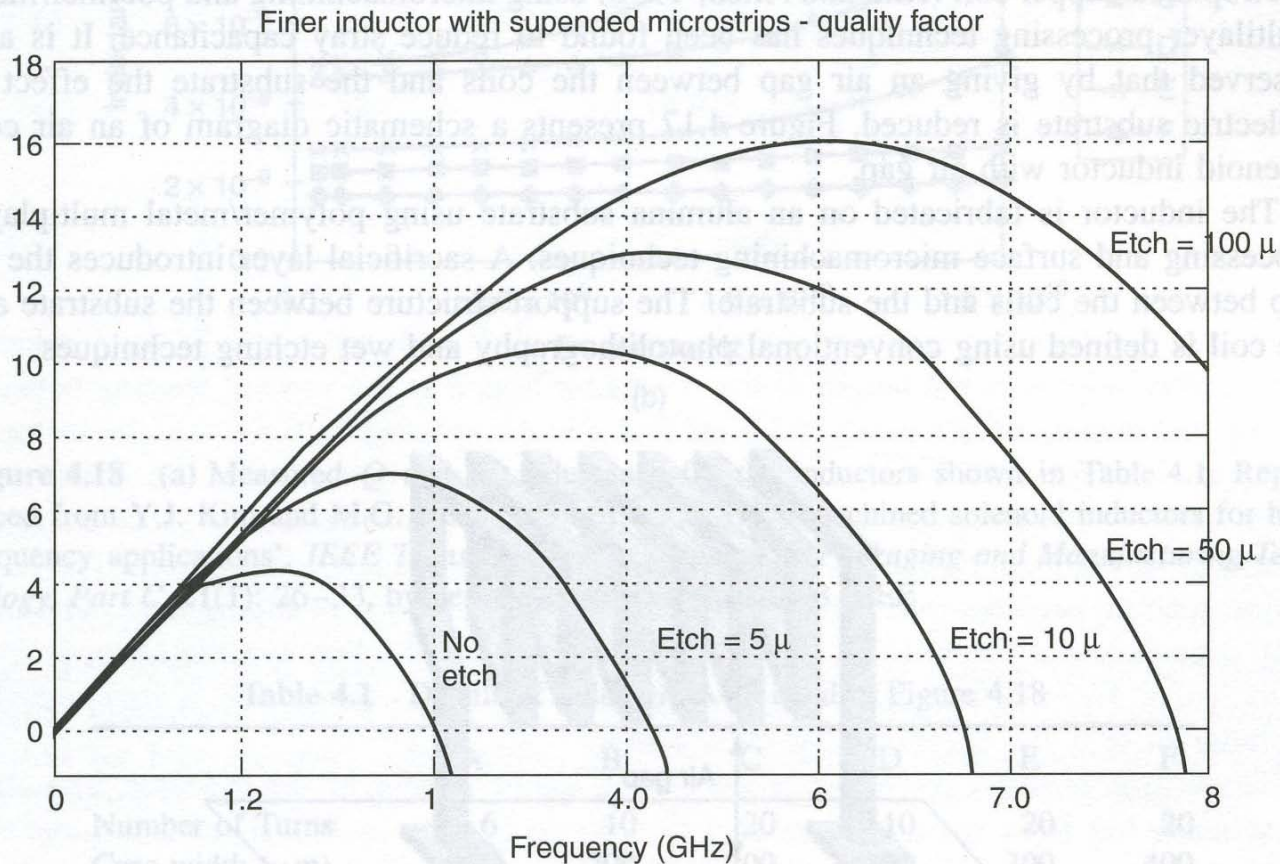


Figure 4.16 The change in Q for a suspended planar inductor for different etch depth. Reproduced from R.P. Ribas, N. Bennouri, J.M. Karam and B. Courtois, 1997, 'GaAs MEMS design using $0.2\mu\text{m}$ HEMT MMIC technology', in *Proceedings of the 19th Annual IEEE Gallium Arsenide Integrated Circuit Symposium*, IEEE, Piscataway, NJ, USA: 127–130, by permission of IEEE, © 1997 IEEE

Q-factor for substrates with different resistivities

”Eddy current”-effects are present at high frequency

High resistivity substrate increases performance

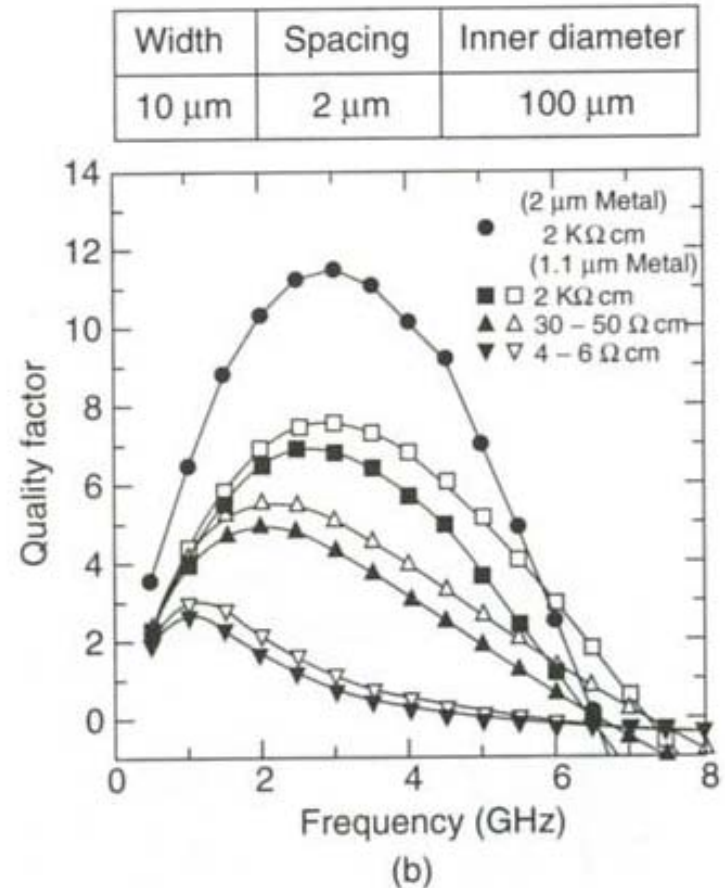
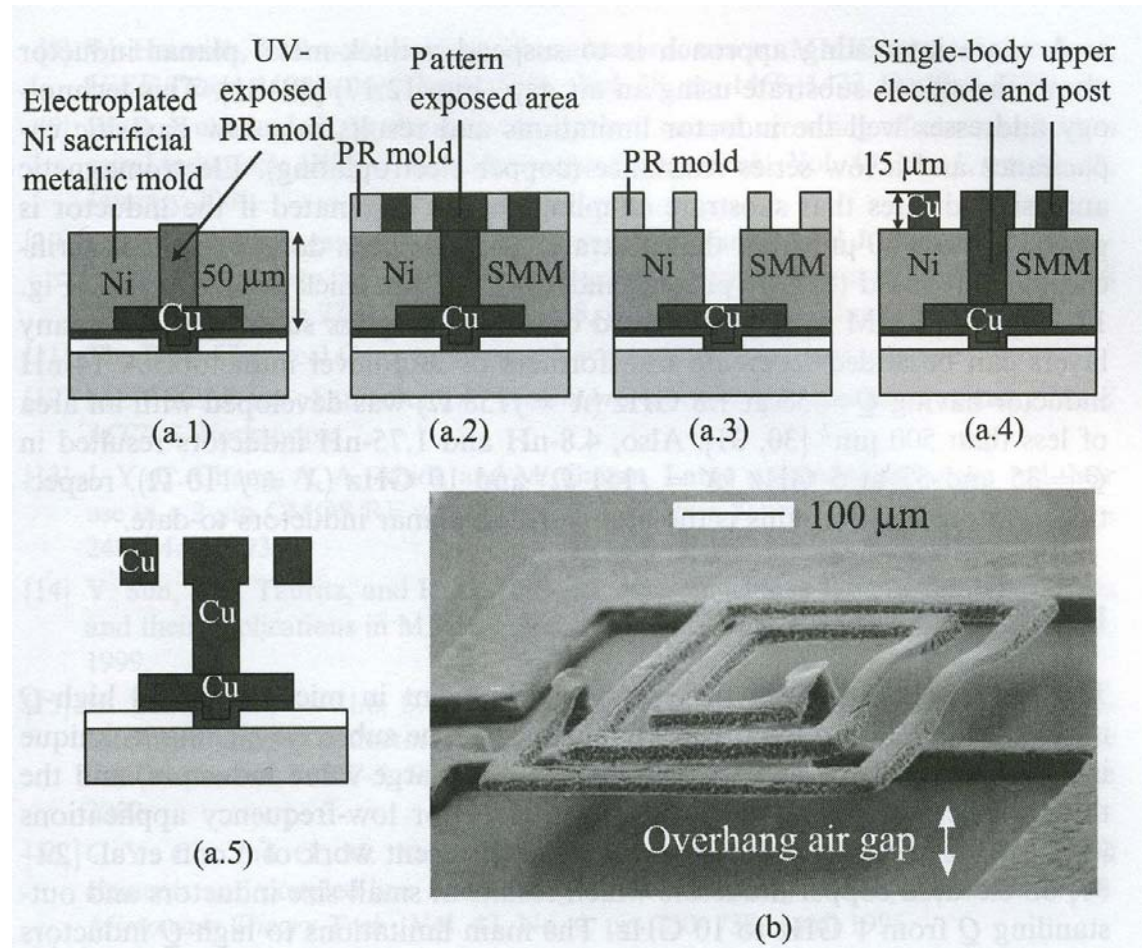


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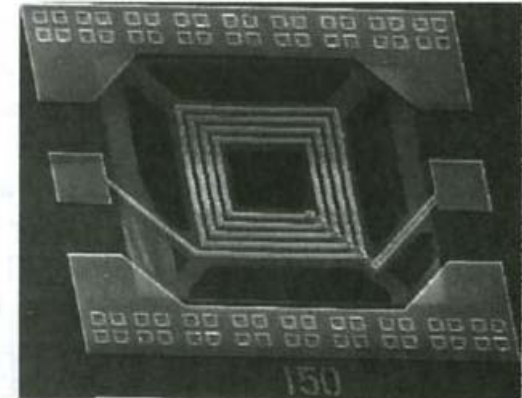
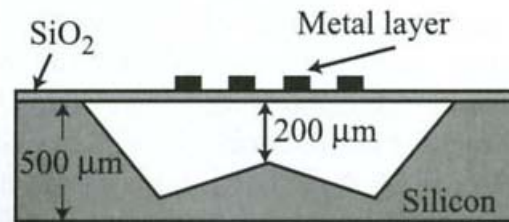
"Air gap" - inductor

- **Thick metal** planar inductor over substrate with an **air gap** in-between
 - Elimination of substrate coupling: 30 μm elevation
 - "Sacrificial metallic mold" (SMM) process used + 10-15 μm copper layer



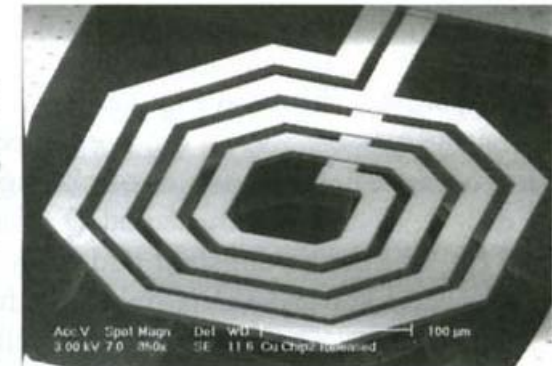
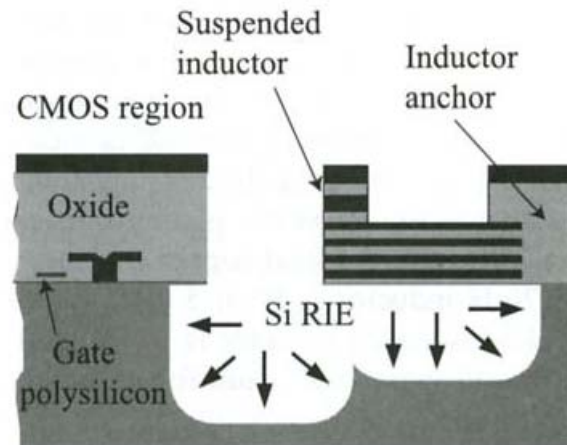
Classical examples

- Ex. from the first known work, fig 12.8 a: anisotropic etching



(a)

- Fig 12.8 b: suspended inductor
 - One anchor: sensitive to mechanical vibrations
 - $Q = 17$ at 8.6 GHz



(b)

Figure 12.8. Suspended inductors using front-etching techniques and compatible with CMOS processing: UCLA and Delft [13, 14] (a), Carnegie Mellon (b), effort [15] (Copyright IEEE).

Effect of air-gap for spiral inductors

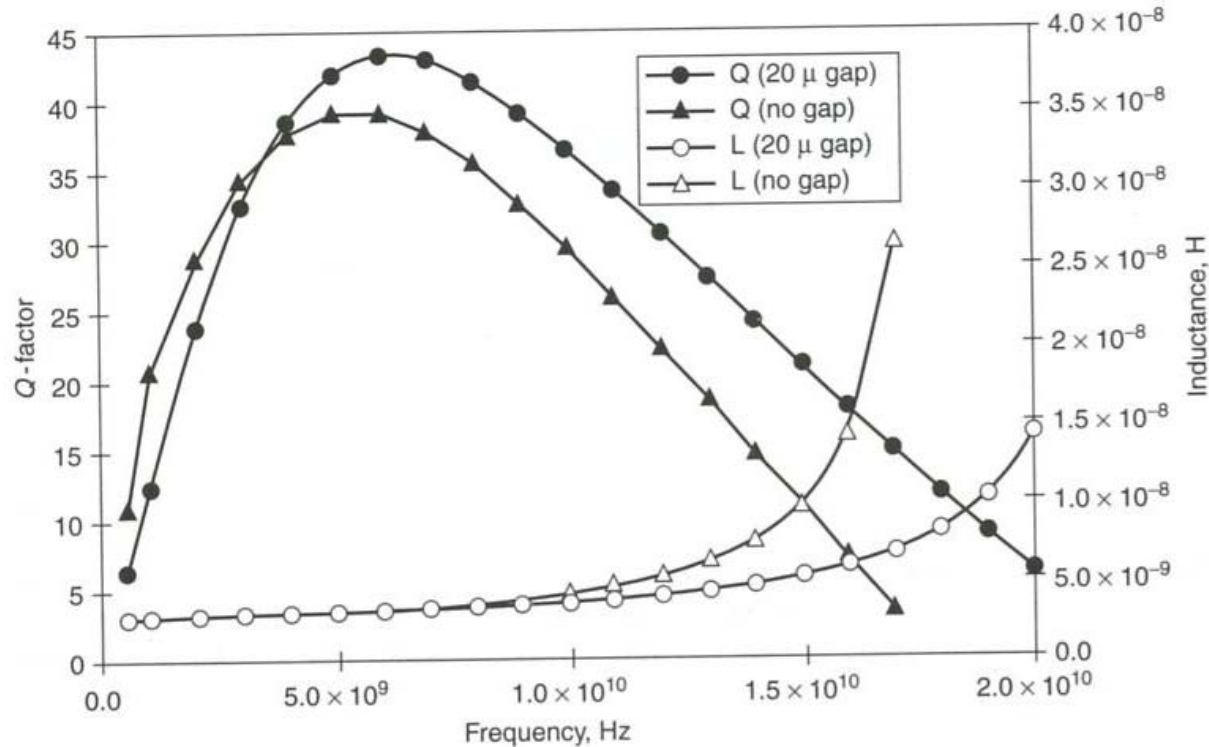


Figure 4.22 Effect of air gap on Q factor. Reproduced from Y.J. Kim and M.G. Allen, 1998, 'Surface micromachined solenoid inductors for high frequency applications', *IEEE Transactions on Components, Packaging and Manufacturing Technology, Part C* 21(1): 26–33, by permission of IEEE, © 1998 IEEE

L benefits from "no-gap" (between inductor and substrate), Q benefits from air-gap

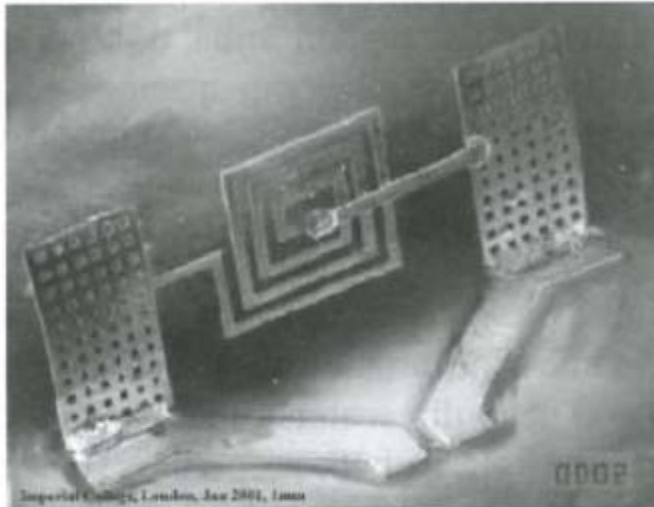
Summary: How to increase performance?

- Have **thick metal layer** with good conductivity
 - To reduce series resistance
- Use **substrate etching**
 - Reduce substrate parasitic capacitance
- Use **3-D** structures
 - For “vertical plane” solenoids the L-value may increase
- Use of **core material**

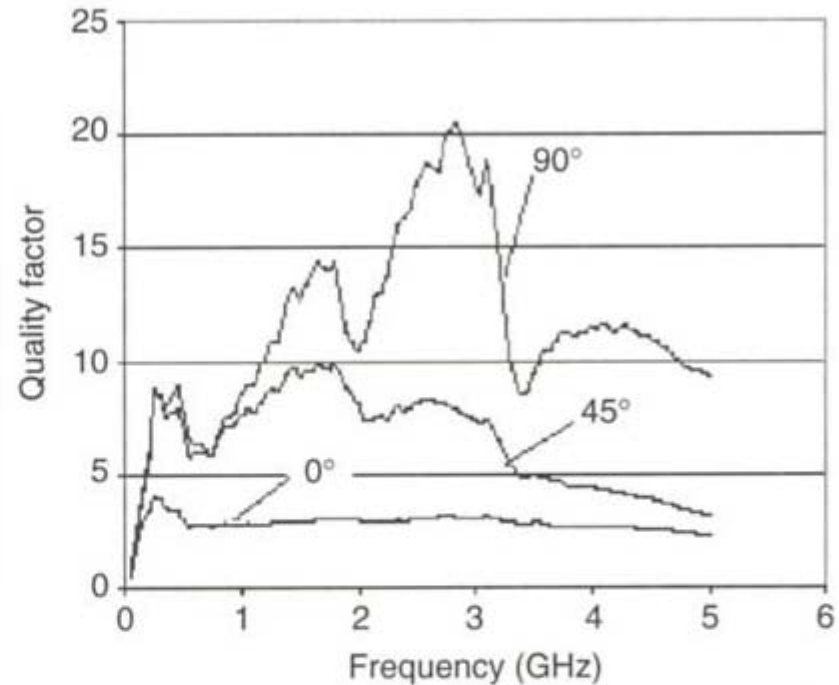
Basic implementation technologies

- Thick metal **electroplating**
 - 0.2 – 6 GHz
- **Substrate etching**
 - 1 – 100 GHz
- Three-dimensional **solenoid type** inductors
 - 0.2 – 6 GHz
- **"Self-assembly" (elevation)** of inductor →
 - Elevate inductor **above substrate** to reduce parasitic capacitance to substrate, 1 – 100 GHz

Folded and elevated inductors



(a)



(b)

Solder surface tension

Figure 4.30 (a) Three-turn spiral folded inductor after self-assembly; and (b) change in Q against frequency for different angles between coil and substrate. All devices are $4\frac{1}{2}$ -turn meander inductors ($L = 2$ nH). Reproduced from G.W. Dahlmann and E.M. Yeatman, 2000, 'High Q microwave inductors on silicon by surface tension self-assembly', *Electronics Letters* **36**(20): 1707–1708, by permission of IEEE, © IEEE 2000

Eric. Yeatman, Imperial College, London

Out of plane inductors

- Inductor can be **elevated** by "scratch actuators"
 - L. Fan et al, MEMS 1998
 - Elevated 250 μm over Si substrate
 - Resonance at 1.8 – 6.6 GHz after elevation of solenoid

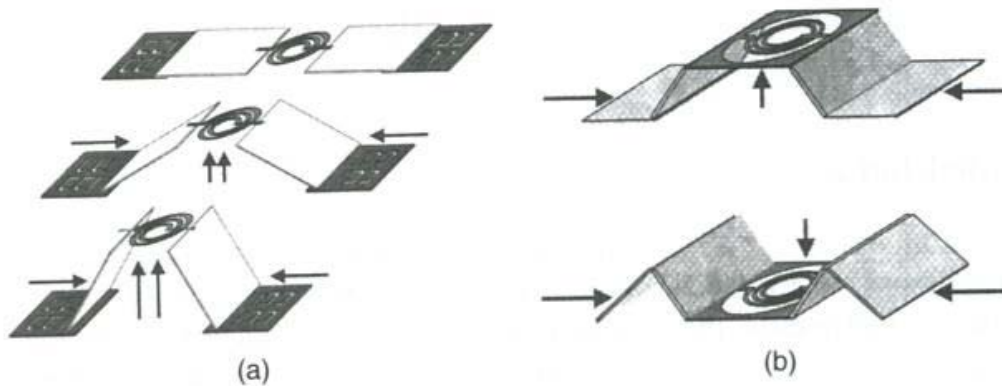
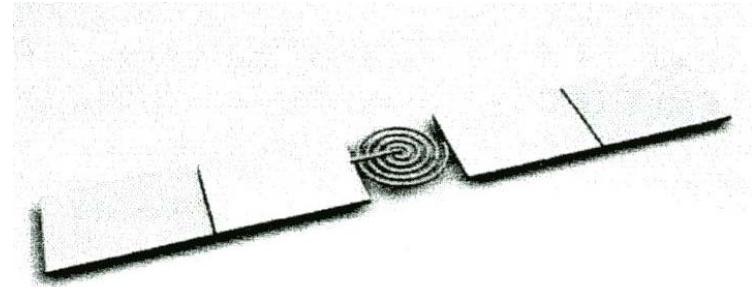


Figure 4.31 (a) Schematic diagram of the MESA micro-elevator by self-assembly structure; (b) the center platform can move upward or downward. Reproduced from L. Fan, R.T. Chen, A. Nepolsa and M.C. Wu, 1998, 'Universal MEMS platforms for passive RF components: suspended inductors and variable capacitors', in *Proceedings of 11th Annual International Workshop on MEMS '98*, IEEE, Washington, DC: 29–33, by permission of IEEE, © 1998 IEEE

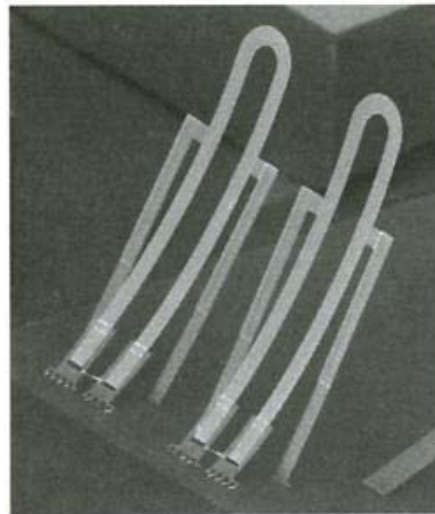
Micromachining using self-assembly

Elevate inductor above substrate to reduce parasitic capacitance

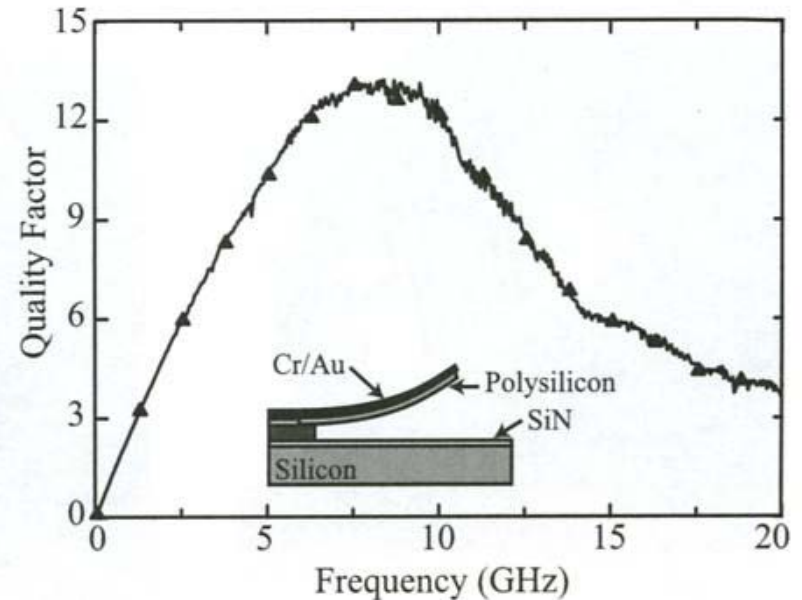
Cr-Au layer over polysilicon layer

Different residual **stress** in materials make the inductor **"curl"** above substrate

Anchor causes a significant parasitic capacitance



(a)



(b)

Figure 12.12. Picture (a) and measured Q (b) of a self-assembled 1.2-nH inductor [20] (Copyright IEEE).

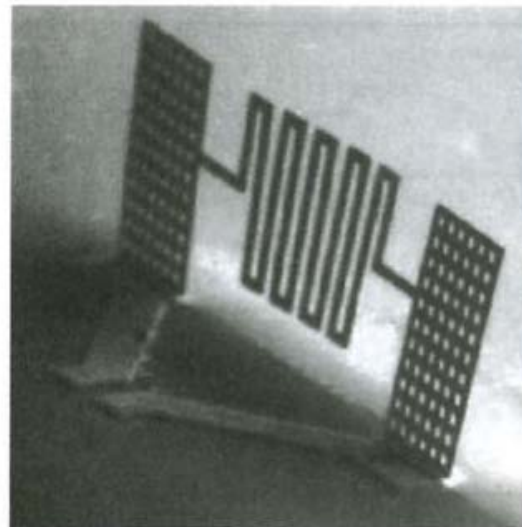
Solder surface tension used

Photo resist as sacrificial layer

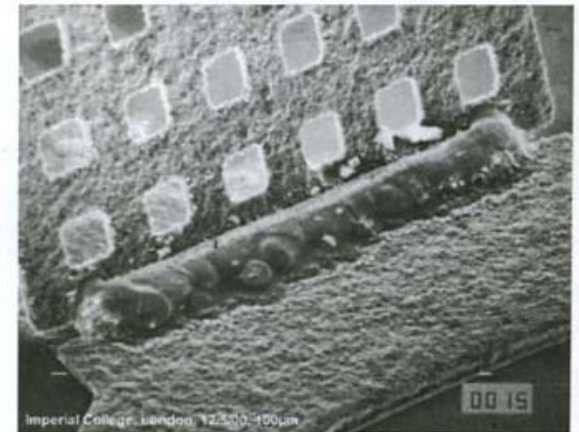
Copper structure with **solder pads** between anchor and a free movable structure

Heating to $185\text{ }^{\circ}\text{C}$ \rightarrow solder pads melt and pull, due to **surface tension force**, the structure to a vertical position

Cooling \rightarrow solder hardens



(a)

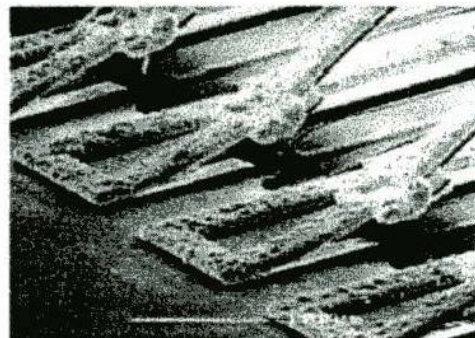
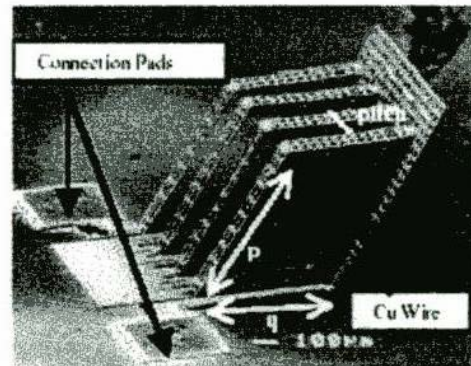
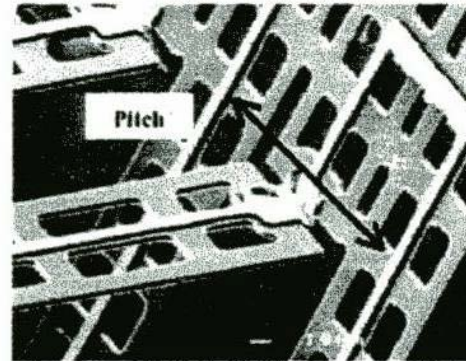


(b)


Figure 12.13. (a) Out-of-plane meander-type inductors after self-assembly, and (b) a blow-up of the solder hinges after heating [22, 23] (Copyright IEEE).

Structure with suspension hinges


- Copper structure can **manually** be folded and glued
- Typical "turns" with large dimensions $\sim 100 \mu\text{m}$
- M. Gel et al, Transducers 2001



Programmable inductor banks



FSRM
FACULTY OF SCIENCE
ROBINSON COLLEGE
CHENNAI

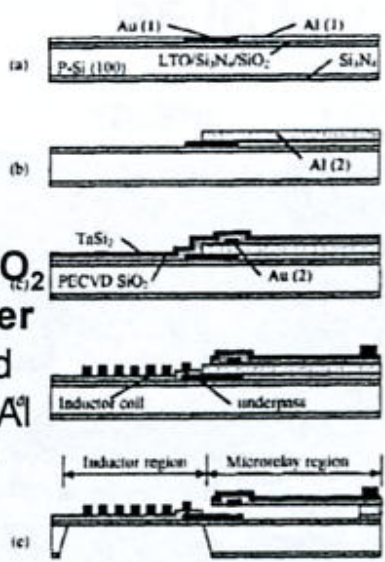
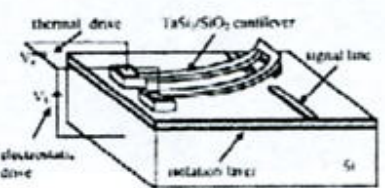


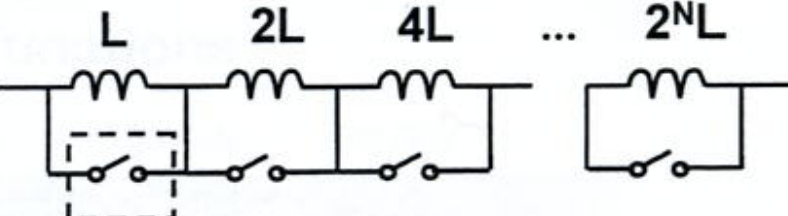
EPFL
ÉCOLE POLYTECHNIQUE
FÉDÉRALE DE LAUSANNE

Micromachined digitized high-Q inductor banks

Design and process (New jersey Institute of Technology)

- micro-relays made on TaSi₂/SiO₂ bimorph cantilever beam, gold-to-gold electrical contact, Alⁿ as sacrificial layer and thermal actuation
- gold inductors and pads



Contact switch (micro-relay) Thermal actuation!

Performance:

- L = 2.5 up to 162.4 nH
- Q=3.3 @ 1.6GHz
- electro-thermal relays with R_{on}=0.6-0.8Ω
- thermal power=8mW, V=20V
- contacts fails after 10⁶ cycles (!!)

D ₃ D ₂ D ₁ D ₀	L (nH)	D ₃ D ₂ D ₁ D ₀	L (nH)
0000	374.8	1000	162.4
0001	277.9	1001	105.7
0010	223.2	1010	67.4
0011	185.0	1011	45.9
0100	166.9	1100	60.5
0101	127.3	1101	31.5
0110	103.8	1110	16.2
0111	83.1	1111	2.5

S. Zhou, X.-Q. Sun, W.N. Carr, TRANSDUCERS '97, Vol. 2, June 1997, pp. 1137 -1140.

How different design parameters influence performance

- Q_{\max} and f_{rez} decrease when area and number of turns increase

Integrated inductor performance versus design space

After Varadan et al. [3]

		Q_{\max}	L	f_{rez}
Conductor thickness	↗	↗	-	-
Sheet resistance	↗	↘	-	-
Insulator thickness	↗	↗	-	↗
Substrate resistivity	↗	↘ ↗	-	↗
Area	↗	↘	↗	↘
Number of turns	↗	↘	↗	↘
Track width	↗	↗	↘	↘
Multilayer inductor (extra layer)	↗	↘	↗	↘

(Double arrow: less influence)